Data Mining Meets Performance Evaluation: Fast Algorithms for Modeling Bursty Traffic

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Abstract

Network, web, and disk I/O traffic are usually bursty, self-similar [9, 3, 5, 6] and therefore can not be modeled adequately with Poisson arrivals[9]. However, we do want to model these types of traffic and to generate realistic traces, because of obvious applications for disk scheduling, network management, web server design.

Previous models (like fractional Brownian motion, FARIMA etc) tried to capture the 'burstiness'. However, the proposed models either require too many parameters to fit and/or require prohibitively large (quadratic) time to generate large traces. We propose a simple, parsimonious method, the b-model *, which solves both problems: It requires just one parameter, and it can easily generate large traces. In addition, it has many more attractive properties: (a) With our proposed estimation algorithm, it requires just a* single *pass over the actual trace to estimate* b*. For example, a one-day-long disk trace in milliseconds contains about 86Mb data points and requires about 3 minutes for model fitting and 5 minutes for generation. (b) The resulting synthetic traces are very realistic: our experiments on real disk and web traces show that our synthetic traces match the real ones very well in terms of queuing behavior.*

1 Introduction

A number of different types of traffic (e.g. Ethernet [9], web [3], video [5] and disk [6] traffic) are self-similar for a wide range of time scales. Such traffic also typically exhibits significant burstiness. Given these relatively recent observations, many standard methods for traffic generation are fundamentally flawed, since they do not incorporate these basic facts.

Of these standard methods, the Poisson arrival model is by far the most commonly and widely used. It has the highly desirable properties of being relatively straightforward and easy to grasp. It is also very concise, since it relies on very few parameters that can be easily estimated from real data. Unfortunately, the traffic it generates is neither self-similar, nor bursty.

A number of other methods have been proposed recently, such as the multiple ON/OFF source aggregation process. Many others draw from and combine self-similar processes from statistics. However, many of these methods are quite complicated or ad-hoc and they employ models that are fine-tuned only to particular classes of traffic. Others suffer from a very large number of parameters. As a result, the parameter estimation and traffic generation processes often require significant computational effort.

We propose a simple and elegant model which has the same desirable properties as the Poisson model. Namely, it is based on a simple and straightforward fundamental process. It relies on very few parameters, which can be easily estimated from actual data. However, although simple, it is powerful enough to successfully characterize self-similar, bursty traffic for a wide range of time scales. It is general enough to be applicable to a wide range of domains. The main goal of the present paper is to describe our model and demonstrate its usefulness in a variety of domains.

An important problem we chose to demonstrate our method is I/O traffic modeling, which is a very difficult problem [4]. Besides being useful for accurate evaluation of disk subsystem performance, a good model is crucial in the very design of such a system. If a scheduling algorithm is to be successful, an understanding of the common traffic patterns is necessary. Furthermore, a simple and fast model could be incorporated directly in access prediction and prefetching subsystems and we are currently working towards that goal.

Furthermore, previous work seldom used domain-specific metrics for evaluation. Most comparisons are based on intrinsic statistical properties of the traces themselves (such as variance, autocorrelation, etc.). Although these are important properties, what matters in the end is how a real system behaves under any given workload. Choosing a particular application domain allows us to compare the real and synthetic traces using detailed simulation. Based on these simulations, we show how the synthetic traces match the real ones in terms of queueing delay and interarrival time distributions.

Our model has only one parameter. Compared to other models, the algorithms involved in our model are extremely efficient. Model fitting is linear and our implementation gives an accurate estimation in less than 3 minutes for a one day-long disk trace in millisecond resolution (more than 86Mb data points). Generation of synthetic traces scales linearly to the trace length and it generates a realistic one-day-long disk trace in 5 minutes.

The b-model is closely related to the well-known "80/20 law" in databases: 80% of the queries access 20% of the data. In fact, most of the distributions in the real world follow the "80/20 law" [7], even in other domains (such as ore and population distributions, highway traffic patterns, or photon distributions in electro-magnetic cavity radiation).

The paper is organized as follows. We give a brief overview of related work in the next section. Section 3 provides some background information on self-similarity. The b-model is introduced in section 4, which also presents the model fitting algorithm and its derivation, as well as the trace generation algorithm. We evaluate the model using several real data sets in section 5. Section 6 presents our conclusions.

2 Survey

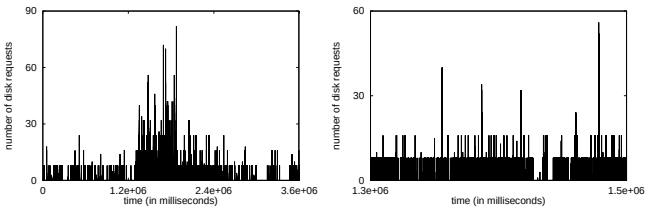
Modeling of bursty time sequences has recently received considerable attention in the literature. Most real-world traffic is self-similar and bursty (e.g. Ethernet [9], web [3], video [5] and disk [6] traffic). This renders many standard methods (such as Poisson arrivals) useless. A comprehensive overview of the area can be found at [14].

A number of models that use self-similar processes have been proposed. For example, Gartett and Willinger [5] used a fractional ARIMA process to generate synthetic Variable Bit Rate (VBR) video traces. Since the model itself is not intrinsically bursty, it is fed with the logarithm of the data in order to create the requisite burstiness.

