

*15-887*

*Planning, Execution and Learning*

*Application:*

*Examples of Planning for  
Mobile Manipulation and Articulated Robots*

*Maxim Likhachev*

*Robotics Institute*

*Carnegie Mellon University*

# Two Examples

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- Planning for Mobile Manipulation
- Planning for Articulated Robots

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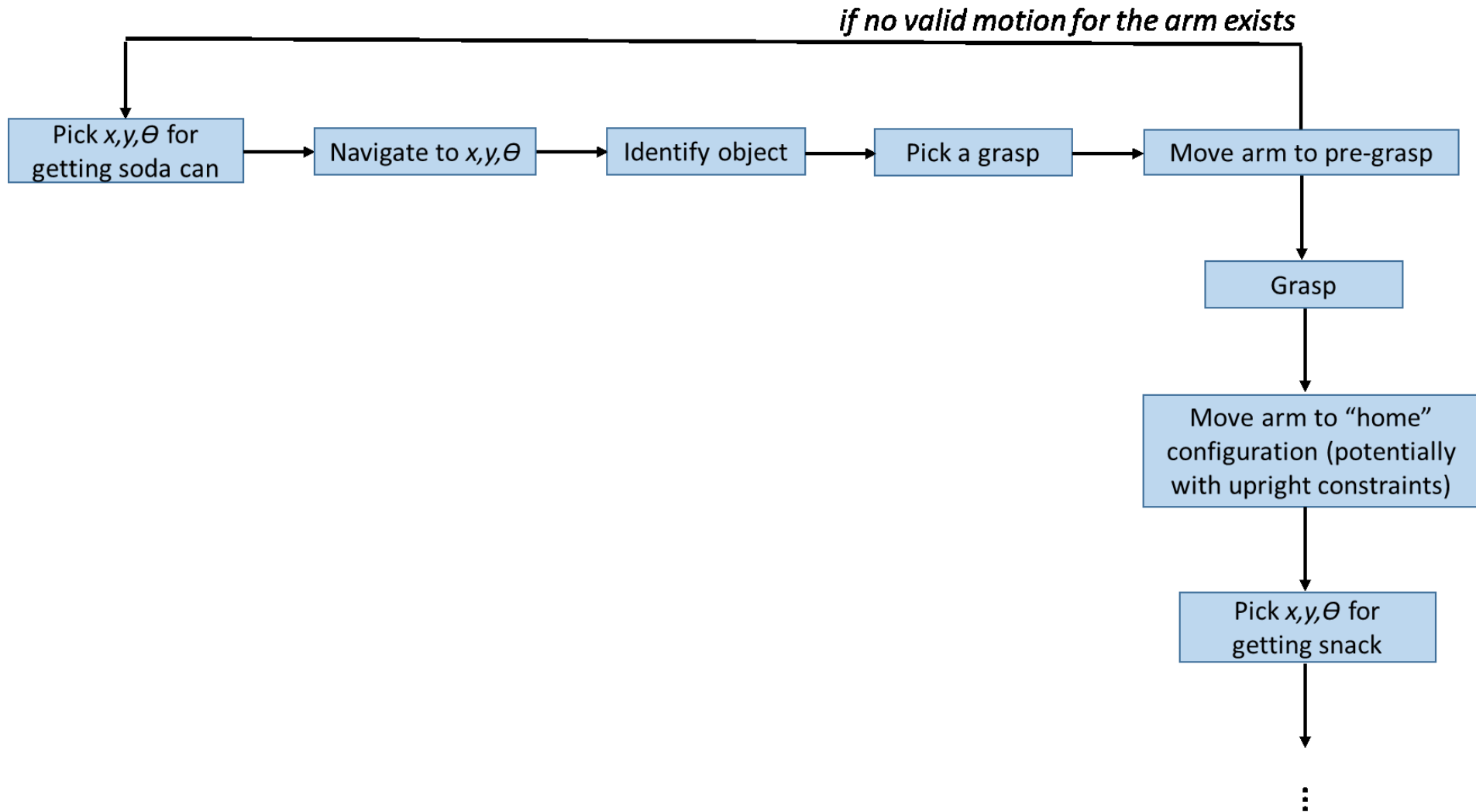
- Planning for Mobile Manipulation
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# Robotic Bartender Demo ([Phillips et al.])

