

The Power of a Leader

In the Stone Age

Stephan Holzer - MIT

Yuval Emek - Technion

Roger Wattenhofer - ETH Zürich

2nd Workshop on Biological Distributed Algorithms, October 11-12, 2014 in Austin, Texas USA

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In the Stone Age

Work in progress!

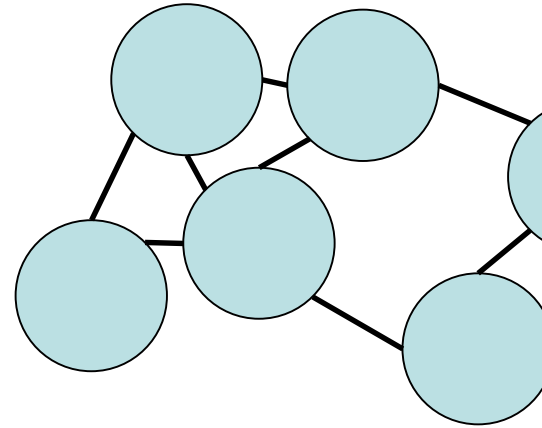
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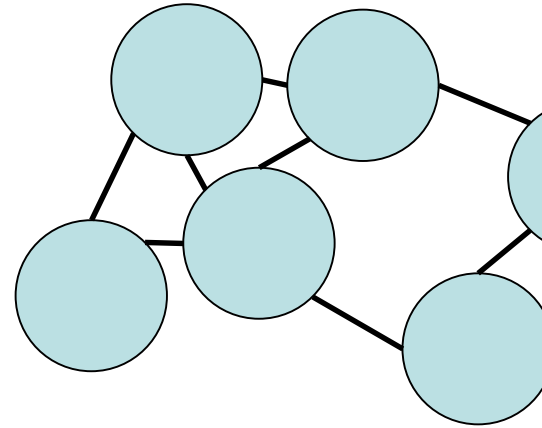
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Stone Age Model of Distributed Computing

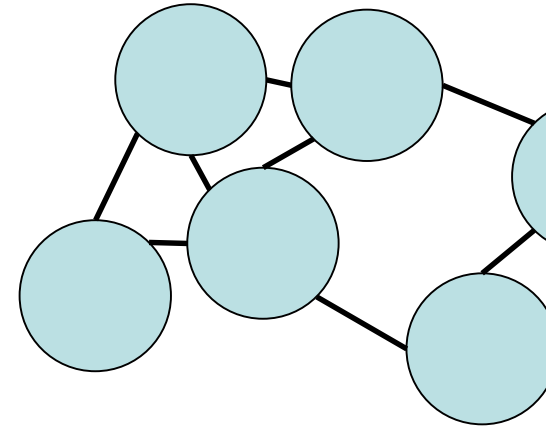
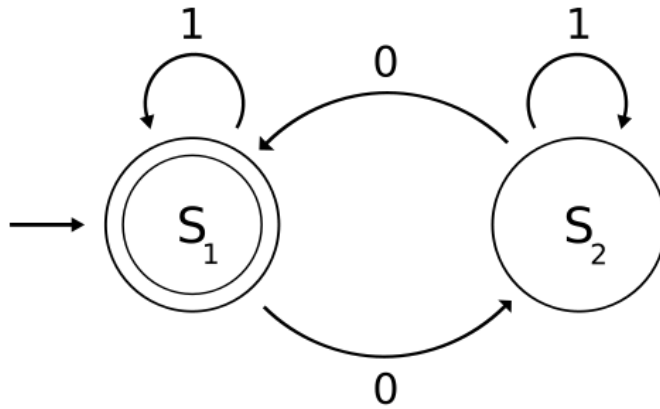


Computational Power of a Cell?

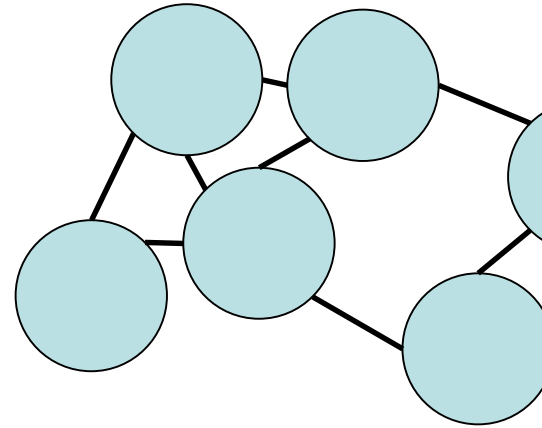


Computational Power of a Cell?

- Finite State Machine

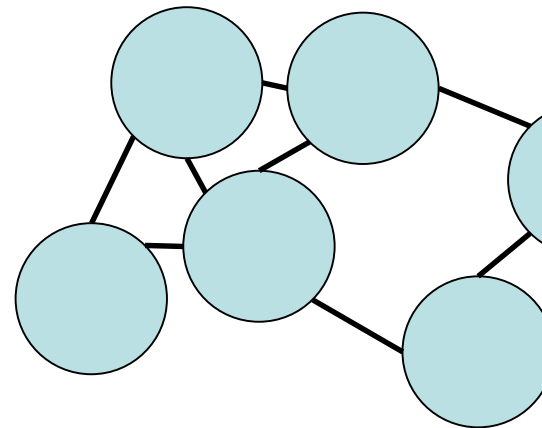


Communication?



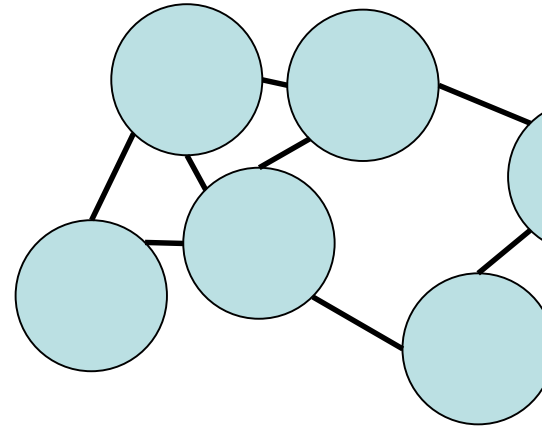
Communication?

- Transmissions:
 - Same message delivered to all neighbors
- Constant size message
- Port for each neighbor
 - Stores the last message delivered



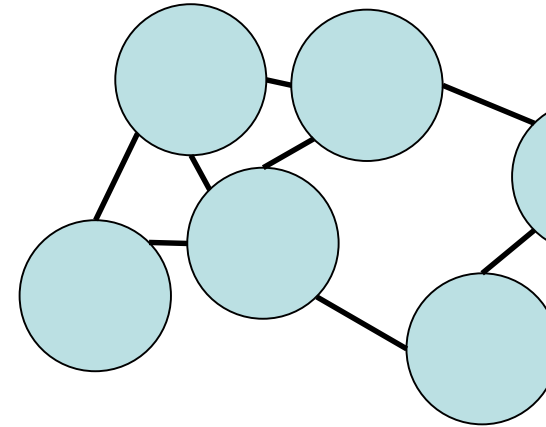
Communication?

- Transmissions:
 - Same message delivered to all neighbors
- Constant size message
- Port for each neighbor
 - Stores the last message delivered
- Can detect if 0, 1 or 2+ ports store message m
- FSM changes state based on this
sends message based on state



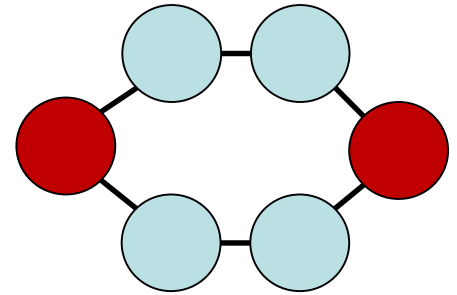
Stone Age Model of Distributed Computing

- All nodes run the same FSM
 - (random)
- Anonymous
- Weak communication
- Fully asynchronous
- Arbitrary network topology
 - (unknown)
- All features of the protocol are constant!



What is known?

- Can be synchronized
- Cannot elect a leader
- Cannot compute shortest paths
 - No Minimum Spanning Tree or Diameter



Edsger W. Dijkstra:

Actually:
I CAN COMPUTE
SHORTEST PATHS!

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Actually:
I CAN COMPUTE
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**Actually:
Me too!**

• (The slime mold)

Physarum polycephalum

- Nuclei are nodes
- Tubes / plasma are edges

?

Computes the Shortest Path

Video can be found at:

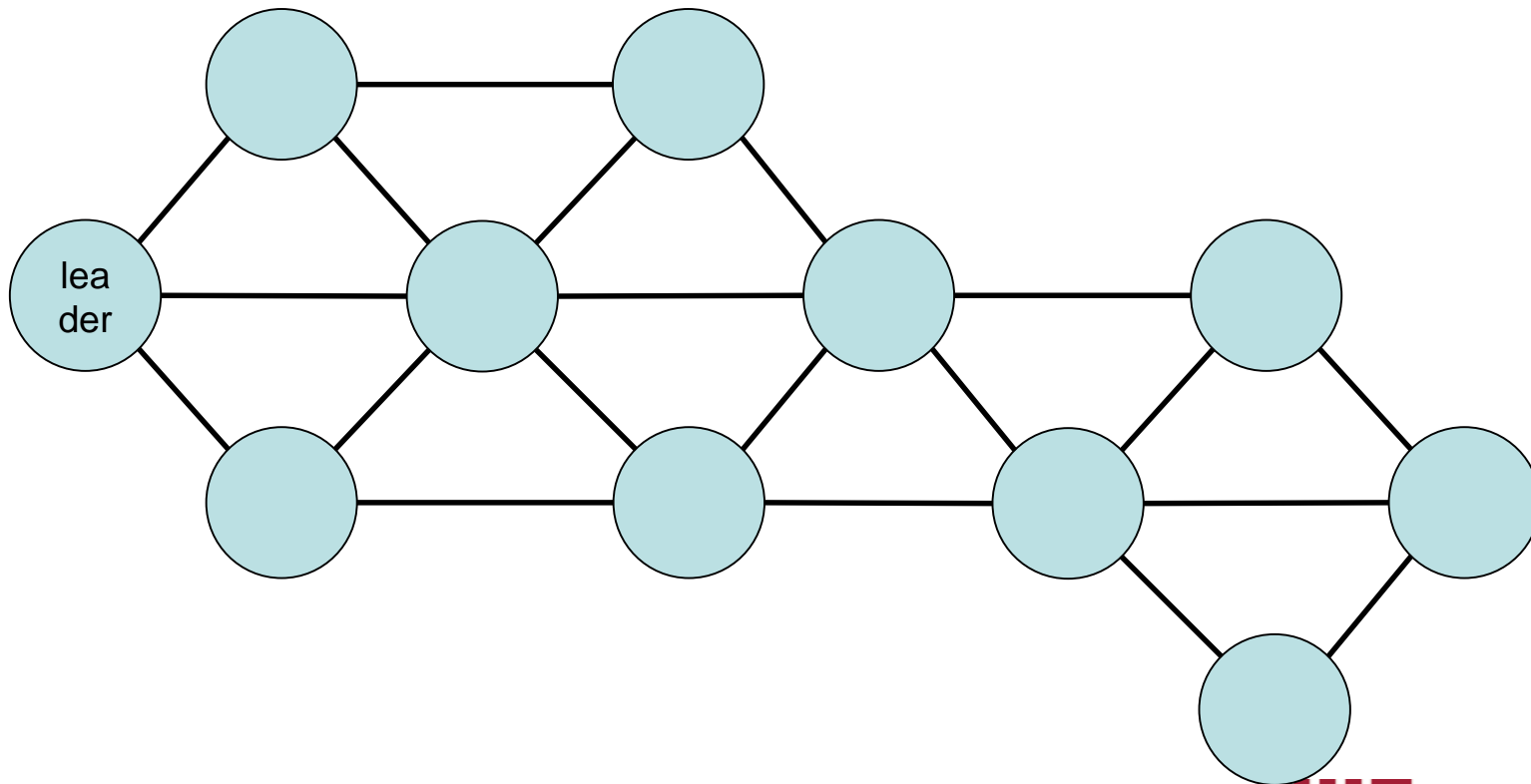
<http://www.youtube.com/watch?v=czk4xgdhdY4>

How a Leader can make a Difference!

- Symmetry is broken
- Can coordinate global computation
- E.g. select unique node at random

