

# Today's Lecture



- Structural generators
- Power laws, HOT graphs, ..
- · Assigned reading
  - A First Principles Approach to Understanding the Internet's Router-level Topology
  - Measuring ISP Topologies with Rocketfuel (2 sections)
- · Optional reading:
  - On Power-Law Relationships of the Internet Topology

# Outline

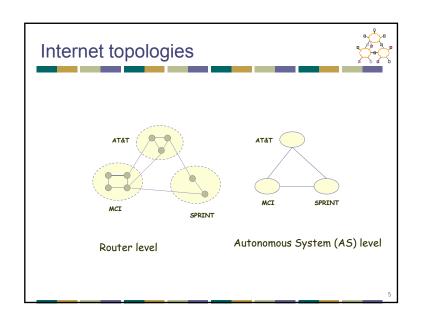


- · Motivation/Background
- Power Laws
- Optimization Models
- Measuring Topology

# Why study topology?



- Correctness of network protocols typically independent of topology
- Performance of networks critically dependent on topology
  - e.g., convergence of route information
- Internet impossible to replicate
- Modeling of topology needed to generate test topologies



## More on topologies..



- Router level topologies reflect physical connectivity between nodes
  - Inferred from tools like traceroute or well known public measurement projects like Mercator and Skitter
- AS graph reflects a peering relationship between two providers/clients
  - Inferred from inter-domain routers that run BGP and publlic projects like Oregon Route Views
- Inferring both is difficult, and often inaccurate

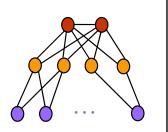
# Hub-and-Spoke Topology

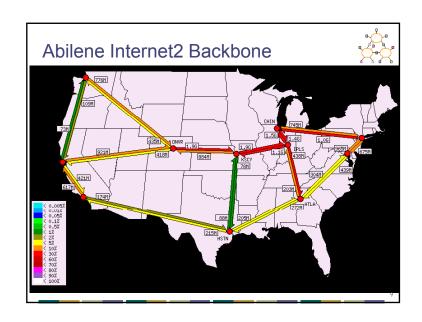


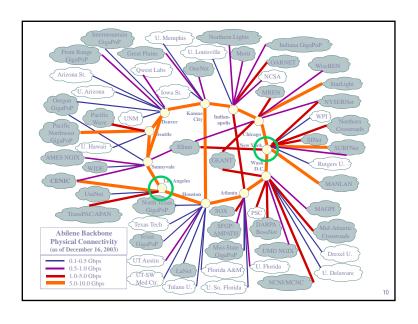
- Single hub node
  - · Common in enterprise networks
  - · Main location and satellite sites
  - · Simple design and trivial routing
- Problems
  - Single point of failure
  - · Bandwidth limitations
  - · High delay between sites
  - · Costs to backhaul to hub

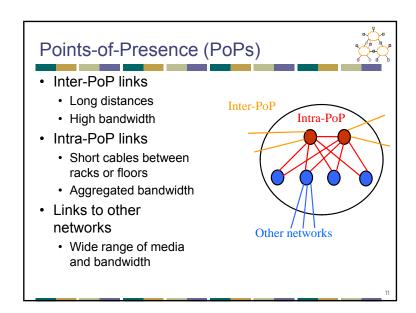
# Simple Alternatives to Hub-and-Spoke

- Dual hub-and-spoke
  - Higher reliability
  - Higher cost
  - Good building block
- · Levels of hierarchy
  - Reduce backhaul cost
  - Aggregate the bandwidth
  - Shorter site-to-site delay









# Deciding Where to Locate Nodes and Links

- Placing Points-of-Presence (PoPs)
  - Large population of potential customers
  - · Other providers or exchange points
  - · Cost and availability of real-estate
  - · Mostly in major metropolitan areas
- Placing links between PoPs
  - · Already fiber in the ground
  - Needed to limit propagation delay
  - · Needed to handle the traffic load

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## Trends in Topology Modeling



#### Observation

- · Long-range links are expensive
- Real networks are not random, but have obvious hierarchy
- Internet topologies exhibit power law degree distributions (Faloutsos et al., 1999)
- Physical networks have hard technological (and economic) constraints.

