

# Formal Modeling and Analysis of Pancreatic Cancer Microenvironment

Qinsi Wang

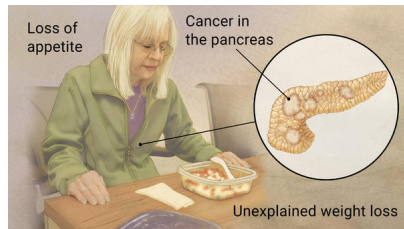
Computer Science Department, Carnegie Mellon University

Natasa Miskov-Zivanov, Bing Liu, James R. Faeder, Michael Lotze,  
Edmund M. Clarke

CMSB 2016

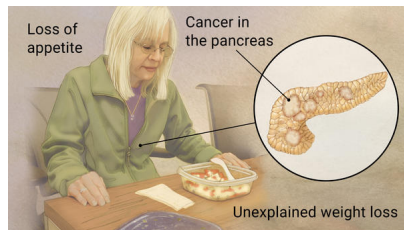
# Pancreatic Cancer

- the **7th** most common cause of cancer deaths globally, and
- the **4th** in US



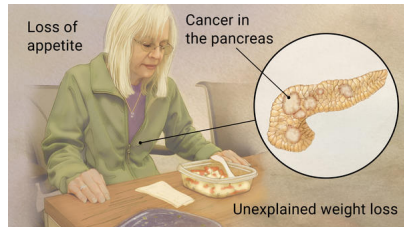
# Pancreatic Cancer

- the **7th** most common cause of cancer deaths globally
- the **4th** in US
- hard to diagnose in the early stages
  - no symptoms
  - the lack of biomarkers allowing early screening



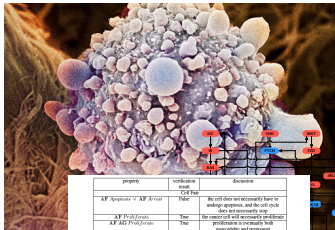
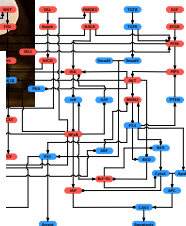
# Pancreatic Cancer

- the **7th** most common cause of cancer deaths globally
- the **4th** in US
- hard to diagnose in the early stages
  - no symptoms
  - the lack of biomarkers allowing early screening
- very poor prognosis

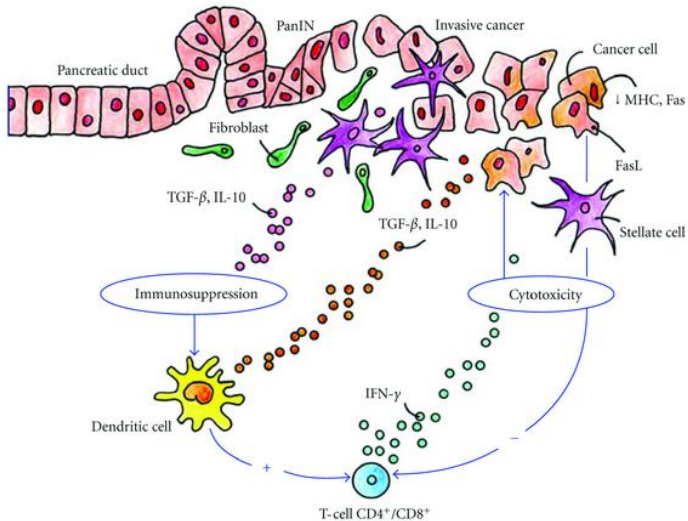




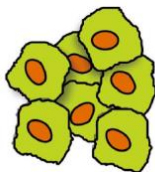
# Studies on Pancreatic Cancer Cells

[illegible]

# Pancreatic Cancer Microenvironment / Stroma



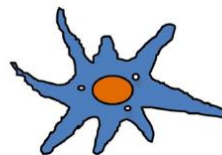
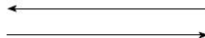
# Pancreatic Cancer Cells and Stellate Cells