Barford and Crovella [1] took another approach in the SURGE web trace generator. They aggregate a large number of ON/OFF heavy tailed distributions to synthesize self-similar web traffic. Gomez [6] employed a similar method to synthesize I/O access traces.

All the models mentioned above require the estimation of a large number of parameters from the original traces. This usually results in high computational costs for model fitting and synthetic trace generation. Also, the evaluation done in this previous work focuses on intrinsic, statistical properties of the real and synthesized workloads.

Another approach similar to ours is taken by Ribeiro et al. [10]. Their Multifractal Wavelets used a similar multiplicative cascading process to generate web traces. Their evaluation is based on the queuing behavior from a simulator. However, their model requires fitting more parameters than ours.



(a) A one-hour disk trace collected on a Unix workstation

(b) Part of the trace, from $t = 1300$ sec, length 200 sec.

Figure 1. Self-similarity of disk traffic. Shown in (b) is a portion of the trace in (a) (total number of disk requests per millisecond). Note that is very similar to the original trace. Self-similar sequences have this property across all (or, in practice, a very wide range) of time scales. Each disk request is of 1 KB.

The b-model presented here is very concise; only one parameter is enough to describe the entire trace. The model is accurate in terms of domain-specific properties such as interarrival time distribution and queuing behavior. Furthermore, the model fitting and trace generation algorithms are linear and require only a single pass on the data. It would therefore be possible to integrate them in network or disk devices (which typically have constrained resources) and use them to collect data on the fly and "learn" the traffic characteristics in real-time.

3 Background: Self-Similarity

After the initial discovery that Ethernet traffic is self-similar [9], a high degree of self-similarity has been observed in many other types of traffic (e.g. TCP [11], video [5], web [3], file system [8], and disk I/O [6] traffic). In this section we give a brief overview of self-similar processes.

Informally, *self-similarity* means invariance with respect to scaling across all time scales. "Invariance" may mean exact identity, in which case we speak of *deterministic* self-similarity. However, it may imply identical statistical properties, in which case we have *statistical* self-similarity. Figure 1 shows the self-similarity in the cello disk traces from [12]. The particular trace records the activities on 8 disks and the figure shows an hour-long trace from disk 2. The number (or *volume*) of disk requests is plotted against time in millisecond resolution in (a) and portion of it in (b); the enlarged portion in a finer scale is statistically similar to the entire trace viewed in a larger time scale.

For these bursty I/O workloads, the traditional Poisson arrival assumption fails horribly because it generates smooth traffic and fails to capture the peaks and troughs of the real data. If we assume the arrival process is Poisson with the same total volume of disk requests, the traffic is very smooth with just 1 or 2 disk requests occurring most of the time.

Symbol	Definition
Y	A time series data (e.g., no. of disk requests)
$Y^{(n)}$	Aggregated Y at aggregation level n.
H	Hurst exponent
l	Length of Y (i.e., number of time ticks)
N	Total volume of Y (e.g., total number of disk requests)
b	Bias in the b-model
$E^{(n)}$	Entropy of Y at aggregation level n
E_b	$-b\log_2 b - (1-b)\log_2(1-b)$

Table 1. Important symbols.

A common measure of self-similarity in the literature is the *Hurst exponent* H [2]. A value of H between $\frac{1}{2}$ and 1 indicates the degree of self-similarity. It is also used as a *global*[1] index for burstiness [9]. There are several exploratory analytic tools to estimate H, such as R/S plots, variance plots, autocorrelation functions, and periodograms [2].

We will very briefly explain the R/S and variance plots, since we will use them to detect self-similarity in the real traces. The *R/S plot* shows the average rescaled range against the window size in log-log scale by aggregating the original data set into equal-sized windows. The *variance plot* show the variance of the data against the window size in log-log scale. The points should approximate a line for a self-similar signals and the slope of both plots can be used to estimate the Hurst exponent.

However, self-similar processes don't always generate bursty time sequences. The parameter H focuses more on the behavior across large time scales. In the next section, we will introduce the b-model , which is intrinsically bursty and matches the irregularity of the original data at fine time scales.

4 Modeling I/O Workloads with the b-model

The b-model has two main advantages. The model is concise; it requires only one parameter, bias b, to describe the burstiness of the entire traces. More importantly, model fitting and synthetic trace generation are very efficient and scale linearly with respect to the data set size.

In the following sections we first introduce the b-model and then present our main theoretical results. The derivation of the model fitting and synthetic trace generation algorithms is presented last. Table 1 lists important symbols used in the paper.

4.1 The b-model

The b-model is closely related to the "$80/20$ law" in databases[7]: 80% of the queries involve 20% of the data. In the b-model , a 'bias' parameter $b = 0.8$ means that, within a given time interval, 80% of the accesses happen on one half of the time interval (and the remaining 20% in the other half) and this continues recursively. More specifically, the whole construction begins with a uniform interval and recursively subdivides the number of accesses to each half, quarter, eighth, etc. according to the bias b.

Thus, step $n+1$ ends with a total of 2^{n+1} time intervals, which are obtained by splitting each of the 2^n points from step n according to the formula:

$$\begin{aligned} Y^{(n+1)}(2i) &= bY^{(n)}(i) \\ Y^{(n+1)}(2i+1) &= (1-b)Y^{(n)}(i) \end{aligned}$$

for $i = 0, 1, \ldots, 2^n - 1$ and $b \in [0.5, 1)$. The superscript of $Y^{(n)}$ indicates the current step and is also called the *aggregation level*. The above formulae are for the *deterministic* version of the model, where the split is always done in the same direction. The value of Y after step n is

$$Y^{(n)}(i) = b^j(1-b)^{n-j}, \qquad i = 0, \ldots, 2^n - 1 \qquad (1)$$

where j is the number of times the data point falls into the left half of the split. Figure 2 (a) gives the first 3 steps of the construction process and (b) shows a sample trace with $b = 0.7$ of length 1024 with total volume of 4096 with b always on the left. In real trace generation, we let b go randomly to left or right to create some randomness in the synthetic trace.

