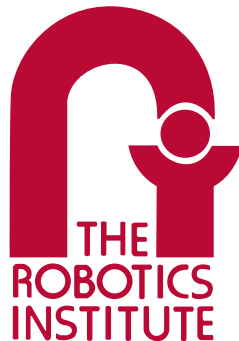


Representation and Matching of Articulated Shapes

Jiayong Zhang, Robert Collins and Yanxi Liu

The Robotics Institute
Carnegie Mellon University



Goal: parse static pictures of people

What does “parse” mean?

- find boundary shape
- locate body parts

Why does it matter?

- gait recognition
- tracking
- activity analysis



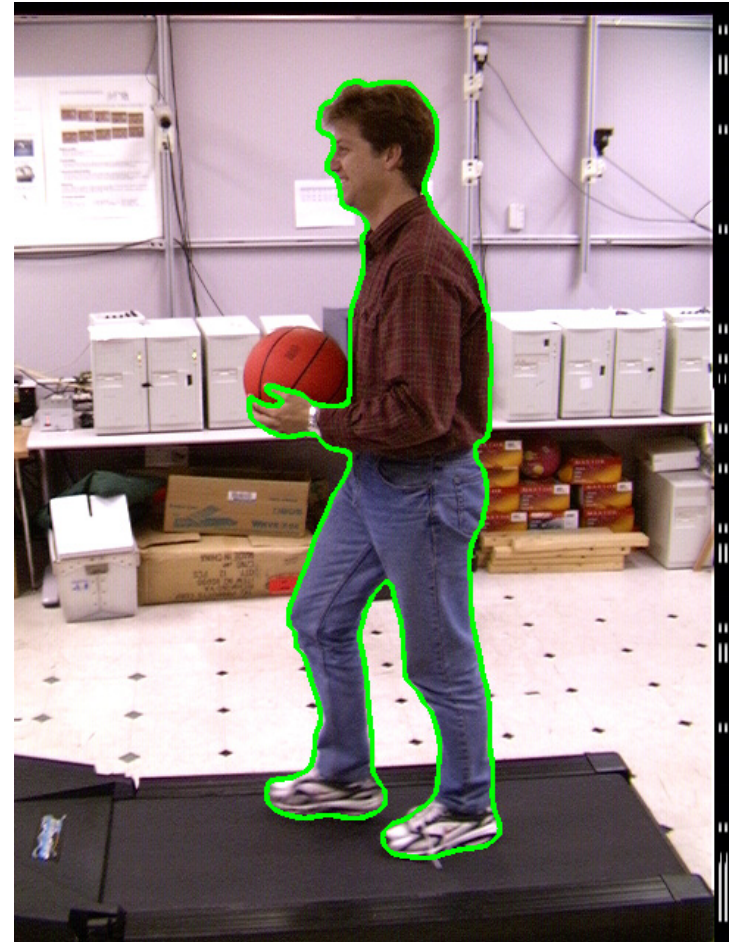
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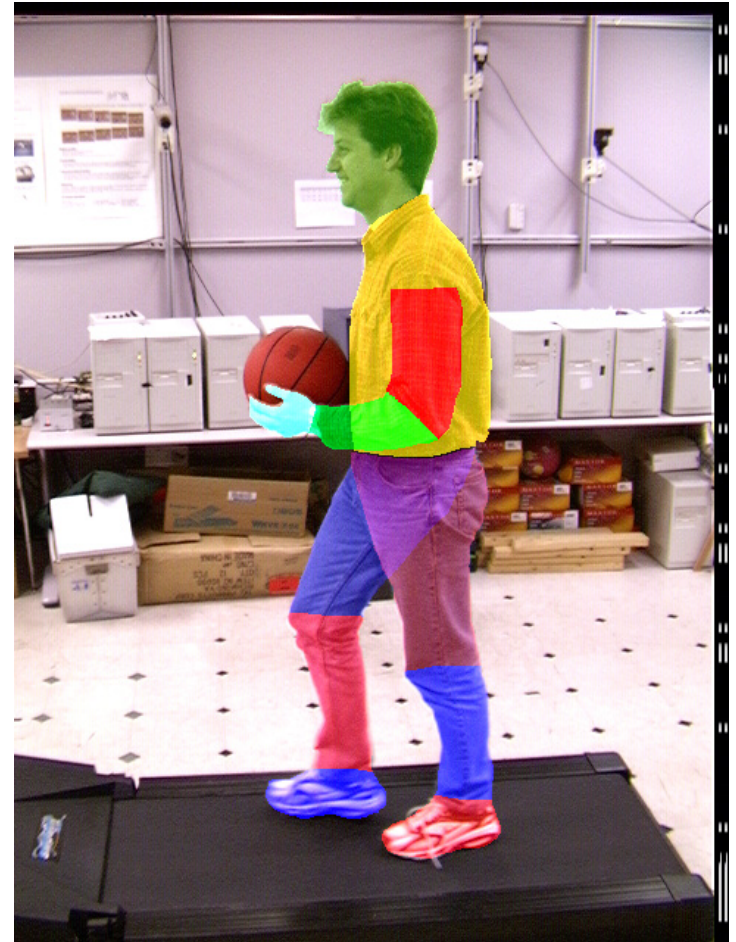
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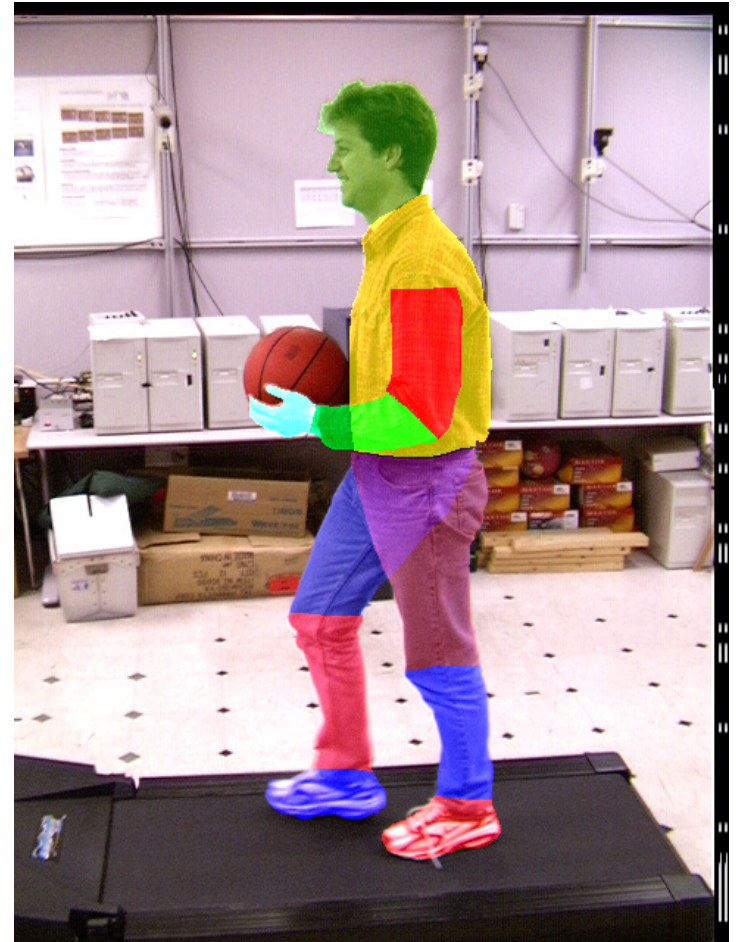
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How to parse?

Goal: parse static pictures of people

What does “parse” mean?

- find boundary shape
- locate body parts

Why does it matter?

- gait recognition
- tracking
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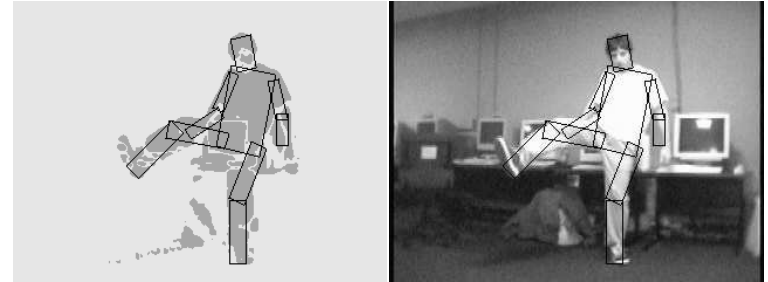
Assumptions

- single person
- side view
- no external occlusion

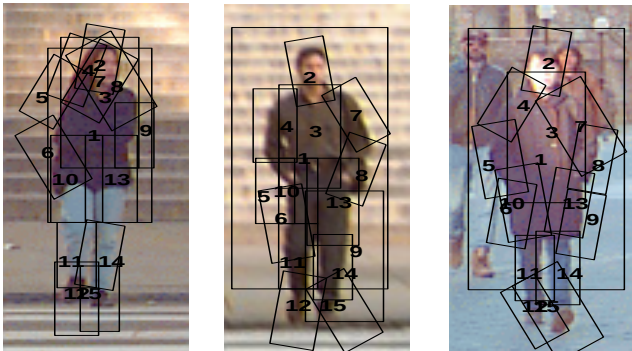
How to parse?

Previous Work

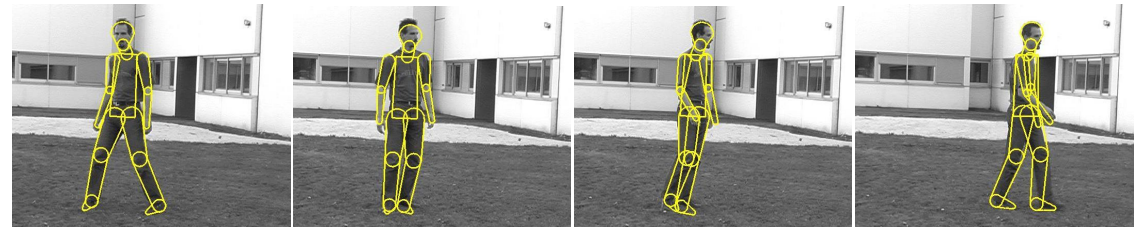
Top-down vs Bottom-up
2D vs 3D
Static vs Dynamic