Pancreatic cancer cells

↑Proliferation  
↓Apoptosis  
↑Migration/invasion  
↑Metastasis  
↑Stem cell niche

↑Survival



Activated pancreatic stellate cells

↑Proliferation  
↑Fibrosis/ECM synthesis  
↑Angiogenic factors, MMPs  
↑Migration and metastasis

## Motivation

- Study the interplay between PCCs and PSCs, and identify major pathways and molecules in PSCs

## Contributions

# Motivation and Contributions

## Motivation

- Study the interplay between PCCs and PSCs, and Identify major pathways and molecules in PSCs

## Contributions

- Construct the first multicellular and multiscale model

# Motivation and Contributions

## Motivation

- Study the interplay between PCCs and PSCs, and Identify major pathways and molecules in PSCs
- Appropriate modeling formalism (multiple cells, cell populations, both cellular and molecular dynamics, ...)

## Contributions

- Construct the first multicellular and multiscale model

# Motivation and Contributions

## Motivation

- Study the interplay between PCCs and PSCs, and Identify major pathways and molecules in PSCs
- Appropriate modeling formalism (multiple cells, cell populations, both cellular and molecular dynamics, ...)

## Contributions

- Construct the first multicellular and multiscale model
- **Propose a multiscale hybrid rule-based modeling language**

# Motivation and Contributions

## Motivation

- Study the interplay between PCCs and PSCs, and Identify major pathways and molecules in PSCs
- Appropriate modeling formalism (multiple cells, cell populations, both cellular and molecular dynamics, ...)
- Validate our model, and then predict possible targets for PC treatments

## Contributions

- Construct the first multicellular and multiscale model
- Propose a multiscale hybrid rule-based modeling language



# Motivation and Contributions

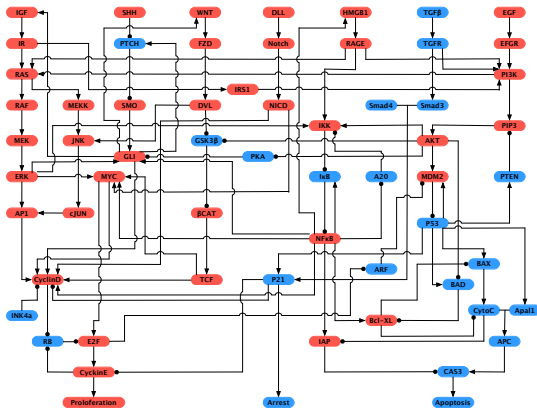
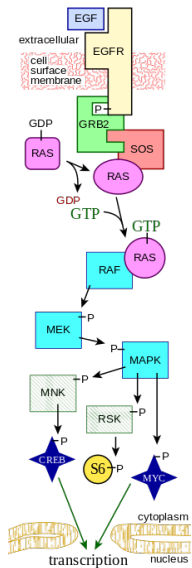
## Motivation

- Study the interplay between PCCs and PSCs, and Identify major pathways and molecules in PSCs
- Appropriate modeling formalism (multiple cells, cell populations, both cellular and molecular dynamics, ...)
- Validate our model, and then predict possible targets for PC treatments

## Contributions

- Construct the first multicellular and multiscale model
- Propose a multiscale hybrid rule-based modeling language
- **Statistical model checking is used to carry out model validation and prediction**

# Cell Signaling Pathways



# Our Pancreatic Cancer Microenvironment Model

Pancreatic cancer cell (PCCs):

Pathways regulating

- Proliferation,
- Apoptosis, and
- Autophagy.

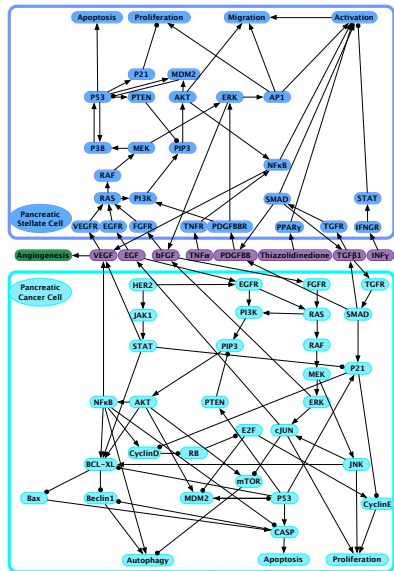
Pancreatic stellate cell (PSCs):

Pathways regulating

- Proliferation,
- Apoptosis,
- Activation, and
- Migration.

