Using a DEM to Determine Geospatial Object Trajectories

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Abstract

This paper addresses the estimation of moving object trajectories within a geospatial coordinate system, using a network of video sensors. A high-resolution (0.5m grid spacing) digital elevation map (DEM) has been constructed using a helicopter-based laser range-finder. Object locations are estimated by intersecting viewing rays from a calibrated sensor platform with the DEM. Continuous object trajectories can then be assembled from sequences of single-frame location estimates using spatio-temporal filtering and domain knowledge.

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1 Introduction

Carnegie Mellon University and the Sarnoff Corporation are developing a Video Surveillance and Monitoring (VSAM) testbed that can seamlessly track human and vehicle targets through a large, visually complex environment. This apparent seamlessness is achieved using a network of active sensors to cooperatively track targets that cannot be viewed continuously by a single sensor alone. As targets move out of the active field-of-view of one sensor, they are "handed-off" to another sensor in the network. Automated target hand-off requires representing the geometric relationships between: 1) multiple sensor locations and their potential fields-of-view, 2) target locations, velocities, and predicted paths, and 3) locations of scene features that may occlude sensor views or influence target motion (roads, doorways). In the VSAM testbed, this information is made explicit by representing all sensor pose information, target trajectories, and site models in a single geospatial coordinate system.

This paper addresses the issue of estimating geospatial target trajectories. In addition to their uses in planning sensor hand-off, such trajectories can be used to generate visual activity synopses for review by a human observer, to perform motion-based inferences about target behavior such as loitering, and to detect multi-agent interactions such as rendezvous or convoying. In regions where multiple sensor viewpoints overlap, object trajectories can be determined very accurately by wide-baseline stereo triangulation. However, regions of the scene that can be simultaneously viewed by multiple sensors are likely to be a small percentage of the total area of regard in real outdoor surveillance applications, where it is desirable to maximize coverage of a large area given finite sensor resources.

Determining target trajectories from a single sensor requires domain constraints, in this case the assumption that the object is in contact with the terrain. This contact location is estimated by passing a viewing ray through the bottom of the object in the image and intersecting it with the a digital elevation map (DEM) representing the terrain. Sequences of location estimates over time are then assembled into consistent object trajectories. Previous uses of the ray intersection technique for object localization have been restricted to small areas of planar terrain, where the relation between image pixels and terrain locations is a simple 2D homography [3, 4, 6]. This has the benefit that no camera calibration is required to determine the backprojection of an image point onto the scene plane, provided the mappings of at least 4 coplanar scene points are known beforehand. However, the VSAM testbed is designed for much larger scene areas that may contain significantly varied terrain.

The remainder of this paper discusses site modeling issues, emphasizing construction of a high-resolution DEM using a laser range-finder, the basic ray intersection technique for producing

an estimate of object location from a single frame, and finally, techniques for producing consistent object trajectories from sequences of location estimates. Everything is illustrated using results from a VSAM testbed demonstration held in November 1997 at CMU's Bushy Run research facility.

2 Site Modeling

The term "geo"spatial refers to coordinate systems that represent locations on the surface of the Earth geoid – the ultimate *absolute* frame of reference for planetary activities. This does not necessarily imply a spherical coordinate system – local coordinate systems such as map projections can be geospatial if the transformation from local to geodetic coordinates is well documented. The primary benefit gained by firmly anchoring the VSAM testbed in geospatial coordinates is the ability to index into off-the-shelf cartographic modeling products. It is envisioned that future VSAM systems could be rapidly deployed to monitor trouble spots anywhere on the globe, with an initial site model being quickly generated from archived cartographic products or via aerial photogrammetry.

2.1 Coordinate Systems

Two geospatial site coordinate systems are used interchangeably within the VSAM testbed. The WGS84 geodetic coordinate system ("GPS" coordinates) provides a reference frame that is standard, unambiguous and global (in the true sense of the word). Unfortunately, even simple computations such as the distance between two points become complicated as a function of latitude, longitude and elevation. For this reason, geometric processing is performed within a site-specific Local Vertical Coordinate System (LVCS) [1]. An LVCS is a Cartesian system oriented so that the positive X axis points east, positive Y points true north, and positive Z points up (anti-parallel to gravity). All that is needed to completely specify an LVCS is the 3D geodetic coordinate of its origin point. Conversion between geodetic and LVCS coordinates is straightforward, so that each can be used as appropriate to a task.