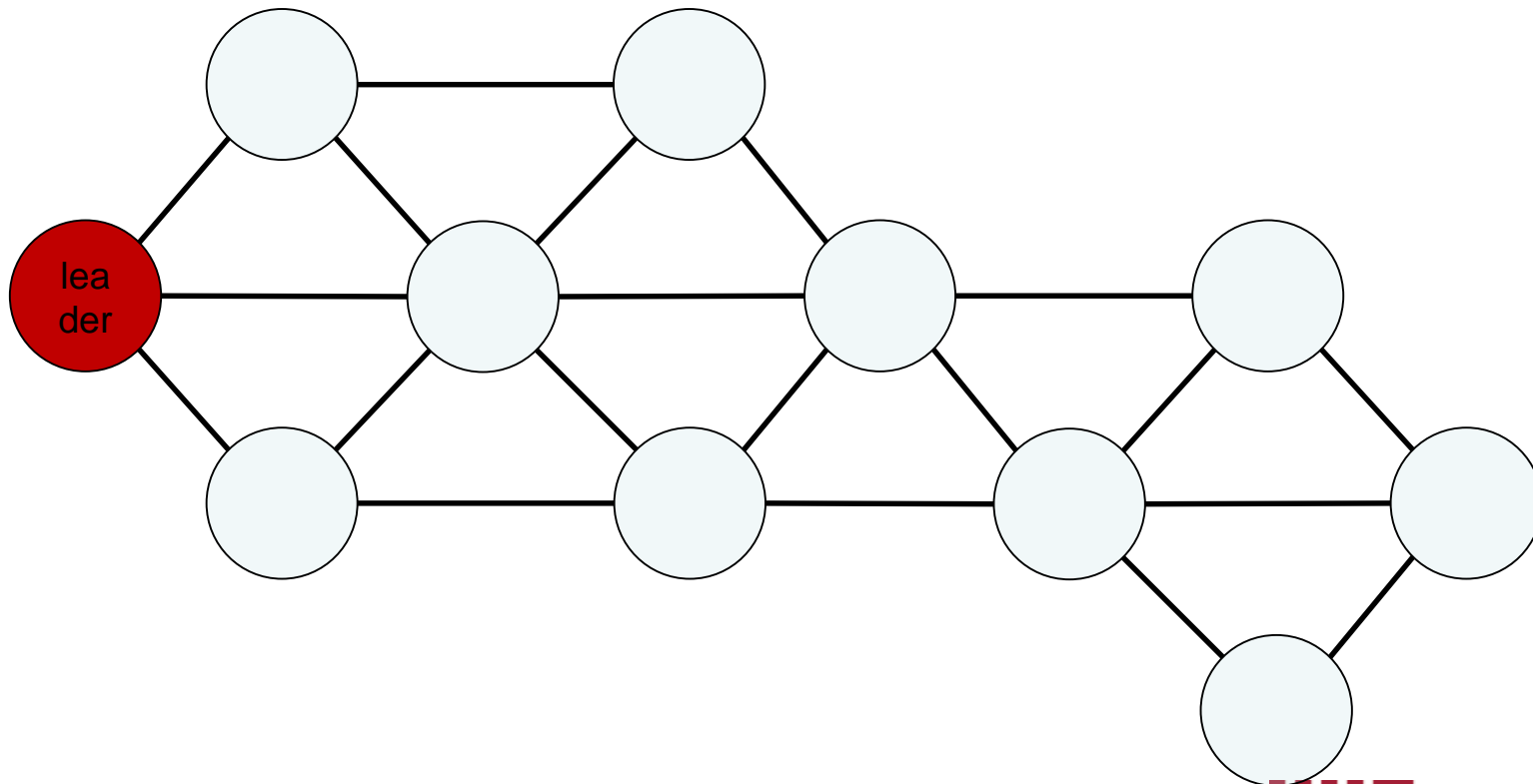
Select Unique Node at Random

- REPEAT: 1. select random neighbor
 2. $\Pr[\text{choose yourself}] = 1/2$



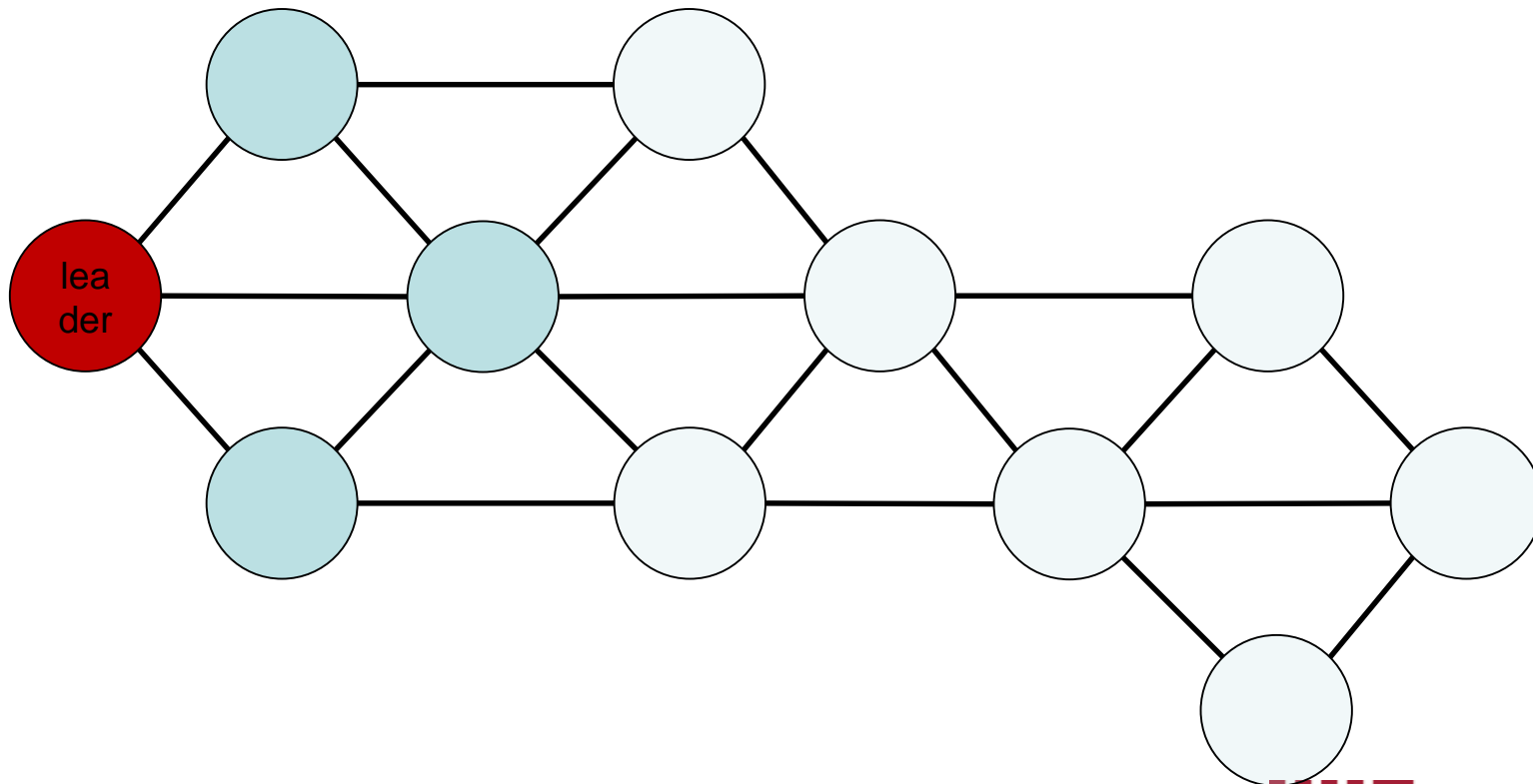
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Wait:

Transmissions:

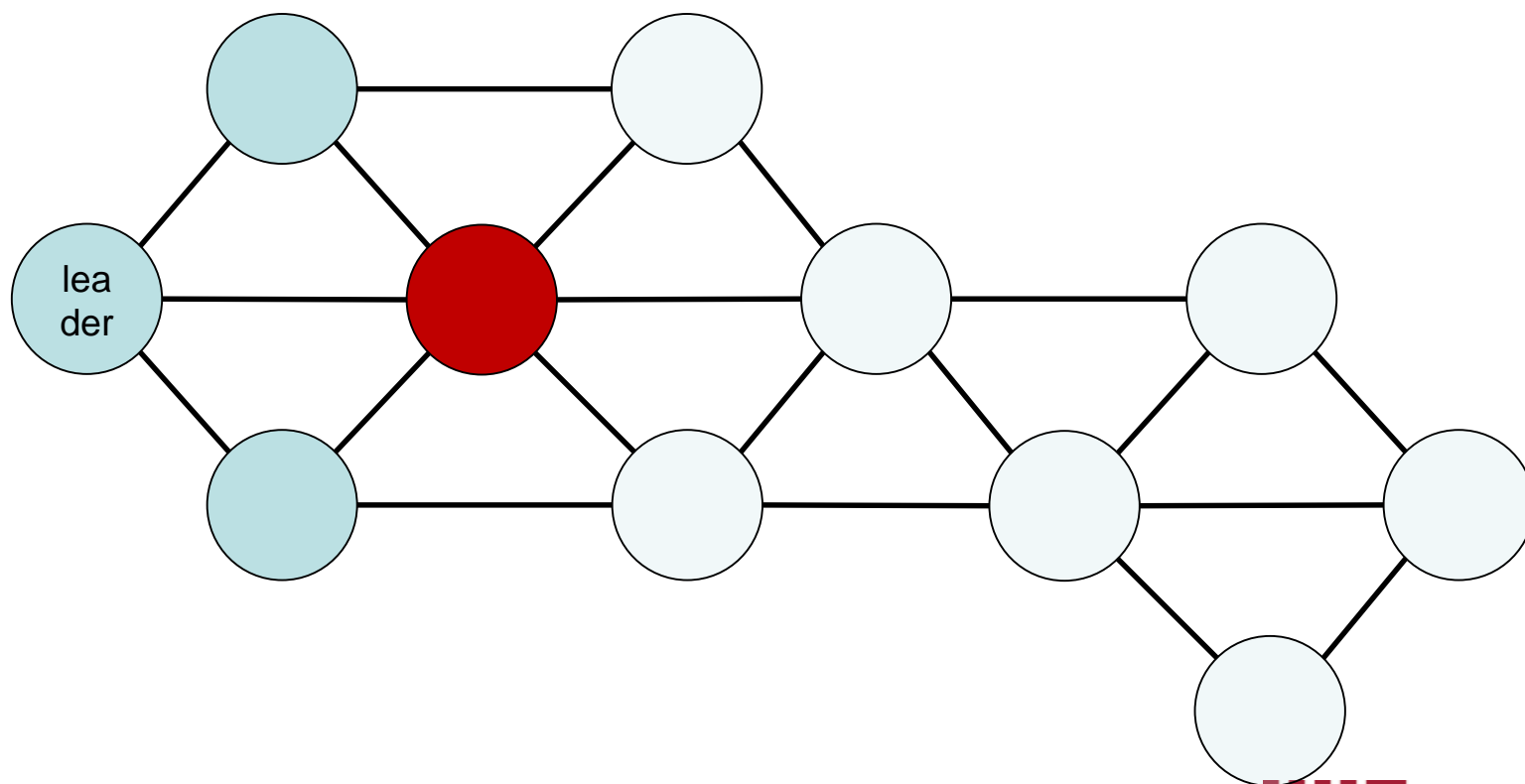
- Same message delivered to all neighbors

Solution:

- Wait until there is a neighbor in a unique state among the neighbors
- Detect this via ports
- Transmit “content of this port”