Interactions between PCCs and PSCs:

EGF, bFGF, VEGF, TGF $\beta$ 1, and PDGFBB



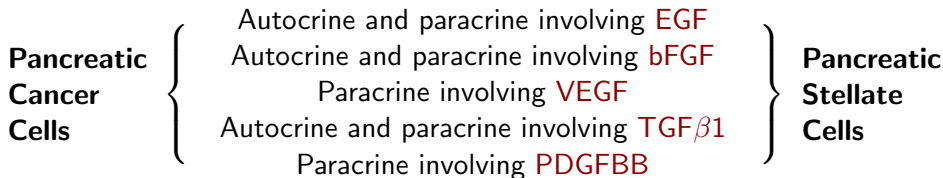
# Biological Background - Pancreatic Cancer Cells

Cell Function	Promote (+) / Inhibit (-)	Pathway
Proliferation	+	K-RAS mutation-induced RAS pathway
	+	HER2/neu mutation-induced EGFR pathway
	+	EGF-EGFR pathway
	+	bFGF pathway
Apoptosis	+	TGF $\beta$ 1 pathway
	-	K-RAS mutation-induced PI3K pathway
	-	HER2/neu mutation-induced PI3K pathway
Autophagy	-	Pathways upregulating mTOR
	+	Overexpressed NF $\kappa$ B and Beclin1

# Biological Background - Pancreatic Stellate Cells

Cell Function	Promote (+) / Inhibit (-)	Pathway
Activation	+	PDGFBB pathway
	+	TGF $\beta$ 1 pathway
	+	TNF $\alpha$ pathway
Migration	+	MAPK pathway upregulated by EGF, bFGF, and VEGF
	+	PDGFBB regulated PI3K pathway
	+	PDGFBB regulated ERK-AP1 pathway
Proliferation	+	ERK-AP1 pathway upregulated by growth factors
	-	Pathways upregulating tumor suppressors
Apoptosis	+	MAPK pathway via P53

# Biological Background - Extracellular Molecules



**(Traditional) Rule-based  
Modeling (i.e. BioNetGen)**

## **(Traditional) Rule-based Modeling (i.e. BioNetGen)**

**aims at:**

- Modeling reactions involving intracellular signaling molecules
- Describing dynamics continuously



## **(Traditional) Rule-based Modeling (i.e. BioNetGen) aims at:**

- Modeling reactions involving intracellular signaling molecules
- Describing dynamics continuously



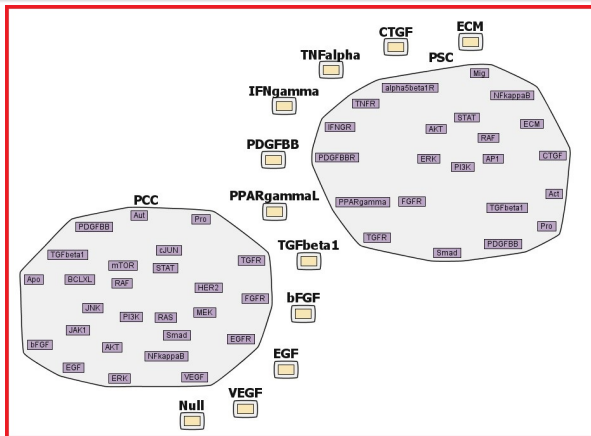
## **Multiscale Hybrid Rule-based Modeling can also:**

- Describe intercellular interplay together with intracellular reactions
- In a hybrid way: continuously for intercellular, and discrete for intracellular

# Multiscale Hybrid Rule-based Modelling

## The basic building blocks

- Cells (with subunits as intracellular molecules), or
- Extracellular molecules (with no subunits)