For purposes of calibration and ground truth surveying, a GPS base station and rover configuration was established at the Bushy Run site using a pair of Ashtech Z-surveyer receivers. Using dual-frequency, carrier phase differential correction techniques, this system can measure locations with a horizontal accuracy of 1 cm (rms) when stationary and to within 3 cm (rms) when on the move. Vertical position estimates are roughly 1.7 times less accurate (1.7 cm static, 5 cm on the move).

2.2 Site Maps

To provide a human observer with a comprehensive site overview, a graphical user interface was built based on a digital orthophoto acquired as a commercial product from the United States Geological Survey (USGS). A small piece of this orthophoto, encompassing the central Bushy Run site, is shown in Figure 1. An orthophoto is a nadir (down-looking) image of the site as it would appear under orthographic projection, leading to an image in which scene features appear in their correct horizontal positions.

Figure 1: *One-meter resolution USGS orthophoto showing the Bushy Run test site.*

The third dimension of the scene is represented by a digital elevation map (DEM), coregistered with the orthophoto, that indicates scene elevation at each pixel. This essentially 2.5D representation has some limitations; for example, it cannot explicitly represent vertical wall surfaces or multiple elevation structures such as road overpasses, however it is a simple, popular representation that can easily handle the overwhelming majority of terrain surfaces at a site. In the case of Bushy Run, the commercially available USGS DEM was not suitable to our purposes. The 30-meter square pixel sampling of the USGS DEM was much too coarse – individual trees, for example, which

have a great impact on occlusion analysis, are completely indistinguishable at this resolution. In addition, USGS DEMs have been edited to explicitly remove building structures, which are useful for high-level reasoning about human activities. For these reasons, a custom DEM with half-meter pixel spacing was constructed using a laser range-finder mounted on a robotic helicopter. Since this high-resolution DEM is crucial to the target geolocation algorithm, the construction process is described in detail below.

2.3 High-Resolution DEM

The CMU autonomous helicopter project is developing an aerial laser mapping system [2, 9]. The CMU helicopter is a mid-sized, unmanned helicopter that is capable of fully autonomous takeoff, flight path tracking, accurate (< 20 cm) stationary hover, and landing. The laser scanning system is one of the sensor packages that can be flown aboard the helicopter. Ultimately, this scanner will automatically develop highly accurate (10 cm) 3D models of large environments, in a more efficient manner than is provided by existing techniques.

2.3.1 Laser Mapping System

Mounted beneath the helicopter is a simple laser scanner that scans the terrain in a plane perpendicular to the helicopter's direction of forward flight (Figure 2). This scanning motion, combined with the forward motion of the helicopter, allows patches of terrain up to 200m wide to be measured in a single pass. Larger areas are scanned by systematically flying patterns that completely cover the area.