Note that all the data points always sum up to 1 (or, in general, the total volume N—we omit this factor for simplicity here):

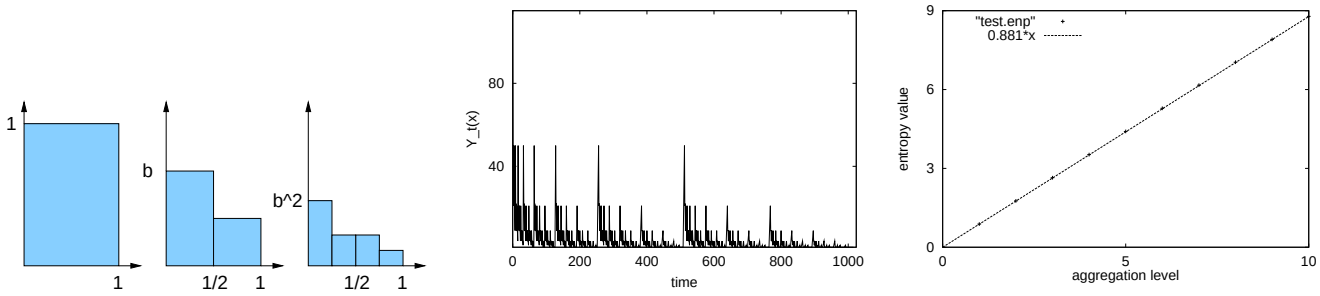
$$\begin{aligned} \sum_{i=0}^{2^n-1} Y^{(n)}(i) &= \sum_{i=0}^{2^n-1} b^j(1-b)^{k-j} \\ &= ((1-b)+b)^n \\ &= 1. \end{aligned}$$

The recursive construction process guarantees the self-similarity of the b-model data. The closer b is to 1, the higher the irregularity of the data. A b value of 0.5 gives a uniform data.

4.2 Theoretical Results

We will now discuss our main theoretical results. The central relation we derive is between entropy and the bias b. This is a fundamental result and the basis for our model fitting algorithm. We also present the relationship of our model to previous work, and in particular to the Hurst exponent.

[1] Other quantities, such as the Hölder exponent (also known as the irregularity index), are used to characterize the burstiness around a *particular* point in a signal.



(a) b-model generation (b) A sample b-model data (c) Entropy plot for (b)

Figure 2. B-model. The sample data of bias 0.7 shows a slope of 0.881 in entropy plot.

4.2.1 Entropy and Bias

First, we briefly re-introduce the concept of entropy. *Entropy* measures the uniformity of a discrete probability function. Equation 2 gives the entropy value of the probability function P, where $P\{E_i\} = p_i$, $0 \leq i \leq n$, $\sum_{i=0}^{n} p_i = 1$. p_i is the probability that event E_i will happen.

$$E(P) = \sum_{i=1}^{n} p_i \log_2 \frac{1}{p_i}. \tag{2}$$

Given fixed number of events, n, the entropy reaches the maximum value when all the p_is have the same value. The entropy approaches 0 when one event dominates. Therefore, the entropy indicates the degree of unevenness of the probabilities.

Entropy can be used to describe the burstiness of the traffic data. Given a b-model data, the $Y^{(n)}$ values can be viewed as p_is for a probability function since $\sum Y^{(n)}(i) = 1$[2]. The burstiness of the data at aggregation level n, then, can be found by calculating the entropy value of the $Y^{(n)}$.

$$E^{(n)} = -\sum_{i=0}^{2^n-1} Y^{(n)}(i) \log_2 Y^{(n)}(i). \tag{3}$$

Plotting the entropy values against the aggregation levels gives the *entropy plot*.

Theorem 1 *The entropy of the 2^n data points at aggregation level n generated by the b-model with bias b is*

$$E^{(n)} = nE_b.$$

where $E_b \equiv E^{(1)} = -b\log_2 b - (1-b)\log_2(1-b)$ is the entropy at aggregation level 1.

Proof: See [13] for proof.

[2]In general, $\sum Y_t = N$, the total volume, in which case we can simply take Y_t/N.

The above theorem suggests linear entropy plots for b-model . Figure 2(c) shows the entropy plot for the synthetic trace in Figure 2(b). The points form a line of slope 0.881, which corresponds to bias 0.7 according to Equation 2.

4.2.2 Hurst Exponent

Previous work on self-similar processes, both in computer science and in a number of other fields (e.g., physics, hydrology, etc.), depends heavily on Hurst exponent as a measure of burstiness. Therefore, it is expected that the bias in b-model is closely related to *Hurst exponent*.

