

Inferring Movement Trajectories from GPS Snippets

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Motivation

- ◆ Every 2/3 has a smartphone/tablet nowadays, typically has GPS



- ◆ Not only learn the current position, but also predict where people will go, and when arrive
- ◆ It benefits mobile apps

- ▶ navigation



- ▶ shop, restaurant recommendation

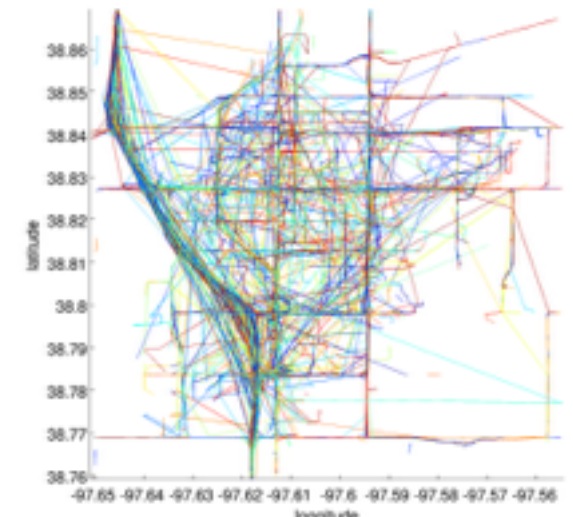
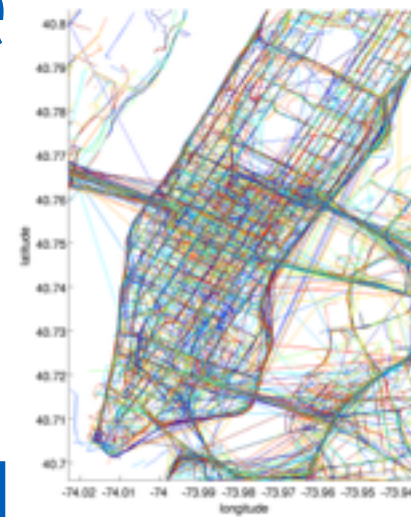
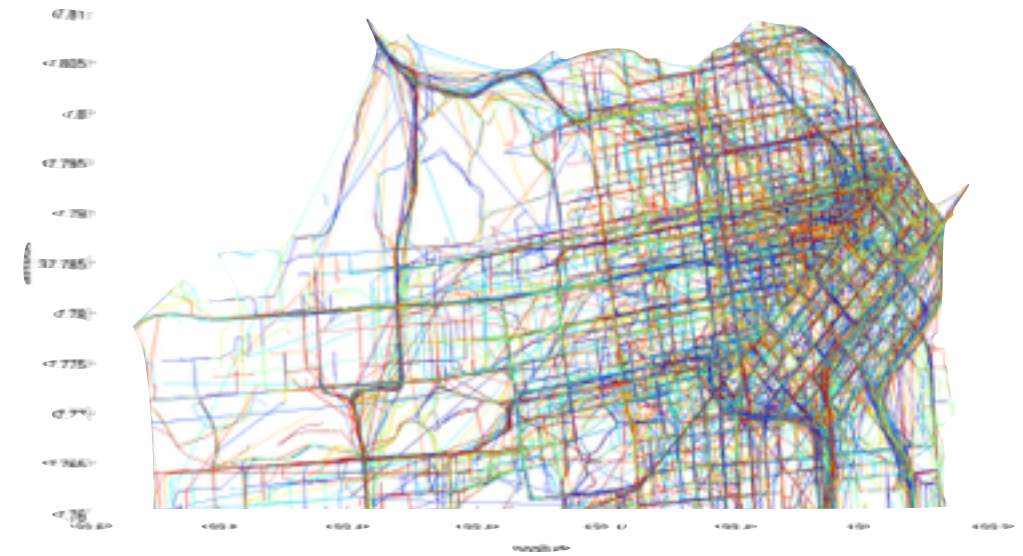
- ▶ context-aware assistance

- ▶ contextual metadata



Challenges

- ◆ Data is big because of the huge amount of users
 - ▶ trillions sequence, worldwide coverage
- ◆ Data is sparse due to energy and privacy constraints
 - ▶ GPS sequence is short, only has several points
- ◆ Data is noisy
 - ▶ inexact positions in city
 - ▶ irrational path planing
 - ▶ travel speeds vary



An aerial night photograph of a city, likely Seoul, showing a dense cluster of skyscrapers with glowing windows and light trails from traffic on a multi-lane highway. A prominent roundabout with a central landscaped area is visible in the lower half of the image. The text 'Model and Inference' is overlaid in a blue serif font on a semi-transparent white rectangular background.