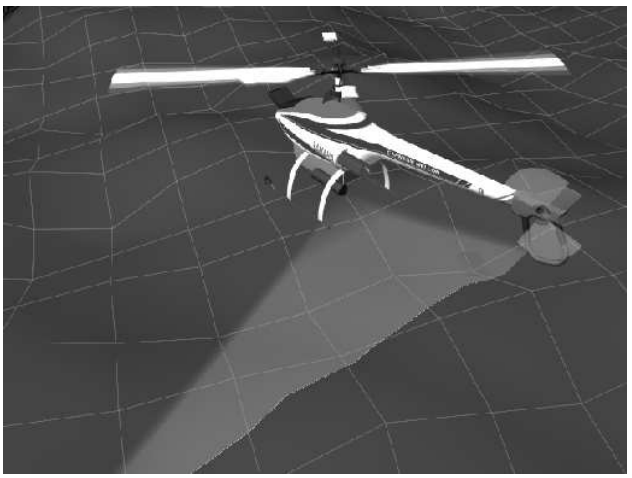

Figure 2: *Aerial mapping with a single planar scanner.*

The scanner uses a Riegl LD-90 time-of-flight laser range-finder to measure the straight line distance from the scanner to a target point on the terrain. A single motor/encoder combination positions a mirror to scan the laser's beam through the scanning plane. The scanning system requires that the position and attitude of the helicopter be known at all times to correctly determine the real coordinates of the sampled points. The test system uses a Novatel RT-20 GPS receiver to measure position, a pair of Gyration gyroscopes to measure pitch and roll, and a KVH flux-gate compass to measure yaw.

2.3.2 Bushy Run Mapping Procedure

The Bushy Run site was scanned to provide a high resolution DEM for object geolocation. The procedure for generating the DEM was as follows: 1) A GPS differential correction base station was setup at the Bushy Run site. 2) The helicopter mapping system was prepared for flight, and a local navigation frame was selected. 3) The helicopter mapping system was flown to scan the entire Bushy Run site. During the scan, the helicopter's position and attitude were collected and sent to ground computers for storage. Similarly, the laser scanner's measurements were also stored on the ground computers. 4) After the flights, the stored helicopter position and attitude were combined with the laser scanner's data to compute 3D coordinates of each point sampled by the laser range-finder. 5) The 3D data points were transformed from the helicopter's local navigation frame to the VSAM LVCS frame. 6) A DEM grid with cell size 0.5 m x 0.5 m was initialized. Each 3D point was assigned to one of the cells of the DEM by simply ignoring its Z component and allowing it to fall into one of the cells. For each cell of the DEM, three statistics were computed: the mean elevation of all points landing in that cell, the variance in the elevation of these points, and the total number of points. These three matrices comprise the resulting DEM.

2.3.3 Bushy Run Results

The Bushy Run site is approximately 300m x 300m, and has an asphalt road surrounding an open field with two large buildings and trees surrounding the area. A test pilot manually flew the helicopter about 10 meters above the road as the system scanned the surrounding environment. The flight was approximately 5 minutes in duration, and collected over 2.5 million 3D data points. Figure 3 shows a point cloud visualization of the data. For display purposes, each point is shaded based on a combination of elevation, and on return intensity of the laser. As such, the road is readily visible. It should also be noted that since the helicopter was flown above the road, the low density of measurements from the center of the field is expected.

Figure 4 shows a digital elevation map with 0.5m square grid spacing, generated from the scan

Figure 3: *Perspective view of 3D point cloud from test scan.*

data. The intensity of each pixel indicates the average elevation measured for that location. A side-by-side comparison of this image with the orthophoto in Figure 1 indicates that the mapping system is producing reasonable results. For purposes of geolocation estimation, holes in the DEM (black areas in Figure 4) were filled be inserting bilinearly interpolated values from the USGS 30-meter DEM. This fusion of information was possible since both DEMS are precisely geolocated.