Theorem 2 *The Hurst exponent H (as estimated from the variance plot) of a trace generated with the b-model using bias b follows the following approximate relation:*

$$\hat{H}_b \approx \frac{1}{2} - \frac{1}{2}\log_2(b^2 + (1-b)^2). \tag{4}$$

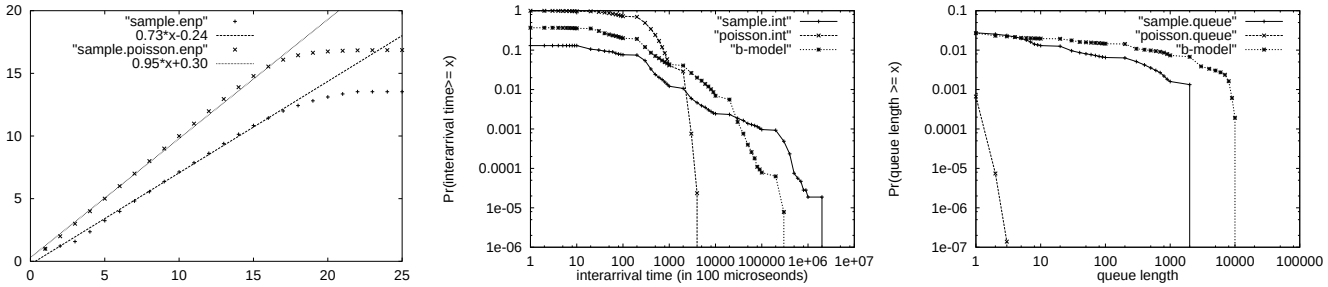
Proof: See [13] for proof.

The above theorem provides a method to find the bias b for a given trace. Solving Equation 4 gives the bias after the Hurst exponent is estimated from the R/S plot or variance plot. However, the approximation in the equation requires b to be close to 1. Thus, the estimation is not accurate for lower degrees of burstiness. Instead, we use entropy plot for model fitting.

4.3 Model Fitting

The close relationship between the bias and E_b given by Equation 2 provides yet another way to find the best bias for a given trace. The bias can be solved from the equation after E_b is estimated from the trace. The slope of the entropy plot for a given data set is a good estimation for E_b when the entropy plot is linear. Fortunately, self-similarity of real world traffic data ensures linear entropy plots because the burstiness of the data is stable across all the aggregation levels.

Computing the entropy plot for a given trace is to find the entropy value of the trace by aggregating it in different



(a) Entropy plot

(b) Interarrival time distribution

(c) Queue length distribution

Figure 3. Comparison between the b-model and Poisson arrival in entropy plot, interarrival time distribution, and queuing behavior. Poisson arrival, having a slope close to 1 in the entropy plot, generates smooth traffic and results in short queue length. The b-model , on the other hand, produces bursty traffic and simulates the original traffic very well.

bucket sizes. Suppose that the original trace has 2^n data points (for simplicity, we truncate the traces so their length is a power of 2). We can aggregate it into 2, 4, 8, etc. buckets (corresponding to aggregation levels 1, 2, 3, etc.) and calculate the entropy for each number of buckets. Once again, $E^{(n)}$ is the entropy for at aggregation level n (i.e., for 2^n buckets).

A naive implementation needs one scan for each aggregation level. However, note that all the passes are independent. Thus, they can be integrated into one and $E^{(1)}, E^{(2)}, \ldots, E^{(n)}$ can be calculated simultaneously, in a single pass.

In Figure 3 (a), we show the entropy plot for the sample data shown from Figure 1(a). We should note that the entropy plot tail is flat because we are using integer values for Y. The entropy plot shows a perfect fit for a line with slope 0.73. This indicates that the irregularity of the data stays the same for all aggregation levels. Otherwise, the slope would change at each aggregation level. Given Theorem 1, we can use the slope to estimate the bias b. The bias turns out to be 0.795 for the sample trace. In contrast, a Poisson arrival process with the same total volume of data works like the b-model with bias 0.5. The entropy value scales linearly in this case as well, but with a slope close to 1 which means an essentially uniform trace.

We compare the Poisson arrival process to the b-model using several different tools in Figure 3. The synthetic trace is generated using the b-model with bias 0.795. The interarrival time distribution and queuing behavior of the synthetic data is similar to the original trace, while the Poisson arrival gives really smooth traffic, thus, exhibiting markedly different behavior in both the interarrival time and queue length. In fact, the Poisson process could be viewed as a "special case" of the b-model . When we use bias close to 0.5, the generated data is very close to Poisson arrivals, particularly in terms of burstiness.

Algorithm 1 *Efficient b-model Data Generation*
INPUT: Bias b, aggregation level n, total volume N
OUTPUT: Y_t with 2^n points following the b-model
ALGORITHM: A stack is used to keep track of the data points.

1. *Initialize the stack and push pair (0, N) onto the stack.*
2. *If the stack is empty, all the 2^n data points have been generated and the process ends.*
3. *Pop a pair (k, v) from the stack. If $k = n$, output v as the next data point and go back to Step 2.*
4. *Flip a coin. If heads, push pairs $(k+1, v \times b)$ and $(k+1, v \times (1-b))$ onto the stack. Otherwise, push pairs $(k+1, v \times (1-b))$ and $(k+1, v \times b)$ onto the stack. Go back to Step 2.*

Figure 4. Data generation using the b-model

4.4 Trace Generation

Although the b-model requires estimation of only one parameter (b), two more parameters are needed to generate the traces: total volume N and aggregation level n. N is simply the total number of requests in the output trace. The aggregation level n determines the number of data points that will be generated; that is, $l = 2^n$. In practice, we can easily extend the algorithm to generate traces of arbitrary length.