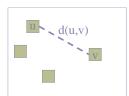
#### **Modeling Approach**

- Random graph (Waxman88)
- Structural models (GT-ITM Calvert/Zegura, 1996)
- Degree-based models replicate power-law degree sequences
- Optimization-driven models topologies consistent with design tradeoffs of network engineers

Waxman model (Waxman 1988)



- Router level model
- Nodes placed at random in 2-d space with dimension L
- Probability of edge (u,v):
  - a \* exp{-d / (b \* L)}
  - d is Euclidean distance (u,v)
  - · a and b are constants
- · Models locality



# Real world topologies

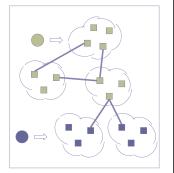


- Real networks exhibit
  - Hierarchical structure
  - Specialized nodes (transit, stub..)
  - · Connectivity requirements
  - Redundancy
- Characteristics incorporated into the Georgia Tech Internetwork Topology Models (GT-ITM) simulator (E. Zegura, K.Calvert and M.J. Donahoo, 1995)

Transit-stub model (Zegura 1997)



- Router level model
- · Transit domains
  - placed in 2-d space
  - · populated with routers
  - · connected to each other
- Stub domains
  - · placed in 2-d space
  - populated with routers
  - connected to transit domains
- Models hierarchy



#### So...are we done?



- No!
- In 1999, Faloutsos, Faloutsos and Faloutsos published a paper, demonstrating power law relationships in Internet graphs
- Specifically, the node degree distribution exhibited power laws

That Changed Everything.....

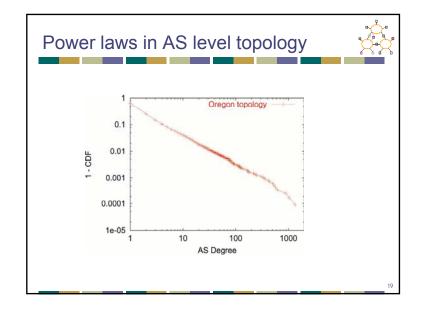
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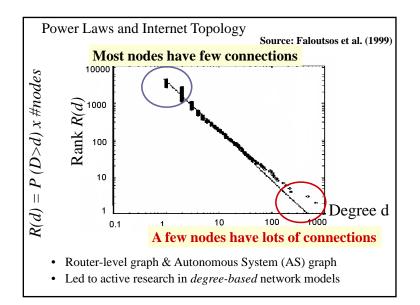
#### Outline



- · Motivation/Background
- Power Laws
  - Slides John Dickerson
- Optimization Models
- Measuring Topology

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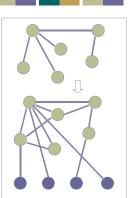
#### GT-ITM abandoned..

- GT-ITM did not give power law degree graphs
- New topology generators and explanation for power law degrees were sought
- Focus of generators to match degree distribution of observed graph

Inet (Jin 2000)



- Generate degree sequence
- Build spanning tree over nodes with degree larger than 1, using preferential connectivity
  - randomly select node u not in tree
  - join u to existing node v with probability d(v)/∑d(w)
- Connect degree 1 nodes using preferential connectivity
- Add remaining edges using preferential connectivity



Power law random graph (PLRG)



- Operations
  - assign degrees to nodes drawn from power law distribution
  - create kv copies of node v; kv degree of v.
  - randomly match nodes in pool
  - · aggregate edges



may be disconnected, contain multiple edges, self-loops

contains unique giant component for right choice of parameters

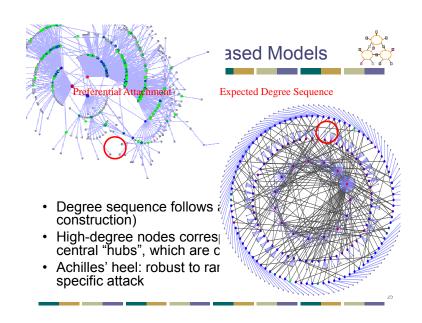
Barabasi model: fixed exponent



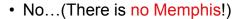
- · incremental growth
  - initially, m0 nodes
  - step: add new node i with m edges
- linear preferential attachment
  - connect to node i with probability ki /  $\sum$  kj



may contain multi-edges, self-loops



### Does Internet graph have these properties?



- Emphasis on degree distribution structure ignored
- Real Internet very structured
- · Evolution of graph is highly constrained

# **Problem With Power Law**



- ... but they're descriptive models!
- No correct physical explanation, need an understanding of:
  - the driving force behind deployment
  - · the driving force behind growth