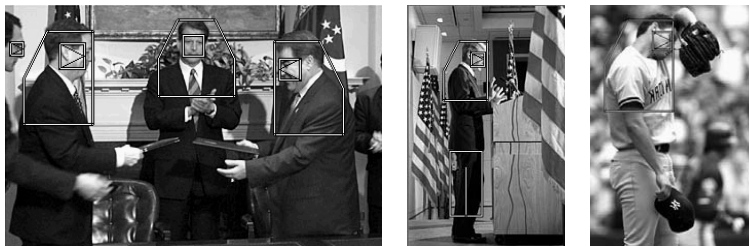
Felzenszwalb & Huttenlocher



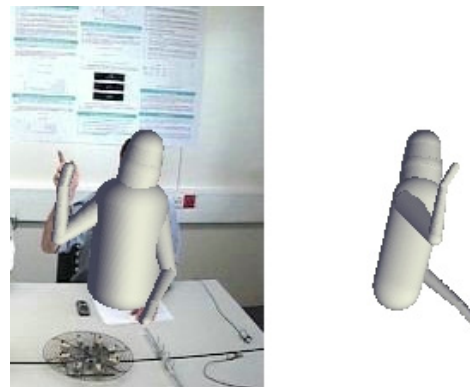
Ronfard, Schmid & Triggs, ECCV02



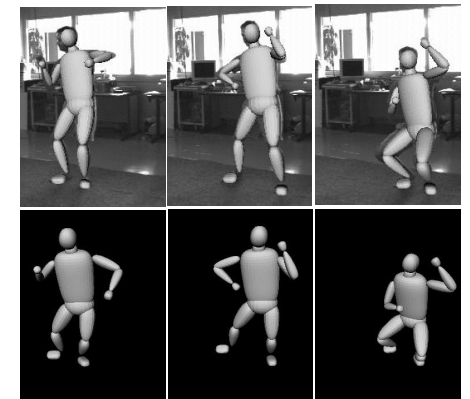
Agarwal & Triggs, ECCV04



Mikolajczyk, Schmid & Zisserman, ECCV04



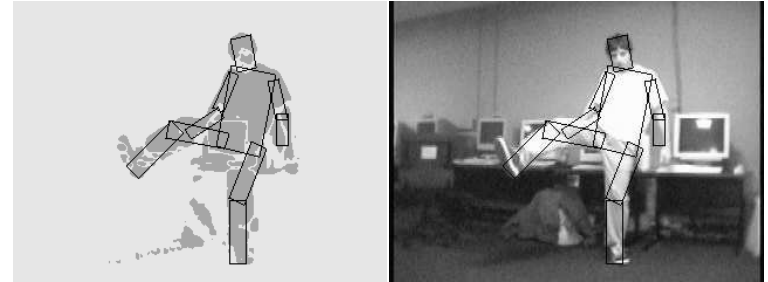
Lee & Cohen
ECCV04



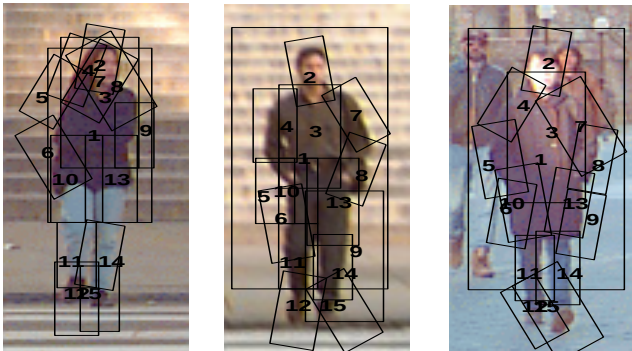
Sminchisescu & Triggs, CVPR03

Previous Work

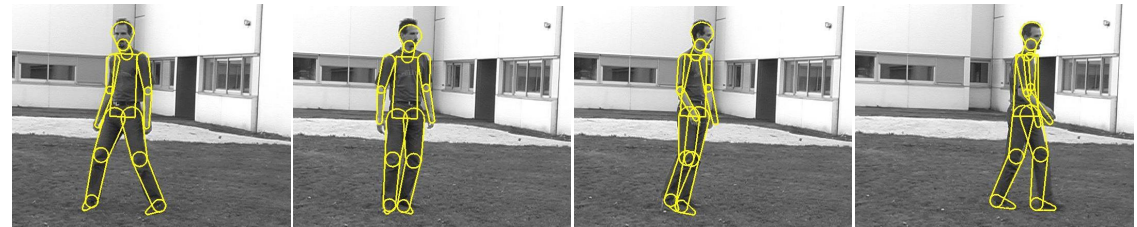
Top-down vs Bottom-up
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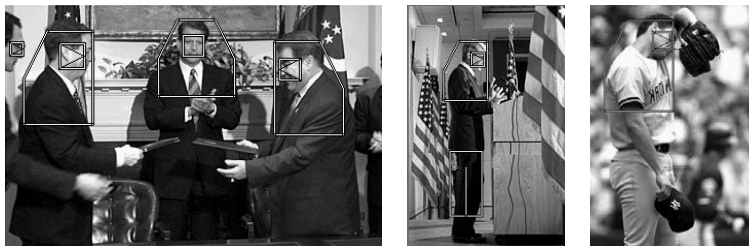
Felzenszwalb & Huttenlocher



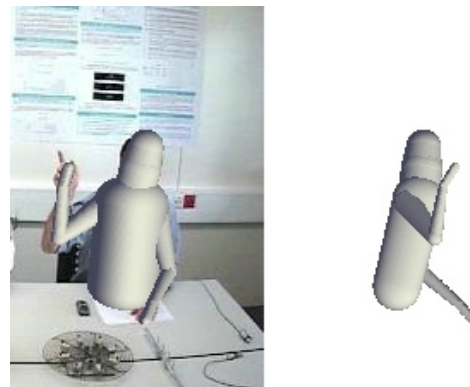
Ronfard, Schmid & Triggs, ECCV02



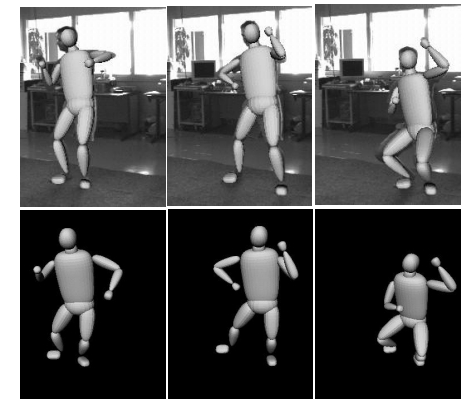
Agarwal & Triggs, ECCV04



Mikolajczyk, Schmid & Zisserman, ECCV04



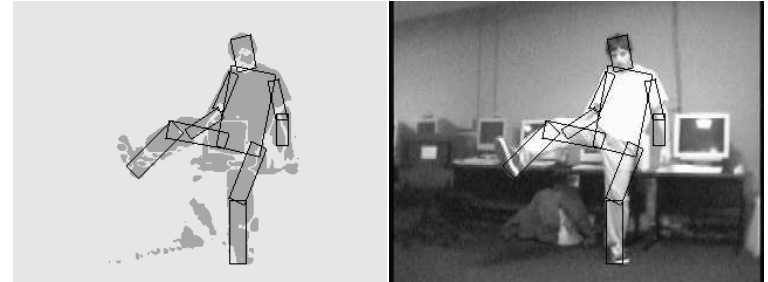
Lee & Cohen
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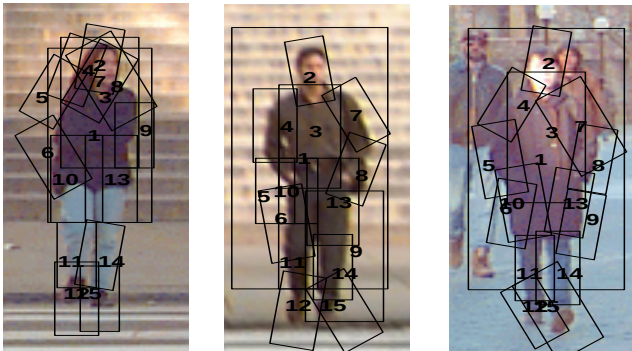
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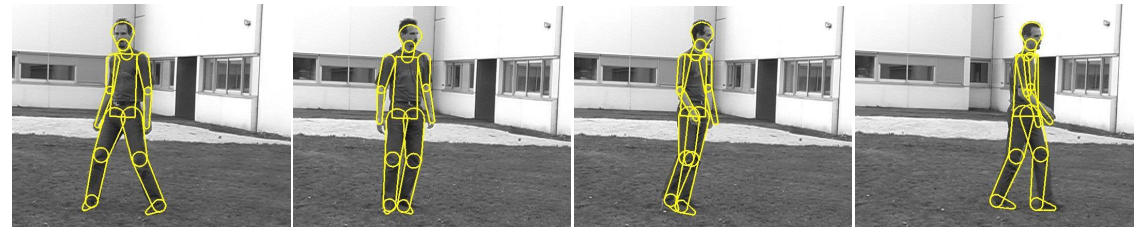
Top-down vs Bottom-up
2D vs **3D**
Static vs Dynamic



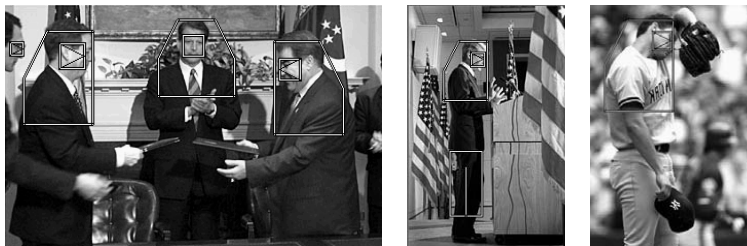
Felzenszwalb & Huttenlocher



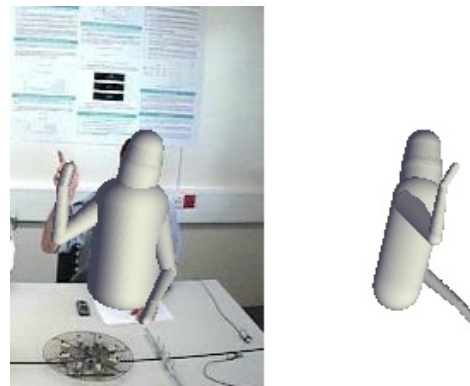
Ronfard, Schmid & Triggs, ECCV02



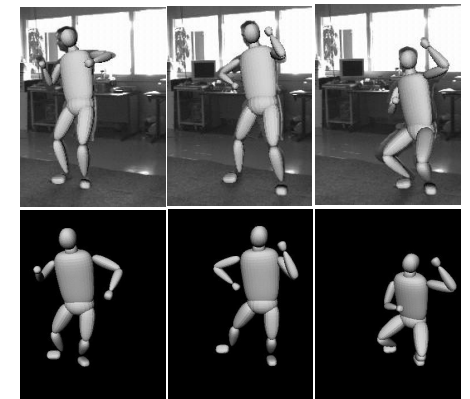
Agarwal & Triggs, ECCV04



Mikolajczyk, Schmid & Zisserman, ECCV04



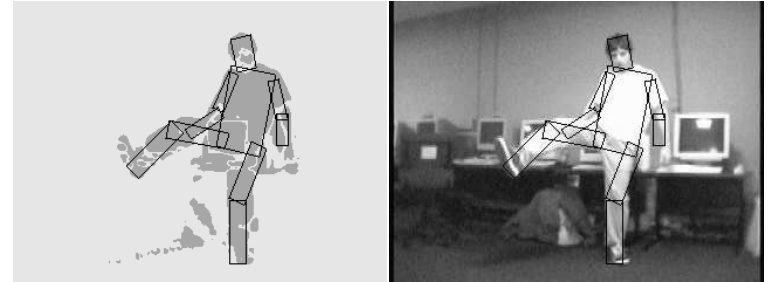
Lee & Cohen
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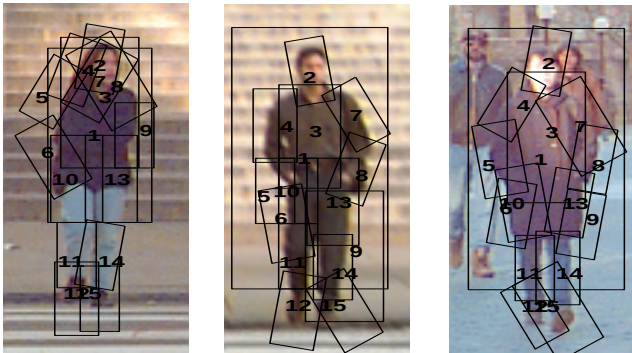
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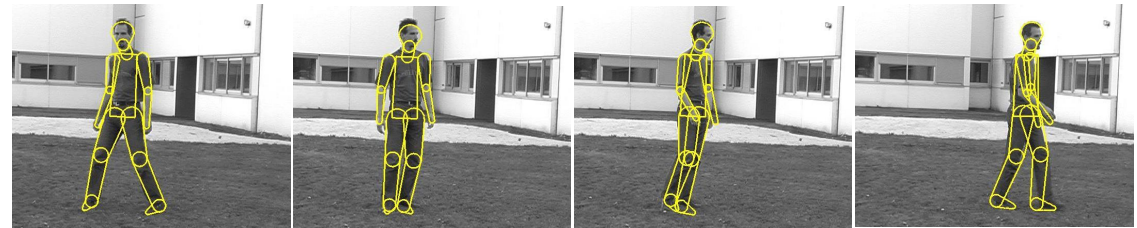
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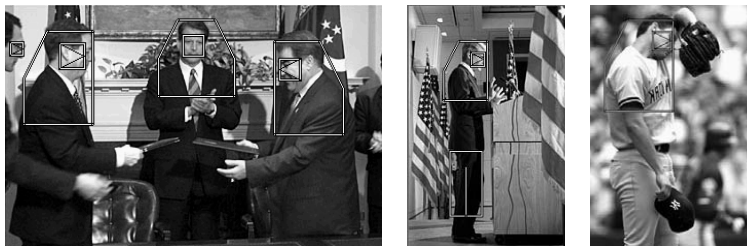
Felzenszwalb & Huttenlocher