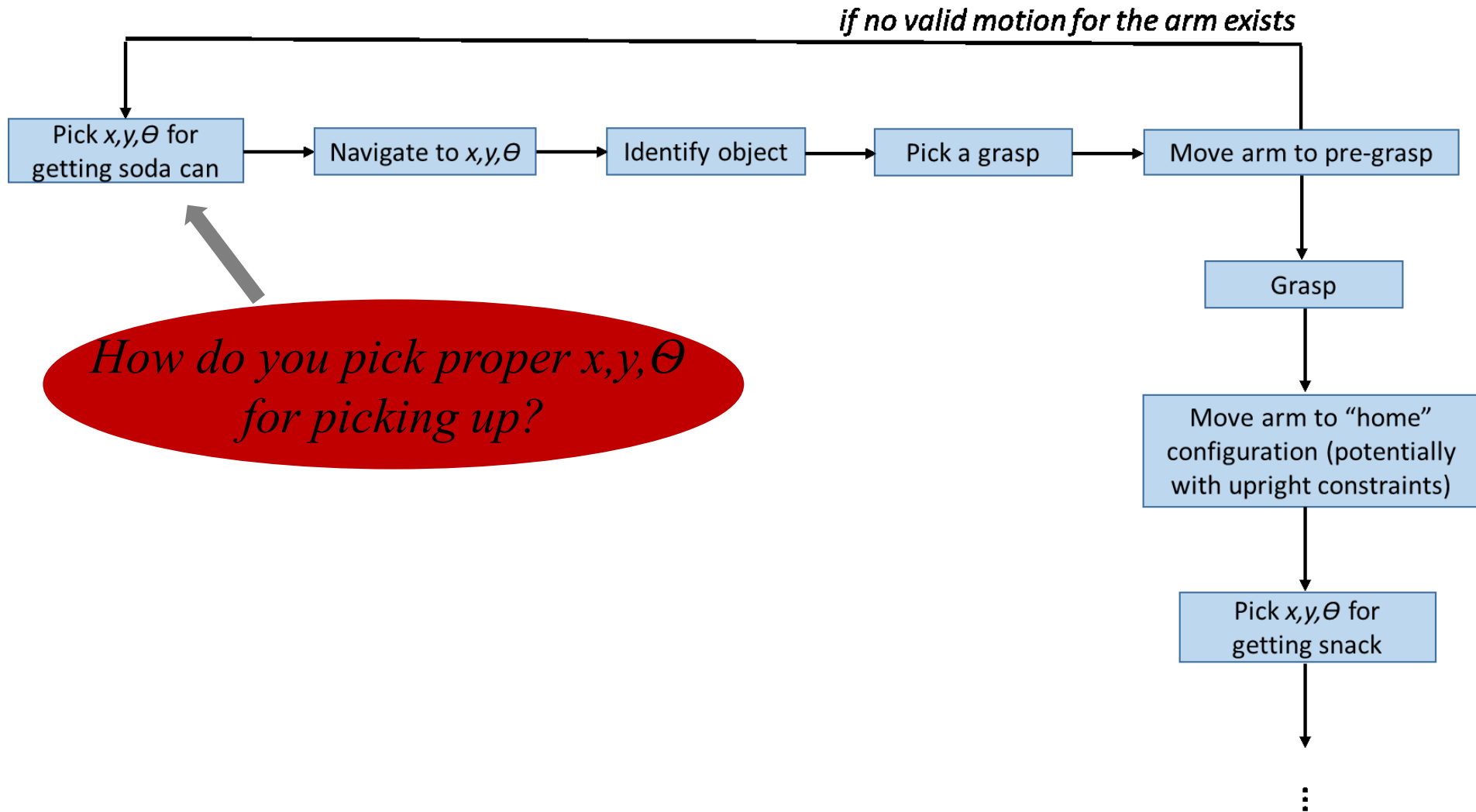
- Robot takes in a command from User Interface as to what soda can and snack to deliver



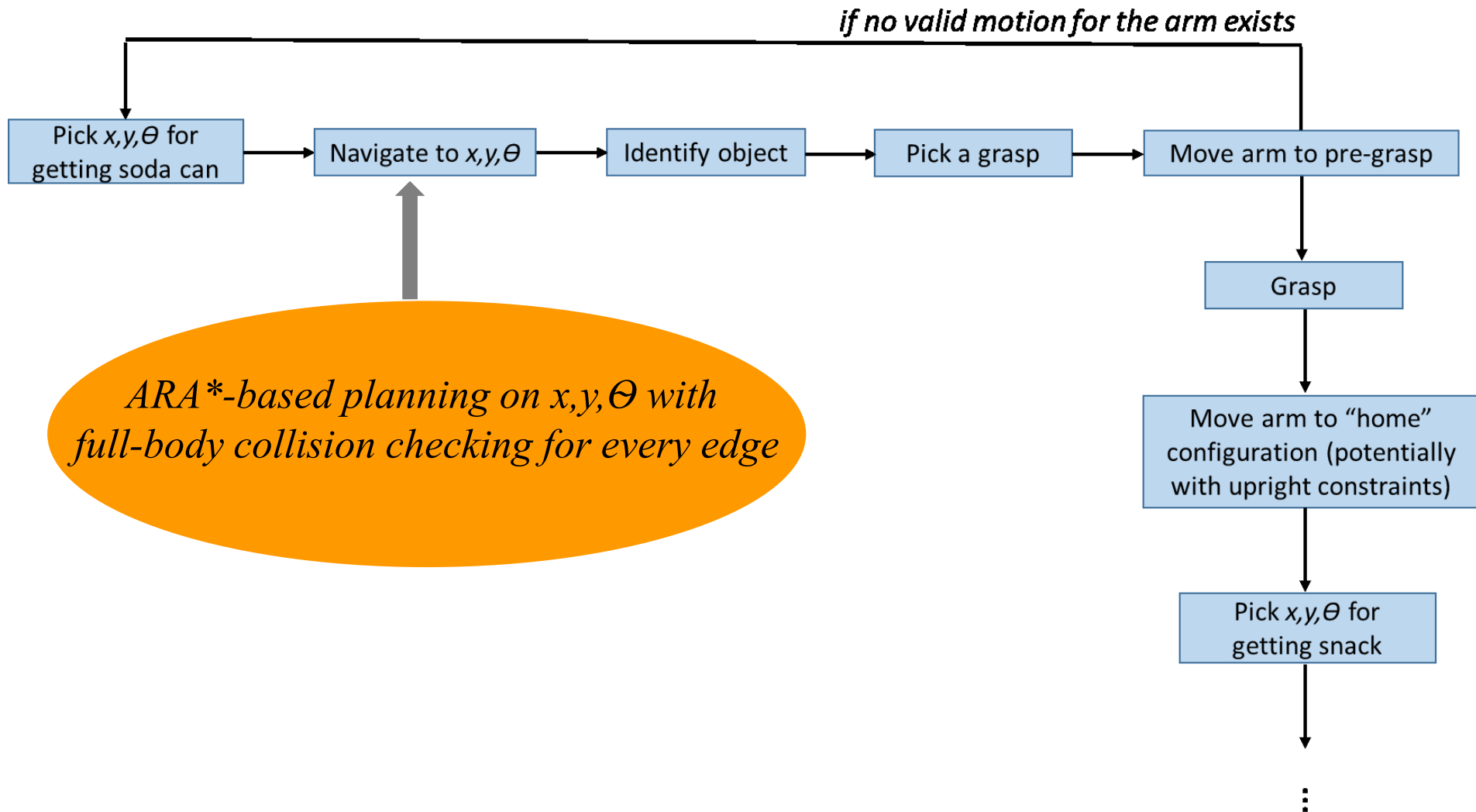
# Typical Sequence of Operations (State Machine)



