

$$P(D|\theta)P(\theta)$$

$$= \theta^{\alpha_H} (1-\theta)^{\alpha_T} \theta^{\beta_H-1} (1-\theta)^{\beta_T-1}$$

$$\ln \frac{L(\theta)}{L(\theta)} = (\alpha_H + \beta_H - 1) \ln \theta + (\alpha_T + \beta_T - 1) \ln(1-\theta)$$

$$\frac{\alpha_H + \beta_H - 1}{\theta} = \frac{\alpha_T + \beta_T - 1}{1-\theta} = 0$$

$$q = \frac{\#M}{n}$$

$$q = \frac{\#M+1}{n+1}, \quad q = \frac{\#M}{n+1}$$

$$P(D|\theta) = P(X|\theta) = \prod_i P(x_i|\theta)$$

$$\frac{P}{M} = \prod \left[\frac{1}{2\pi \sqrt{\sigma^2}} e^{-\frac{(x_i - \mu)^2}{2\sigma^2}} \right]$$