A straightforward implementation is to build the model by exactly following the construction in subsection 4.1, step-by-step for each aggregation level. In this case, the time required, expressed in terms of multiplication opera-

tions, is

$$T_{\text{naive}}(l) = 1 + 2 + \cdots + \log_2 l = O(l).$$

To output 2^n data points, we need to keep track of the 2^{n-1} data points in the next-to-last aggregation level. Thus, the space is at least is at least 2^{n-1}, i.e.

$$S_{\text{naive}}(l) = l/2 = O(l).$$

A more efficient way is to use a stack, as described in Figure 4. First, the total volume N (which is the value of the trace at aggregation level 0) is pushed onto the stack. At each step, the algorithm examines the value at the top of the stack. Conceptually, each point is associated with an aggregation level (although, in practice, that can be deduced from the size of the stack and does not need to be stored). The algorithm outputs the data point, if its aggregation level is n. Otherwise, the top data point is split according to the bias b and replaced by the two new points of a higher aggregation level.

At any time during the process, the aggregation level of the data points in the stack is 1, 2, etc., from bottom up. The size of the stack reaches its maximum when the aggregation level of the top data point is n. Therefore, the maximum size of the stack is n.

Lemma 1 *The time and space requirements of the efficient generation algorithm are*

$$T_{\text{efficient}}(l) = l/2 = O(l)$$

$$S_{\text{efficient}}(l) = n = O(\log_2 l)$$

Proof: Follows from the previous observations.

Although the time requirements are the same, the space requirements are just logarithmic with respect to the data set size.

5 Experiments

In this section, we evaluate our model on two kinds of data sets: disk and web traces. Summary of the data sets are in Table 2. All show high degrees of self-similarity and burstiness. We use the entropy plot to estimate b and compare the generated traces to real ones in terms of domain-specific properties: interarrival time and queue length distribution.

The disk traces were captured on an HP-UX workstation with 8 drives [12]. All traces are one day long. From these we use the following: `Disk-a` aggregates all accesses on all disks. `Disk-r` aggregates only reads-accesses and `Disk-w` only write-accesses. `Disk0`, `Disk2`, `Disk7` are the activities on three individual disks (the remaining 5 disks are almost always idle and thus not particularly interesting). The disk traces are in resolution of milliseconds, so all the traces have about 86M data points in it. We use the number of requests in the experiment. Each request is for a 1 Kbyte block. The resolution of milliseconds for disk I/O workloads is good enough, since the service time is usually a couple of milliseconds.

Name	Description	N	$\hat{b}$
`Disk-a`	all disks aggregated	4,575,798	0.837
`Disk-r`	reads on all disks	1,822,781	0.748
`Disk-w`	writes on all disks	3,300,628	0.763
`Disk0`	requests on disk 0	1,101,416	0.800
`Disk2`	requests on disk 2	1,396,649	0.726
`Disk7`	requests on disk 7	371,320	0.837

(a) Disk trace summary (length 86,400,000)

Name	Description	N (in Kb)	$\hat{b}$
`lbl-all`	All activities	28,678,088,807	0.705
`lbl-nntp`	nntp activities	11,564,204,118	0.619
`lbl-smtp`	smtp activities	989,984,211	0.747
`lbl-ftp`	ftp activities	10,268,918,659	0.789

(b) Web trace summary (length 2,592,000,000)

Table 2. Description of the data sets.

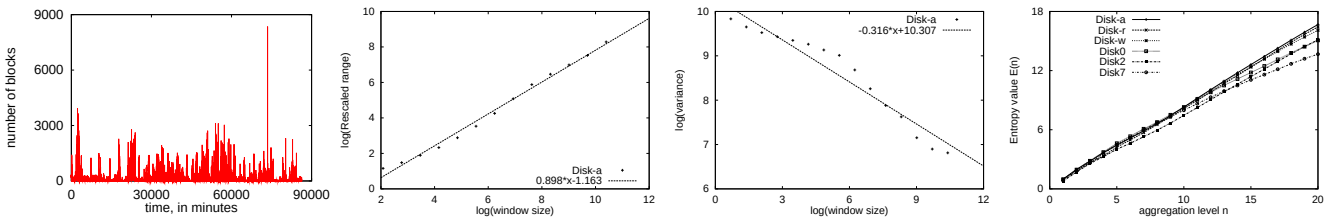
The web traffic is from public Internet traces available on `http://repository.cs.vt.edu/` named `lbl-conn-7`. It contains thirty days' worth of all wide-area TCP connections between the Lawrence Berkeley Laboratory (LBL) and the rest of the world. Four web traces are used(Table 2) and they are in millisecond resolution as well.

The main questions for our experimental investigation are the following: To what extent are the real traces self-similar and bursty? How realistic are the traces generated by the b-model ? How efficient is the b-model in generating the traces based on the real data? We proceed to answer these questions in each of the following sections.