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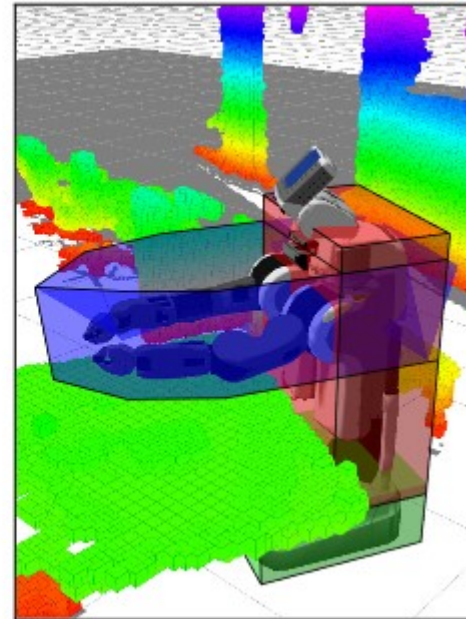


# Typical Sequence of Operations (State Machine)



# Graph for Navigation with Complex 3D Body [Hornung et al., '12]

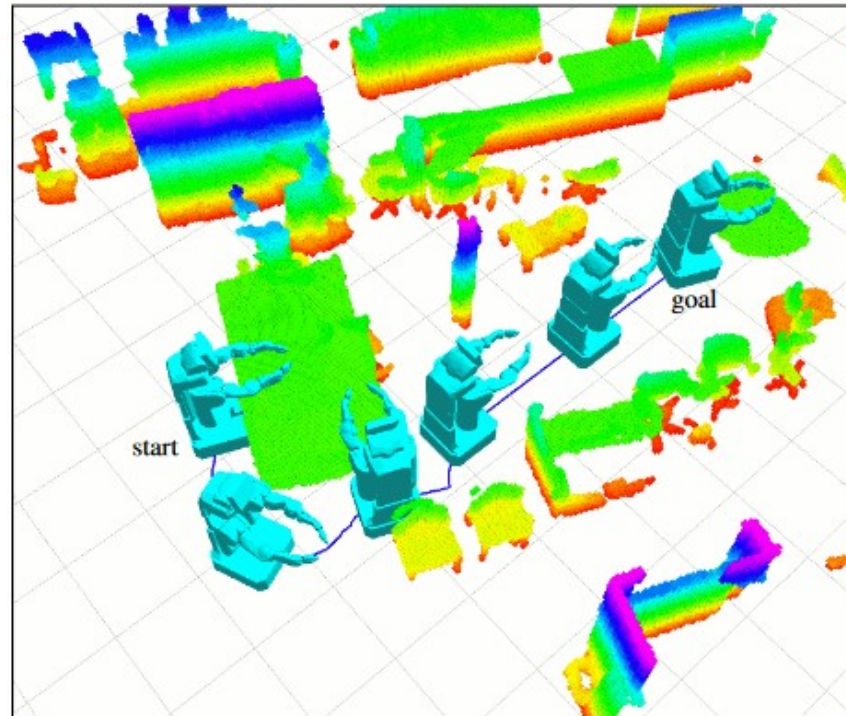
- 3D  $(x, y, \theta)$  lattice-based graph representation for full-body collision checking
  - takes set of motion primitives as input
  - takes  $N$  footprints of the robot defined as polygons as input
  - each footprint corresponds to the projection of a part of the body onto  $x, y$  plane
  - collision checking/cost computation is done for each footprint at the corresponding projection of the 3D map