## The basic building blocks (Con.)

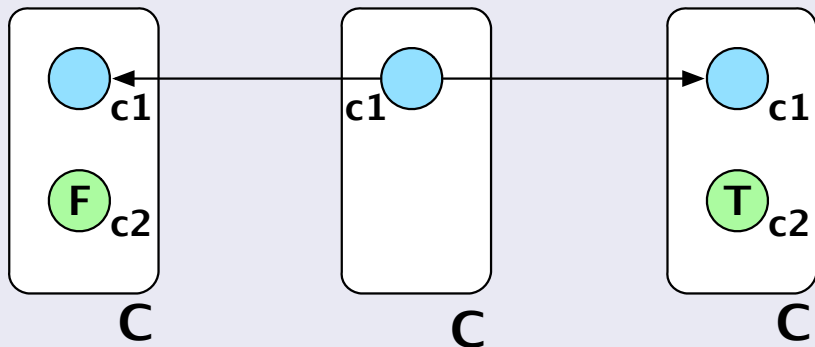
- Boolean values (**T** or **F**), easy to extend to discrete values
- Different biological meanings

Subunit	T	F
cell function / secretion	being triggered	not being triggered
receptor	being bounded	being free
protein	high concentration	low concentration
...	...	...

# Multiscale Hybrid Rule-based Modelling

## Patterns

- To identify **a set of species that share a set of features**
- Provides a rich yet concise description



# Multiscale Hybrid Rule-based Modelling - Rules

Rules
Rule 1: Ligand-receptor binding
Rule 2: Mutated receptors form a heterodimer
Rule 3: Downstream regulation: Encoding Logical Functions as Rules
Rule 4: Cell functions
Rule 5: Secretion
Rule 6: Degradation of extracellular molecules
Rule 7: Mutation
Rule 8: Constantly over-expressed extracellular molecules
Rule 9: Human/treatment intervention

## Rule 1: Ligand-receptor binding

$$Lig + Cell(Rec \sim F) \rightarrow Cell(Rec \sim T) \quad brate$$

## Rule 3: Downstream regulation: Encoding Logical Functions as Rules

Given a logical updating function  $Mol_3^{(t+1)} = \neg Mol_1^{(t)} \times (Mol_2^{(t)} + Mol_3^{(t)})$  where “ $Mol_1$ ” is the inhibitor and “ $Mol_2$ ” is the activator of “ $Mol_3$ ”.

$$Cell(Mol_1 \sim F, Mol_2 \sim T, Mol_3 \sim F) \rightarrow$$
$$Cell(Mol_1 \sim F, Mol_2 \sim T, Mol_3 \sim T) \quad \text{trate}$$
$$Cell(Mol_1 \sim T, Mol_3 \sim T) \rightarrow Cell(Mol_1 \sim T, Mol_3 \sim F) \quad \text{trate}$$

## Rule 7: Mutation

$$\text{Cell}(Mol \sim F) \rightarrow \text{Cell}(Mol \sim T) \quad mrate$$
$$\text{Cell}(Mol \sim T) \rightarrow \text{Cell}(Mol \sim F) \quad mrate$$



## Rule 9: Human/treatment intervention

$Cell(Mol \sim T) \rightarrow Cell(Mol \sim F) \quad intrate$

$Cell(Mol \sim F) \rightarrow Cell(Mol \sim T) \quad intrate$

$CancerEnv \rightarrow extraMol \quad intrate$

$extraMol \rightarrow Null() \quad intrate$

## Bounded Linear Temporal Logic (BLTL)

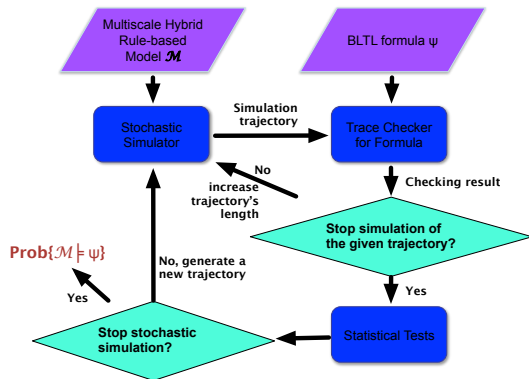
The syntax of BLTL is given by:  $\psi ::= x \sim v \mid \neg\psi \mid \psi_1 \vee \psi_2 \mid \psi_1 U^t \psi_2$