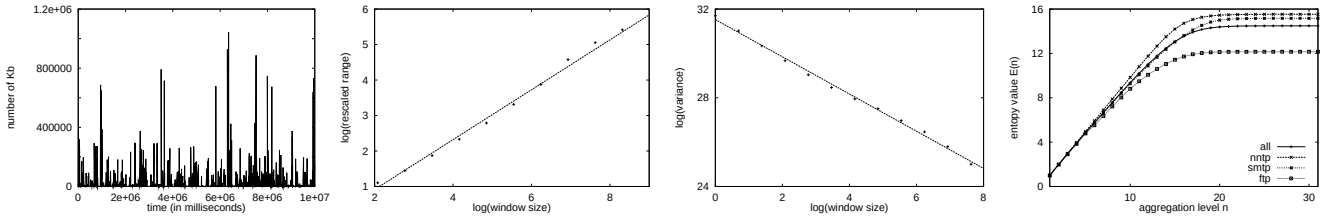
5.1 Self-similarity and Model Fitting

All the data sets show strong self-similarity and are very bursty. This can be easily verified by simply looking at the data sets. Figure 5 (a) and (e) show `Disk-a` and `lbl-a`. The linear behavior of R/S plots and variance plots gives an estimated Hurst exponent around 0.75 to 0.85, confirming strong self-similarity. We only show the R/S plots and variance plots for the two traces due to space limitations—all the data sets and their R/S and variance plots are very similar.

We use the entropy plot to fit our model. In all the data sets, the points in the entropy plots approximate a line very well (Figure 5 (d) and (h)). The slope of the entropy plots and the estimated bias b are listed in Table 2. All the traces have bias ranging from 0.63 to 0.8. The traditional Poisson arrival is not able to deal with these traces.



(a) `Disk-a` (b) R/S plot for `Disk-a` (c) Variance plot for `Disk-a` (d) Entropy plots for disk traces



(e) Part of `lbl-all` (f) R/S plot for `lbl-all` (g) Variance plot for `lbl-all` (h) Entropy plots for web traces

Figure 5. Raw data, R/S plots, variance plots, and entropy plots for disk and web traces.

The entropy plots show a plateau at the tail part for LBL web traces. To simulate this, we can use the *truncated* b-*model* : beyond certain aggregation level, we set b to 1 to force no further splitting on the value of the data points.

5.2 Domain-specific evaluation

The b-model is further evaluated by comparing the synthetic traces with the real workloads in terms of domain-specific properties. The synthetic traces are generated by the b-model with bias estimated from the entropy plots.

Domain-specific properties include queuing behavior and interarrival time distribution. These properties are more important than the statistical properties, because the ultimate goal of modeling is to help to develop better systems. For the these workloads, interarrival time distribution and queuing behavior are critical to the throughput of the disk subsystems and networks. Bursty workloads often cause unusually long queues, requiring larger buffer pools and making the end users suffer long response times. The b-model should be able to replicate these behavior.

Figure 6 and 7 compare the interarrival time and queue length distributions in negative cumulative format and in log-log scale for disk traces. A simple disk model assuming a uniform service time of 10 milliseconds is used to produce the queue length distribution because only timestamps of the disk requests are available.

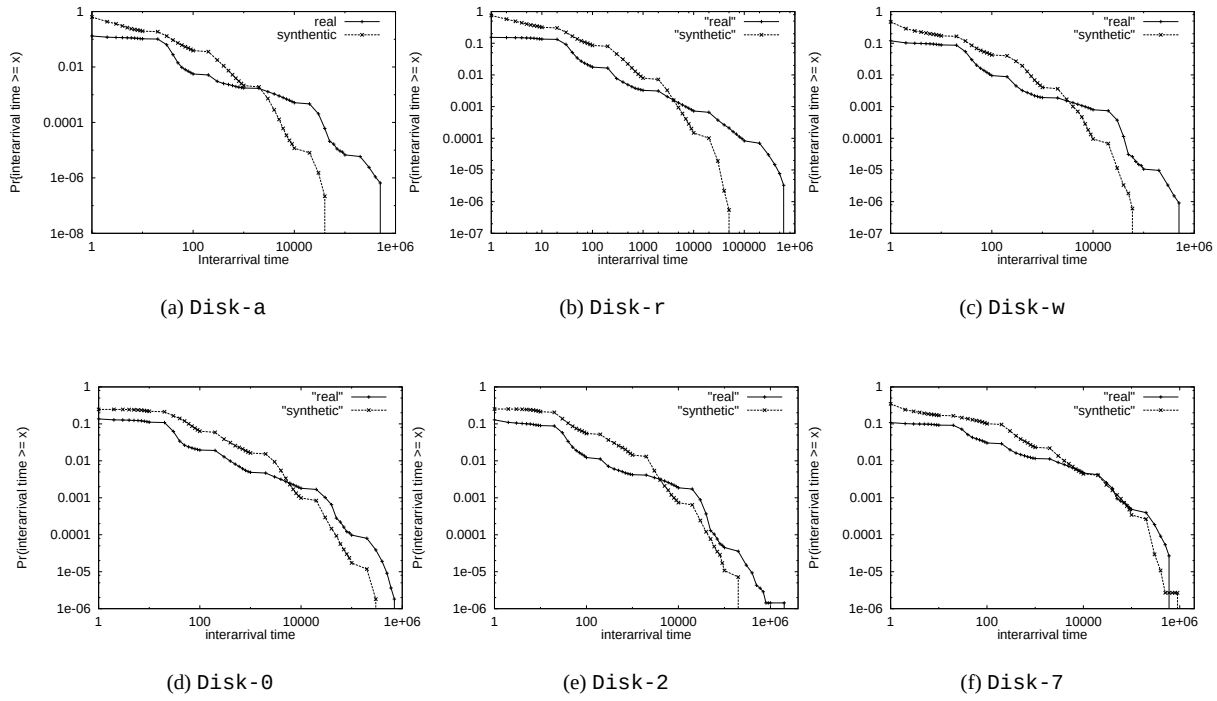
Overall, the interarrival time distributions of the synthetic traces and the original ones agree very well as shown by Figure 6. For the real workloads, about 90 per cent of the disk requests have interarrival time of 0, which means they are sent to the disk within 1 millisecond after the previous ones. Here 1 millisecond is the resolution of the data set. Another 10 per cent of the disk requests have different interarrival times, ranging from 1 msec to 1000 sec. The synthetic traces capture this irregularity very well.