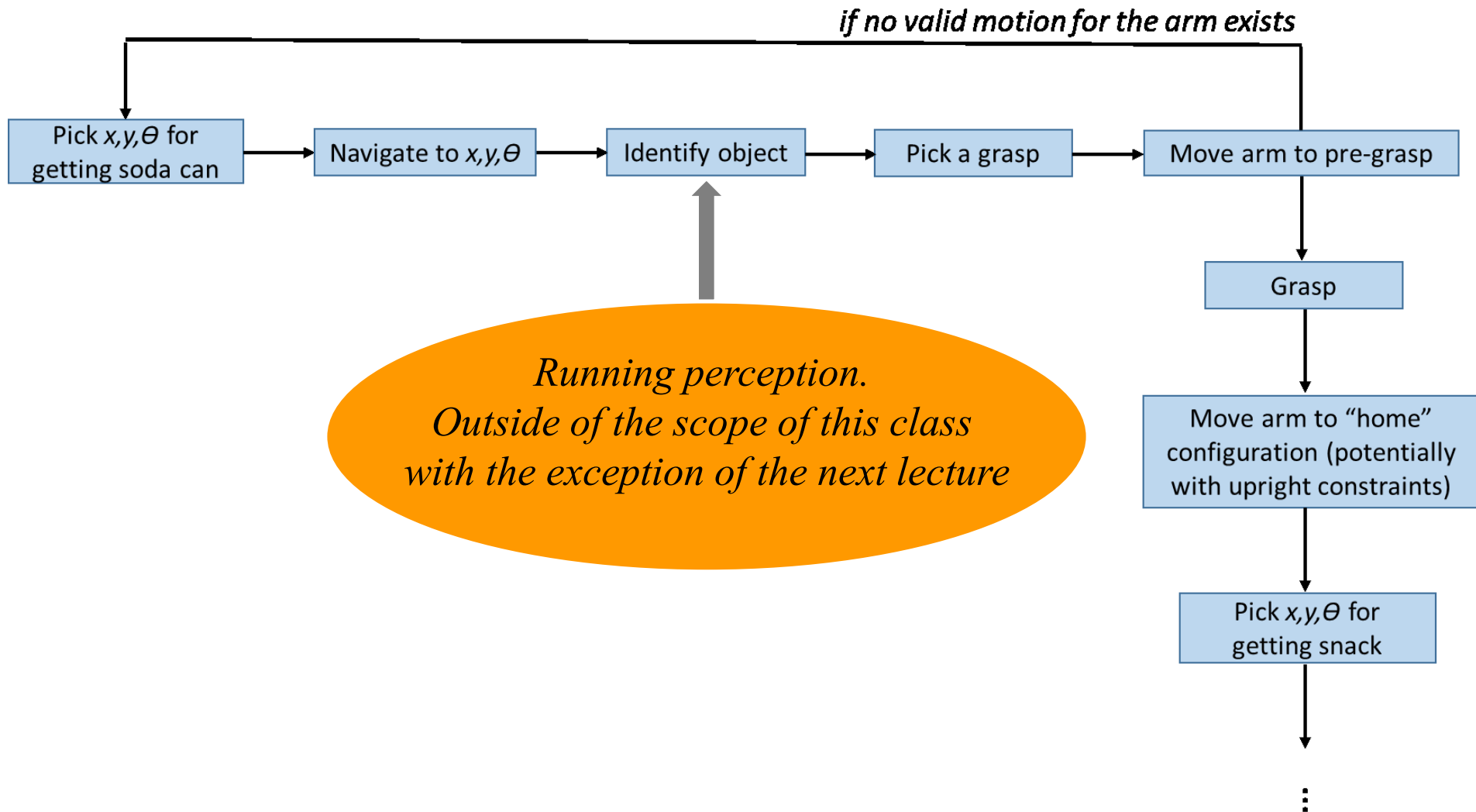


# Graph for Navigation with Complex 3D Body [Hornung et al., '12]

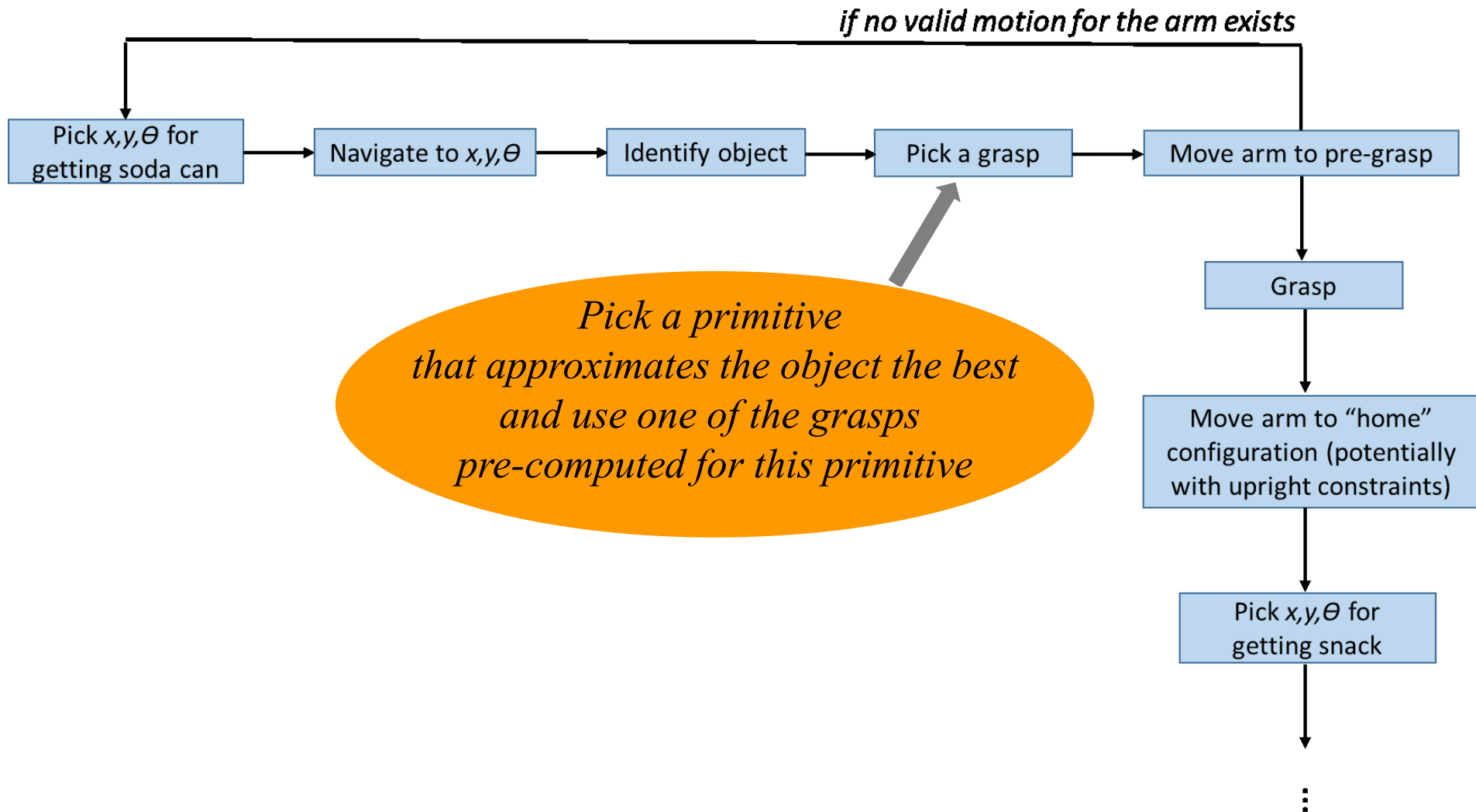
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