Example BLTL formula:  $\neg F^5 G^{10}(Ras = 1 \wedge P53 = 0)$

F: eventually, G: always, U: until

# Statistical Model Checking to Estimate $Prob_{=?}(\mathcal{M} \models \psi)$

- State Space Exploration unavoidable for complex systems
- Easier to simulate a complex system than to build its transition relation
- Goal: Provide probabilistic guarantees using fewer simulations
- Method: Trace Checker + Statistical Testing Methods



# Results - Three Scenarios

Property	Estimated Prob	# Succ	# Sample	Time (s)	Note
Scenario I: mutated PCCs with no treatments					
1	0.4053	10585	26112	208.91	w.o. PSCs
	0.9961	256	256	1.83	w. PSCs
	0.1191	830	6976	49.69	w.o. PCCs
2	0.9961	256	256	1.75	w. PCCs
	0.9961	256	256	5.21	-
	0.9961	256	256	4.38	-
Scenario II: mutated PCCs with different existing treatments					
5	0.0004	0	2304	17.13	cetuximab and erlotinib
	0.0012	10	9152	68.67	gemcitabine
	0.7810	8873	11360	114.25	nab-paclitaxel
	0.8004	7753	9686	73.83	ruxolitinib
Scenario III: mutated PCCs with blocking out on possible target(s)					
6	0.0792	38363	484128	3727.99	w.o. inhibiting ERK in PSCs
	0.9822	2201	2240	17.37	w. inhibiting ERK in PSCs
7	0.1979	3409	17232	136.39	w.o. inhibiting ERK in PSCs
	0.9961	256	256	2.01	w. inhibiting ERK in PSCs
8	0.2029	2181	10752	92.57	w.o. inhibiting MDM2 in PSCs
	0.9961	256	256	2.18	w. inhibiting MDM2 in PSCs
9	0.0004	0	2304	15.77	w.o. inhibiting RAS in PCCs and ERK in PSCs
	0.9961	256	256	3.15	w. inhibiting RAS in PCCs and ERK in PSCs
10	0.9797	1349	1376	11.98	w.o. inhibiting STAT in PCCs and NF $\kappa$ B in PSCs
	0.1631	1476	9056	81.61	w. inhibiting STAT in PCCs and NF $\kappa$ B in PSCs

## Results - Scenario I: with no treatments

Property 1: To estimate the probability that the population of PCCs will eventually reach and maintain in a high level.

$$Prob_{=?} \{ (PCC_{tot} = 10) \wedge F^{1200} G^{100} (PCC_{tot} > 200) \}$$

Estimated Prob	# Succ	# Sample	Time (s)	Note
0.4053	10585	26112	208.91	w.o. PSCs
0.9961	256	256	1.83	w. PSCs

## Results - Scenario I: with no treatments

Property 2: To estimate the probability that the number of migrated PSCs will eventually reach and maintain in a high amount.

$$Prob_{=?} \{ (MigPSC = 0) \wedge F^{1200} G^{100} (MigPSC > 40) \}$$

Estimated Prob	# Succ	# Sample	Time (s)	Note
0.1191	830	6976	49.69	w.o. PCCs
0.9961	256	256	1.75	w. PCCs

## Results - Scenario II: with existing treatments

Property 5: To estimate the probability that the population of PCCs will eventually drop to and maintain in a low amount.

$$Prob_{=?} \{ (PCC_{tot} = 10) \wedge F^{1200} G^{400} (PCC_{tot} < 100) \}$$

Estimated Prob	# Succ	# Sample	Time (s)	Note
0.0004	0	2304	17.13	cetuximab and erlotinib
0.0012	10	9152	68.67	gemcitabine
0.7810	8873	11360	114.25	nab-paclitaxel
0.8004	7753	9686	73.83	ruxolitinib