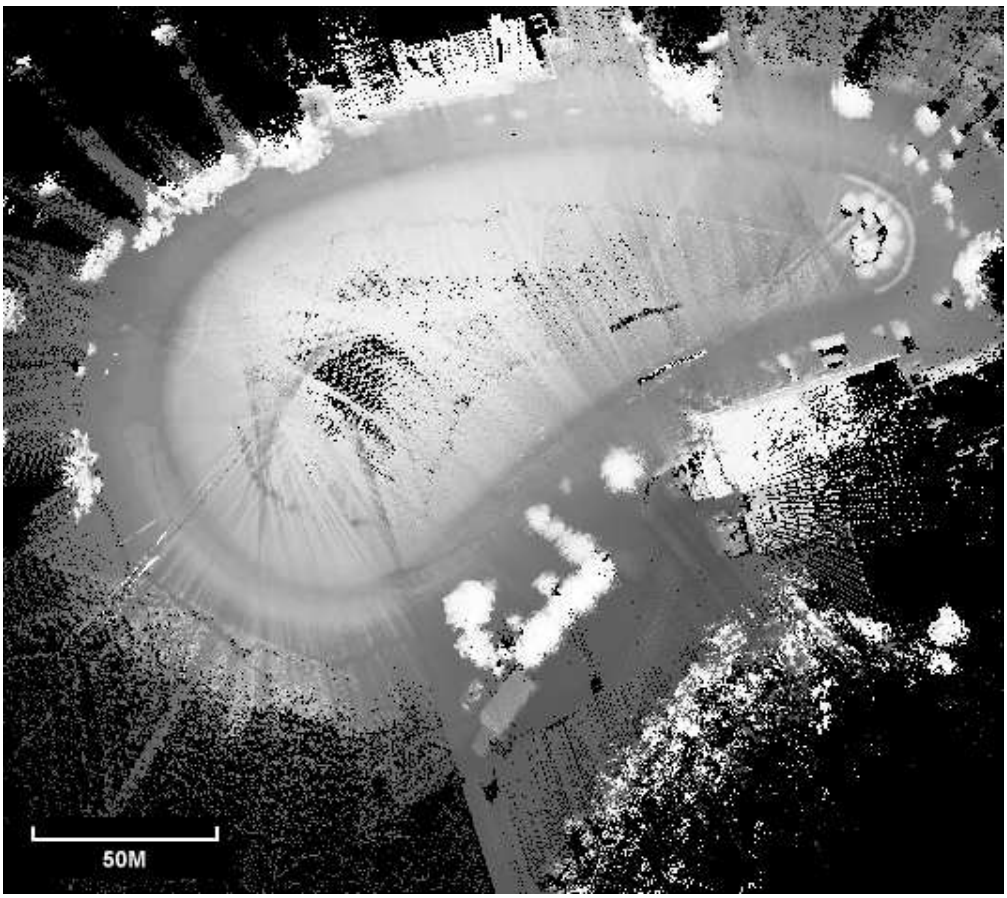

Figure 4: *Half-meter resolution DEM showing same area as orthophoto in Figure 1. Intensity has been enhanced to emphasize terrain variation.*

3 Estimating Target Location

The VSAM testbed contains highly effective algorithms for detecting, classifying and tracking moving targets through a 2D video sequence [7]. Target locations in the scene are estimated from the bounding box of stable motion regions in each frame of the sequence. Each location estimate is obtained by shooting a 3D viewing ray through the center of the bottom edge of the target image

bounding box out into the scene, and determining where it intersects the terrain. This procedure is illustrated in Figure 5.