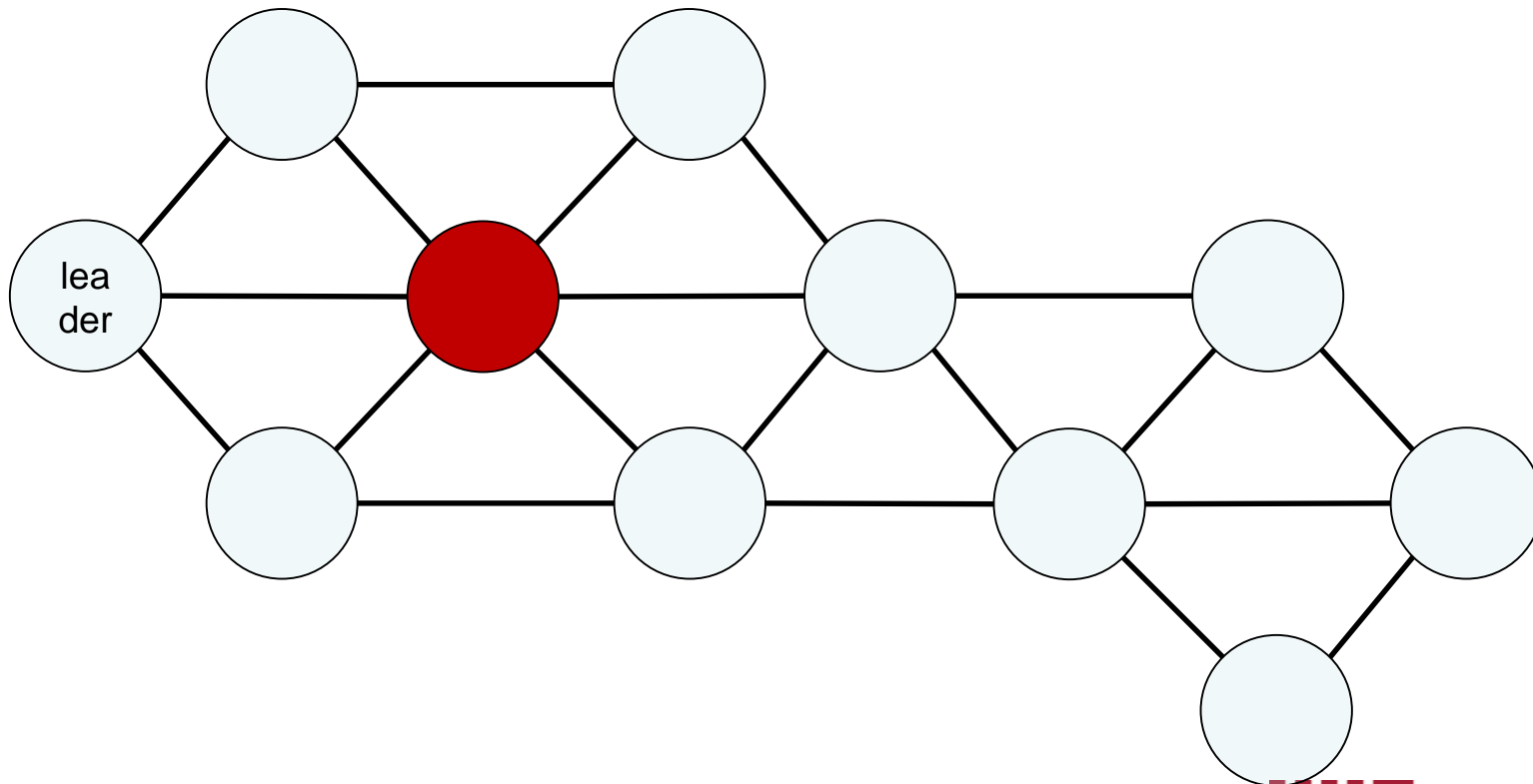
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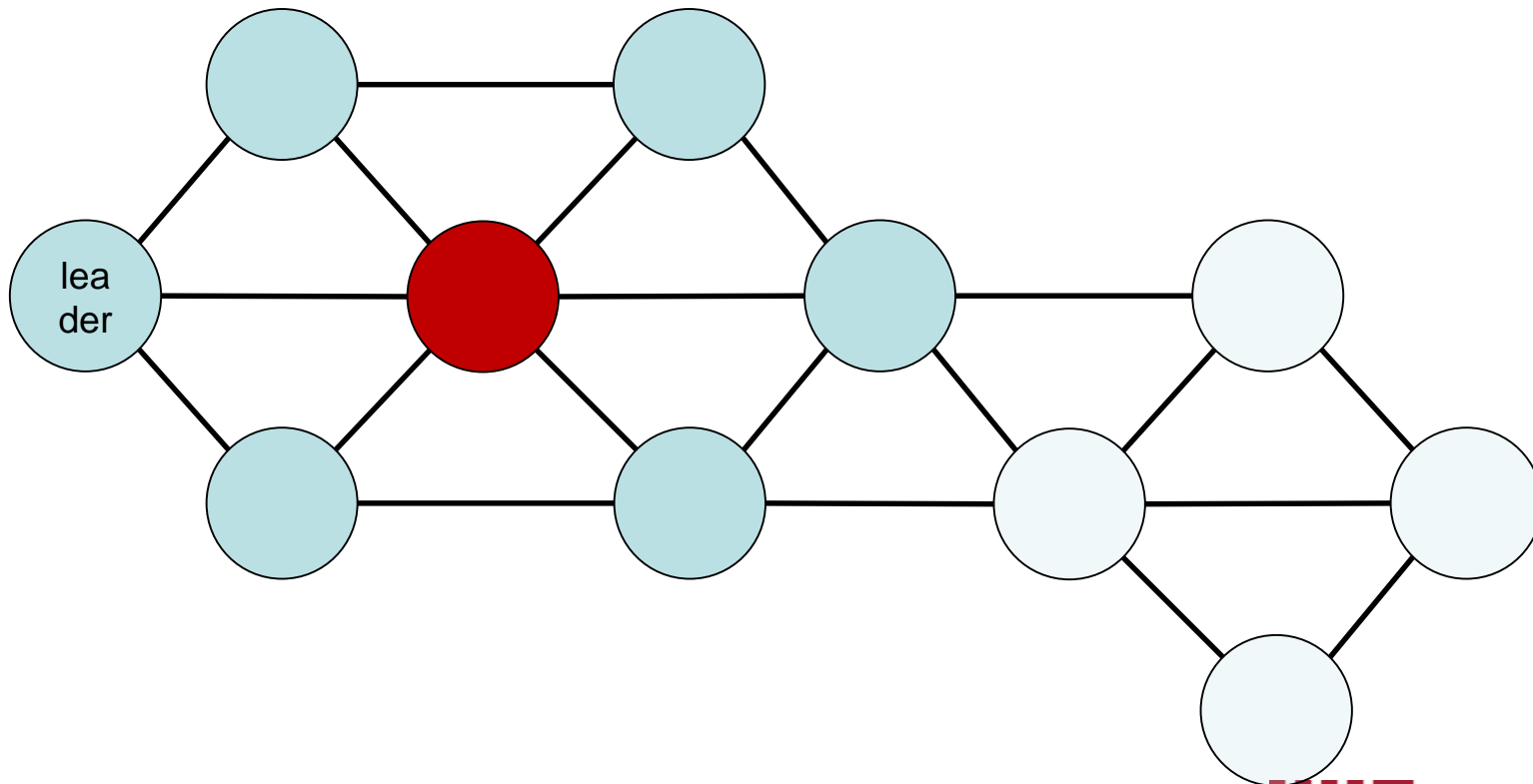
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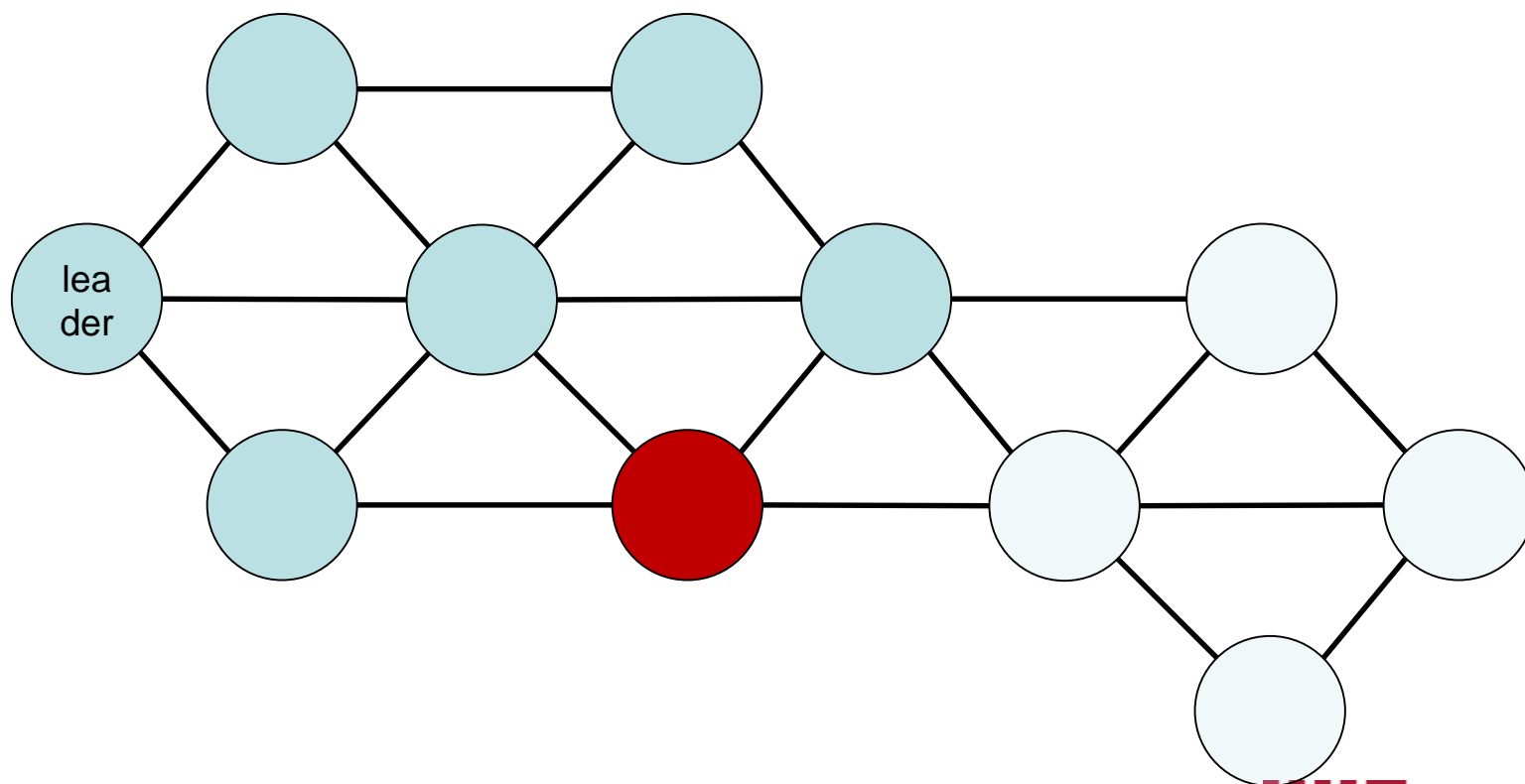
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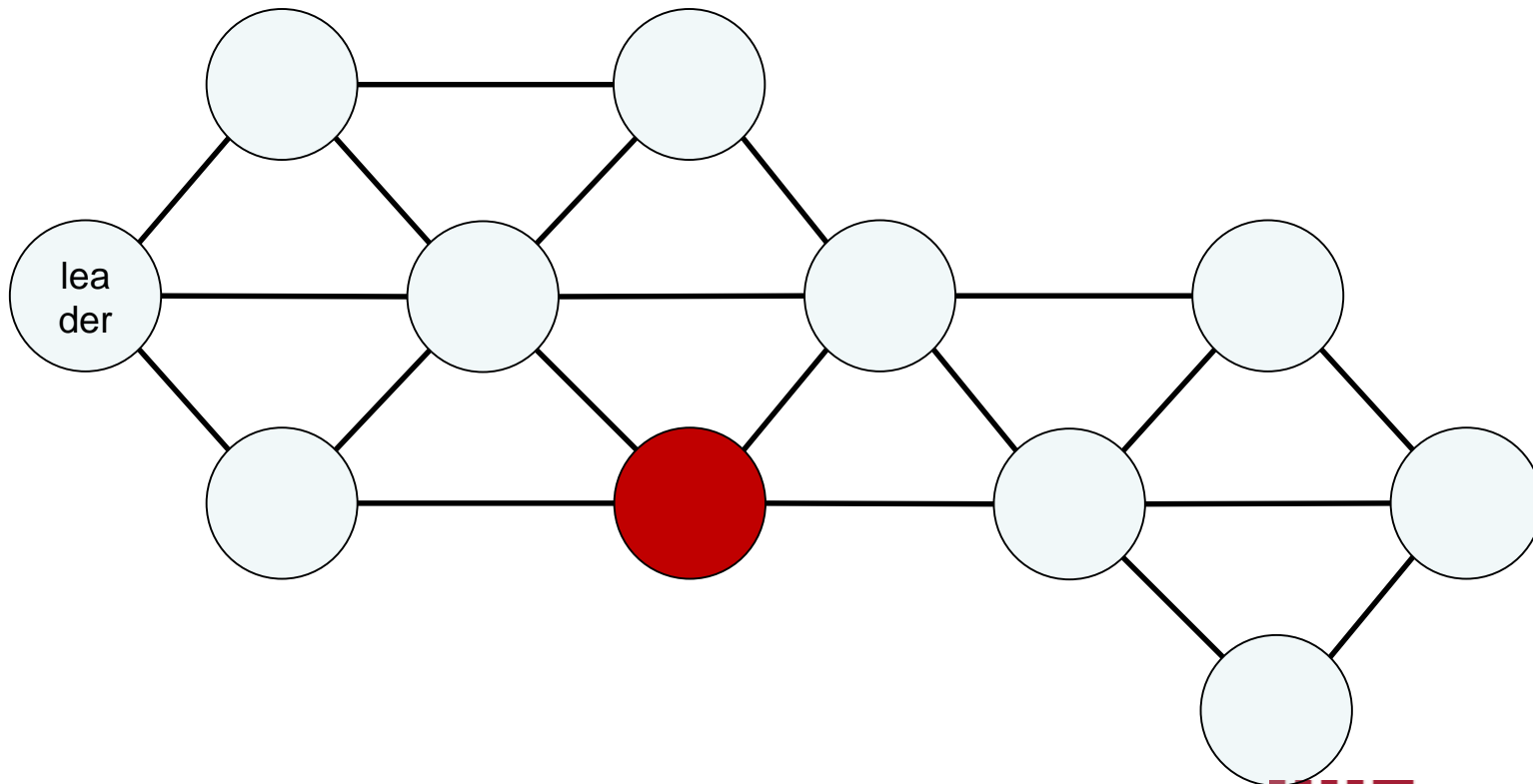
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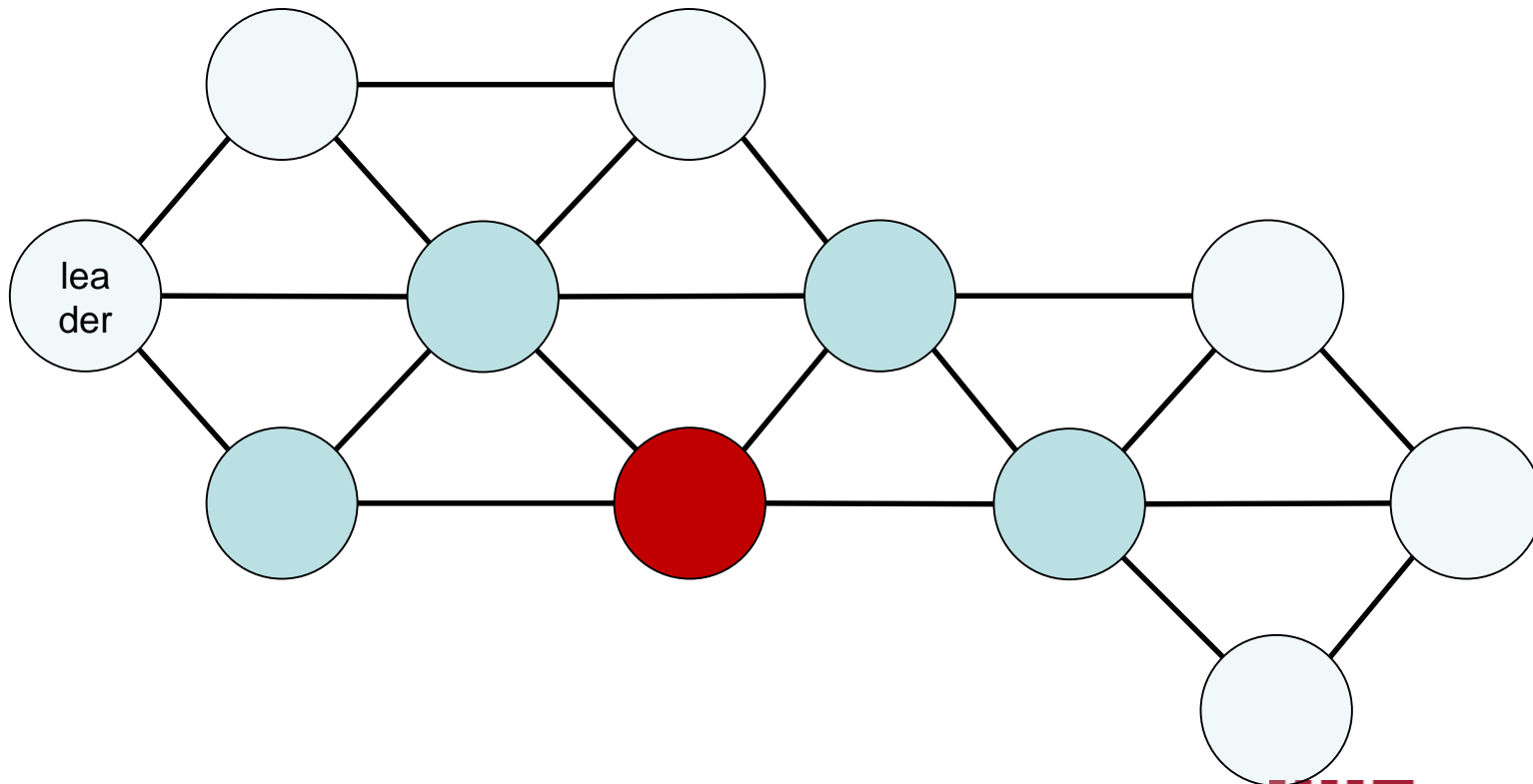
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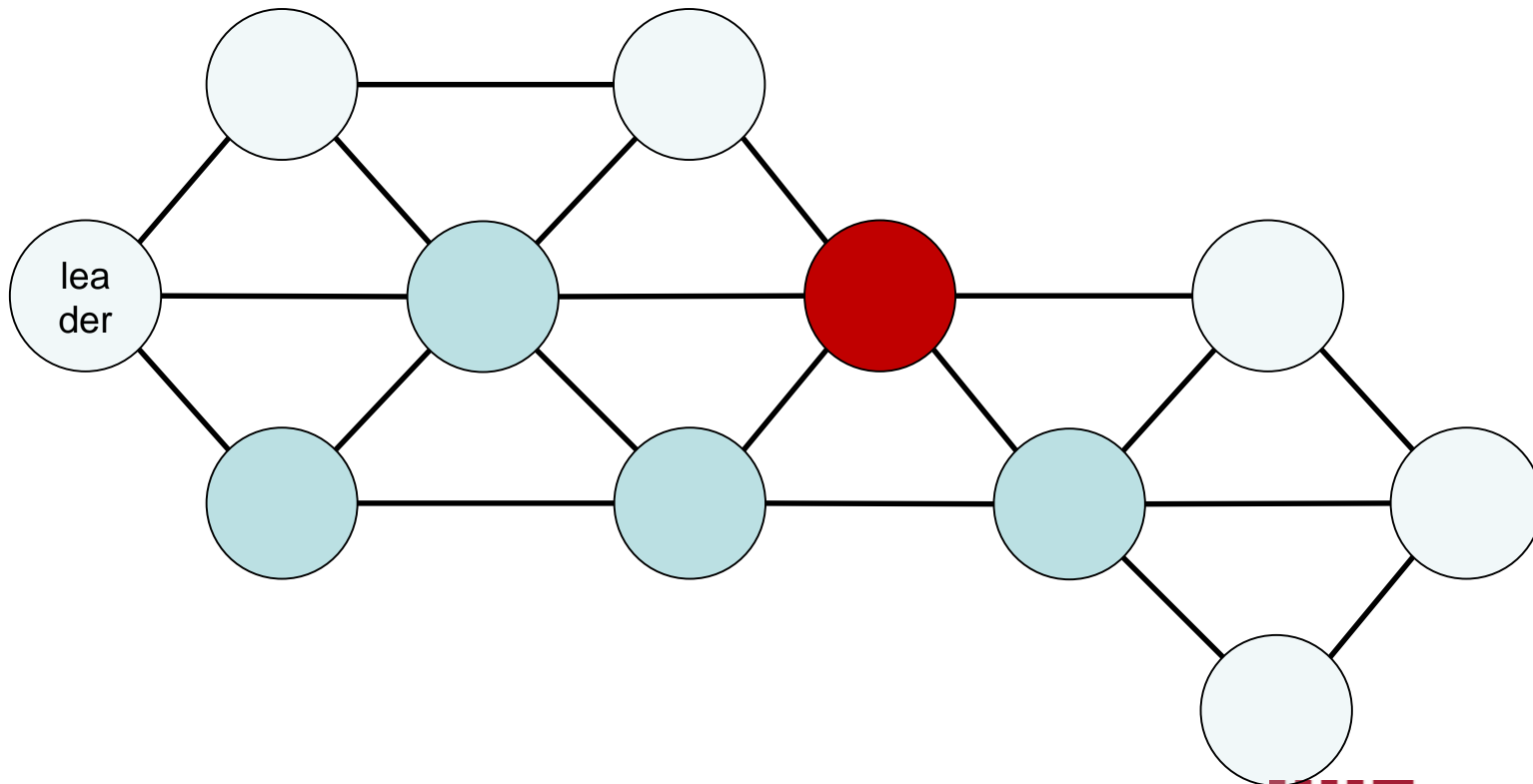
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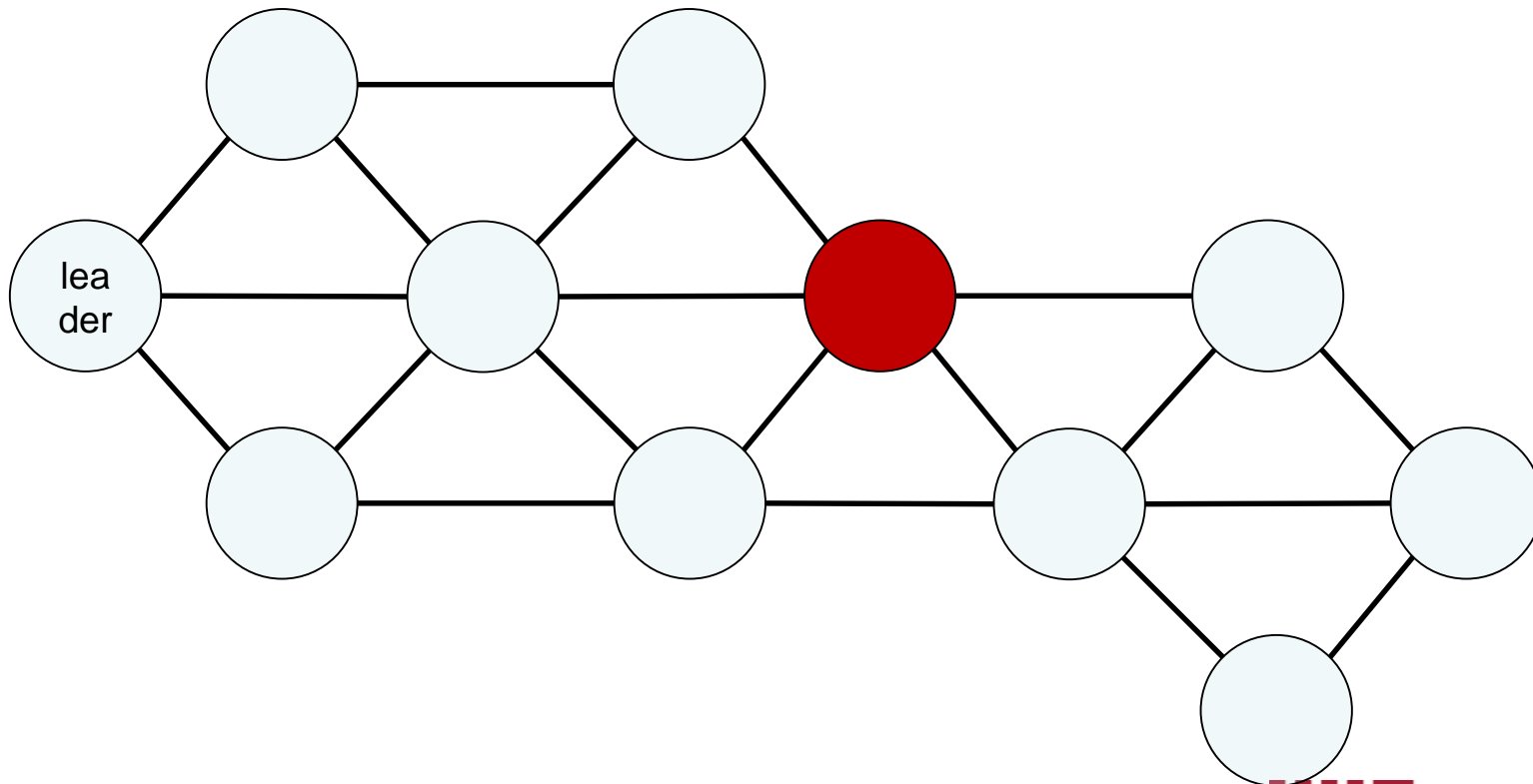
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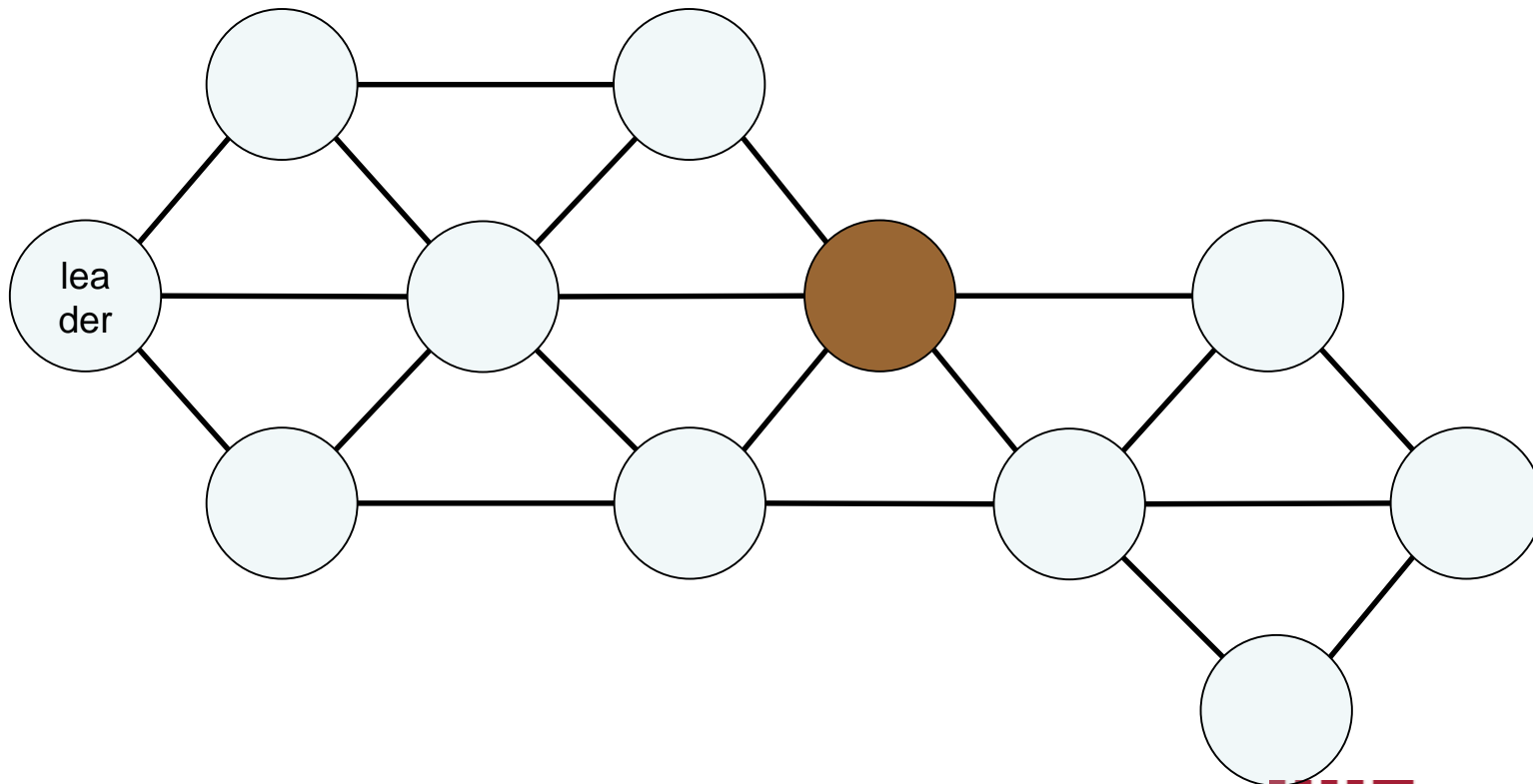
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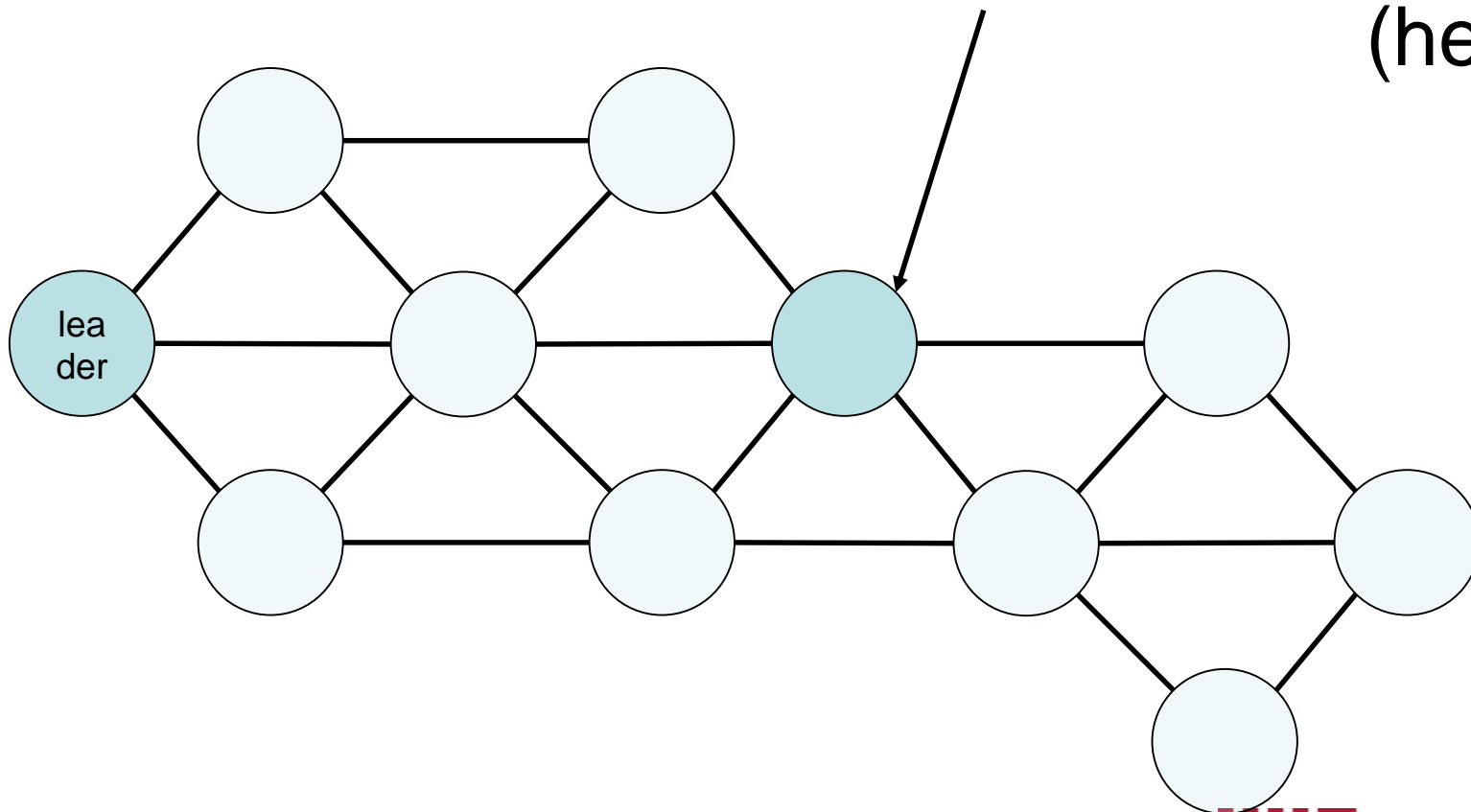