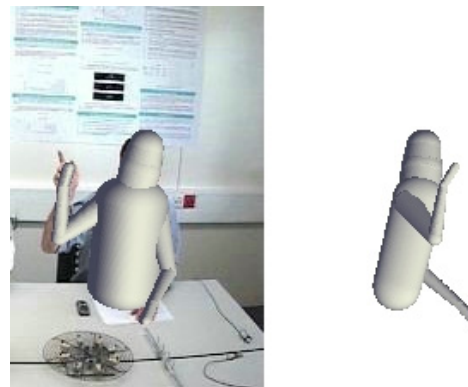
Ronfard, Schmid & Triggs, ECCV02



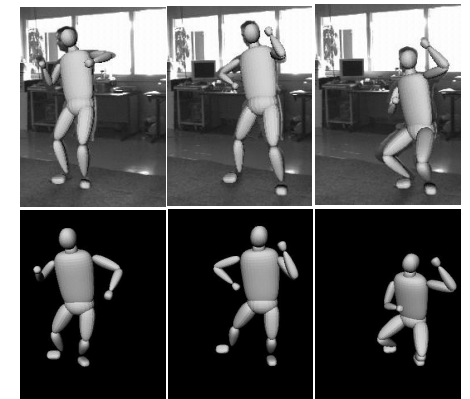
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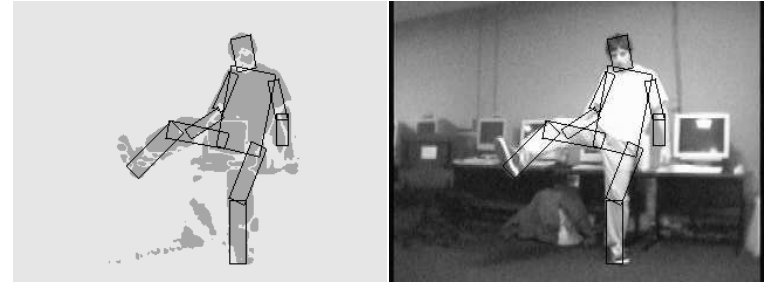
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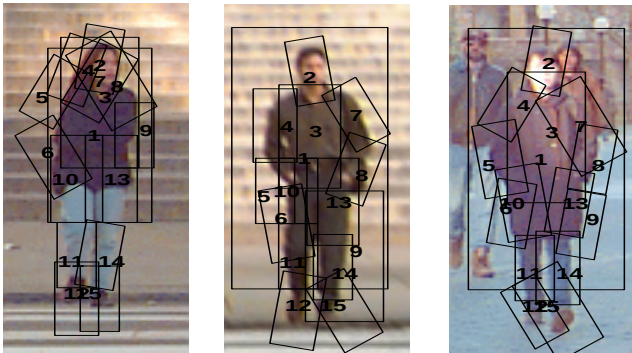
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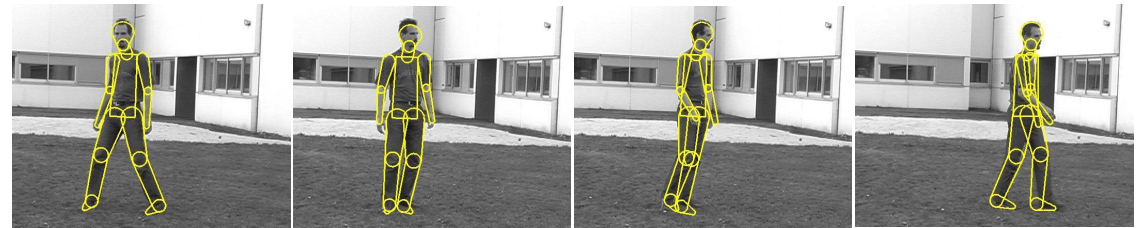
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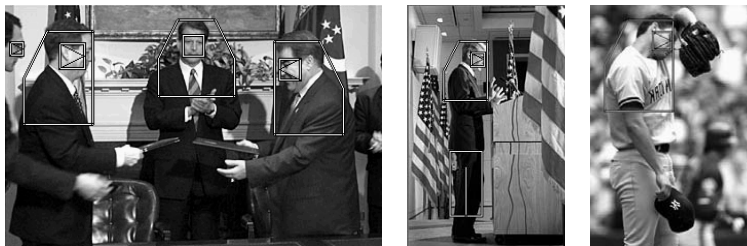
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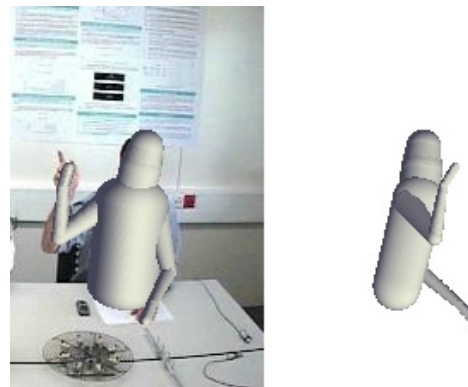
Ronfard, Schmid & Triggs, ECCV02



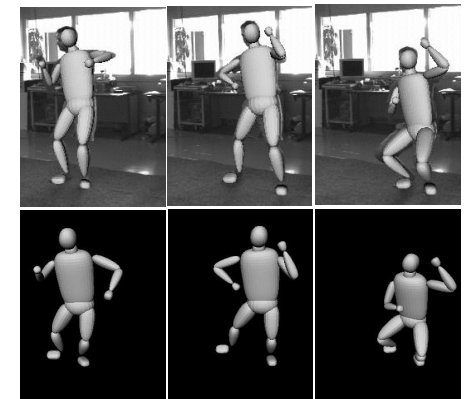
Agarwal & Triggs, ECCV04



Mikolajczyk, Schmid & Zisserman, ECCV04



Lee & Cohen
ECCV04



Sminchisescu & Triggs, CVPR03

Outline: A Bayesian Approach

$$p(\Omega) \quad + \quad p(\mathcal{I}|\Omega) \quad \Rightarrow \quad P(\Omega|\mathcal{I})$$

Shape Prior

Image Likelihood

Posterior Distrib.

Outline: A Bayesian Approach

$$p(\Omega) + p(\mathcal{I}|\Omega) \Rightarrow P(\Omega|\mathcal{I})$$

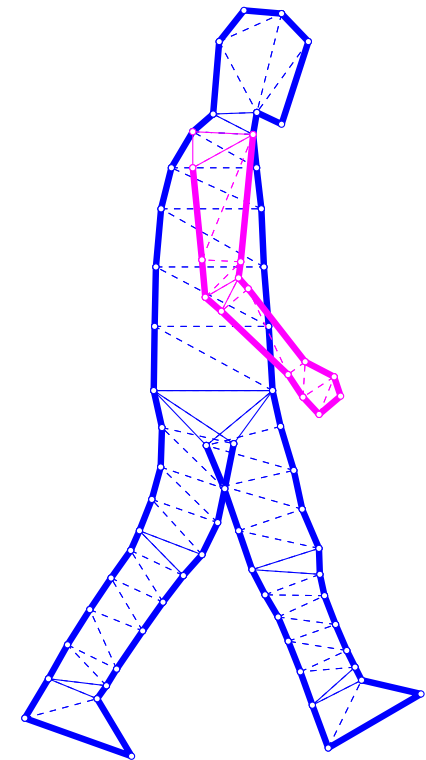
Shape Prior

Image Likelihood

Posterior Distrib.

$p(\Omega)$ modeled as Bayes Net

- global & local deformation
- chain-like structure



Outline: A Bayesian Approach

$$p(\Omega) + p(\mathcal{I}|\Omega) \Rightarrow P(\Omega|\mathcal{I})$$

Shape Prior

Image Likelihood

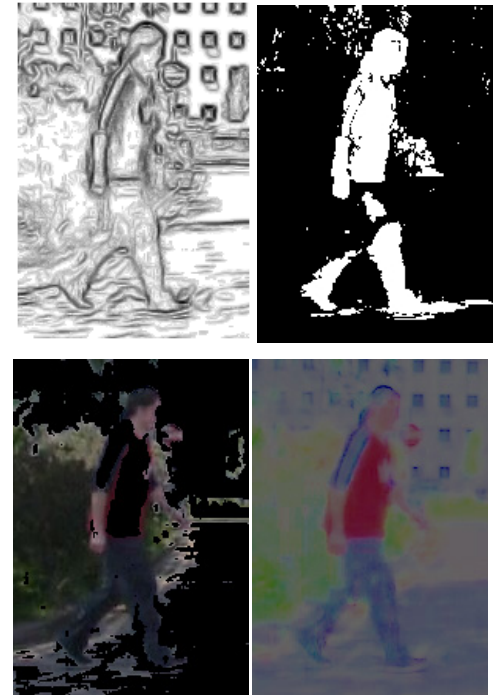
Posterior Distrib.

$p(\Omega)$ modeled as Bayes Net

- global & local deformation
- chain-like structure

$p(\mathcal{I}|\Omega)$ combines 4 types of cues

- edge, intensity & color based



Outline: A Bayesian Approach

$$p(\Omega) + p(\mathcal{I}|\Omega) \Rightarrow P(\Omega|\mathcal{I})$$

Shape Prior

Image Likelihood

Posterior Distrib.

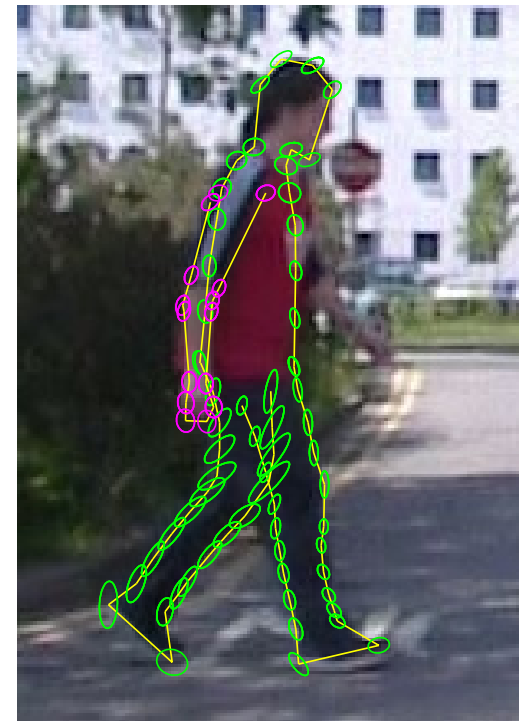
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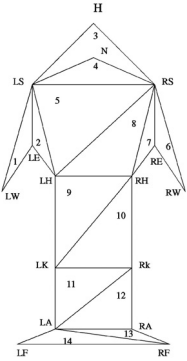
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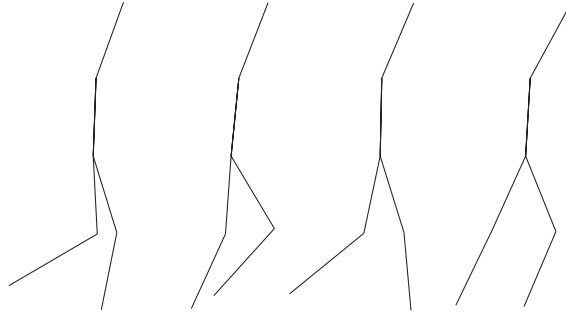
$\tilde{\Omega} \sim p(\Omega|\mathcal{I})$ by Sequential MC



Shape = Joint Config + *Anthropometry*

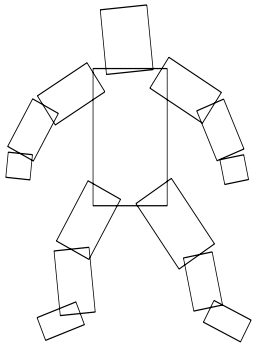


POINT

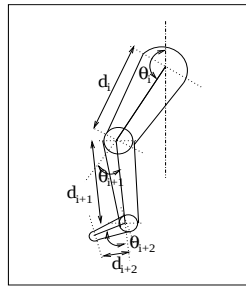


STICK FIGURE

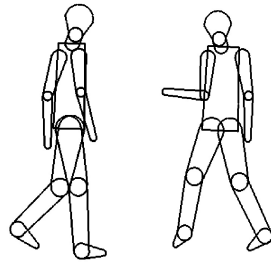
*Slim, fat, pear, apple,
chest, belly,
straight, crooked,
sexy ...*



PICTORIAL
STRUCTURE

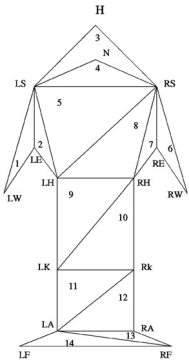


SCALED PRISMATIC
MODEL

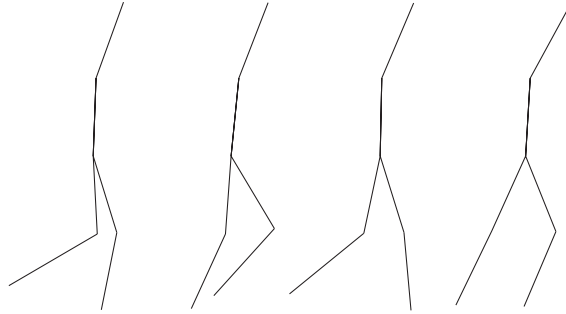


Typical part representations.