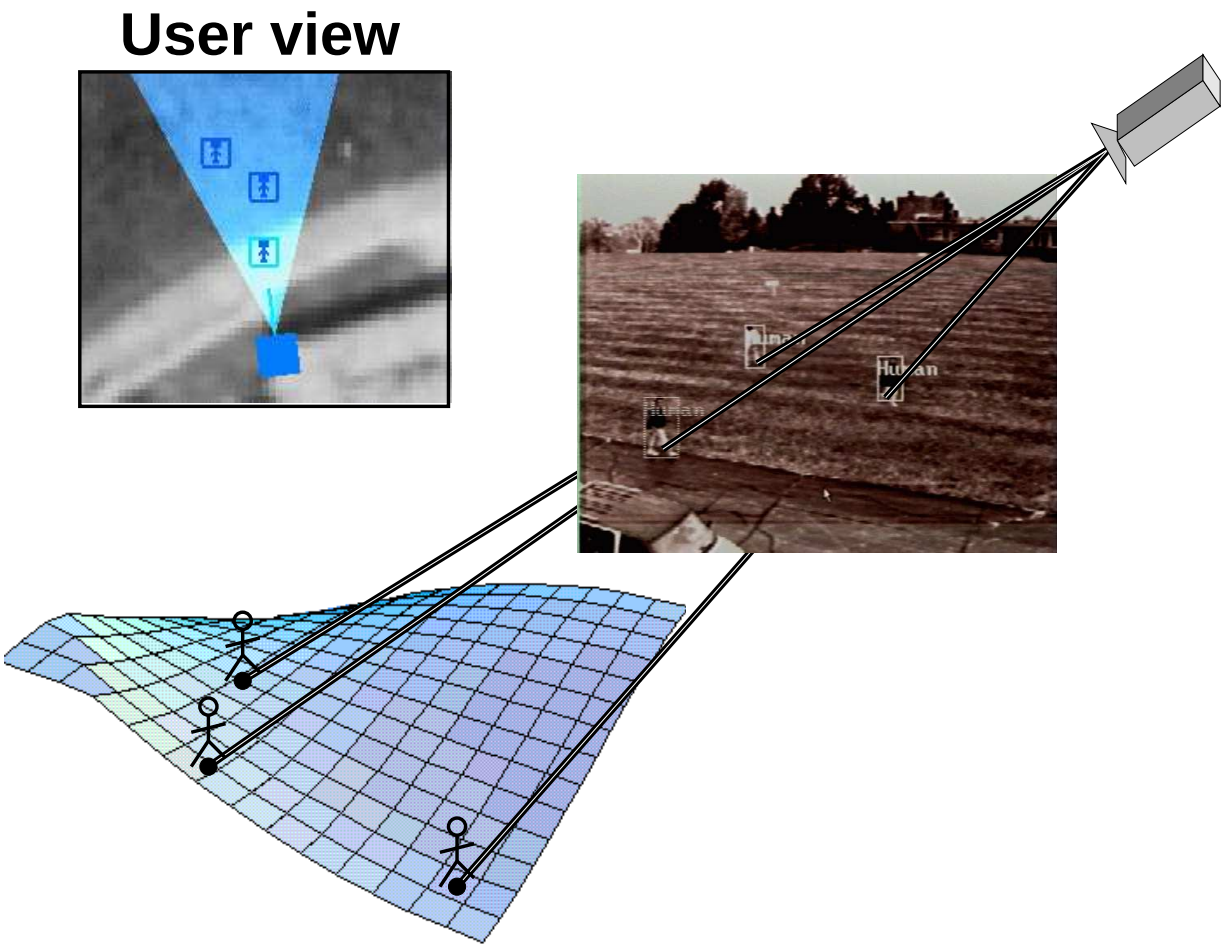

Figure 5: *Estimating object locations by intersecting view rays with a terrain model.*

3.1 Camera Calibration

Calibration of the internal (lens) and external (pose) sensor parameters is necessary in order to determine how each pixel in the image relates to a viewing ray in the scene. The internal parameters of the sensor are determined manually, off-line. The external parameters consist of sensor location and orientation, measured with respect to the site LVCS. These are determined as part of the sensor setup procedure. Each sensor is mounted rigidly to a pan-tilt head, which in turn is mounted on a leveled tripod, thus fixing the roll and tilt angles of the pan-tilt-sensor assembly to be zero. The location (x_0, y_0, z_0) of the sensor is determined by GPS survey.

The only other degree of pose freedom is the yaw angle (horizontal orientation) of the sensor assembly. This angle is estimated using a set of vertical landmarks distributed around the site, whose horizontal locations (x_i, y_i) are known (surveyed by GPS). For each visible landmark the pan-tilt assembly is guided (by hand) to pan until the landmark is centered in the camera image, thereby measuring a set of pan angles $\{\text{pan}_i | i = 1, ..., n\}$. Each measured pan angle yields an independent estimate θ_i of camera yaw as

$$\theta_i = \text{atan2}(y_i - y_0, x_i - x_0) \; - \; \text{pan}_i \quad .$$

A final yaw estimate $\hat{\theta}$ is computed as the average of these angles, taking care to use the appropriate formula for averaging angular data [8], namely

$$\hat{\theta} = \text{atan2}(\sum_1^n \sin\theta_i, \sum_1^n \cos\theta_i) \quad .$$

