Quite simply, the versatility of computers is exactly equal to the versatility of the languages by which we prescribe their behaviour, and this appears to be unbounded.

1997 University of Bologna
We believe that ML contains features worthy of serious consideration; these are the escape mechanism, and the polymorphic type discipline ..., and also the attempt to make programming with functions—including those of higher type—as easy and natural as possible.

Edinburgh LCF 1979
Classic ML

- Polymorphic type inference.
  - Crucial for concision and convenience.
  - Minimizes bureaucracy of types.
- Escape mechanism = exceptions.
  - Supports backtracking proof search.
Classic ML

- Abstract Types.
  - Enforcement of representation invariants.
  - Confines trusted computing base in provers.
- Higher-order functions.
  - Crucial for tactic-based interactive provers.
  - Mathematically natural.
Polymorphic Type Inference

• Principal Typing Theorem
  • If $\vdash e : \tau$, then there is principal type scheme $\sigma$ such that $\vdash e : \sigma$ and $\sigma \geq \tau$.
  
  • The type scheme $\sigma$ may be found by first-order unification.

• The single most important and influential theorem in the theory of PL’s!
Polymorphic Type Inference

- Milner’s Theorem is both an inspiration and a torment to language designers.
  - Extremely hard to do significantly better!
  - Many useful extensions, including record and object types, type classes, and modules.
  - Complete for DEXPTIME, yet amazingly practical.
Abstract Types

• Classic ML introduced (one of?) the first abstract type mechanisms.

  • abs/rep mediate between an abstract type and its representation

  • Isolates enforcement of representation invariants for an abstraction.

• Bounds trust for LCF-style interactive provers!
Abstract Types

absrectype thm = form list # form
with hyps t = h
    where h,c = repthm t
and concl t = ...
and truthI = absthm (nil, TRUE)
and ...

The representation of thm is hidden from clients
so that the only values of type thm are theorems.
Influence of ML

- Appel: “POPL = Symposium on the Principles of ML!”
  - ML is the standard against which all FPL’s are judged.
- Gave rise to Hope, Miranda, Haskell, Caml, and Standard ML.
  - Pattern matching, modules/type classes, exceptions, mutation, records, objects/classes.
ML Modules

- **Modules** generalize abstract types and type classes.
  - Components are called **structures**.
  - Interfaces are called **signatures**.
  - Functions are called **functors**.
- Apply functional programming “in the small” to programs “in the large”.

Sunday, January 23, 2011
signature THEOREM = sig
  type thm
  val truthI : thm
  val andI : thm -> thm -> thm
  val andEL : thm -> thm
  ...
end

structure Thm :> THEOREM = ...
The aim of a language definition is ... to establish a theory of semantic objects upon which the understanding of particular programs may rest.

The Definition of Standard ML 1997
Language Definition

• What does it mean for a programming language to exist?
  • Precise definitions support rigorous theory.
  • Precise definitions support implementation by ensuring compatibility.
• The Definition of Standard ML remains the best example of rigorous language definition at scale.
Language Definition

- **Operational**, rather than *denotational*.
  - Contrary to conventional wisdom (at the time).
  - Readable, scalable, applicable.
- Symmetry between **static** and **dynamic** semantics.
  - Safety as coherence of statics and dynamics.
Language Definition

- Static semantics: elaboration of programs.
  - $\vdash program \Rightarrow type$
- Dynamic semantics: evaluation of programs.
  - $\vdash program \Rightarrow result$
- The result can be either an answer or wrong.
Type Safety

**Theorem:** Well-typed programs do not go wrong.

If $\vdash \text{program} \rightarrow \text{type}$ and $\vdash \text{program} \rightarrow \text{result}$, then \text{result} is a value of \text{type}, and hence cannot be wrong.

States the coherence of the static and dynamic semantics.
Mechanizing Type Safety

- The Definition supports *mechanized reasoning* about full-scale languages.
  - Variant using Structural Operational Semantics mechanized in Twelf.
- Thus Milner’s dream of mechanized reasoning about languages is realized!
  - Will be standard procedure in the future!