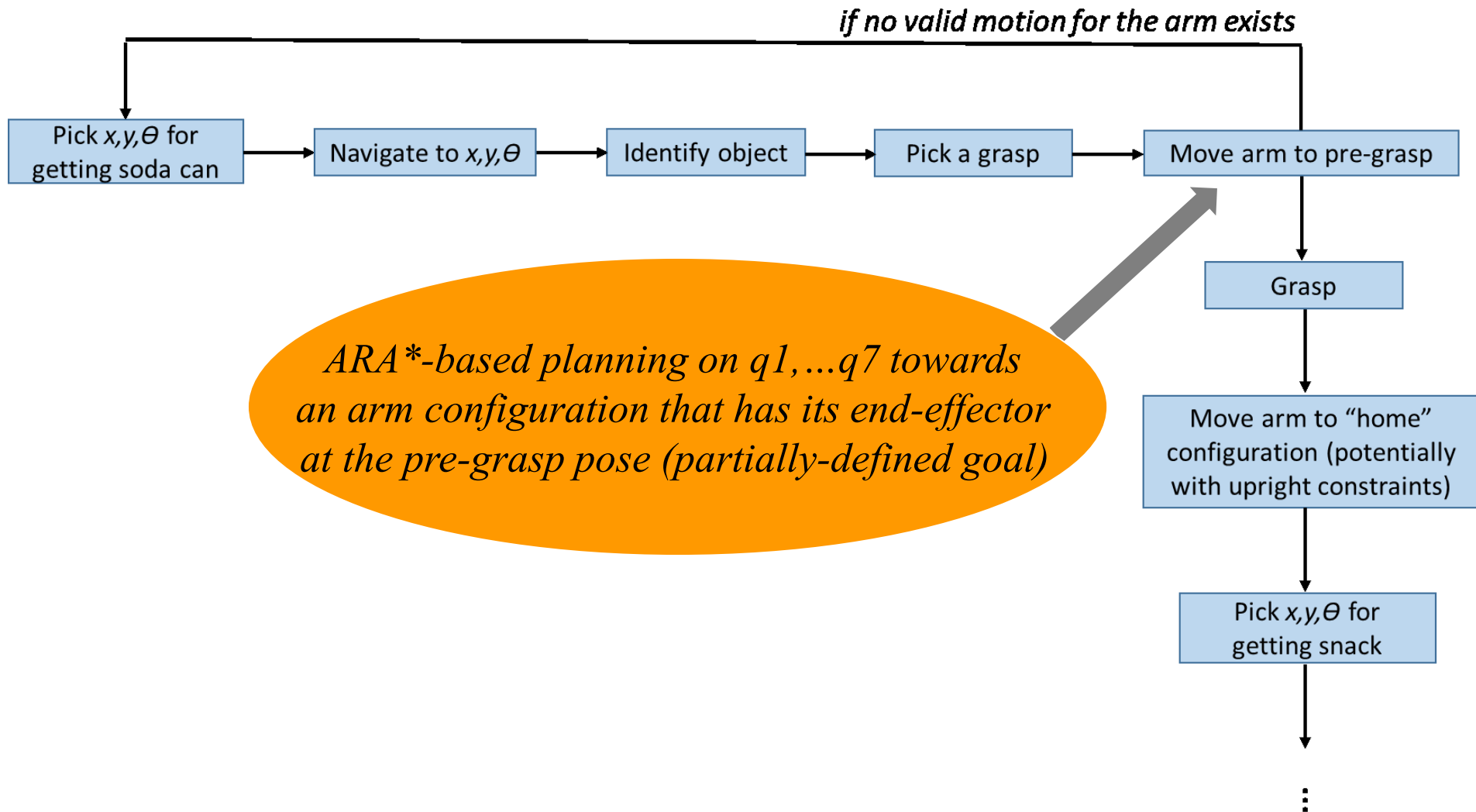
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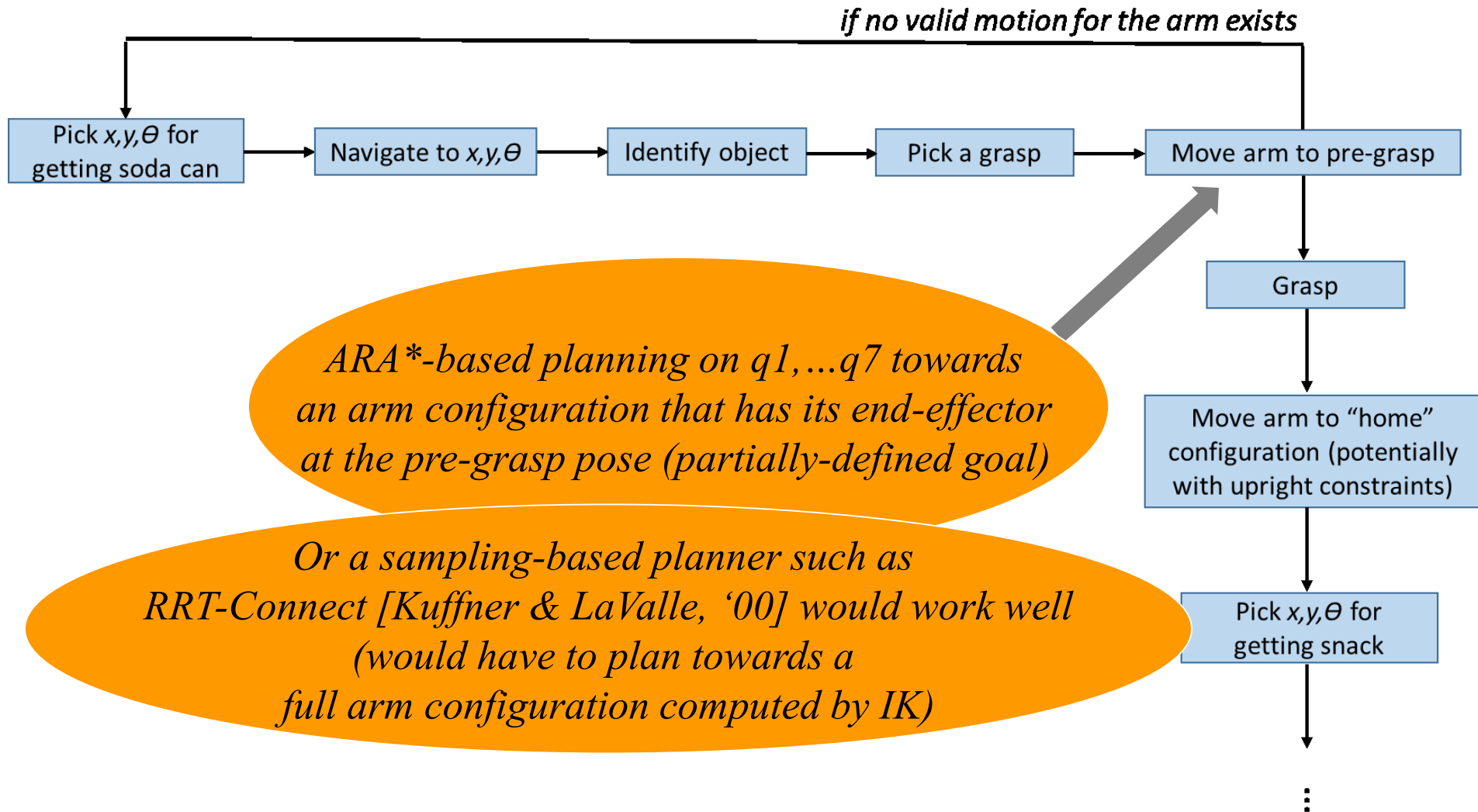