How a Leader can make a Difference!

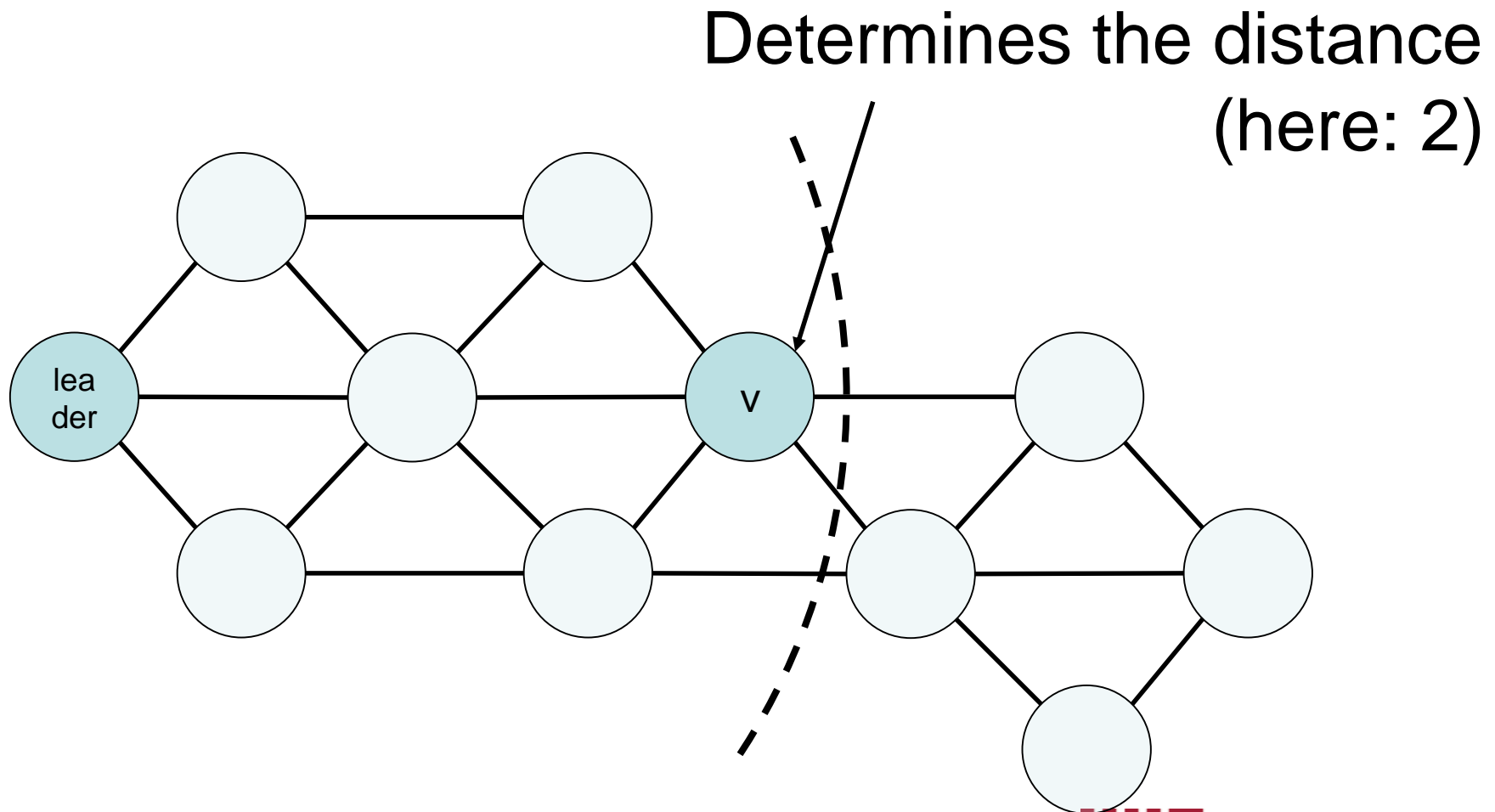
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Determines the distance
(here: 2)



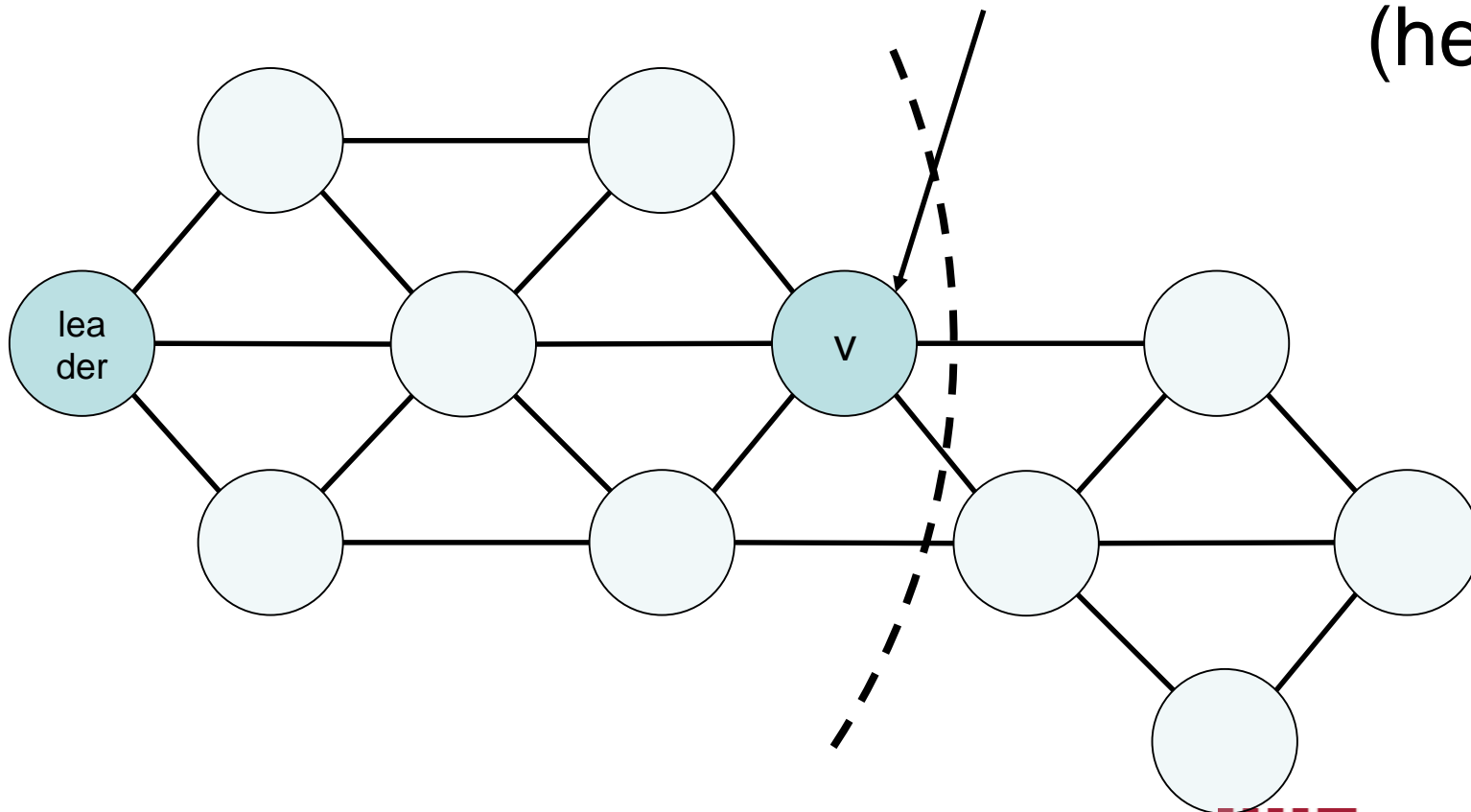
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Use ping to check properties