Model and Inference

Model



$$p(O, S|\theta) = \prod_{k=1}^n p(o_k|s_k, \theta) p(s_{k+1}|s_k, \theta)$$

observation model

motion model

◆ Observation model:

$$p(o|s) \propto \exp \left(-\frac{1}{2\sigma_d^2} \|o^{\text{loc}} - s^{\text{loc}}\|^2 - \frac{1}{2\sigma_1^2} \|o^{\text{dir}} - s^{\text{dir}}\|^2 \right)$$

◆ Motion model:

$$p(s'|s, \theta) = \sum_{\xi} p(\xi|s, \theta) p(s'|s, \xi, \theta)$$

all possible paths

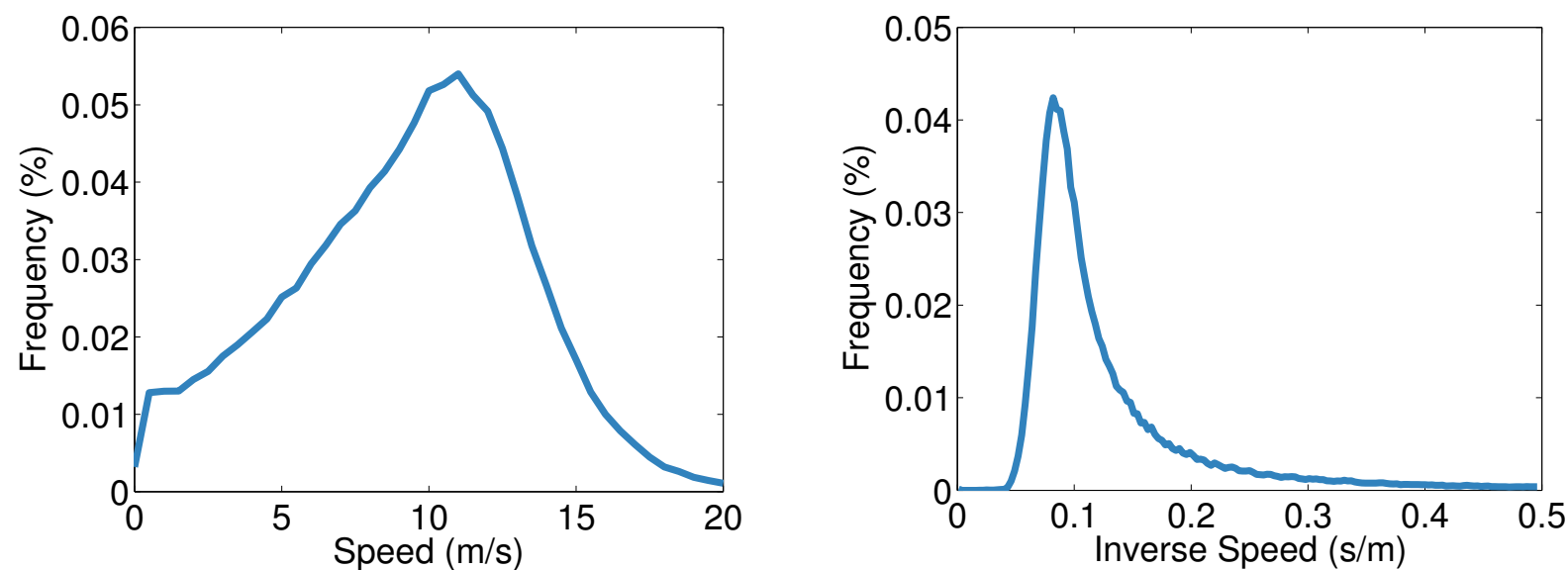
$$= \sum_{\xi} \left[\prod_{\iota=1}^n \pi(i_{\iota}, i_{\iota+1}) \right] p(s'|s, \xi, \theta)$$

transition probability

from s to s' along path ξ

Travel time of a road segment

Histogram of speed and travel time



- ◆ Key observation: speed somewhat follows Gaussian, and travel time follows an **inverse Gaussian** (IG) distribution
 - Time from s to $s' \sim \text{IG}(\text{length}/\text{speed}, \delta^2 \cdot \text{length}^2)$

Travel time of a path

- ◆ We made two assumptions: the mean and variance of the speed
 - ▶ for a path is a weighted linear combination of all road segments
 - ▶ for a road segment is a weighted linear combination of all associated attributes
 - ★ road type, #lanes, speed limit, location, time, etc...