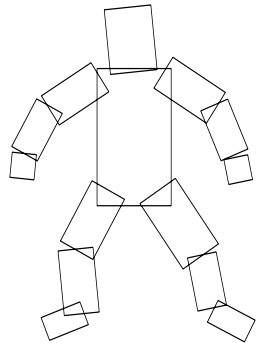
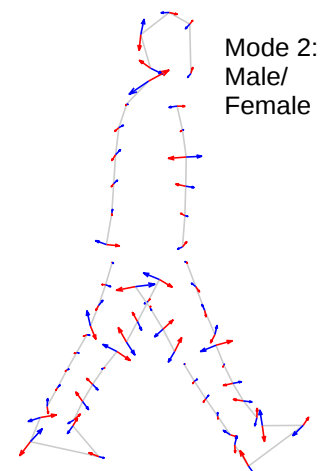
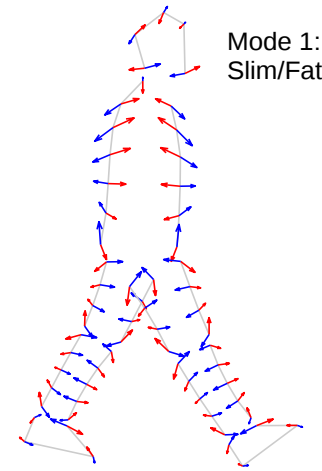
Shape = Joint Config + *Anthropometry*



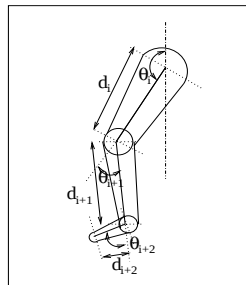
POINT



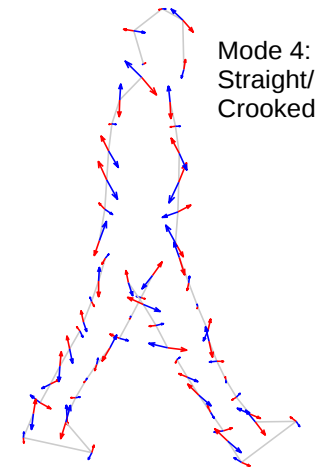
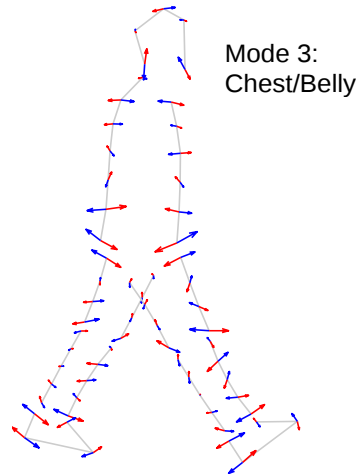
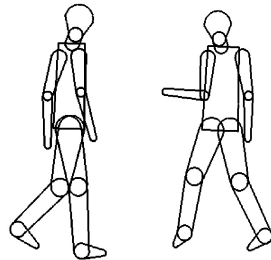
STICK FIGURE



PICTORIAL
STRUCTURE



SCALED PRISMATIC
MODEL



Typical part representations.

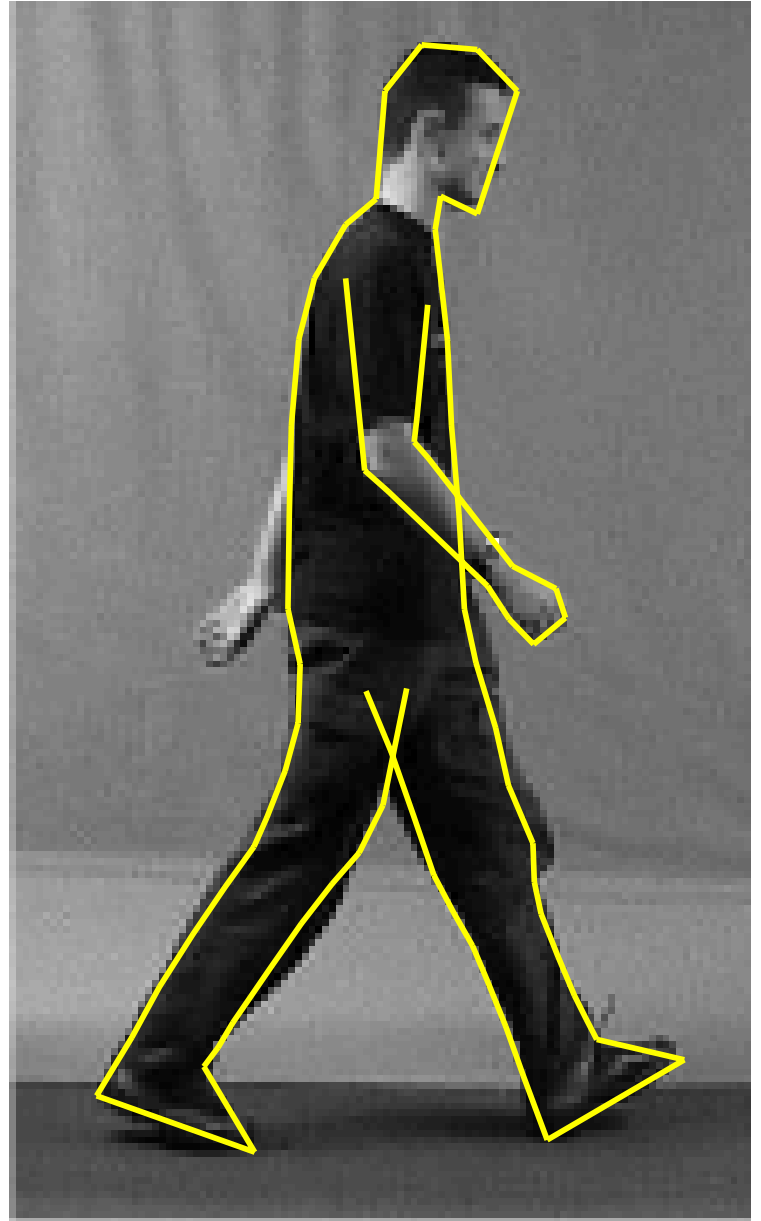
Var. across subject & gait cycle
from hand-labeled dataset.

Shape Prior

Shape $\sim K$ landmark points

$$\mathbf{v}_{1:K} = \Omega = \{(x_k, y_k)\}_{k=1}^K$$

Prior $\sim p(\Omega), \Omega \in \mathcal{R}^{2K}$

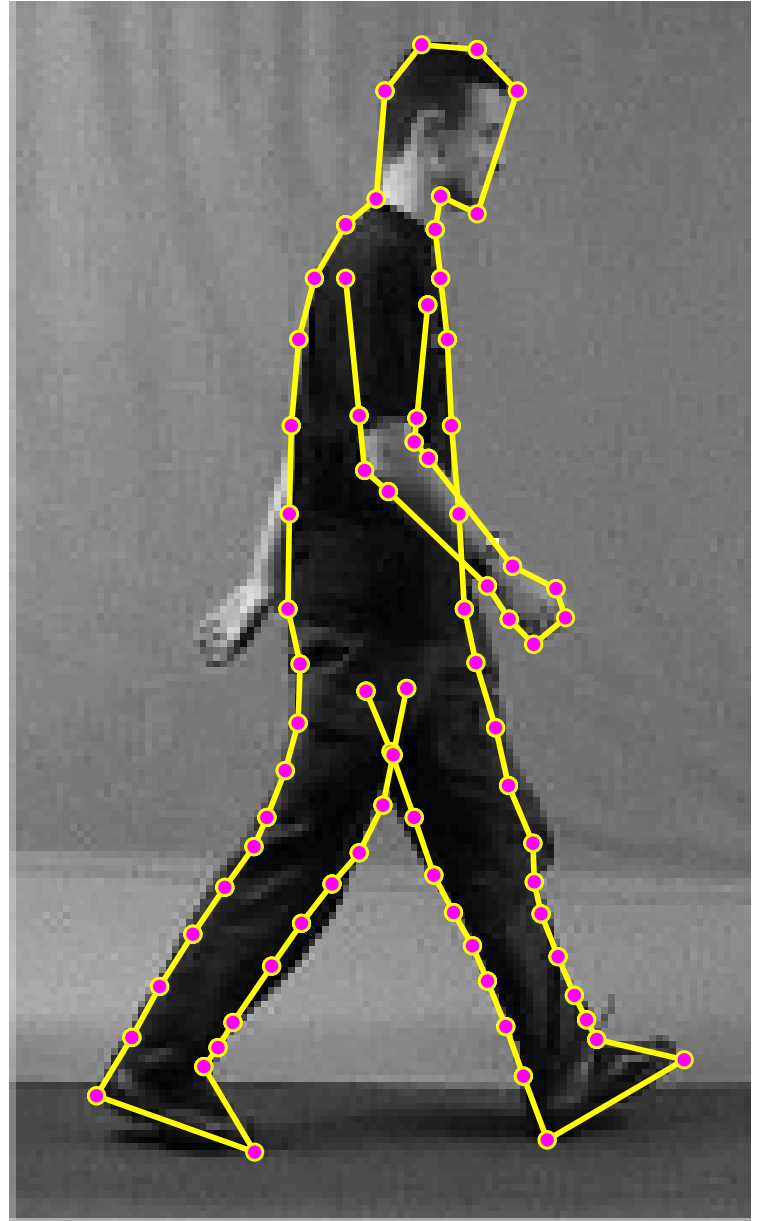


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Shape Prior

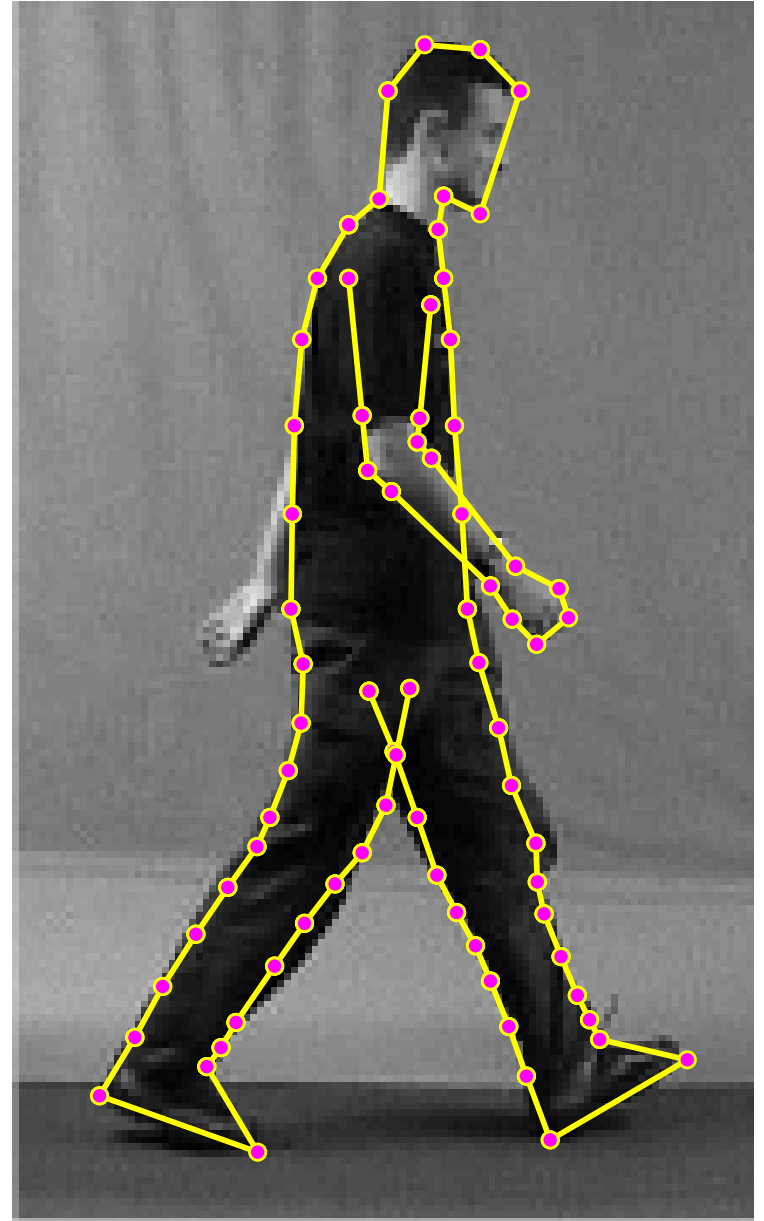
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Procrustes analysis on Ω ?

