## 15-122: Principles of Imperative Computation

## QuickCheck 2 Solutions

Today, you can hold on to your copy of this QuickCheck and your TA will go over the answers at the end. The main purpose today is to give you some practice before the graded quiz (which should be available Sunday night - keep an eye on Piazza for details). We hope you will use the feedback from this QuickCheck to improve on your weaker areas before the quiz.

Name:
Andrew ID:
Section (circle one): A $\quad$ B $\quad$ C $\quad$ D $\quad$ E $\quad$ F $\quad$ G $\quad$ H

Simplicio and Sagredo (you) are a couple of 122 students. They are trying to complete an exercise, but are a bit stuck. Help them out!

Simplicio does not believe that for and while loops can be used interchangeably. For example, he believes that the following code cannot be written with a while loop, while maintaining the loop invariants.

```
for(int i = 0; i < n-2; i++)
//@loop_invariant i >= 0;
} {
4 A[i+2] = A[i+1] + A[i];
5}
```

Show him that you can do it!

## Solution:

```
int i = 0;
while(i < n-2)
//@loop_invariant i >= 0;
{
    A[i+2] = A[i+1] + A[i];
    i++;
7}
```

Simplicio now thinks that you can convert for loops to while loops but not vice-versa. Write the following while loop as a for loop to show him that he's wrong!

```
int e = y;
while (e > 0)
3//@loop_invariant e >= 0;
4//@loop_invariant POW(x,y) == accum * POW(b,e);
5 {
6 accum = accum * x;
7 e = e - 1;
8}
```


## Go Sagredo!

## Solution:

```
for(int e = y; e > 0; e--)
//@loop_invariant e >= 0;
3 //@loop_invariant POW(x, y) == accum * POW(b, e);
4 {
    accum = accum * x;
6}
```

Simplicio concedes defeat and you both move on to finish the rest of the exercise

And he's stuck again - this time he's having a problem with the two's complement representation. If $n=$ $0 \times 68 \mathrm{~A} 1$, calculate $-n$ (assume that the standard 32 bit representation of ints in C 0 is followed)

## Solution:

$\mathrm{n}=0 \mathrm{x} 000068 \mathrm{~A} 1, \sim_{\mathrm{n}}=0 \mathrm{xFFFF} 975 \mathrm{E}$
$-\mathrm{n}=\sim_{\mathrm{n}}+1=0 \times \mathrm{FFFF} 975 \mathrm{~F}$
Also, Simplicio has been given a color, color $=0 \times 18962213$. He needs the color with the same RGB composition, but which is completely opaque.

## Solution:

0xFF962213

## BONUS (if you're done early, try these out!)

Seeing that you're basically smarter that poor Simplicio is, Salviati, the TA, decides to give you something more challenging.

He has a magic color represented as int magic. He won't tell you what magic is, but wants you to come up with a way to store an opaque version of magic in magical (Hint: Try to use bitwise operators)

## Solution.

int magical $=$ magic $\mid(0 x F F \ll 24) ;$
OR
pixel magical = magic | (0xFF << 24);

Salviati now wants you to do an in place swap of two numbers $x$ and $y$, without using a temporary variable to store one value while modifying the other. Complete the code below to achieve this.

```
void inPlaceSwap (int x, int y){
    x = x^y;
    y = y^x;
    x = 剂y;
5}
```

Solution:
$x$ ~ y
because,

1) $x \prime=x-y ; y=y$
2) $x^{\prime}=x \wedge y ; y^{\prime}=y \wedge(x \sim y)=x$
3) $x^{\prime},=x, ~ x^{\prime}=(x-y) \sim y=x ; y^{\prime}=x$