Determines the distance
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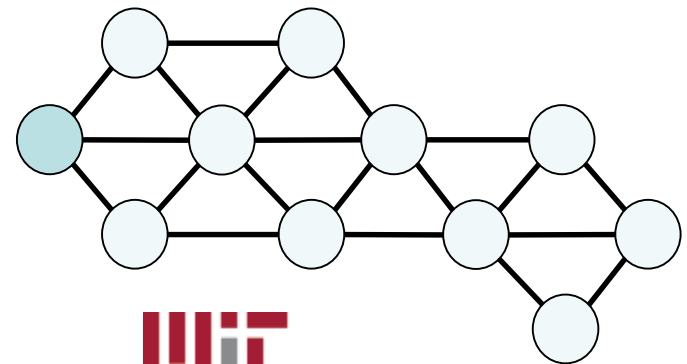
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- Iterate through all nodes (**for** $v \in V$ **do** TASK)

Iterate through all nodes (**for** $v \in V$ **do**)

$v_{max} := leader;$
while not all nodes at distance $\leq \text{dist}(leader, v_{max}) + 1$
are marked **do**
 select random node u ; // u marks itself
 if $\text{dist}(leader, u) > \text{dist}(leader, v_{max})$ **then**
 $v_{max} := u$;
 u performs TASK;

Iterate through all nodes (**for** $v \in V$ **do**)

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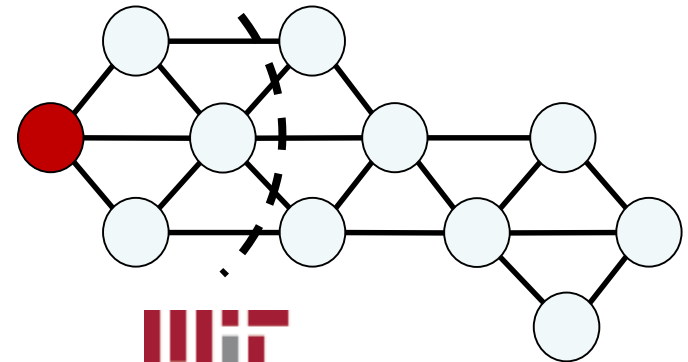
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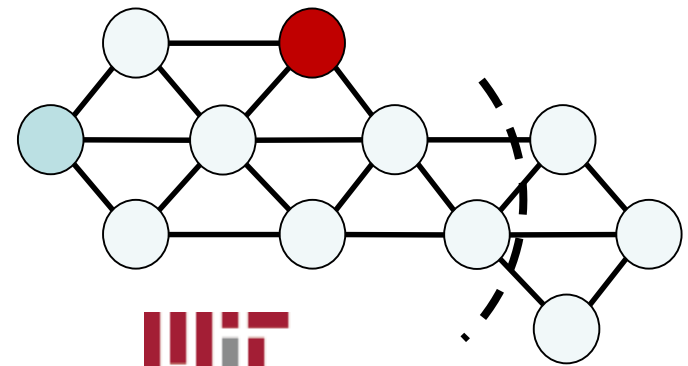
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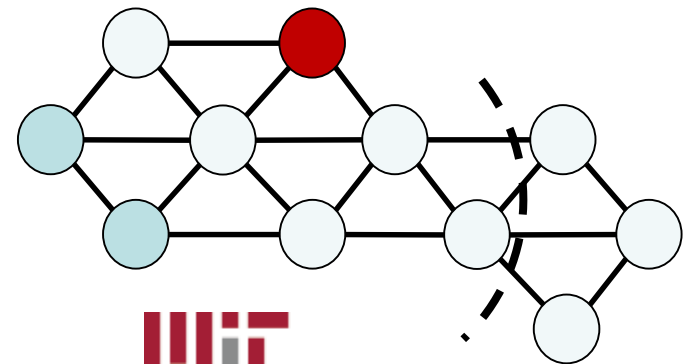
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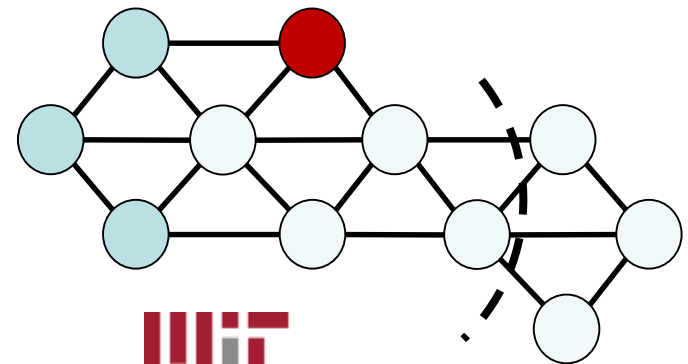
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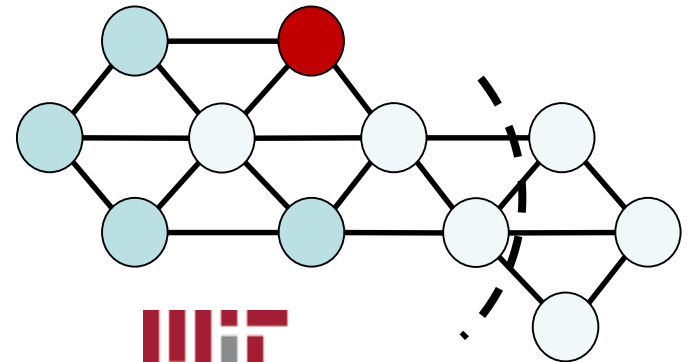
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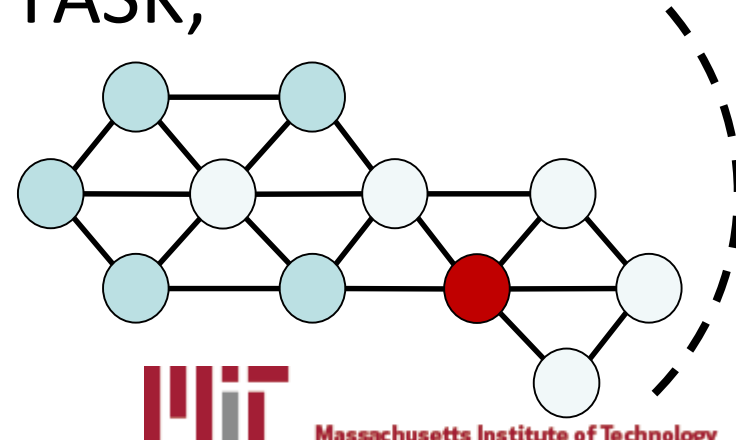
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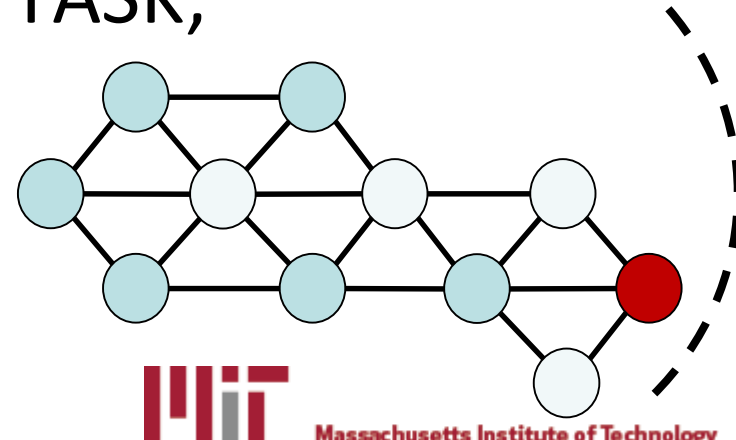
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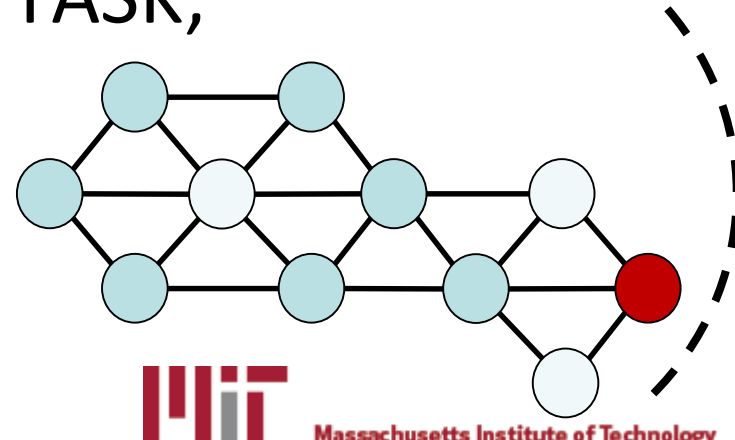
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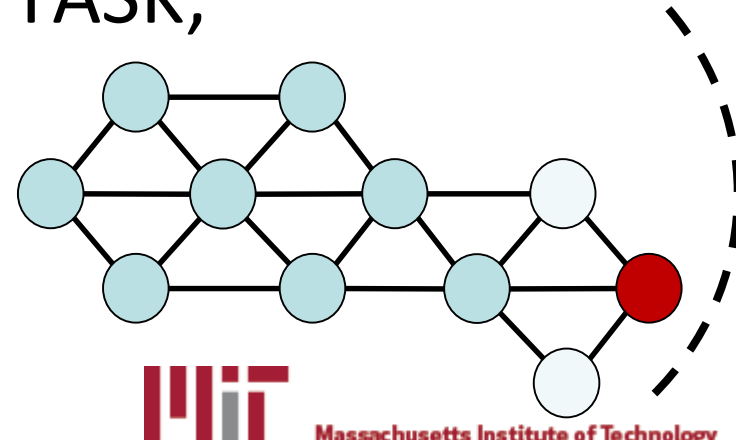
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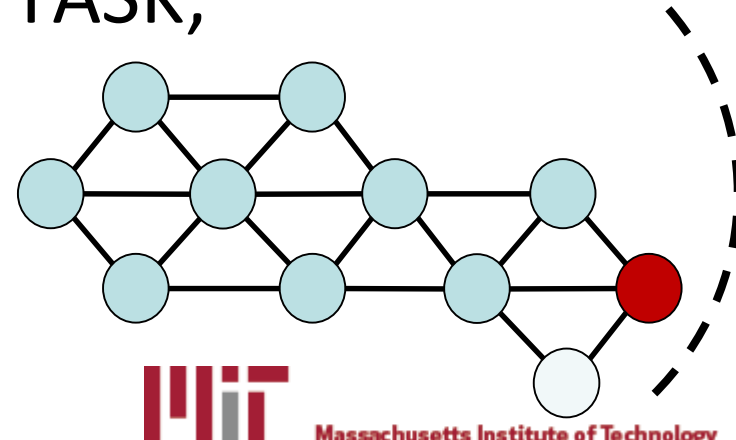
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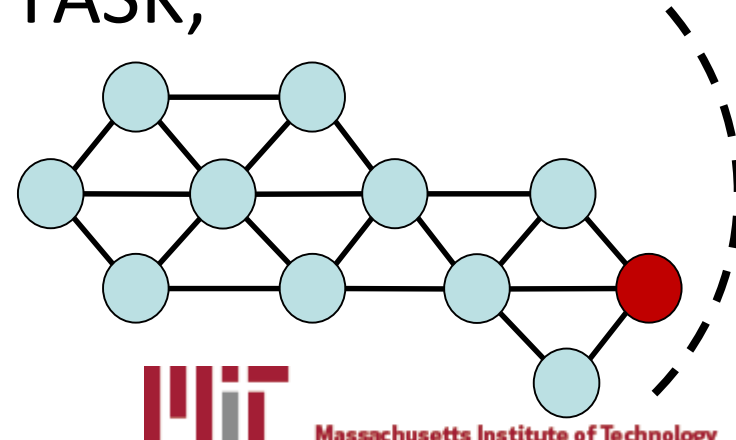
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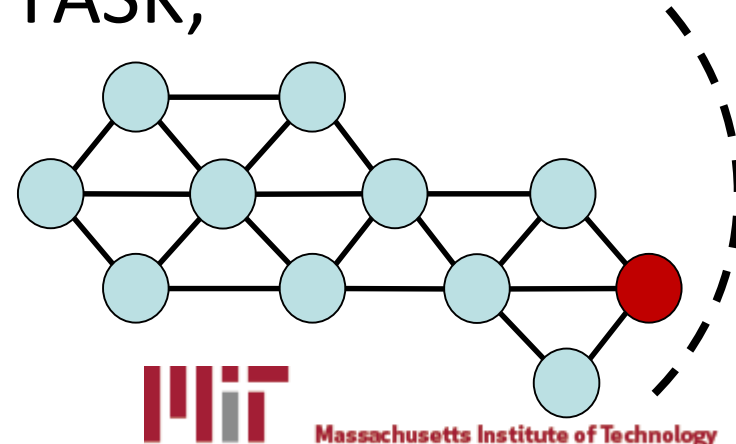
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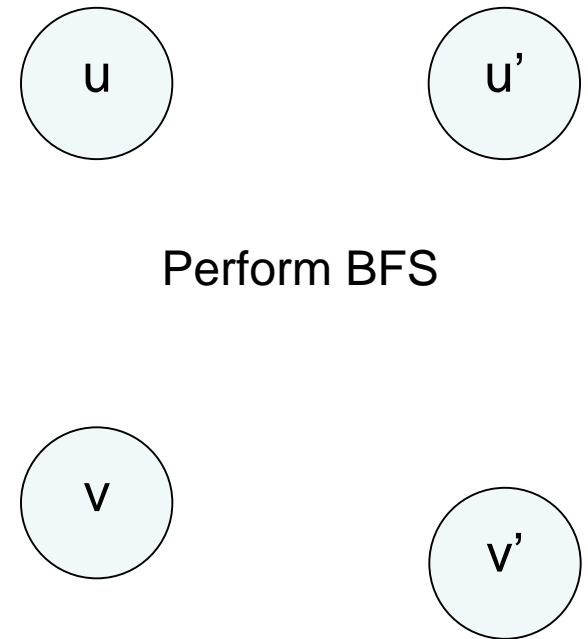
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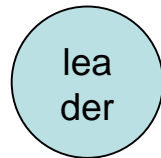
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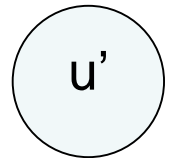
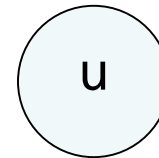
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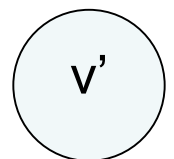
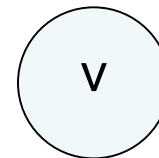
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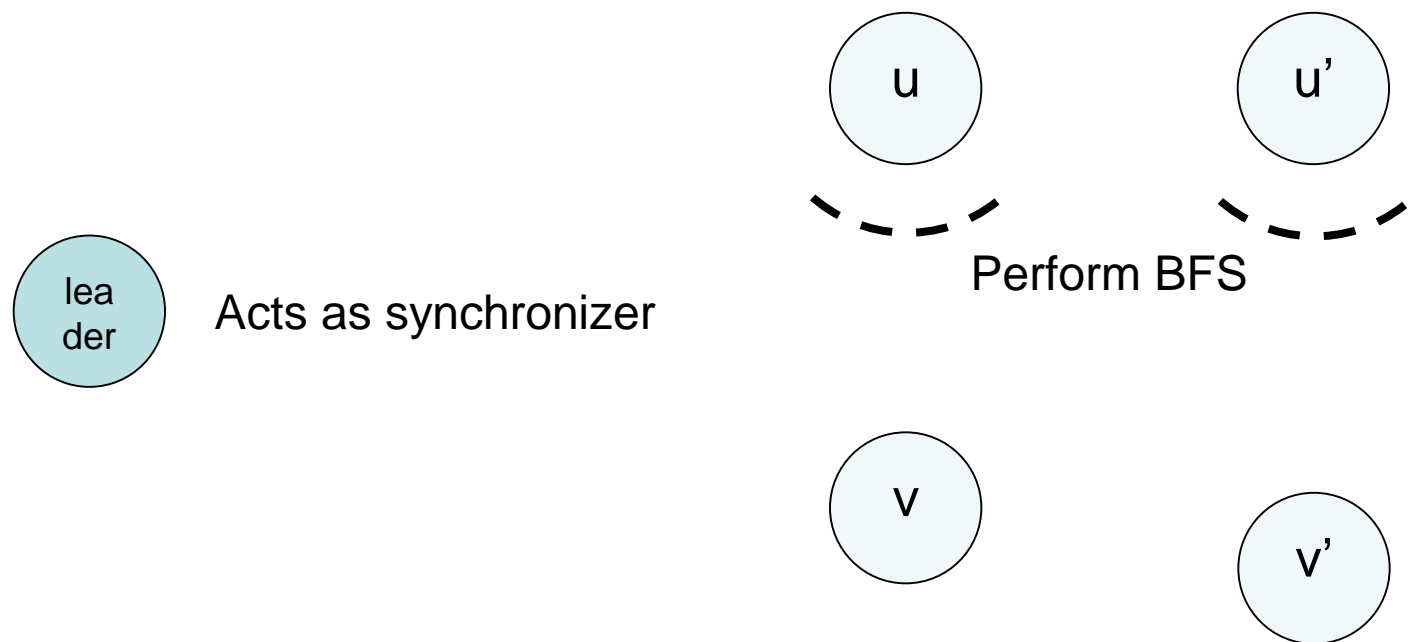
Acts as synchronizer