- articulated motion
- efficient inference



Shape Prior

Shape $\sim K$ landmark points

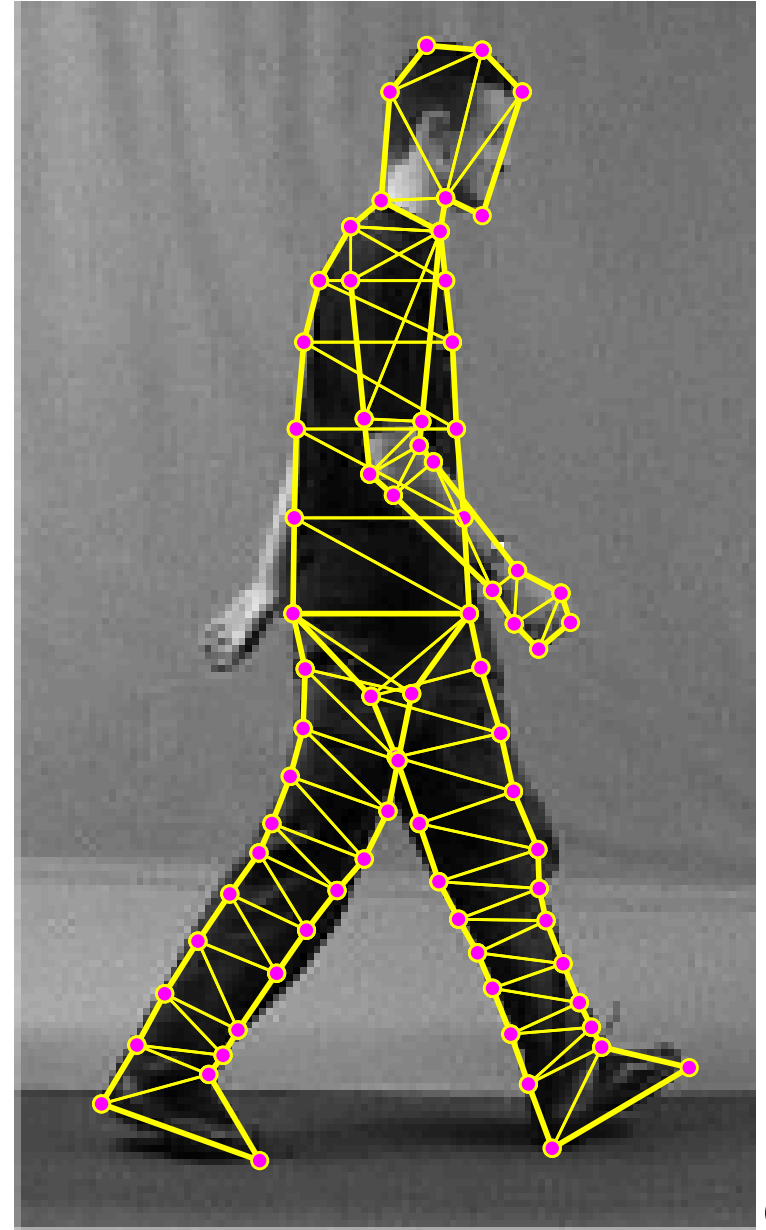
$$\mathbf{v}_{1:K} = \Omega = \{(x_k, y_k)\}_{k=1}^K$$

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Shape as Bayes network by

- triangulation
- cond. independence

$$\begin{aligned} p(\mathbf{v}_{1:K}) &= \prod_k p(\mathbf{v}_k | \mathbf{v}_{1:k-1}) \\ &= \prod_k p(\mathbf{v}_k | \text{parent of } \mathbf{v}_k) \end{aligned}$$



Shape Prior (cont.)

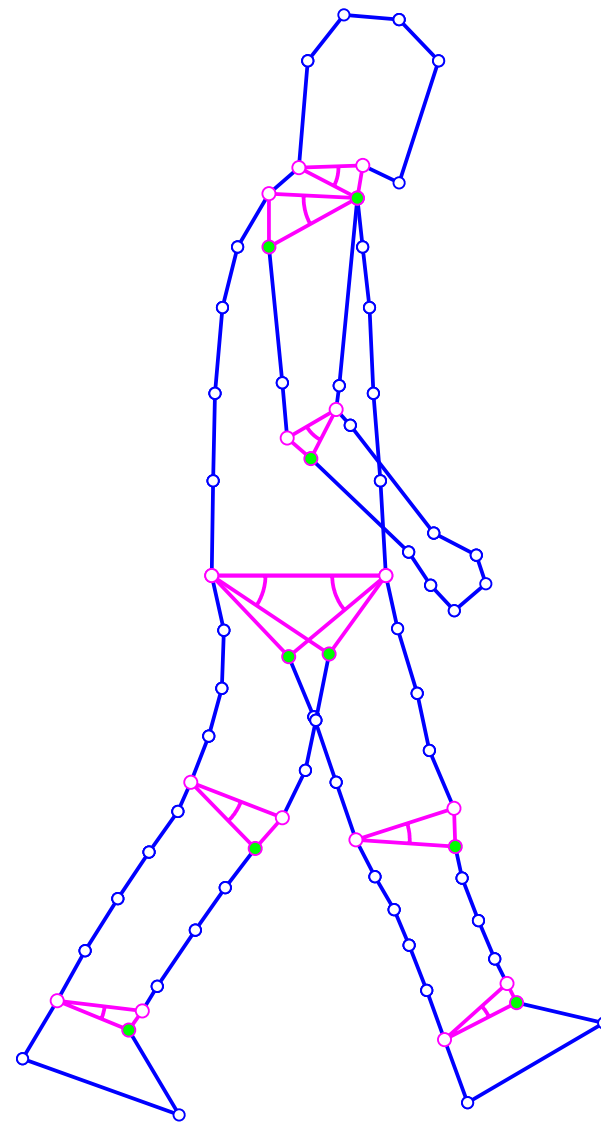
Two deformation mechanisms to specify $p(\mathbf{v}_k | \mathbf{v}_{1:k-1})$.

I. Rotation of Joints

Joint vertex $\mathbf{v}$ and its parent edge $\mathbf{e}$ define joint angle θ .

$$\mathbf{v} = \rho \cdot \text{Rot}(\theta) \cdot \vec{\mathbf{e}} + p(\theta_{1:9}), p(\rho_{1:9})$$

$$\Rightarrow p(\mathbf{v}_k | \mathbf{v}_{1:k-1}) = p(\mathbf{v}_k | \mathbf{e}_k, \theta\text{'s visited})$$



Shape Prior (cont.)

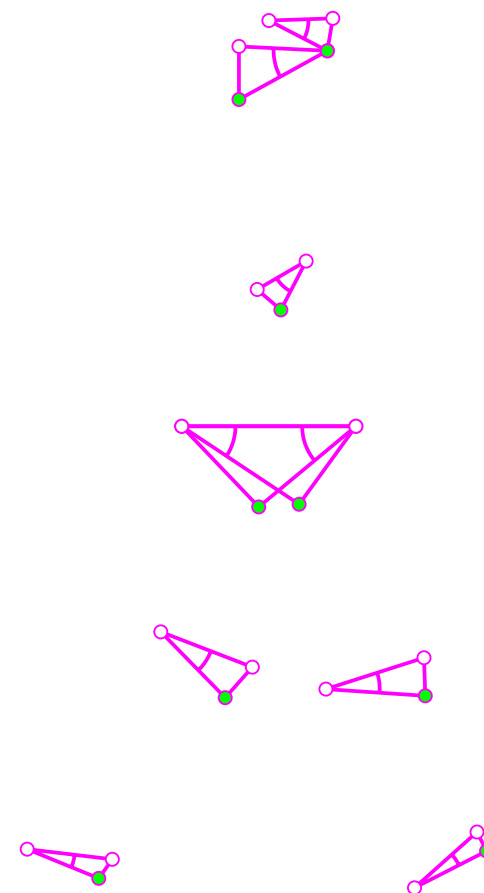
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Shape Prior (cont.)

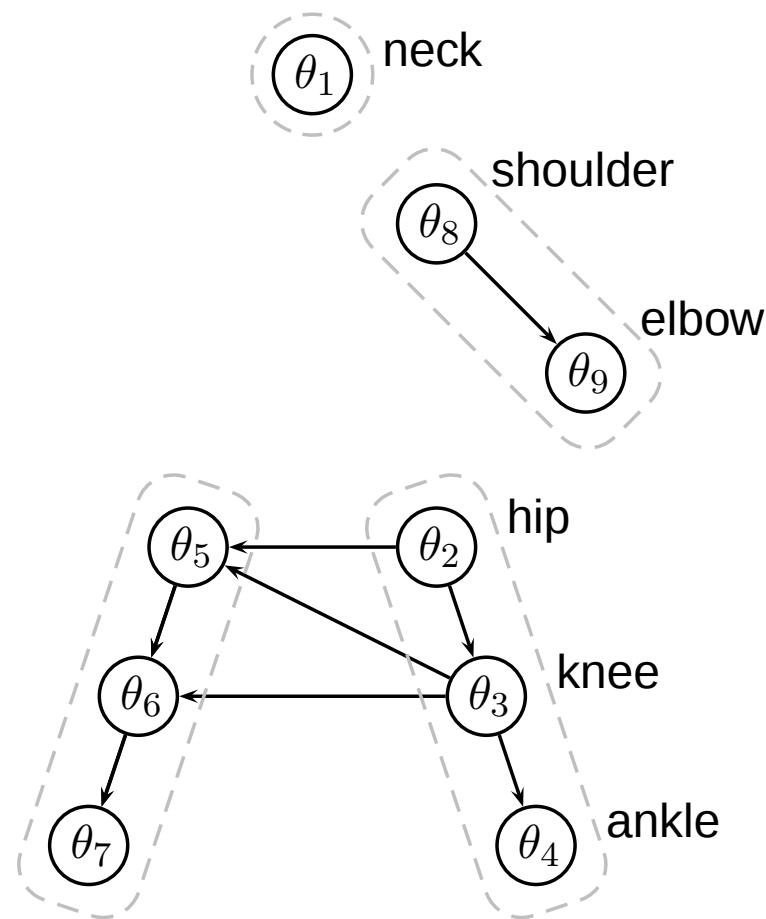
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$$p(\Theta) = p(\theta_{1:9})$$

Shape Prior (cont.)

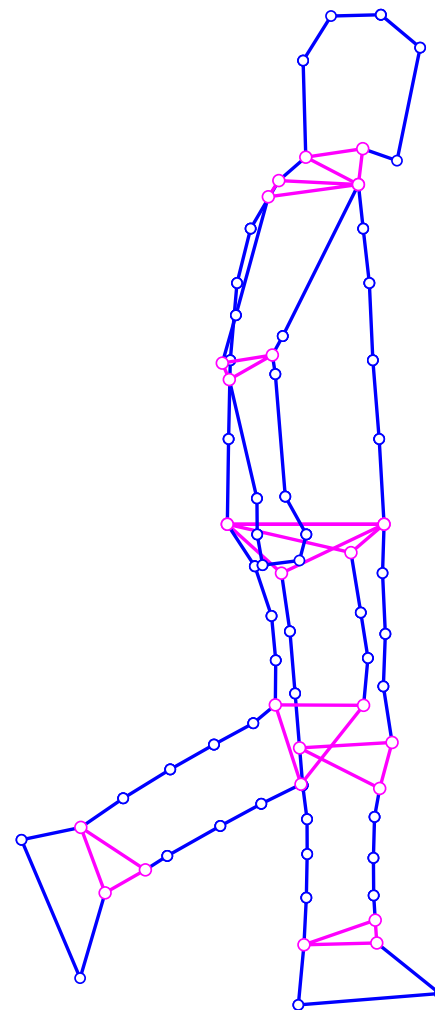
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$$\tilde{\Theta} \sim p(\Theta)$$



Shape Prior (cont.)

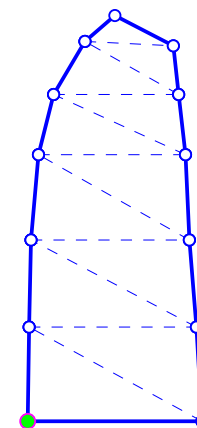
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II. Local Nonrigid Motion

Parent triangle $\mathbf{g} \rightarrow$ affine trans. (A, b) .

$$\mathbf{v} = (A \cdot \bar{\mathbf{v}} + b) \circ \mathbf{n} + p(\mathbf{n}_k)$$

$$\Rightarrow p(\mathbf{v}_k | \mathbf{v}_{1:k-1}) = p(\mathbf{v}_k | \mathbf{g}_k)$$

Shape Prior (cont.)