#### Outline

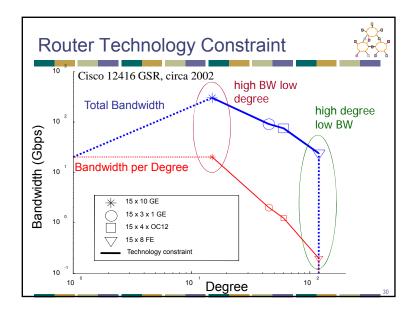


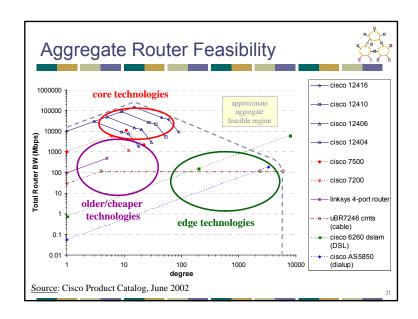
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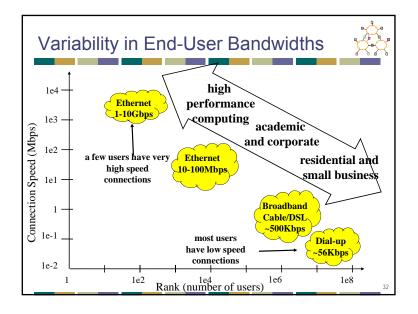
#### Li et al.

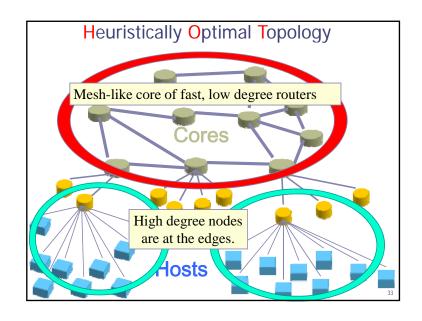


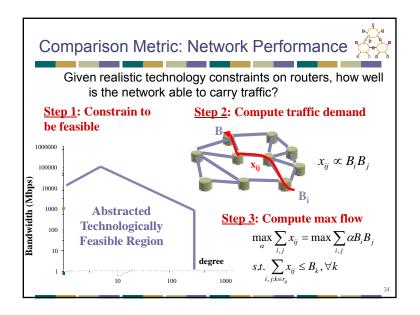
- · Consider the explicit design of the Internet
  - Annotated network graphs (capacity, bandwidth)
  - · Technological and economic limitations
  - · Network performance
- Seek a theory for Internet topology that is explanatory and not merely descriptive.
  - · Explain high variability in network connectivity
  - Ability to match large scale statistics (e.g. power laws) is only secondary evidence









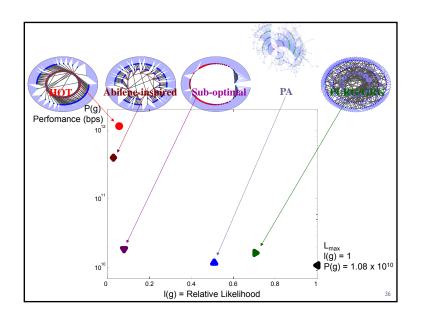


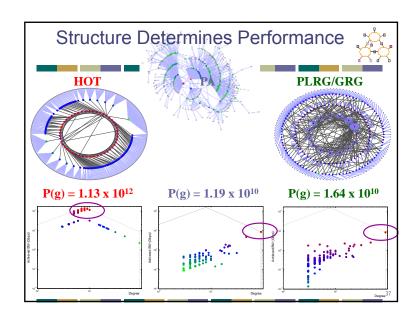
### Likelihood-Related Metric



Define the metric  $L(g) = \sum_{\substack{i,j \text{connected} \\ \text{connected}}} d_i d_j$   $(d_i = \text{degree of node } i)$ 

- · Easily computed for any graph
- Depends on the structure of the graph, not the generation mechanism
- · Measures how "hub-like" the network core is
- Graphs that connect nodes with high (low) degree will have high value
- · Used here to distinguish between different graphs
  - Has a more specific meaning in the context of the general model of random graphs





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  - · Slides John Wright

# **Summary Network Topology**



- Faloutsos<sup>3</sup> [SIGCOMM99] on Internet topology
  - Observed many "power laws" in the Internet structure
    - Router level connections, AS-level connections, neighborhood sizes
  - Power law observation refuted later, Lakhina [INFOCOM00]
- Inspired many degree-based topology generators
  - Compared properties of generated graphs with those of measured graphs to validate generator
  - What is wrong with these topologies? Li et al [SIGCOMM04]
    - · Many graphs with similar distribution have different properties
    - Random graph generation models don't have network-intrinsic meaning
    - Should look at fundamental trade-offs to understand topology
      Technology constraints and economic trade-offs
    - Graphs arising out of such generation better explain topology and its properties, but are unlikely to be generated by random processes!

### **Announcements**



- · No lecture Friday and Monday
- Next course segment is on overlay networks and future Internet architecture
  - Readings are up to date for the semester
  - May need to reshuffle final few lectures a bit
- Project update: good progress but need to become more concrete quickly
  - · What will be your initial results?
  - Timeline for the remaining seven weeks?
  - Short reports on status by Oct 28 (e-mail)

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