3.2 Ray Intersection with the DEM

Given a calibrated sensor, and an image pixel corresponding to the assumed contact point between an object and the terrain, a viewing ray $(x_0 + ku, y_0 + kv, z_0 + kw)$ is constructed, where (x_0, y_0, z_0) is the 3D sensor location, (u, v, w) is a unit vector designating the direction of the viewing ray emanating from the sensor, and $k \geq 0$ is an arbitrary distance. General methods for determining where a viewing ray first intersects a 3D scene (for example, ray tracing) can be quite involved. However, when scene structure is stored as a DEM, a simple geometric traversal algorithm suggests itself, based on the well-known Bresenham algorithm for drawing digital line segments. Consider the vertical projection of the viewing ray onto the DEM grid (see Figure 6). Starting at the grid cell (x_0, y_0) containing the sensor, each cell (x, y) that the ray passes through is examined in turn, progressing outward, until the elevation stored in that DEM cell exceeds the z-component of the 3D viewing ray at that location. The z-component of the view ray at location (x, y) is computed as either

$$z_0 + \frac{(x - x_0)}{u} w \quad \text{or} \quad z_0 + \frac{(y - y_0)}{v} w \tag{1}$$

depending on which direction cosine, u or v, is larger. This approach to viewing ray intersection localizes objects to lie within the boundaries of a single DEM grid cell. A more precise sub-cell location estimate can then be obtained by interpolation. If multiple intersections with the terrain beyond the first are required, this algorithm can be used to generate them in order of increasing distance from the sensor, out to some cut-off distance.