Inference method

- ◆ Solve the non-convex optimization problem

$$\text{maximize}_{\pi, \omega, \gamma} \log p(O|\pi, \omega, \gamma),$$

- ▶ where O is the training data, π transition probability, ω and γ are coefficient about speed mean and variance

- ◆ Repeat until convergence

- ▶ randomly sample several GPS sequence
- ▶ run an **optimized** dynamic programming to update π
- ▶ update ω, γ by subgradient descent



Experiment

Setup

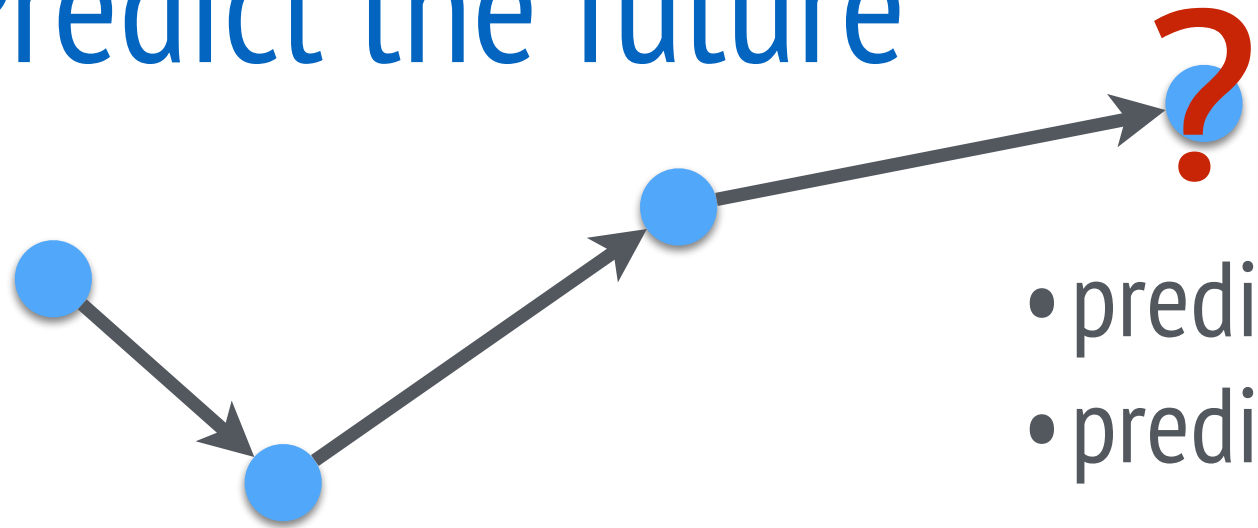
◆ Dataset

	SF	Boston	NYC	Salina
Road segment	18K	7K	17K	9K
Intersection	35K	10K	29K	23K
Trajectories	8M	7M	4M	3M