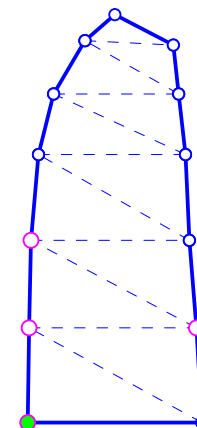
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Shape Prior (cont.)

Two deformation mechanisms to specify $p(\mathbf{v}_k | \mathbf{v}_{1:k-1})$.

I. Rotation of Joints

Joint vertex $\mathbf{v}$ and its parent edge $\mathbf{e}$ define joint angle θ .

$$\mathbf{v} = \rho \cdot \text{Rot}(\theta) \cdot \vec{\mathbf{e}} + p(\theta_{1:9}), p(\rho_{1:9})$$

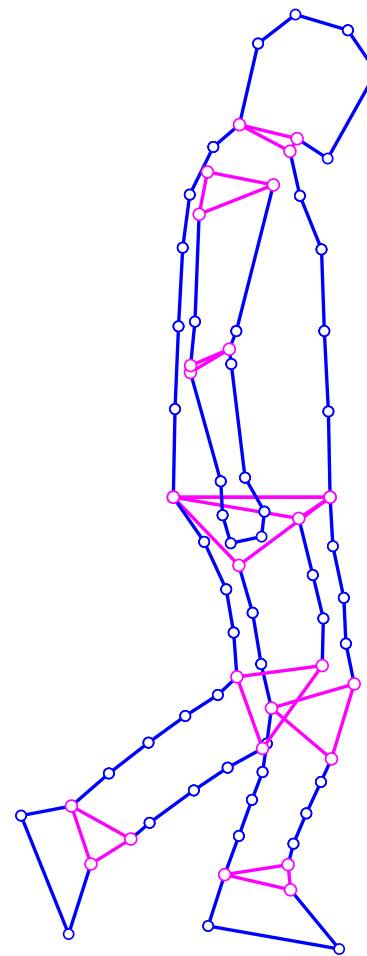
$$\Rightarrow p(\mathbf{v}_k | \mathbf{v}_{1:k-1}) = p(\mathbf{v}_k | \mathbf{e}_k, \theta\text{'s visited})$$

II. Local Nonrigid Motion

Parent triangle $\mathbf{g} \rightarrow$ affine trans. (A, b) .

$$\mathbf{v} = (A \cdot \bar{\mathbf{v}} + b) \circ \mathbf{n} + p(\mathbf{n}_k)$$

$$\Rightarrow p(\mathbf{v}_k | \mathbf{v}_{1:k-1}) = p(\mathbf{v}_k | \mathbf{g}_k)$$



$$\tilde{\Omega} \sim p(\Omega)$$



Image Likelihood

Cover $\mathbf{v}_{1:K}$ by set of clusters $\mathcal{C}$.

- cluster size from 2 to 6

Define $\phi(\mathbf{v}_C) \propto p(f_C | \mathbf{v}_C), C \in \mathcal{C}$.

- independence assumption

Four types of image features f_C

- Edge Gradient Map
- Foreground Mask
- Skin Color Mask
- Appearance Consistency

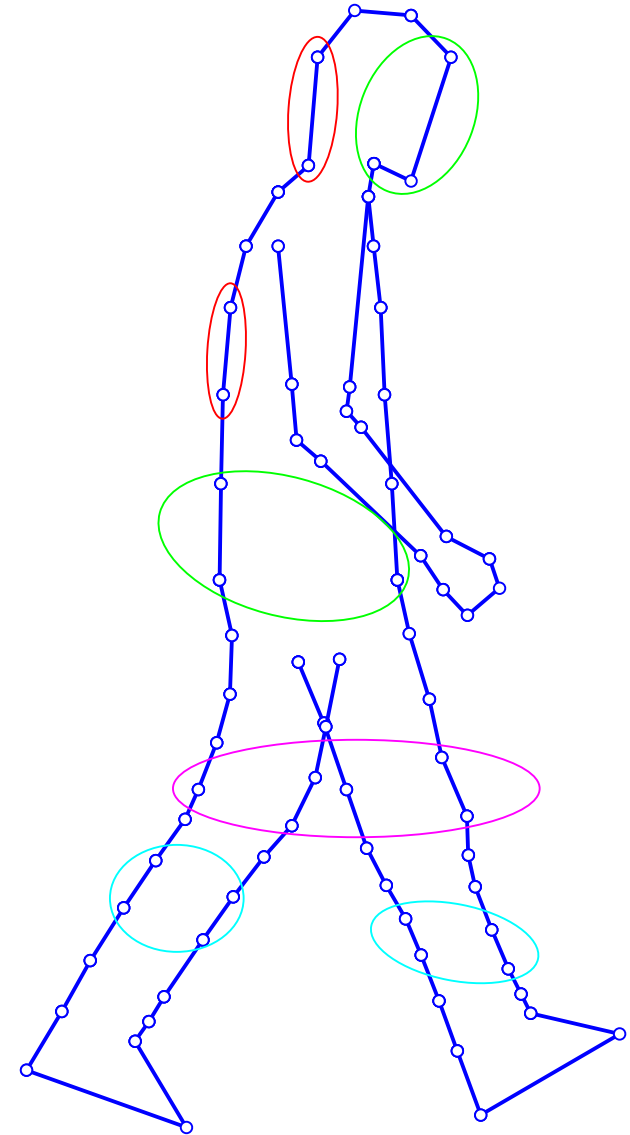


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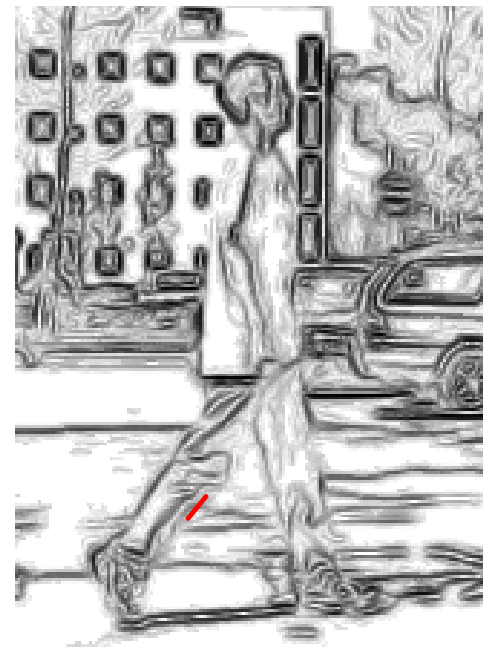


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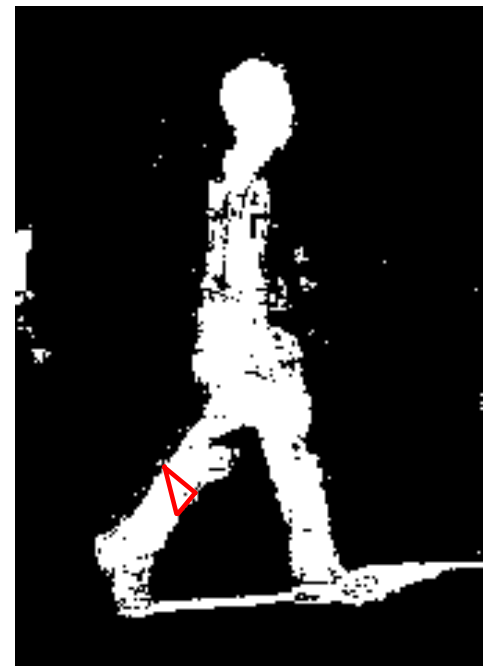


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Four types of image features f_C

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Image Likelihood

Cover $\mathbf{v}_{1:K}$ by set of clusters $\mathcal{C}$.

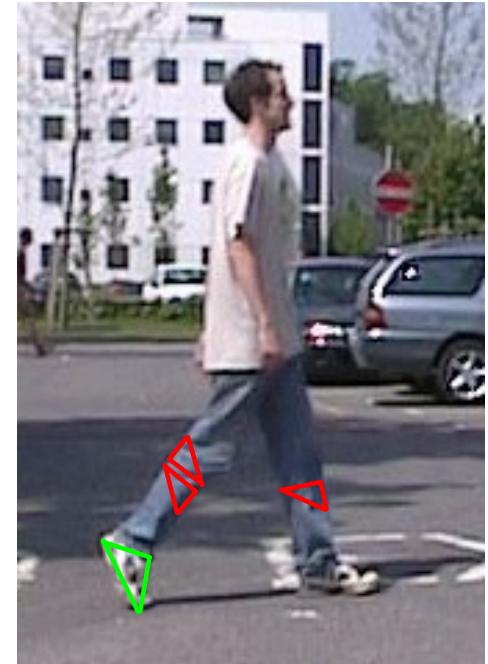
- cluster size from 2 to 6

Define $\phi(\mathbf{v}_C) \propto p(f_C | \mathbf{v}_C), C \in \mathcal{C}$.

- independence assumption

Four types of image features f_C

- Edge Gradient Map
- Foreground Mask
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- Appearance Consistency



Posterior Distribution

$$p(\mathbf{v}_{1:K}|\mathcal{I}) \propto \underbrace{p(\Theta) \prod_{k \in \mathcal{J}} p(\rho_k) \prod_{k \notin \mathcal{J}} p(\mathbf{n}_k)}_{\text{Prior}} \underbrace{\prod_{C \in \mathcal{C}} \phi(\mathbf{v}_C)}_{\text{Likelihood}}$$

$\mathcal{J}$ index set of joint vertices, $|\mathcal{J}| = 9$

Θ joint angles, $\theta_{1:9}$

ρ_k radius scaling in polar coordinates

$\mathbf{n}_k$ residual noise in Cartesian coordinates

$\mathcal{C}$ index set of clusters

$\phi(\mathbf{v}_C)$ likelihood potential, $\propto p(f_C|\mathbf{v}_C)$

Posterior Distribution

$$p(\mathbf{v}_{1:K}|\mathcal{I}) \propto \underbrace{p(\Theta) \prod_{k \in \mathcal{J}} p(\rho_k) \prod_{k \notin \mathcal{J}} p(\mathbf{n}_k)}_{\text{Prior}} \underbrace{\prod_{C \in \mathcal{C}} \phi(\mathbf{v}_C)}_{\text{Likelihood}}$$

Inference Tools Available

- DP (Dynamic Programming)
- MF (Mean Field)
- BP (Belief Propagation)
- MCMC (Markov Chain Monte Carlo)
- SMC (Sequential Monte Carlo)

Posterior Distribution

$$p(\mathbf{v}_{1:K}|\mathcal{I}) \propto \underbrace{p(\Theta) \prod_{k \in \mathcal{J}} p(\rho_k) \prod_{k \notin \mathcal{J}} p(\mathbf{n}_k)}_{\text{Prior}} \underbrace{\prod_{C \in \mathcal{C}} \phi(\mathbf{v}_C)}_{\text{Likelihood}}$$

Inference Tools Negative

• DP ☹️

• MF ☹️

• BP ☹️

• MCMC

• SMC

• continuous variables

• clique size as high as 9

• complex likelihood

Posterior Distribution

$$p(\mathbf{v}_{1:K}|\mathcal{I}) \propto \underbrace{p(\Theta) \prod_{k \in \mathcal{J}} p(\rho_k) \prod_{k \notin \mathcal{J}} p(\mathbf{n}_k)}_{\text{Prior}} \underbrace{\prod_{C \in \mathcal{C}} \phi(\mathbf{v}_C)}_{\text{Likelihood}}$$

Inference Tools

- DP 😞
- MF 😞
- BP 😞
- MCMC
- SMC 😊

Negative

- continuous variables
- clique size as high as 9
- complex likelihood

Positive

- chain-like model structure

Sequential Importance Sampling

Proposal Distribution

$$\begin{aligned}\pi_k &= \pi_{k-1} \cdot p(\mathbf{v}_k | \mathbf{v}_{1:k-1}) \\ &= \pi_{k-1} \cdot \begin{cases} p(\mathbf{v}_k | \mathbf{e}_k, \Theta_{k-1}) & \text{if } \mathbf{v}_k \text{ is joint vtx} \\ p(\mathbf{v}_k | \mathbf{g}_k) & \text{otherwise} \end{cases}\end{aligned}$$