# Results - Scenario III: block out possible target(s)

## Targeting at ERK in PSCs

Property 6: To estimate the probability that the number of PSCs will eventually drop to and maintain in a low level.

$$Prob_{=?} \{ (PSC_{tot} = 5) \wedge F^{1200} G^{400} (PSC_{tot} < 30) \}$$

Property 7: To estimate the probability that the population of migrated PSCs will eventually stay in a low amount.

$$Prob_{=?} \{ (MigPSC = 0) \wedge F^{1200} G^{100} (MigPSC < 30) \}$$

Property	Estimated Prob	# Succ	# Sample	Time (s)	Note
6	0.0792	38363	484128	3727.99	not inhibit
	0.9822	2201	2240	17.37	inhibit
7	0.1979	3409	17232	136.39	not inhibit
	0.9961	256	256	2.01	inhibit



## Results - Scenario III: block out possible target(s)

Property 8: To estimate the probability that the number of PSCs entering the proliferation phase will eventually be less than the number of PSCs starting the apoptosis programme and this situation will maintain. (Target at MDM2 in PSCs)

$$Prob_{=?} \{F^{1200} G^{400} ((PSCPro - PSCApop) < 0)\}$$

Estimated Prob	# Succ	# Sample	Time (s)	Note
0.2029	2181	10752	92.57	not inhibit
0.9961	256	256	2.18	inhibit

## Results - Scenario III: block out possible target(s)

Property 9: To estimate the probability that the number of bFGF will eventually stay in such a low level. (RAS in PCCs and ERK in PSCs)

$$Prob_{=?} \{F^{1200} G^{400} (bFGF < 100)\}$$

Estimated Prob	# Succ	# Sample	Time (s)	Note
0.0004	0	2304	15.77	not inhibit
0.9961	256	256	3.15	inhibit

## Results - Scenario III: block out possible target(s)

Property 10: To estimate the probability that the concentration of VEGF will eventually reach and keep in a high level. (STAT3/4 in PCCs and NF $\kappa$ B in PSCs)

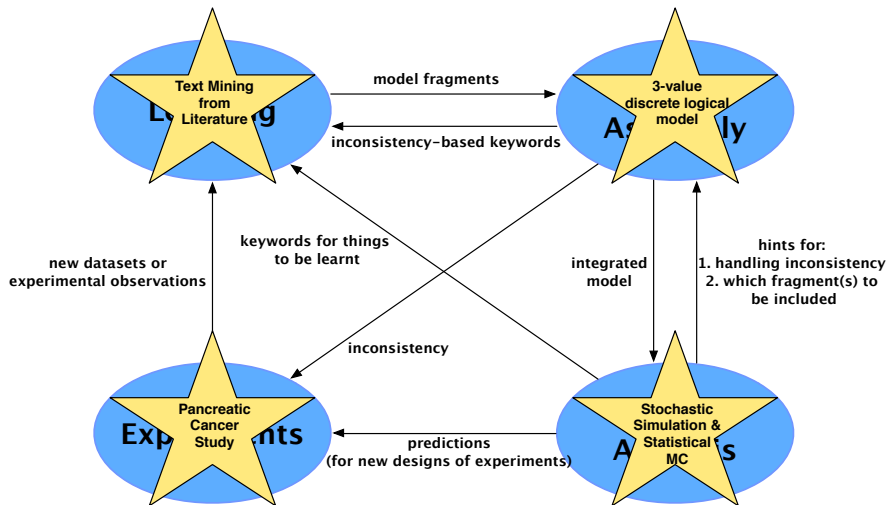
$$Prob_{=?} \{F^{400} G^{100} (VEGF > 200)\}$$

Estimated Prob	# Succ	# Sample	Time (s)	Note
0.9797	1349	1376	11.98	not inhibit
0.1631	1476	9056	81.61	inhibit