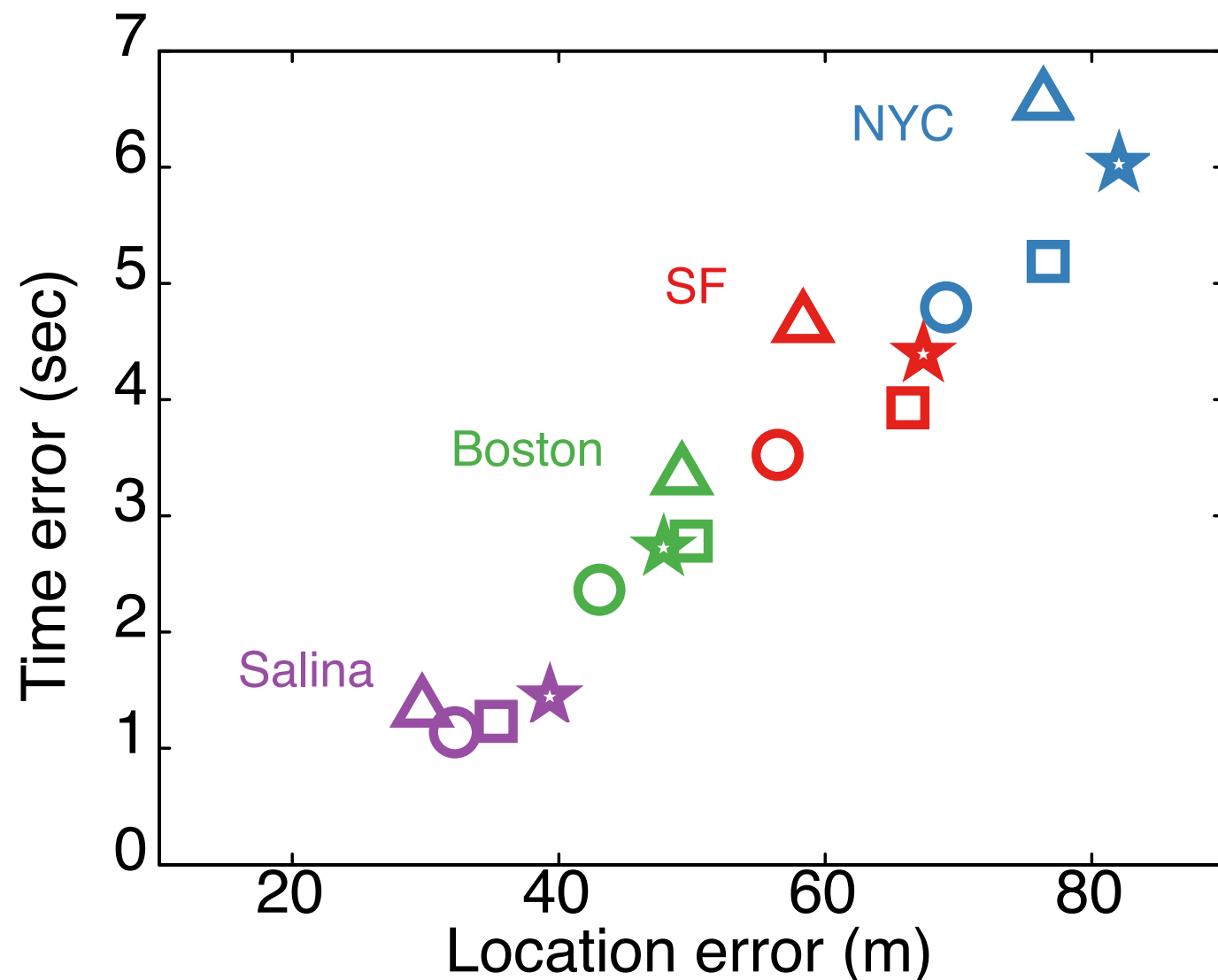
◆ Binary feature

- ▶ road features: road attributes such as major road/high way, number of lanes, speed limit
- ▶ temporal features: slice workday and weekend hours
- ▶ personalized speed: use trajectory ID as a feature

Predict the future



- predict the position based on time
- predict the travel time based on position

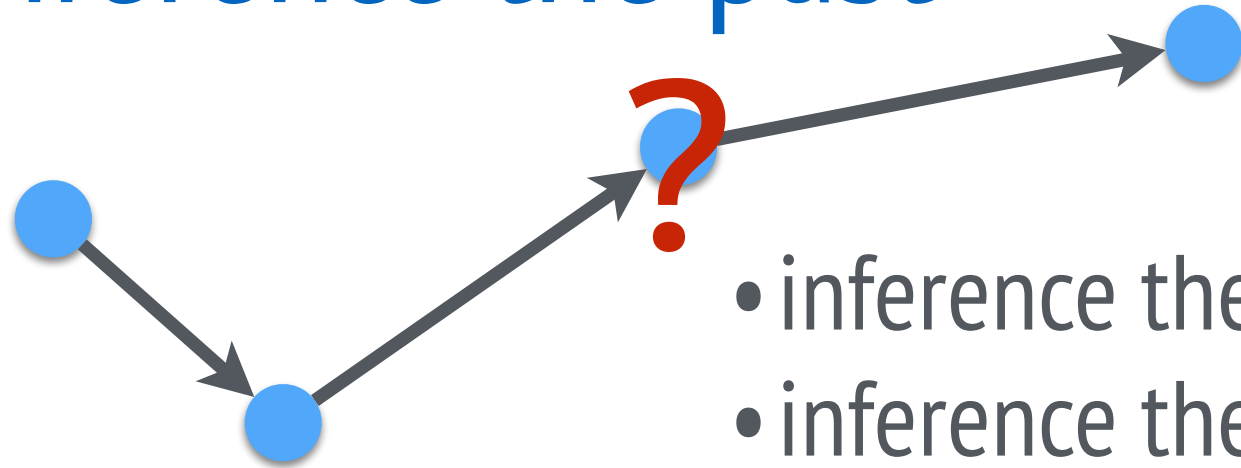


- △ use GPS recored speed
- ☆ only use the shortest path
- no personalized modeling
- the full model