Importance Weights

$$w_k \propto w_{k-1} \cdot \prod_{C \in \mathcal{C}_k} \phi(\mathbf{v}_C)$$

Resampling Scheme: Stratified resampling

Experimental Dataset



Training

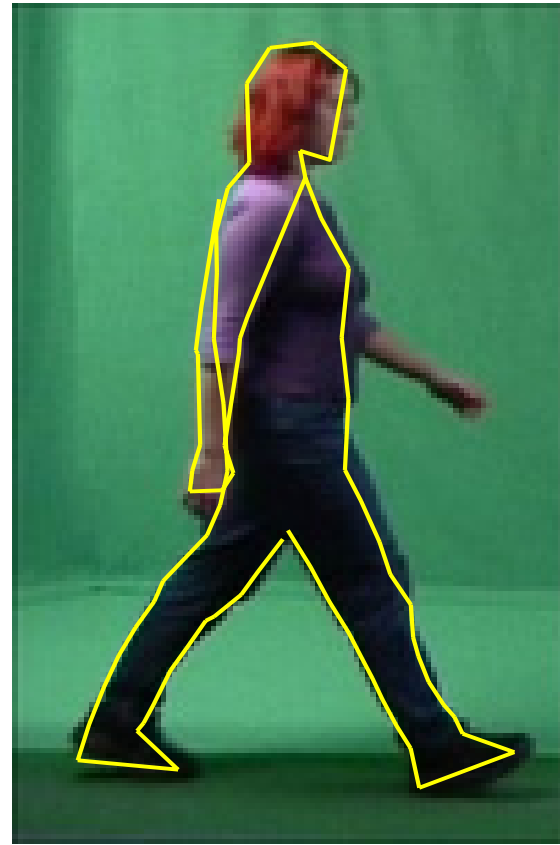
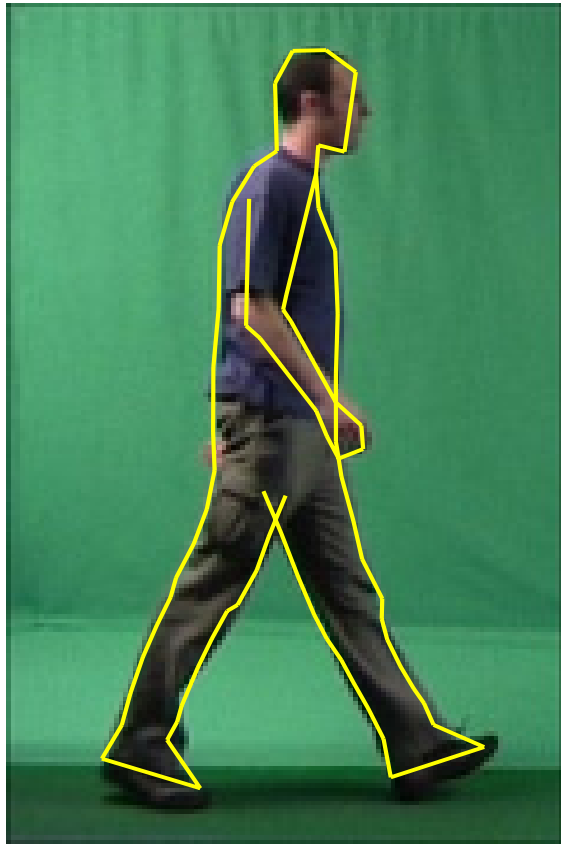
- indoor, green backdrop, controlled lighting
- 28 subj, 112 seq, 3126 frm



Test

- outdoor, cluttered bg, natural lighting
- 10 subj, 10 seq, 963 frm
- 50 frames selected w/ ground truth

Bootstrap with Uniform Prior



- Hand-label one frame of the indoor data.
- Fit training set using uniform $p(\Theta)$, $p(\rho)$, $p(\mathbf{n})$.
- Learned prior $\Rightarrow$ more challenging seqs.

Visualizing SMC Inference

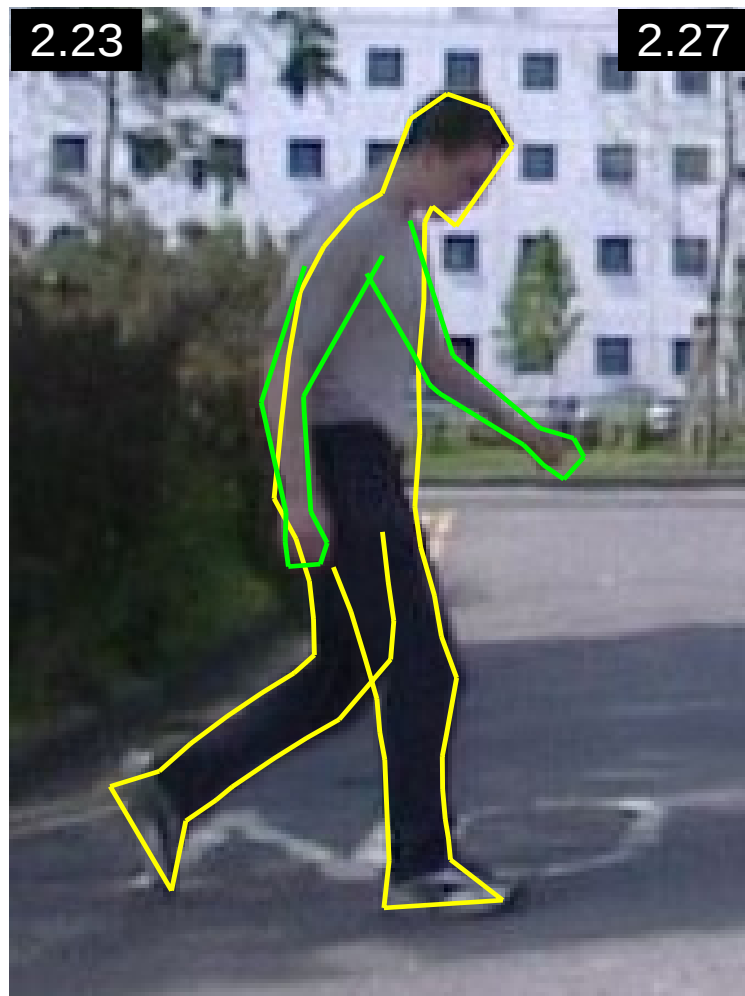


Marginal distrib. of each vertex is summarized by its covariance ellipse (error ellipse).

Quantitative Evaluation on 50 Frames

Body Error

Arm Error

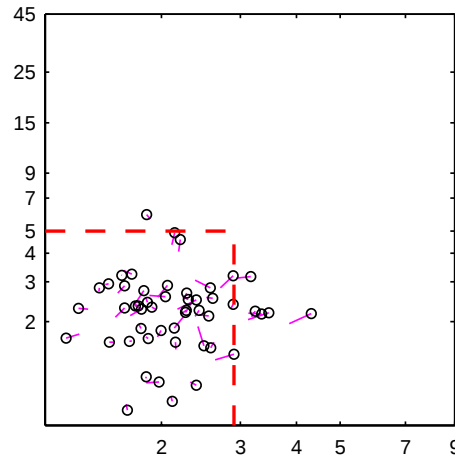


$\phi_e \phi_f \phi_s \phi_c$	Chamfer Distance	
	Body	Arm
● ○ ○ ○	4.00 ± 3.52	4.41 ± 4.08
○ ● ○ ○	2.53 ± 0.91	6.25 ± 5.95
○ ● ● ●	2.19 ± 0.61	2.36 ± 0.94
● ○ ● ●	2.77 ± 1.62	4.13 ± 6.83
● ● ○ ●	2.00 ± 0.59	2.96 ± 1.51
● ● ● ○	2.02 ± 0.53	2.25 ± 1.30
● ● ● ●	1.87 ± 0.42	2.18 ± 0.99

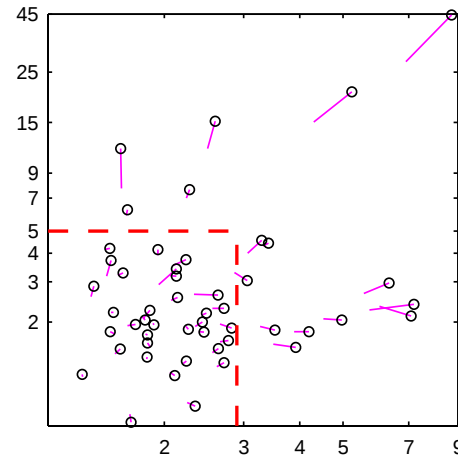
● error unit in pixels

● avg height ~ 200 pixels

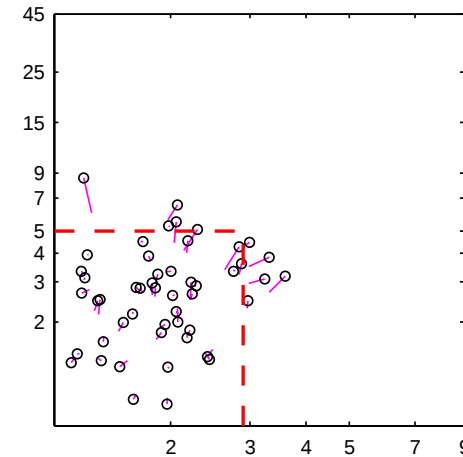
Each image cue has a role to play



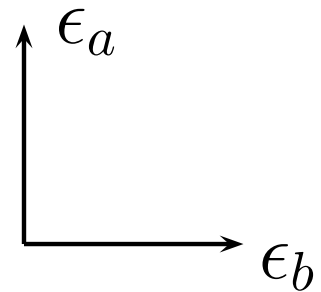
(a) ~~E~~, F, S, C
(+0.32, +0.18)



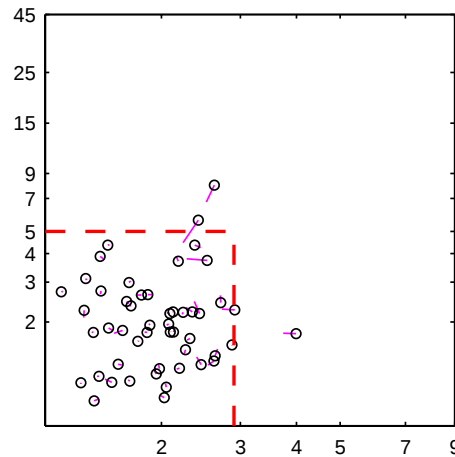
(b) E, ~~F~~, S, C
(+0.90, +1.95)



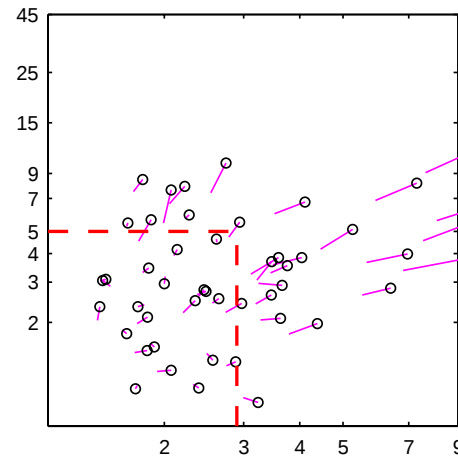
(c) E, F, ~~S~~, C
(+0.13, +0.78)



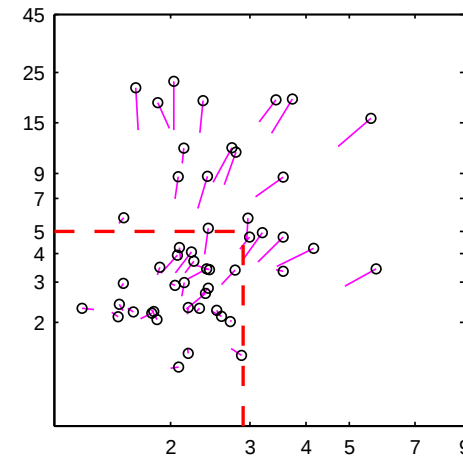
$(\Delta \bar{\epsilon}_b, \Delta \bar{\epsilon}_a)$



(d) E, F, S, ~~C~~
(+0.15, +0.07)



(e) E, ~~F~~, ~~S~~, ~~C~~
(+2.13, +2.23)