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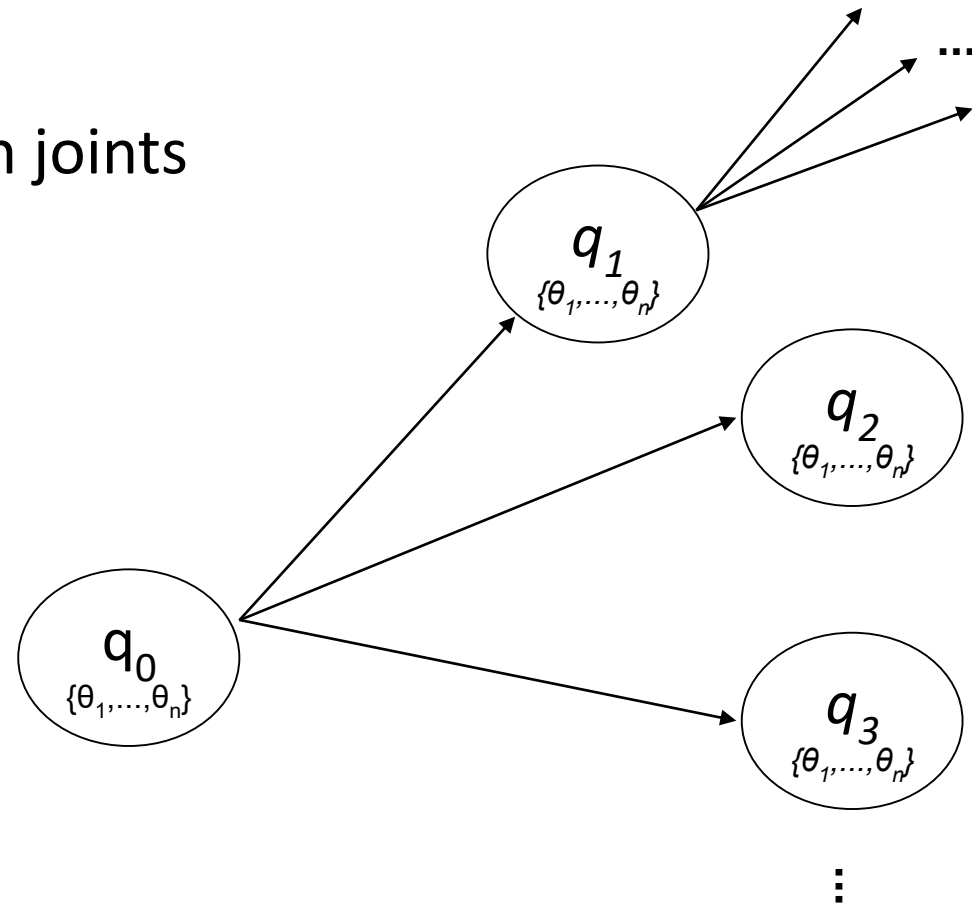
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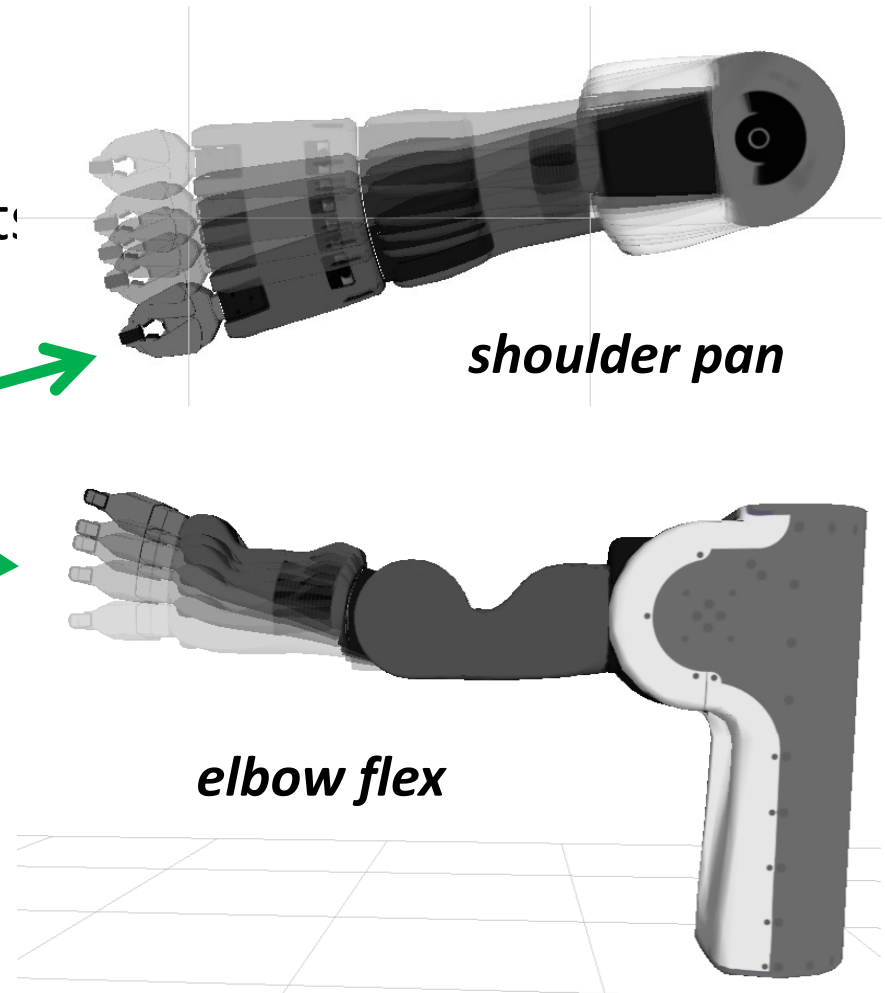