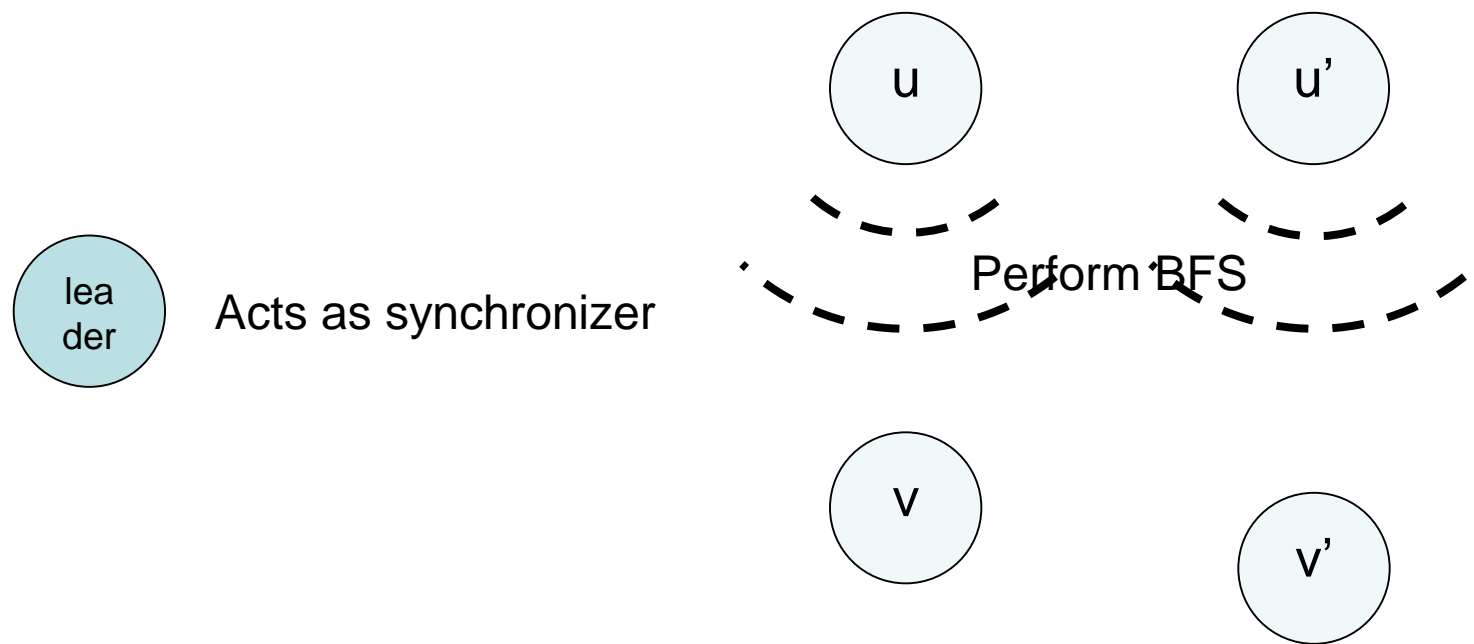
Perform BFS



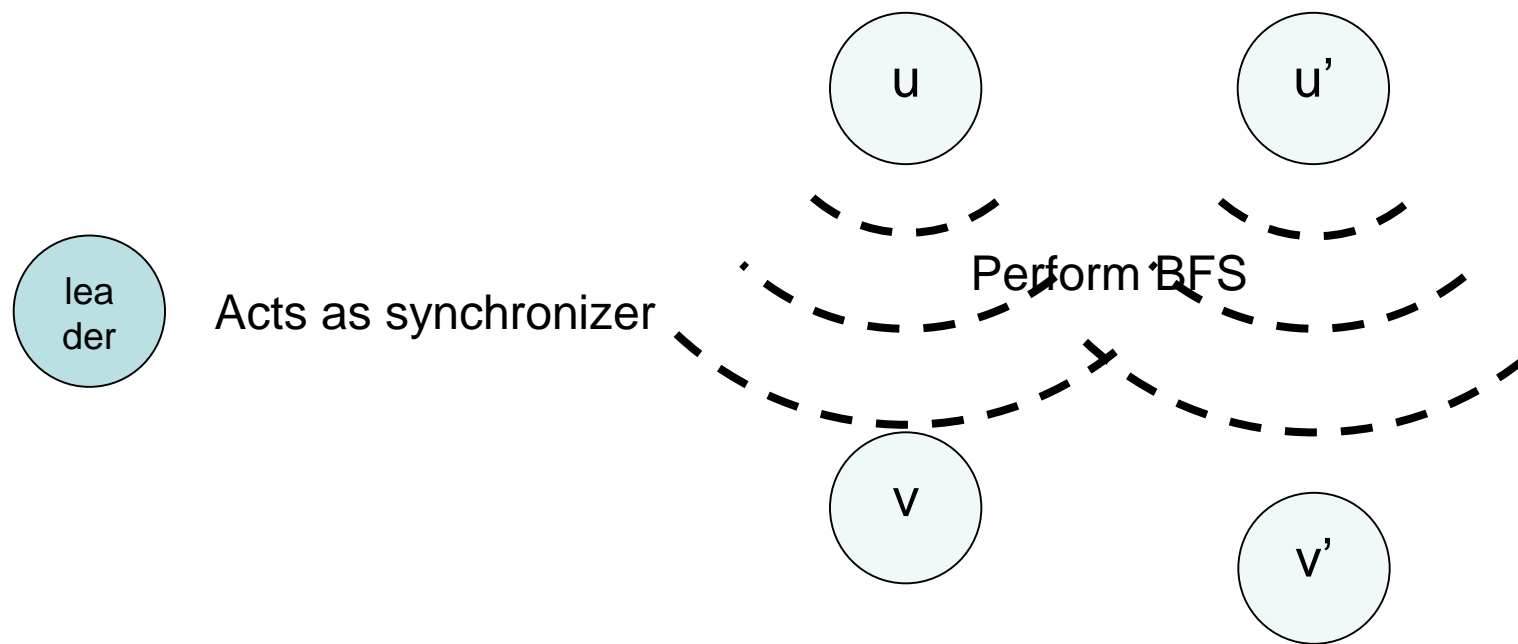
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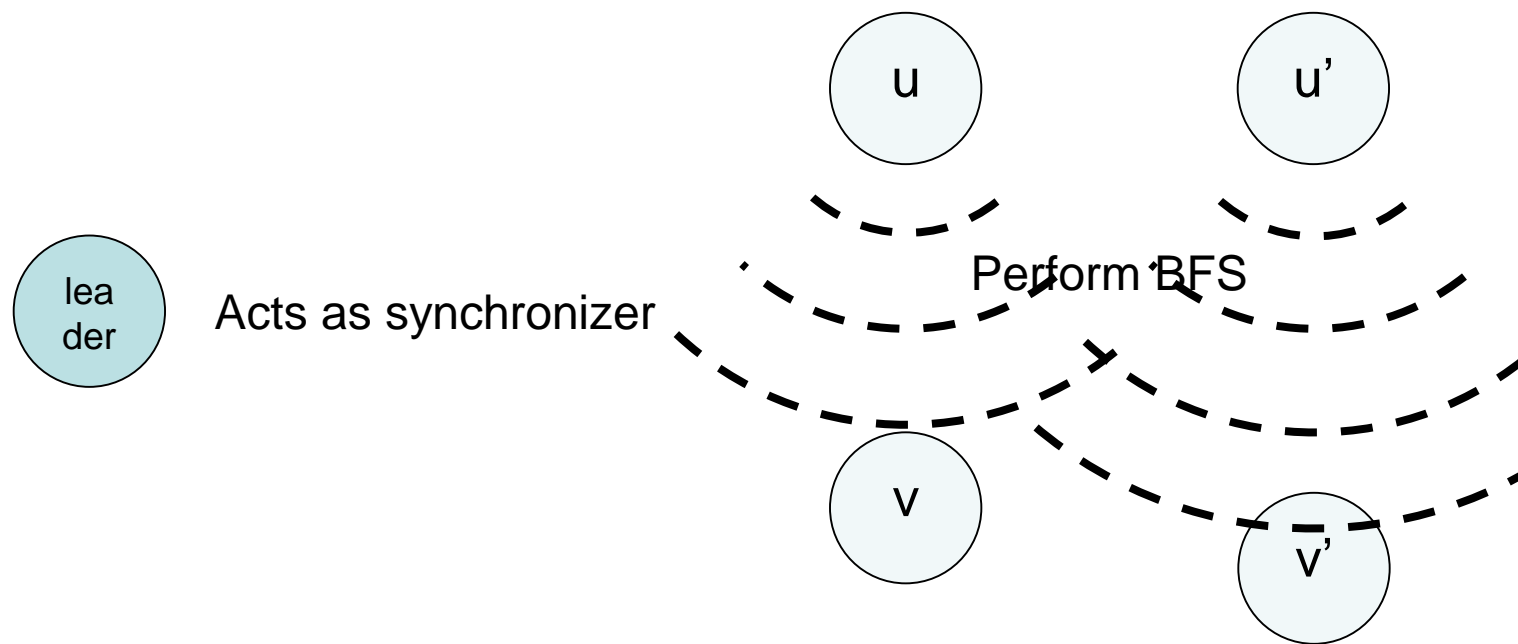
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- Constant combination of all these

Shortest Path

INPUT: nodes u, v (assume v is leader)

While $u \neq v$ **do**

u marks itself to be on the shortest path

for each neighbor w of u **do**

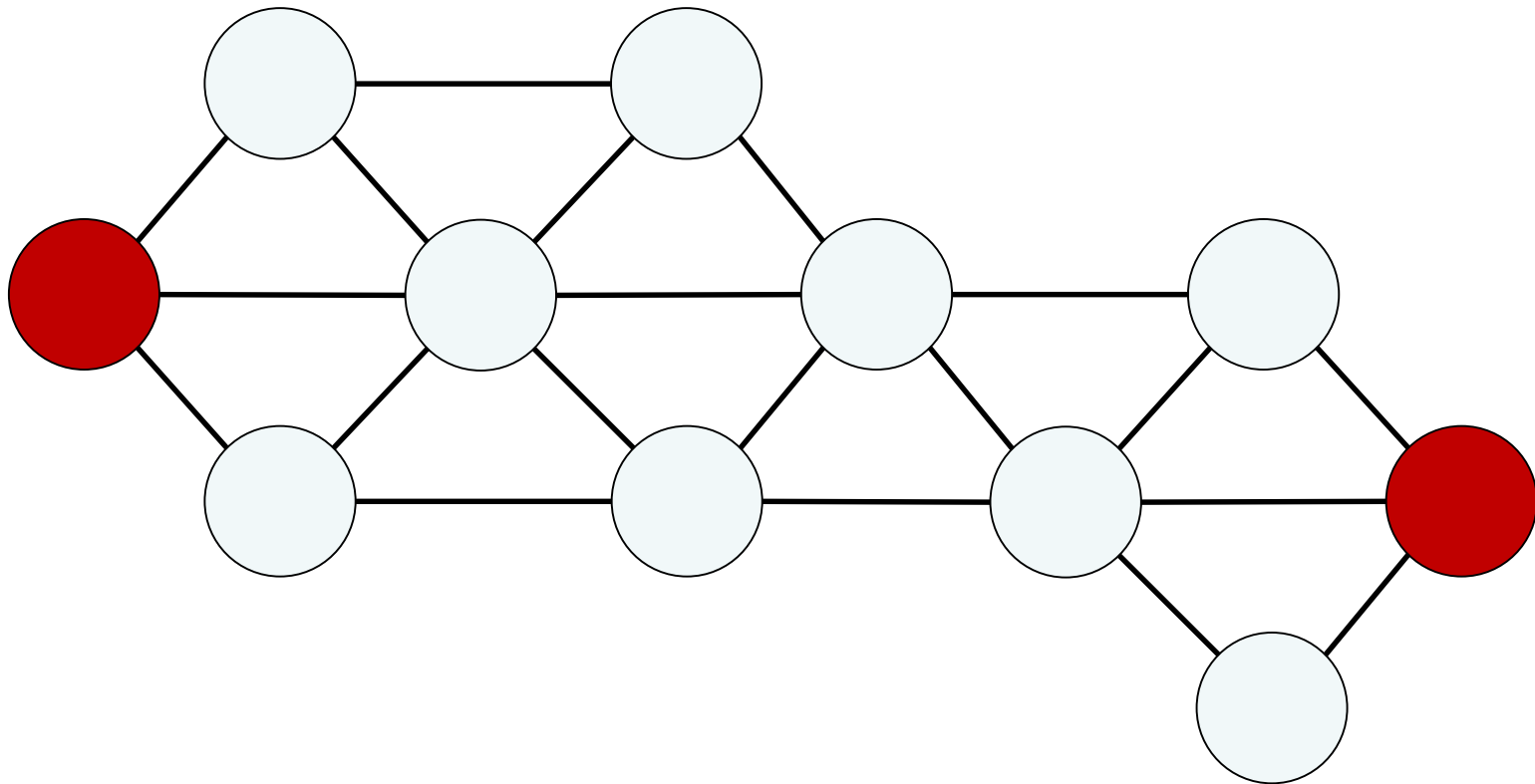
if $\text{dist}(w, v) < \text{dist}(u, v)$ **then**