Figure 7 compares the queuing behavior. Most of disk requests can be served immediately without waiting in the queue. But sometimes, there are so many disk requests in a short period of time that the queue becomes extremely long. A few disk requests experience a queue length of about 1 million disk requests. This is caused by the burstiness of workloads. The synthetic data capture the bad queuing behavior and exhibit similarly bad queuing behavior.

Results of similar experiments on the web traces are shown in Figure 8. Different request sizes exist in web traces. Again, we assume that the service time is the transmission time and is proportional to the request size — in particular, we assume 100 μsec for every 1 Kbytes. The queue length is the number of bytes waiting to be sent. While the interarrival time distributions are not so close, the queue length distributions agree very well, which indicates a good approximation of the mean response for the end users.

5.3 Computation Effort

The efficiency and the scalability of the algorithms are also major concerns because of large data set sizes. Efficient



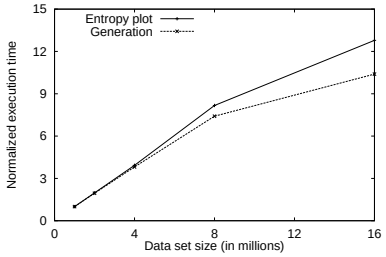
(a) `Disk-a` (b) `Disk-r` (c) `Disk-w`

(d) `Disk-0` (e) `Disk-2` (f) `Disk-7`

Figure 6. Interarrival time distribution in negative cumulative form.

Size	Entropy plot	Generation
1 M	20.50	13.54
2 M	40.52	26.40
4 M	80.51	51.62
8 M	167.49	100.34
16 M	262.12	140.75

(a) Computation time (in seconds)



(b) Normalized time against data set size

Figure 9. Computation time against data set size.

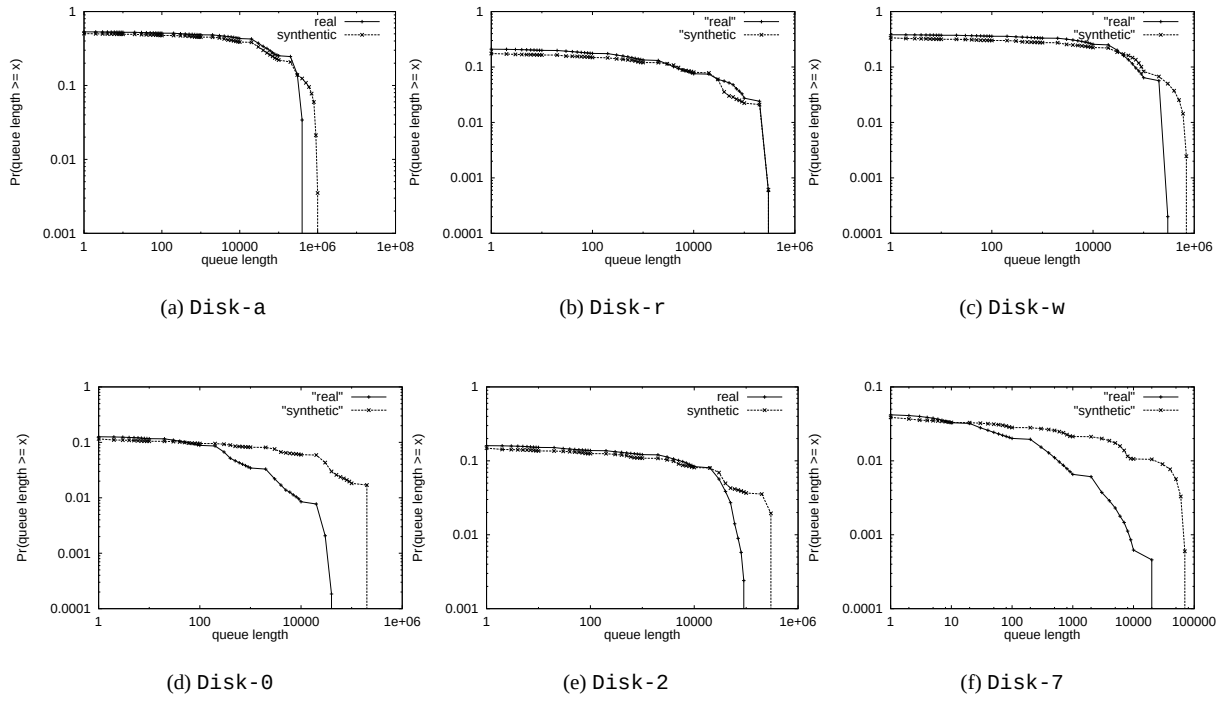
model fitting makes it possible to incorporate the b-model in scheduling subsystems.

subsection 4.4 has already discussed the time and space needed for synthetic trace generation. Requirements of time and space are $O(l)$ and $O(\log_2 l)$ respectively. In this section, we show that all the other tools require only one scan of the data set, thus, offering good scalability, too.

It is straightforward to show that tools like interarrival time distribution and queuing behavior need one pass on the data. A naive implementation for the entropy plot needs one scan for each aggregation level. However, note that all the passes are independent. Thus, they can be integrated into one and $E^{(1)}, E^{(2)}, \ldots, E^{(n)}$ can be calculated simultaneously. All the experiment results are calculated using one-pass algorithms. This is extremely important when for very large data sets.