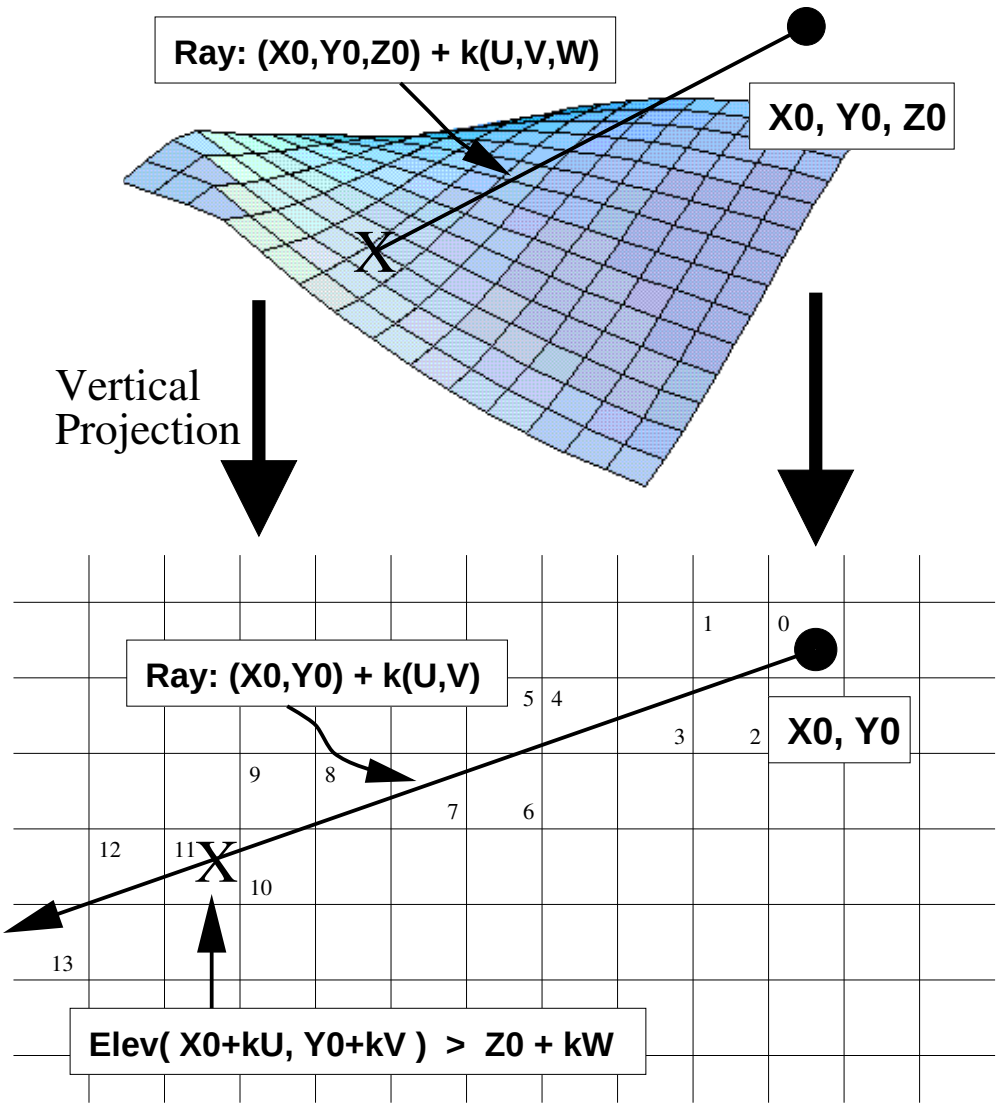

Figure 6: *A Bresenham-like traversal algorithm determines which DEM cell contains the first intersection of a viewing ray and the terrain.*

4 Assembling Target Trajectories

Computation of dynamic object trajectories in the scene is useful for planning sensor hand-off, generating visual activity summaries, and for performing qualitative behavior analysis. The previous section described how target locations can be estimated from each frame by intersecting viewing rays with a DEM. This section discusses the assembly of single-frame location estimates into continuous scene trajectories using spatio-temporal filtering and domain knowledge.

4.1 Spatio-Temporal Filtering

Target trajectories can be created by simply concatenating a sequence of static object geolocations. However, some of these single-frame location estimates may be in error, due to imprecision in the motion region bounding box. Furthermore, a single viewing ray may intersect the terrain multiple times, and the first intersection is not always the correct one, since our "terrain" representation also contains trees and buildings that may occlude parts of the object. An example of this is shown in Figure 7a, corresponding to a video sequence in which a tracked vehicle became partially occluded by a tree. Composing single-frame estimates of the first intersection of the target viewing ray with the terrain generates a scene trajectory that incorrectly appears to swerve into the tree. Figure 7b shows a better trajectory, generated by taking the **last** intersection between the viewing ray and the terrain. Although this simple heuristic is effective in removing errors caused by occluding foliage, it may yield incorrect results in rugged or hilly terrain, when multiple elevation structures such as bridges exist, or in the case of a person walking on a building roof.

A more general mechanism for assembling location estimates into smooth, continuous object trajectories is spatio-temporal filtering. For example, Kalman filtering could be used to build a dynamic model of the target, based on the assumption that the target will not make sharp turns and abrupt accelerations [3, 6]. However, as mentioned above, a viewing ray may intersect the terrain multiple times, resulting in several alternative hypotheses for target location. The Kalman filter, based on unimodal Gaussian densities, cannot simultaneously represent these multiple possible paths, and an incorrect choice of initial value will doom the entire trajectory. What is required is a more advanced filtering method that can handle multiple data associations, such as the CONDENSATION algorithm [5]. This is a topic of current work.

4.2 Domain Knowledge

Notwithstanding the need for a powerful, general mechanism to generate smooth target trajectories, in certain cases domain knowledge can be used to generate simpler, approximate solutions. In