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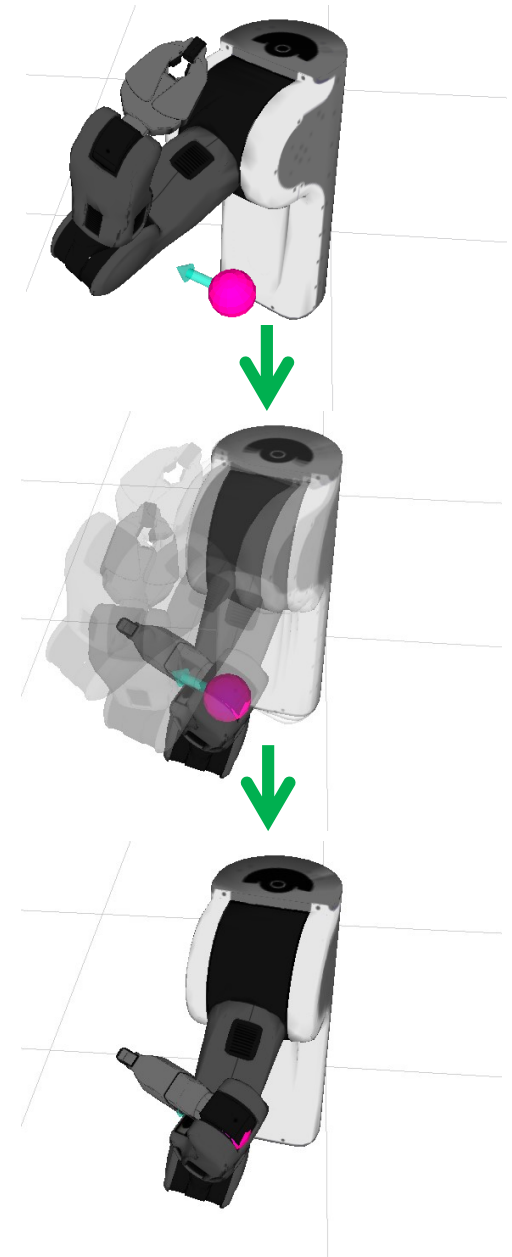
- Representation
  - ex. Single arm with  $n$  joints
    - $\{\theta_1, \dots, \theta_n\}$