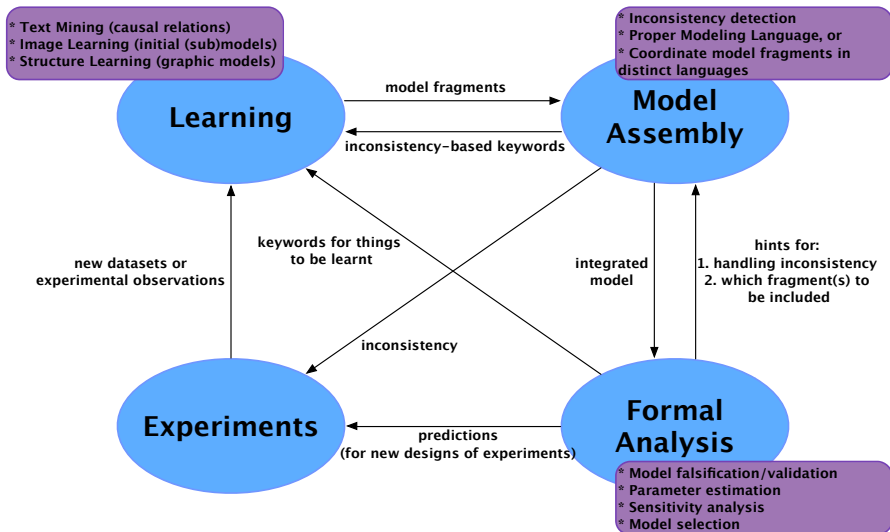
# Conclusion

- Construct a multicellular and multiscale model
- Propose a language for multiscale biological systems using continuous and discrete rules
- Apply stochastic simulation and StatMC to analyze system behaviors under different conditions
- Confirm experimental findings
- Gain insights on how existing treatments latching onto different targets can lead to distinct outcomes
- Predict potential new targets aiming at depleting PSCs and inhibiting the PC development

# Future Work



# Future Work



Thanks for your time! ~~Questions?~~

## Workshop on Formal Methods for Biological and Biomedical Systems (FMBBS)

In conjunction with the 2016 IEEE International Conference on Bioinformatics and Biomedicine, Shenzhen, China, Dec 15-18, 2016



[Home](#)

[Call for Papers](#)

[Organization](#)

[Accepted Papers](#)

[Invited Speakers](#)

[Program](#)

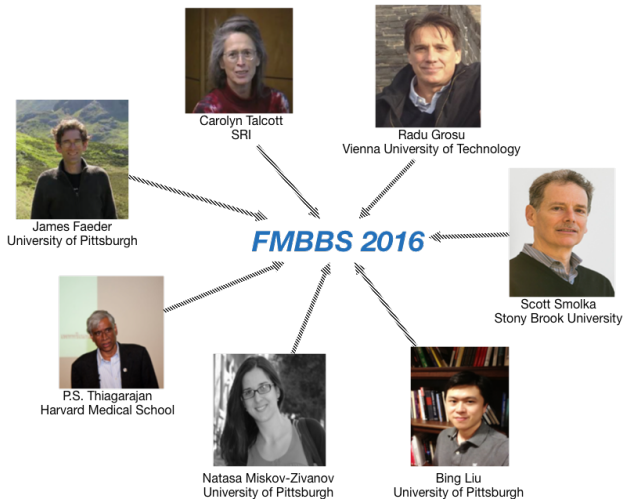
[Venue](#)

[Registration](#)

## FMBBS 2016

As biomedical research advances into more complicated systems, there is an increasing need to model and analyze these systems to better understand them. For decades, biologists have been using diagrammatic models to describe and understand the mechanisms and dynamics behind their experimental observations. Although these models are simple to build and understand, they offer only a rather static picture of the corresponding biological systems, and scalability is limited. Formal specification and analysis methods, such as model checking techniques, hold great promise in promoting further discovery and innovation for complicated biochemical systems. Models can be tested and adapted inexpensively in silico to provide new insights. However, development of accurate and efficient modeling methodologies and analysis techniques for biochemical systems is still an open challenge. This workshop will provide an opportunity for practitioners to present their work in this area to both computer scientists





Questions?