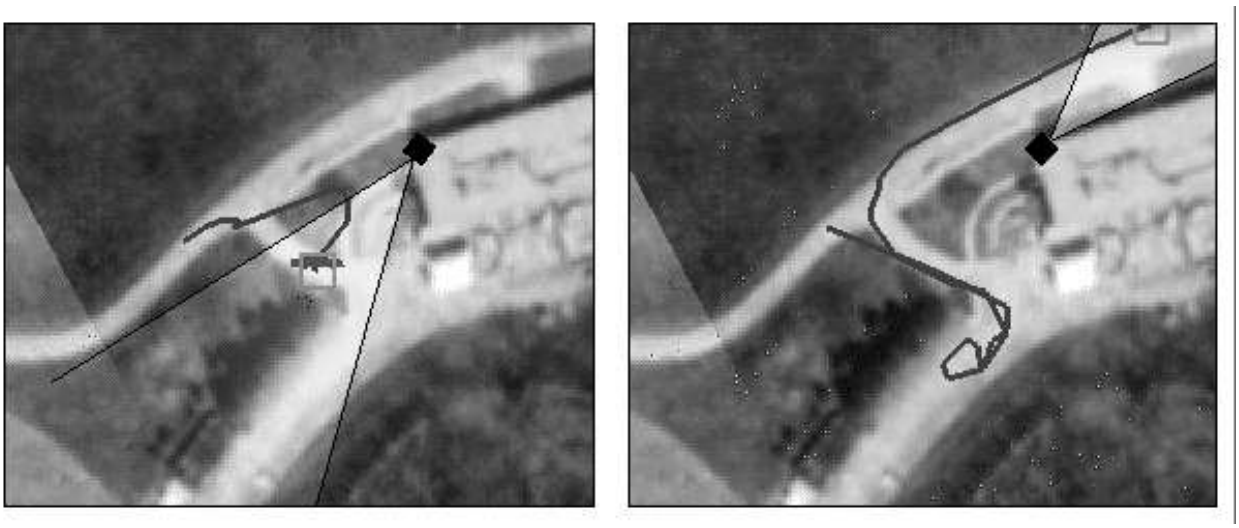

Figure 7: *Left: Unfiltered ray intersection trajectory shows a car "jumping" into a tree. Right: Filtered trajectory removes the treetop detour. Note that sensor locations and fields of view are also depicted on the user interface.*

particular, the VSAM testbed classifies moving objects as being either human or vehicle [7]. Vehicular target motion is typically constrained to lie along roadways in the scene, and this heuristic suggests the use of a road network graph together with the viewing ray DEM intersection algorithm to produce unambiguous, accurate target trajectories.

For public roadways, the USGS digital line graph (DLG) product contains geolocated road networks as a connected graph of line segments. In the case of Bushy Run (private property), a road map was outlined by hand, using the digital orthophoto. Each vehicle location estimate was computed as a function of the target viewing ray, road network and DEM, as follows. As in Section 3.2, let the target viewing ray be written as $(x_0 + ku, y_0 + kv, z_0 + kw)$. Both the viewing ray and road network curves are converted into 2D by vertical projection (ignoring their z-components), and a set of intersection points (x_i, y_i) between the viewing ray and road curves are computed, out to a cutoff distance. In general, the viewing ray will intersect the road map several times. Elevation information from the DEM is used to disambiguate between the multiple road location candidates, by choosing the the location $(\hat{x}, \hat{y})$ where the difference between DEM elevation and the viewing ray z-component is smallest, that is

$$(\hat{x}, \hat{y}) = \arg\min_{x_i, y_i} \quad |\text{elev}(x_i, y_i) - ray_z(x_i, y_i)| \quad ,$$

where the viewing ray z-component is computed as in Equation 1. This approach essentially finds the point with the minimum distance (measured vertically) between a 3D viewing ray and a set of space curves representing roads, but with low computational cost.

Figure 8 shows an activity synopsis generated using this approach, in the form of a long-term vehicle trajectory around the Bushy Run site. Two sensors cooperatively track a vehicle that drives into the site from the left, descends a hill into a parking lot, stops and turns around, then proceeds out of the parking lot and continues in its counterclockwise journey around the site. Gaps in the trajectory correspond to hand-off regions and occlusion areas where neither sensor was reliably tracking the object.

Figure 8: *Activity synopsis of a vehicle driving through Bushy Run.*

5 Current Work

This year the VSAM IFD demo will be held in and around the CMU campus, and feature nearly a dozen sensors tracking objects throughout a cluttered, urban environment. A full geospatial site model of the area is currently being constructed, including terrain, road networks, sidewalks, bridges, building volumes, and specific trees. The VSAM testbed will be able to manipulate these site model elements using libCTDB, a library of geometric utilities for interacting with a geospatial database, developed within the military's synthetic environments program. LibCTDB will sup-

port the VSAM testbed's need for occlusion analysis and ray intersection to support multi-sensor hand-off, as well as offer an interface to fully interactive, 3D dynamic visualization packages. Furthermore, more general methods of performing spatio-temporal filtering given multiple competing location hypotheses are being pursued.

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