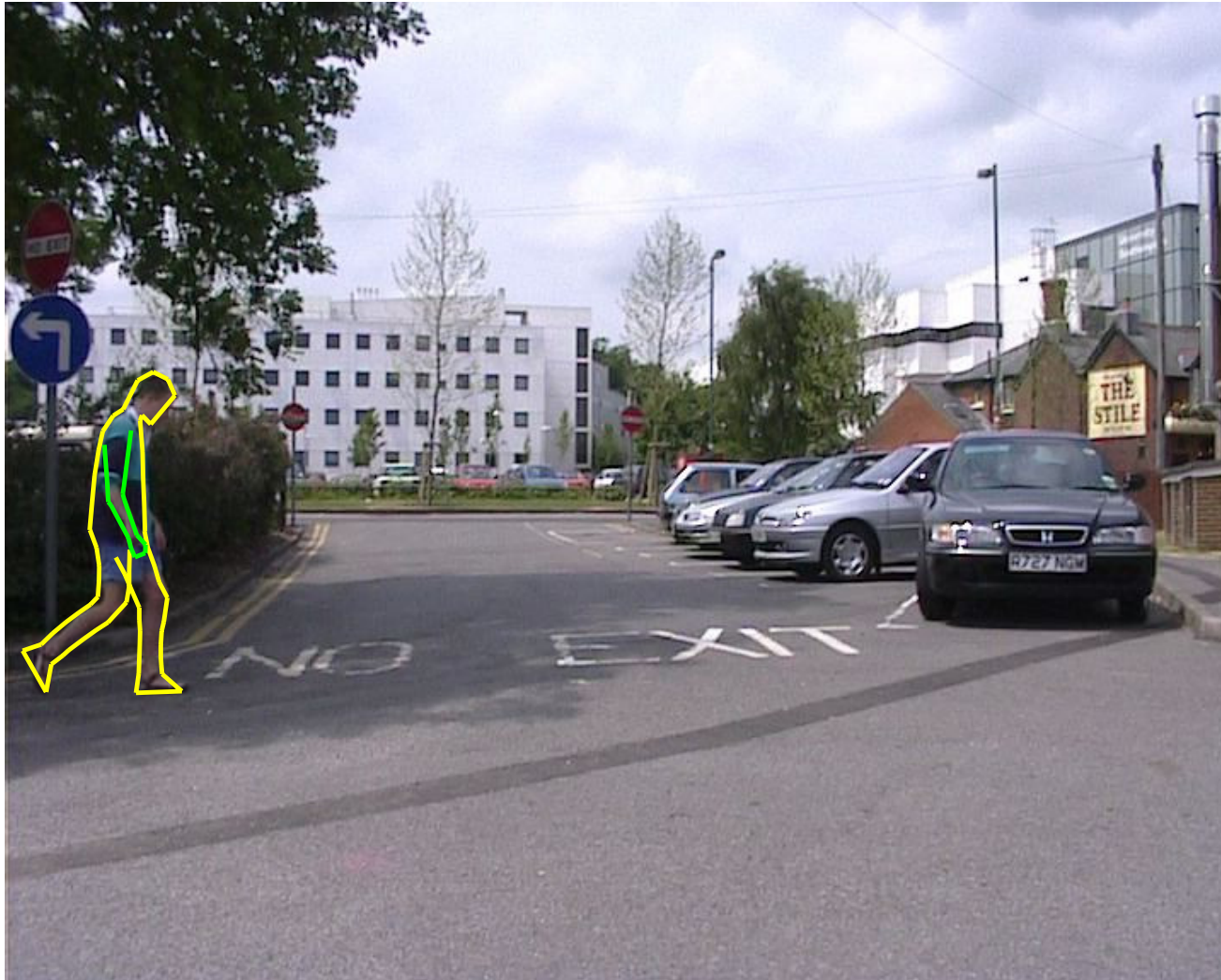


(f) ~~E~~, F, ~~S~~, ~~C~~
(+0.66, +4.07)

Edge
Foreground
Skin
Consistency



Performance on Video Sequences



01
02
03
04
05
06
07
08
09
10

Plotted are the posterior means.
Each frame is matched **independently**.

Summary

Contributions

- Novel Prob. Representation of Body Shapes
- Global Articulation + *Local Deformation*
- Multiple-Cue Integration
- Efficient Spatial Inference via Sequential MC

Work in progress

- motion and dynamics
- multiple viewpoints

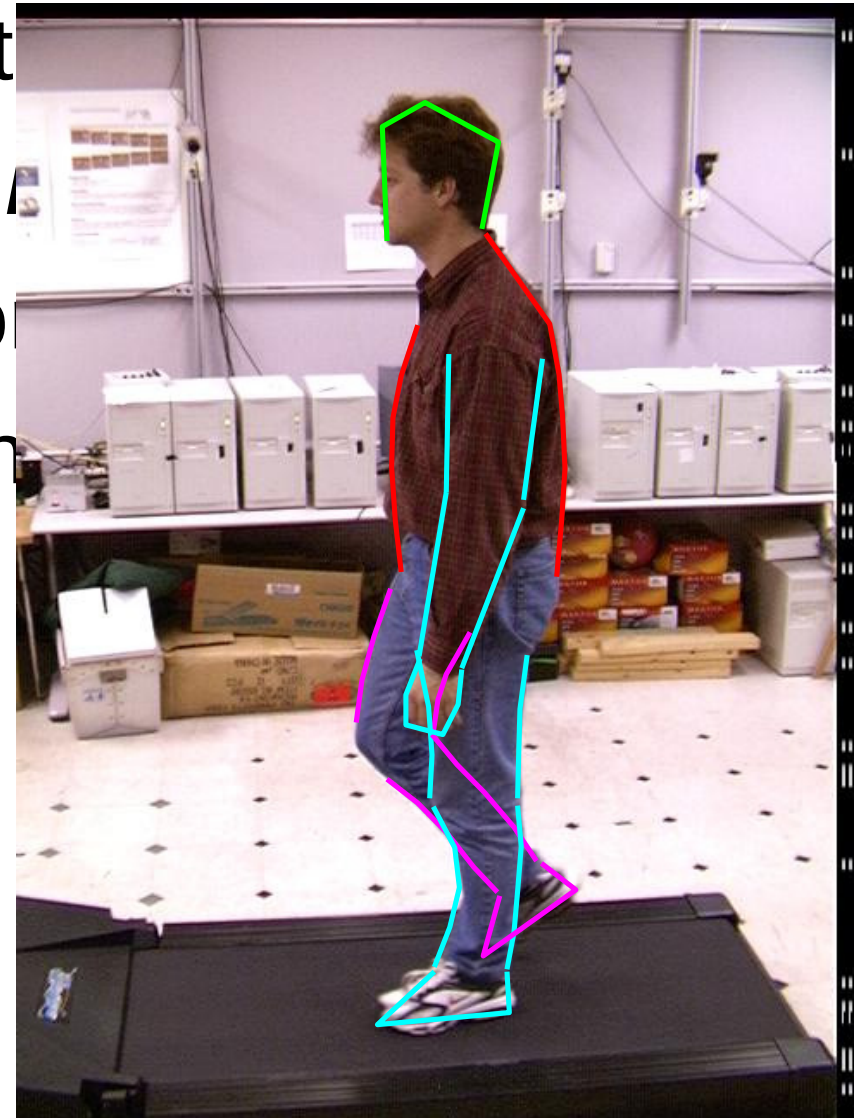
Summary

Contributions

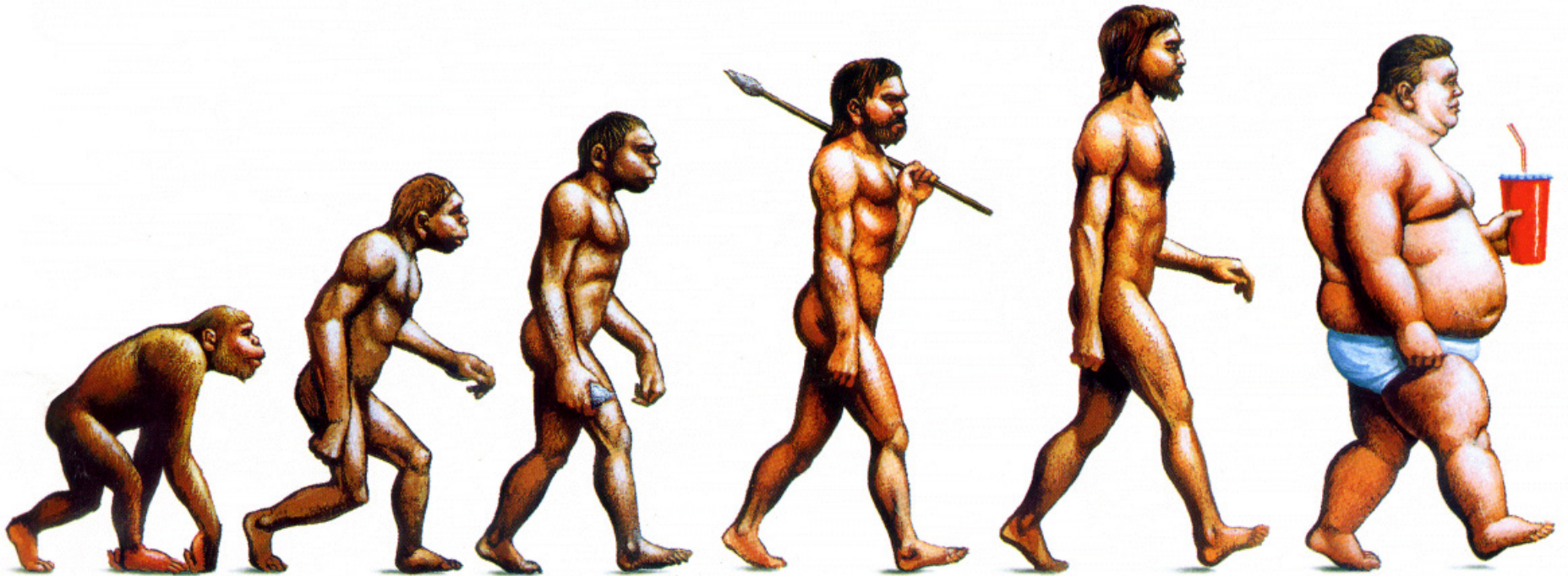
- Novel Prob. Represent
- Global Articulation + A
- Multiple-Cue Integration
- Efficient Spatial Inferen

Work in progress

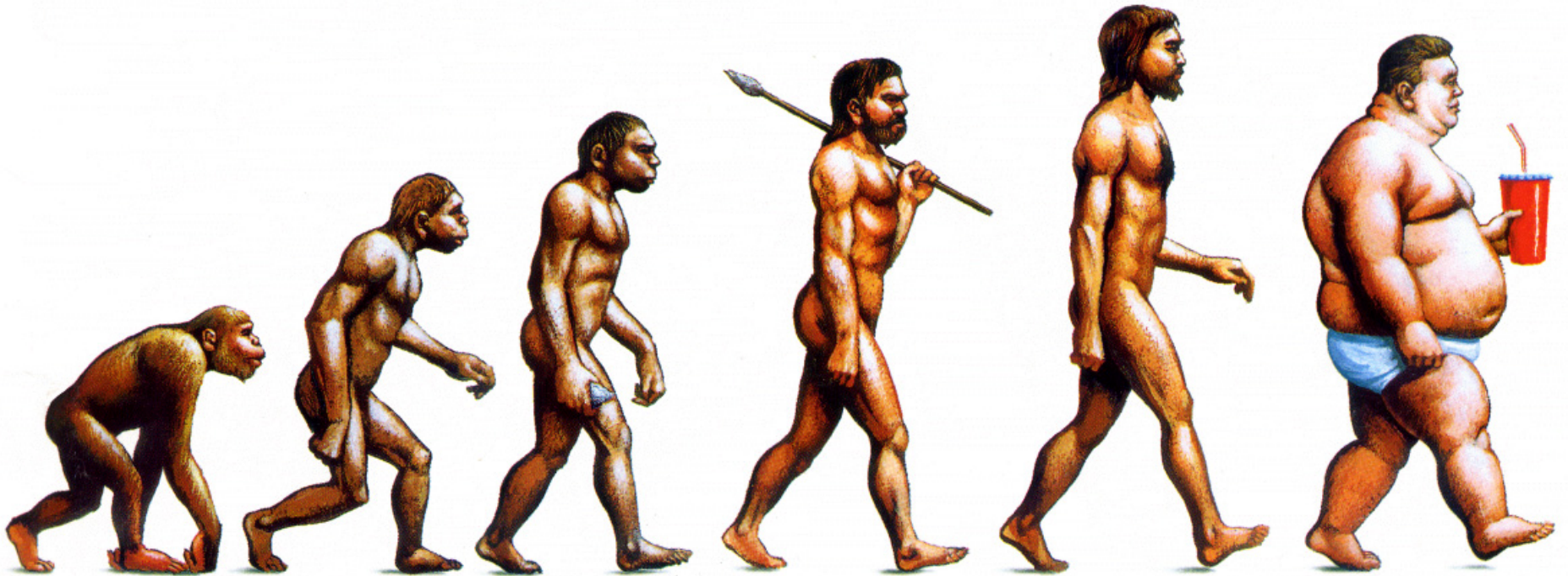
- motion and dynamics
- multiple viewpoints



The shape of things to come ...



The shape of things to come ...



The End!