The actual processing time also depends heavily on the total volume of requests. In practice, all the data points have integer values instead of real values. When the volume is small, some of the data points will become zero before the required aggregation level is met, thus, no further computation is needed on them. In fact, in our experiments, generating a one-day-long disk trace in millisecond resolution usually takes less than 5 minutes and the entropy plot requires less than 3 minutes when implemented in Perl. We expect that a C implementation will perform much faster.

Figure 9 shows the actual wall-clock time for the entropy plot and trace generation. Both scale well with respect to the data set size. We test our tools using traces of different length with the same density. That is, the 1M long trace has 1 million disk requests and 10M long trace has 10 million disk requests. We use a bias of 0.7. Both the algorithms show linear scalability.



(a) `Disk-a` (b) `Disk-r` (c) `Disk-w`

(d) `Disk-0` (e) `Disk-2` (f) `Disk-7`

Figure 7. Queue length distribution in negative cumulative form.

6 Conclusions

Our proposed method is very general in the sense that such self-similar, bursty time sequences arise very often in real-world data. This was recently observed in numerous settings, like TCP [11], video [5], web [3], file system [8], and disk I/O [6] traffic.

The main contribution of this work is the introduction of the b-model as an effective tool for finding and characterizing patterns in real, bursty time sequences. The model is extremely compact, as it effectively needs only one parameter, the bias b. Additional contributions include the following:

- Introduction of the entropy plot to accurately estimate b.
- Fast, single pass, novel algorithms to estimate b and synthesize traces.
- A fast algorithm to generate synthetic and realistic bursty time sequences. The algorithms are extremely efficient: less than 5 minutes for one hour-long disk traces in millisecond resolution and less than 3 minutes for model fitting (implemented in Perl).
- Experiments on real sequences, that showed (a) they are self-similar and (b) they are approximated well by our synthetic traces, both in terms of instrinsic measures, as well as in terms of queue length behavior.

We are currently working on expanding the model to incorporate spatial information (eg. disk block number), besides temporal information. Another possible direction for future work is the analysis of co-evolving, bursty time sequences, like disk traffic on units of a RAID box (or automobile traffic from multiple, nearby highway lanes).

7 Acknowledgement

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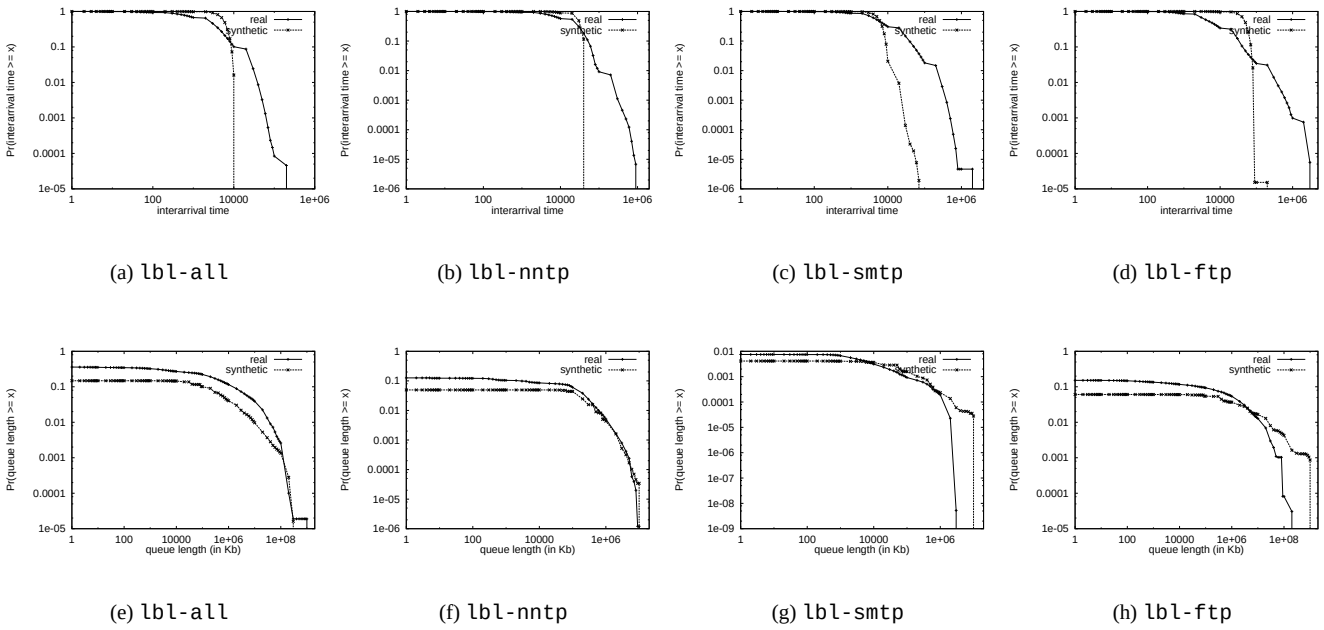

(a) `lbl-all` (b) `lbl-nntp` (c) `lbl-smtp` (d) `lbl-ftp`

(e) `lbl-all` (f) `lbl-nntp` (g) `lbl-smtp` (h) `lbl-ftp`

Figure 8. Interarrival time and queue length distribution for the LBL network traces

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