$u := w;$

OUTPUT: marked nodes

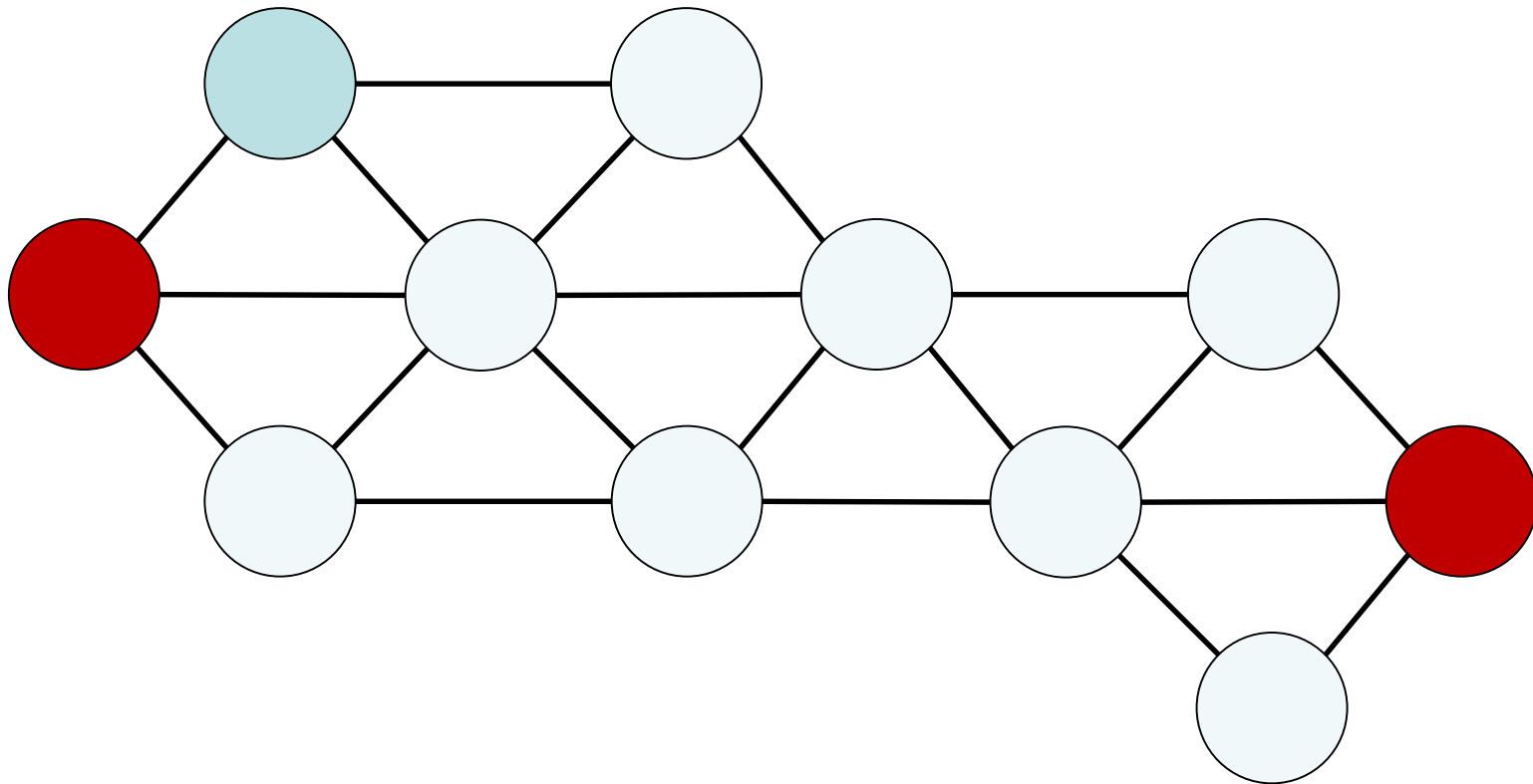
Shortest Path

- Example:



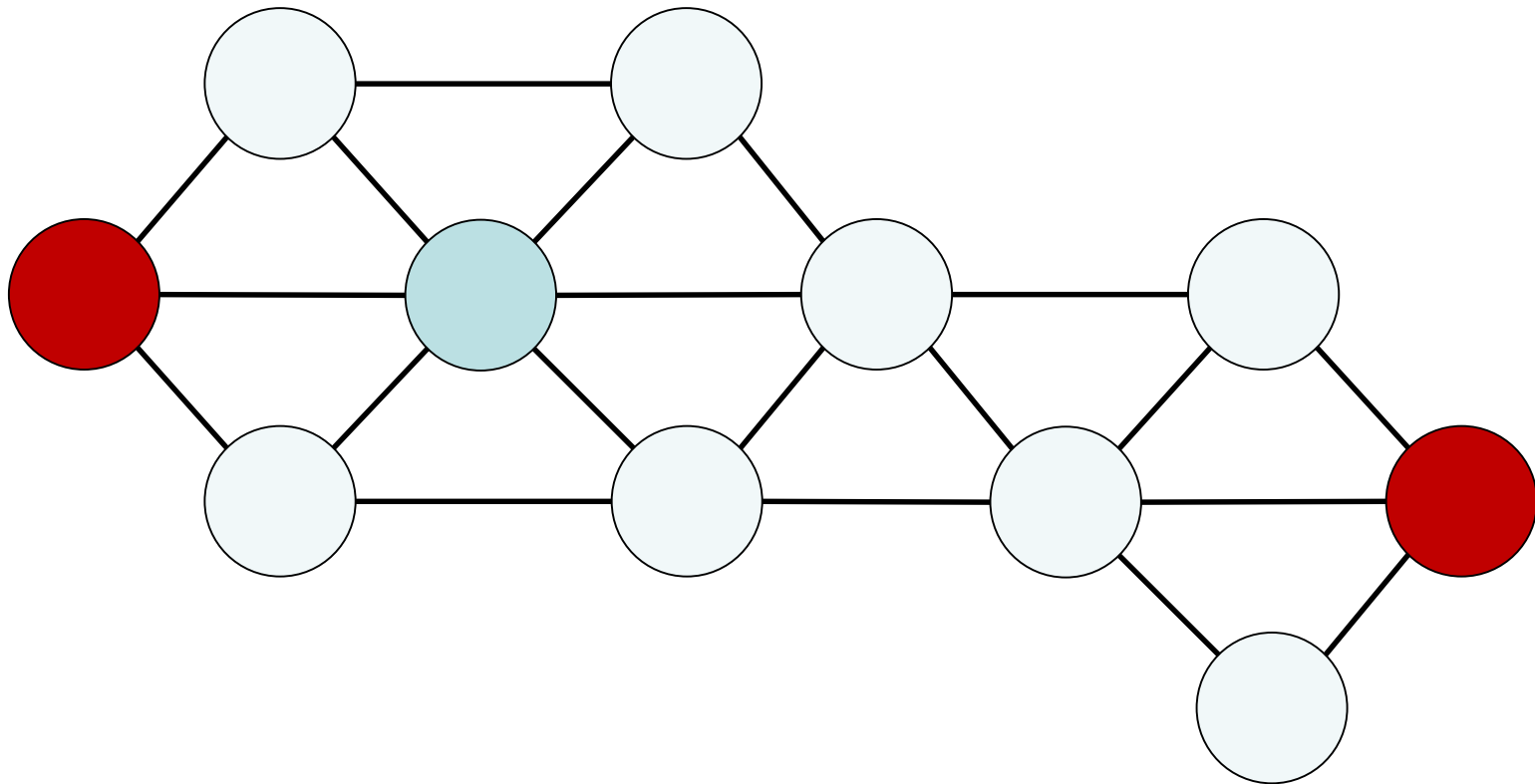
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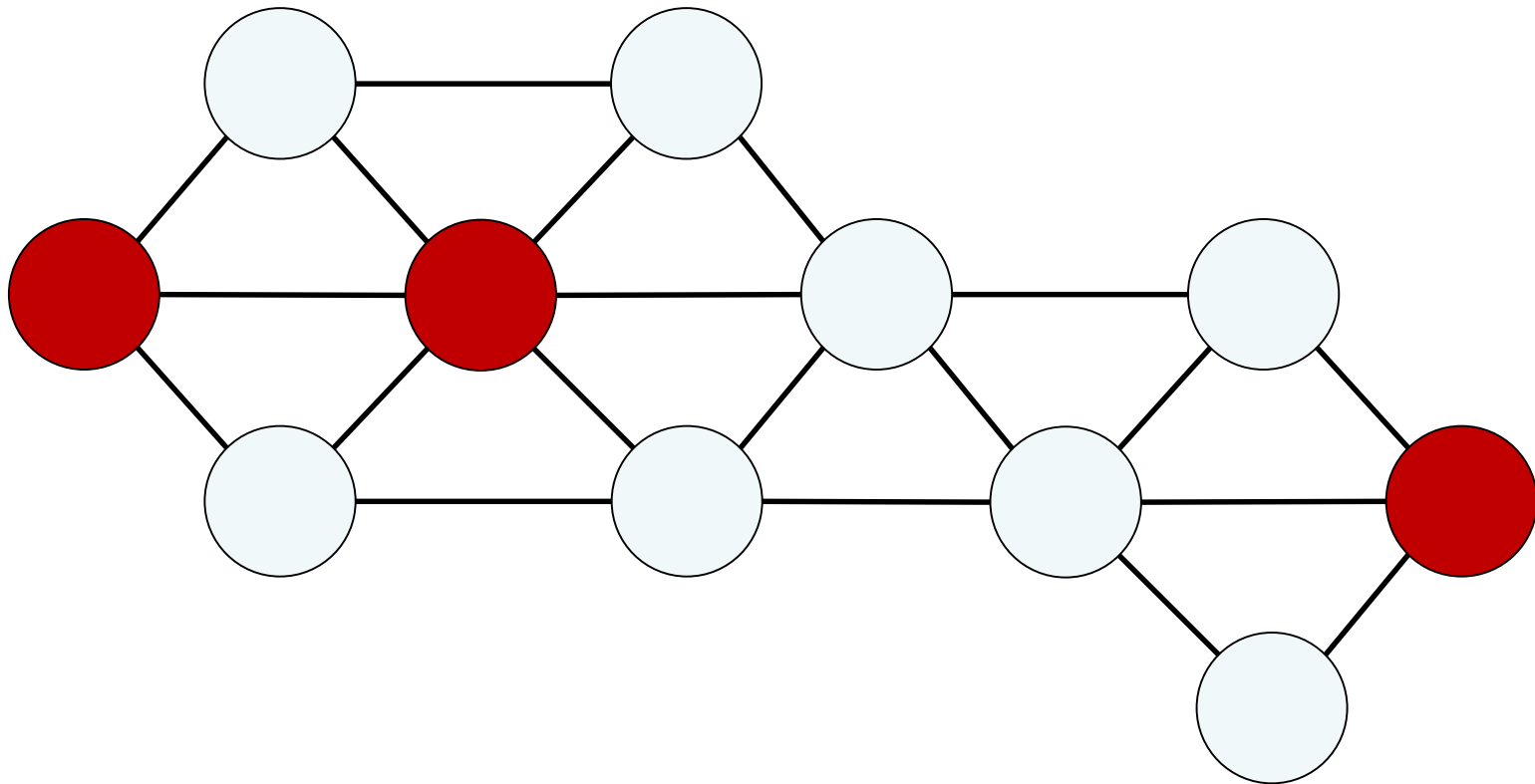
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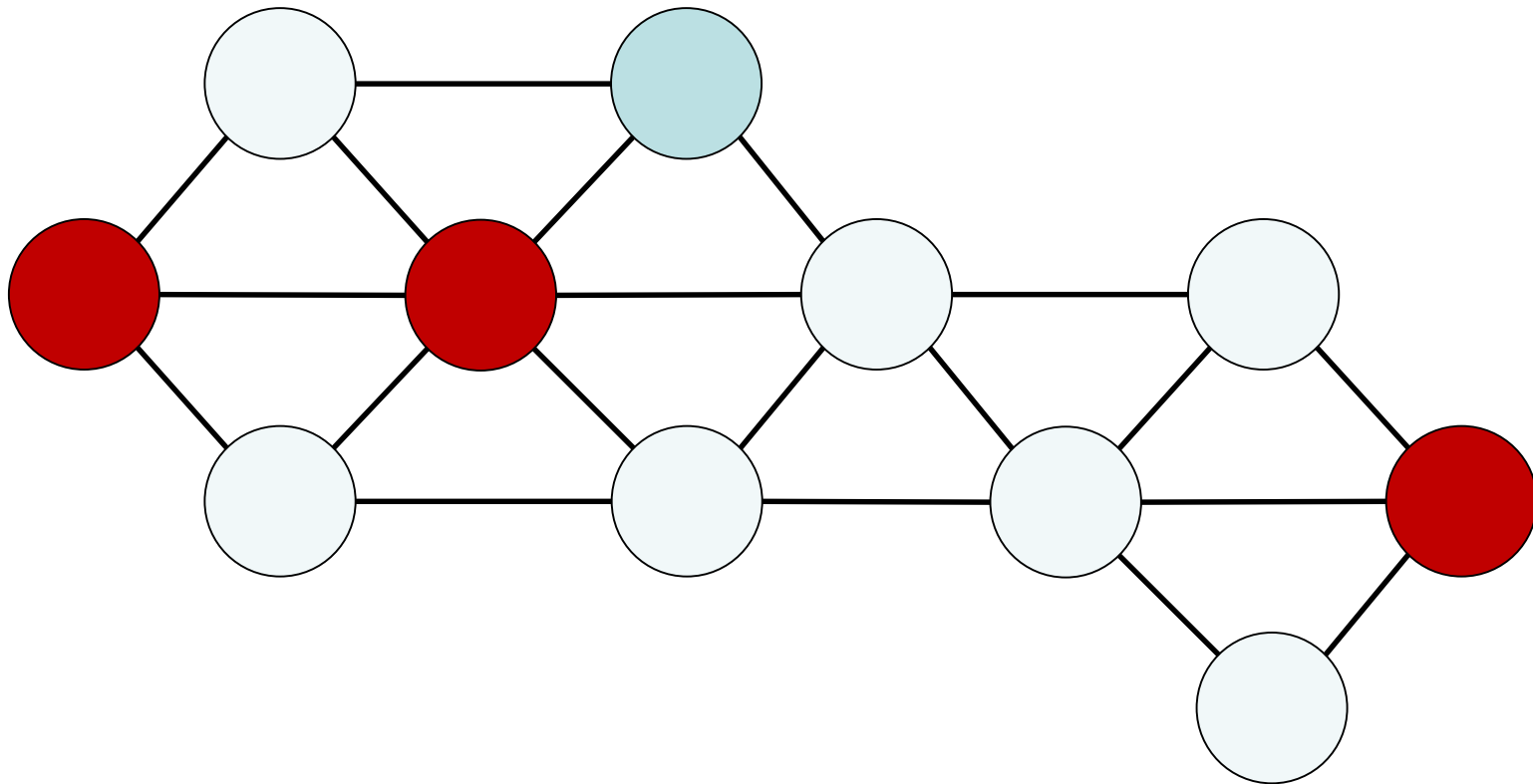
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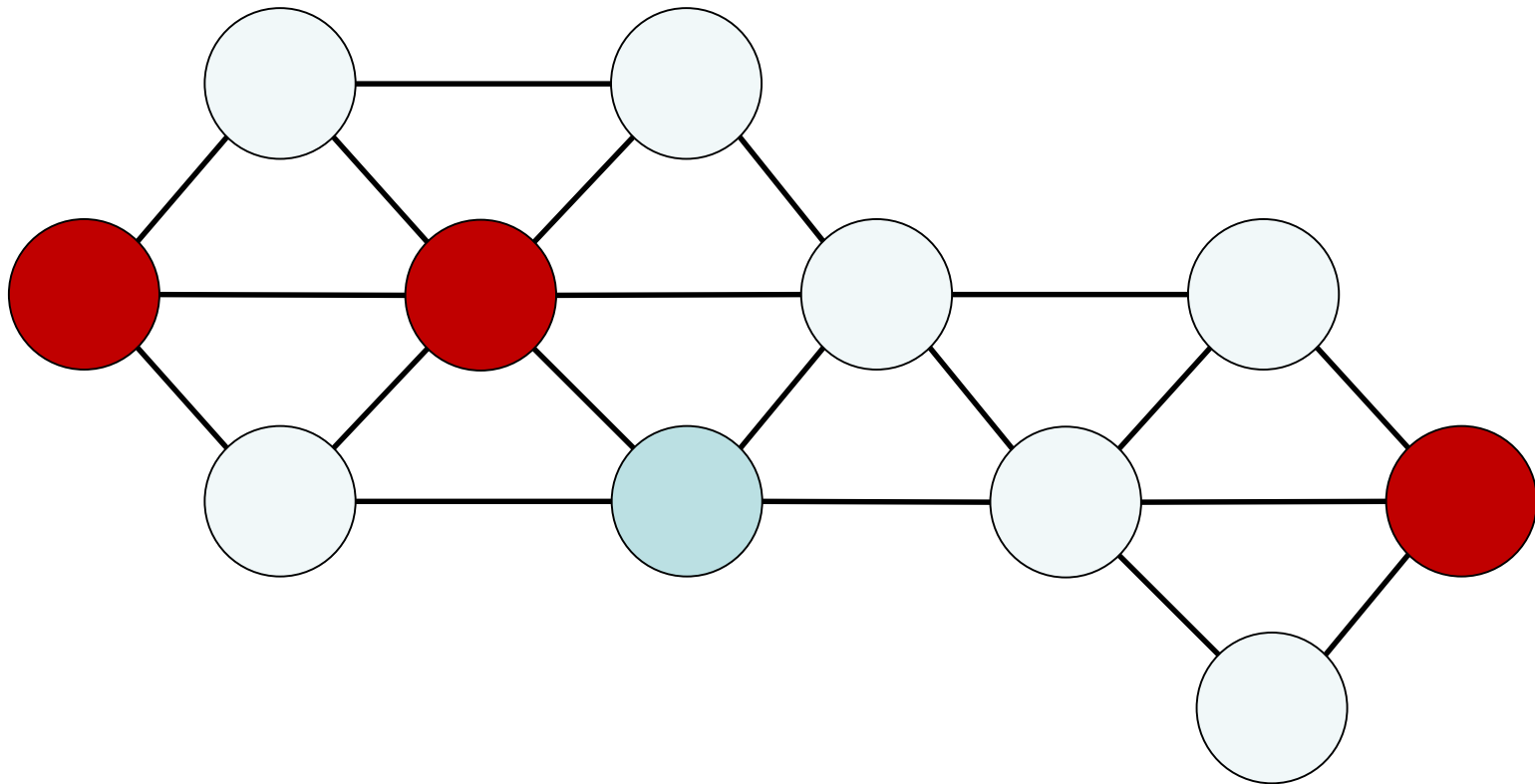
Shortest Path