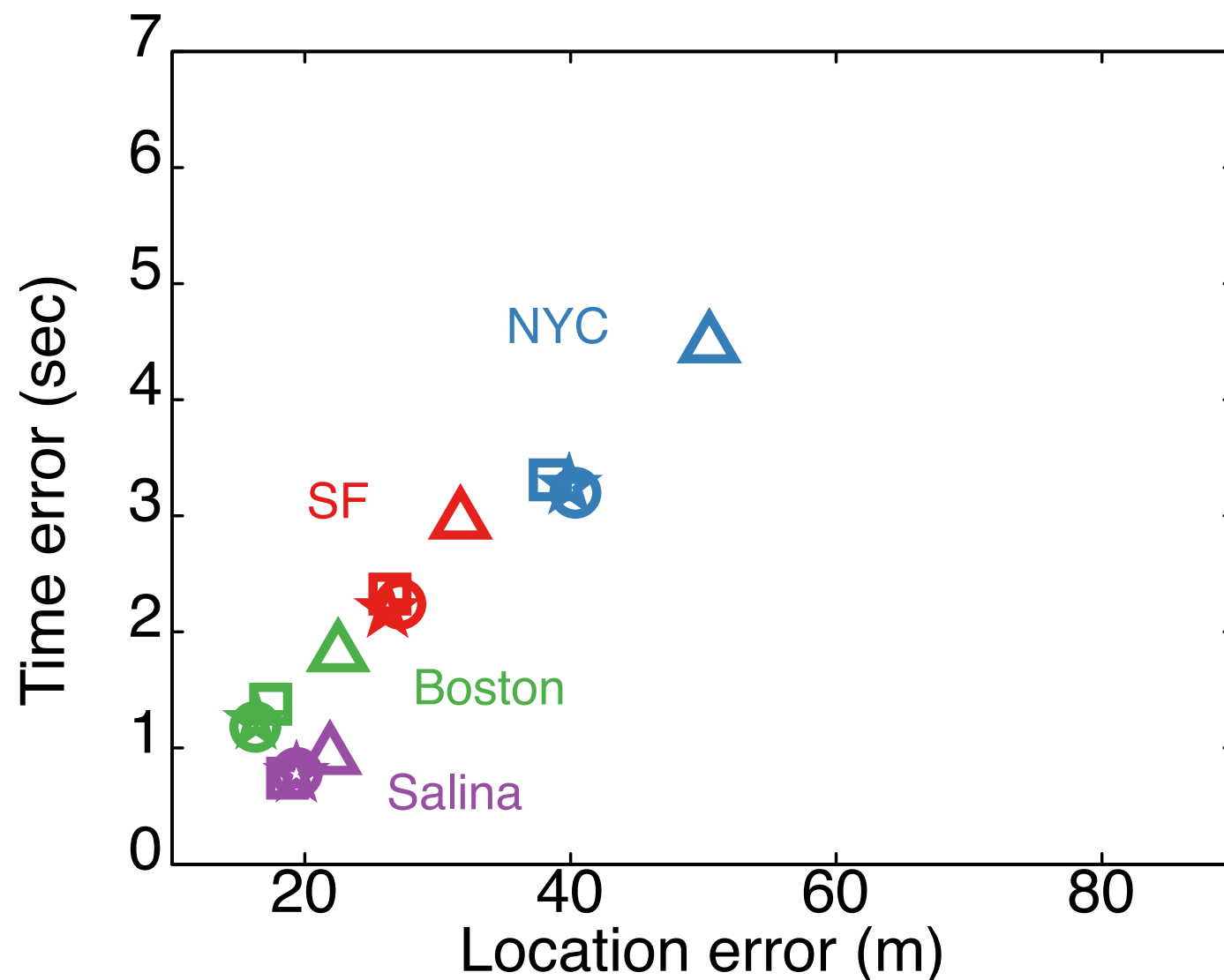
Conclusion

- ◆ A joint model: map trajectory + predict time/position + model road speed/variance
- ◆ Focus on sparse, noise, and anonymous GPS sequence
- ◆ A simple yet powerful model and efficient inference method

Inference the past



- inference the position based on time
- inference the travel time based on position



- △ use GPS recored speed
- ☆ only use the shortest path
- no personalized modeling
- the full model