- Example:



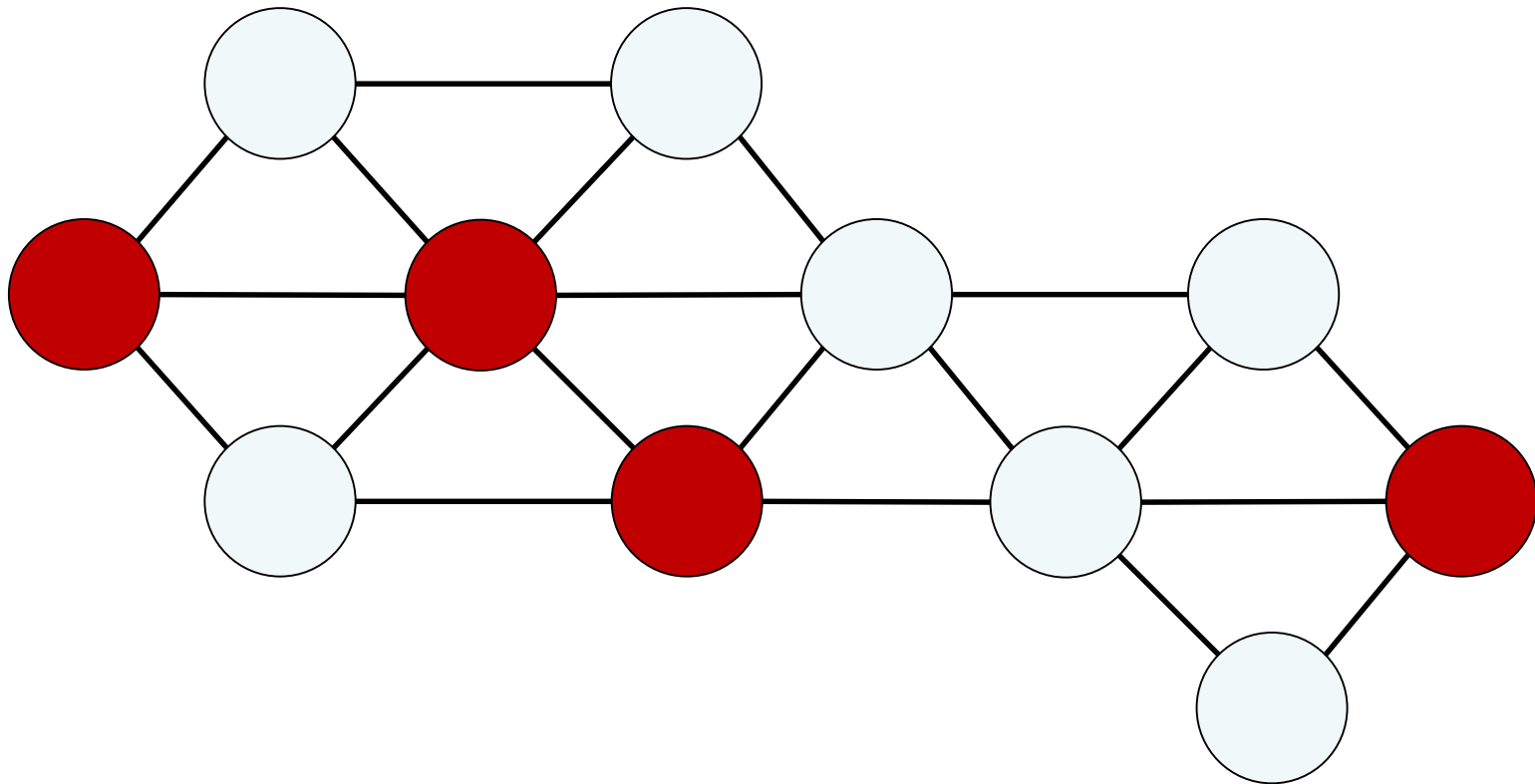
Shortest Path

- Example:



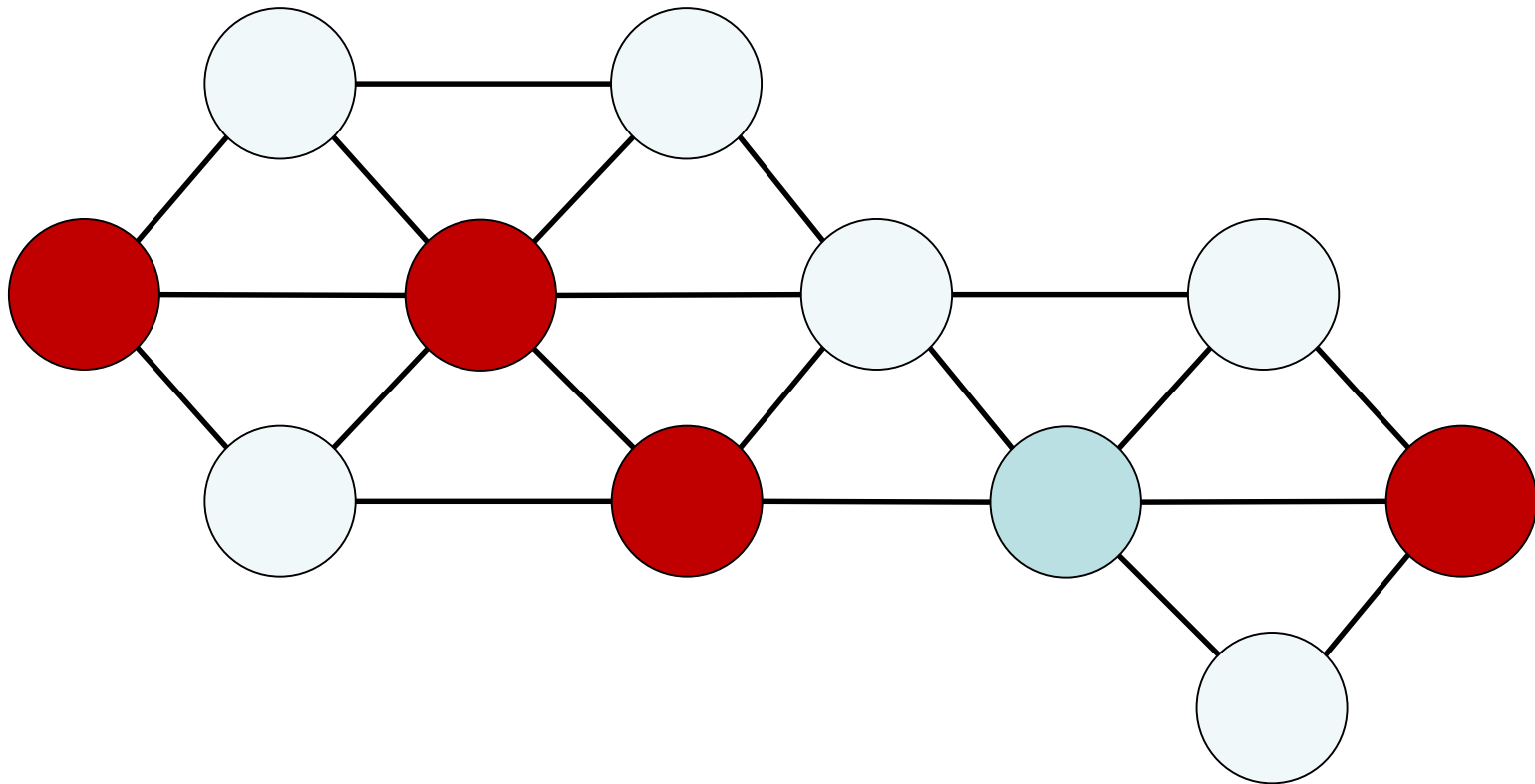
Shortest Path

- Example:



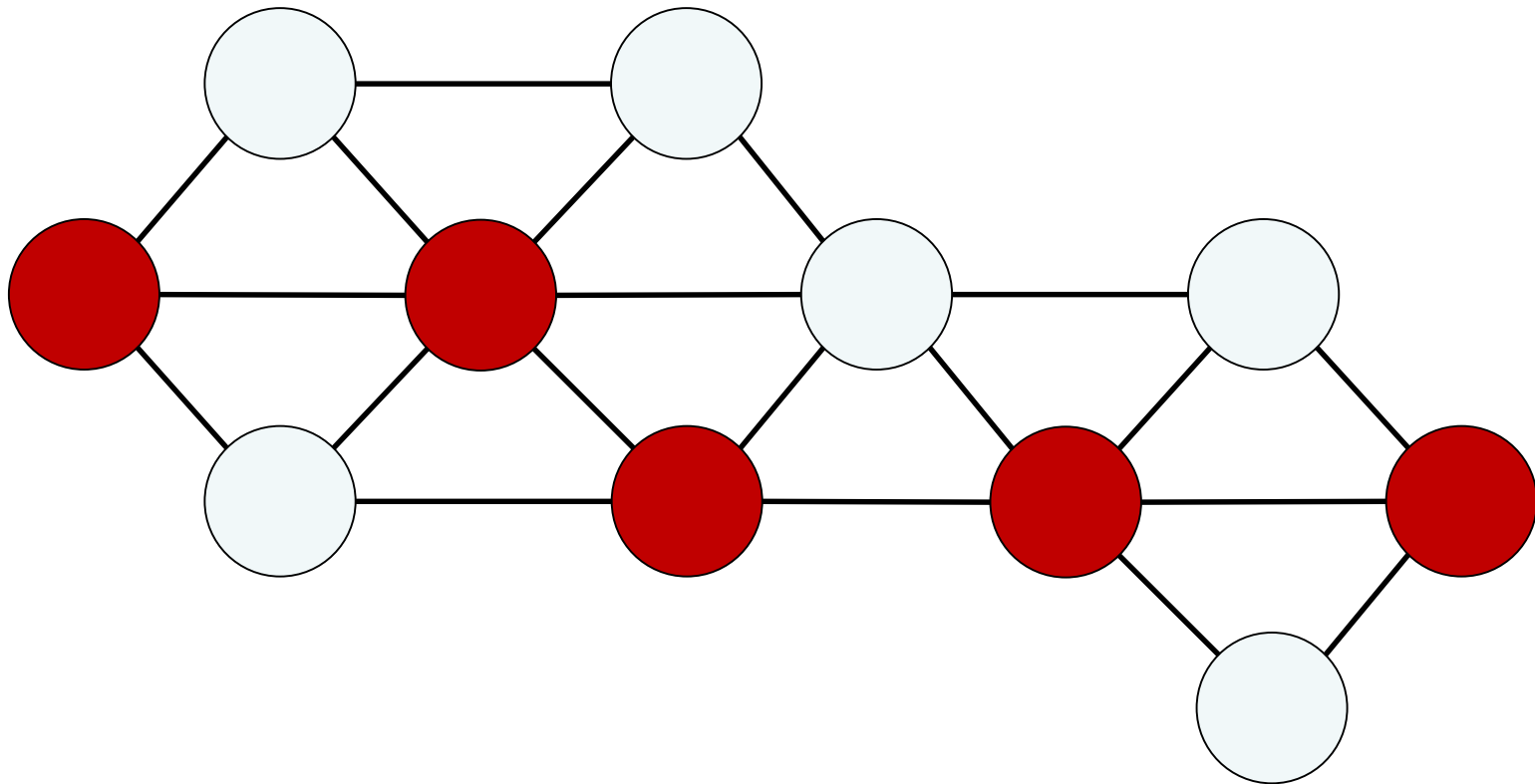
Shortest Path

- Example:



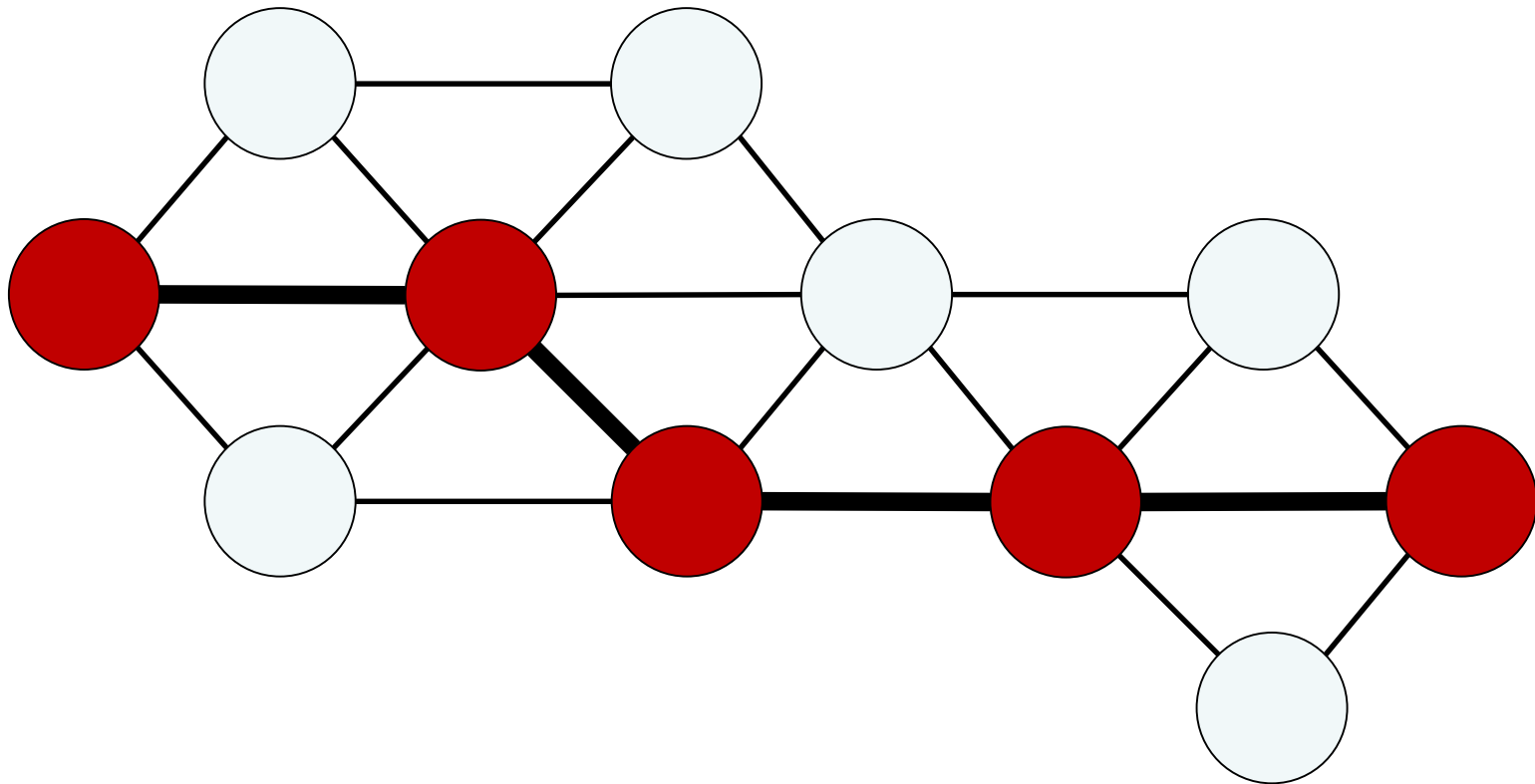
Shortest Path

- Example:



Shortest Path

- Example:



Different Model for the Slime Mold?

- Keep algorithms simple
- How does communication work?
 - Strength of flow through tubes indicates length.
 - We assume additional communication through tubes/plasma.
 - Communicate through moving nuclei?
- Nuclei:
 - How long do they live? Robustness?
 - Do they move?
 - How many are there?
 - Do they communicate / process information?

These are possibility results

- which weak assumptions work
- which don't

Thanks!

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