- Representation
  - ex. Single arm with n joints:
    - $\{\theta_1, \dots, \theta_n\}$
- Motion Primitives
  - **Static**



- Representation
  - ex. Single arm with  $n$  joints
    - $\{\theta_1, \dots, \theta_n\}$
- Motion Primitives
  - Static
  - **Adaptive**
    - Snap-to-goal motion
      - Analytical solver & IK-based (only if feasible)
    - Capable of satisfying arbitrary goal constraint despite discretization

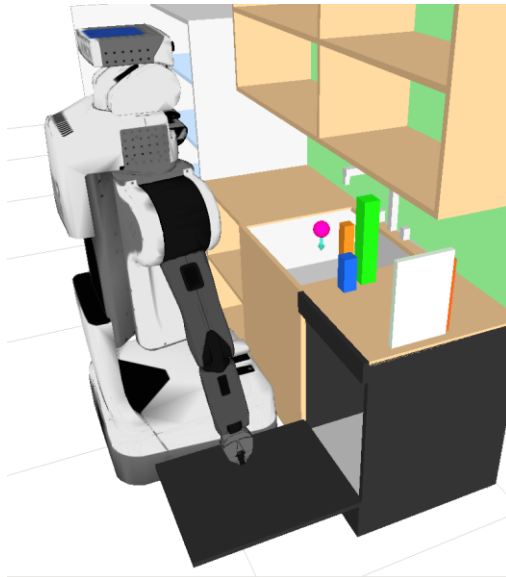




- **Non-uniform Dimensionality**
  - far from goal: only 4 DoFs active
  - around goal: all 7 DoFs are active
- **Non-uniform Resolution**
  - far from goal: larger discretization of joint angles
  - around goal: finer discretization of joint angles

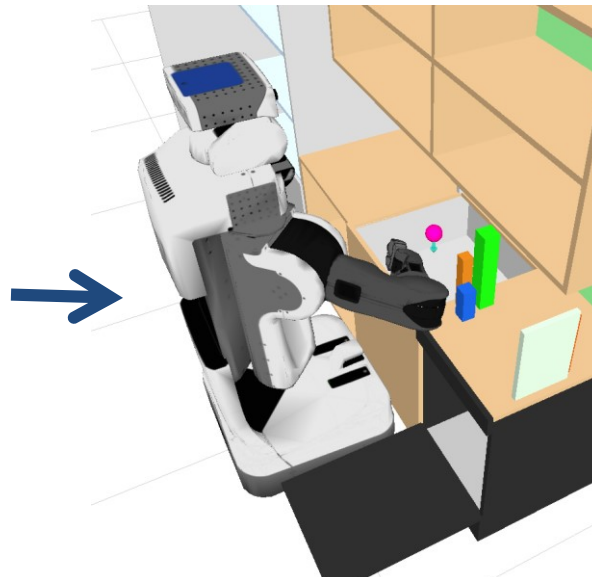
## 4D

1. Shoulder pan
2. Shoulder pitch
3. Upper arm roll
4. Elbow flex



## 7D

1. Shoulder pan
2. Shoulder pitch
3. Upper arm roll
4. Elbow flex
5. Forearm roll
6. Wrist flex
7. Wrist roll



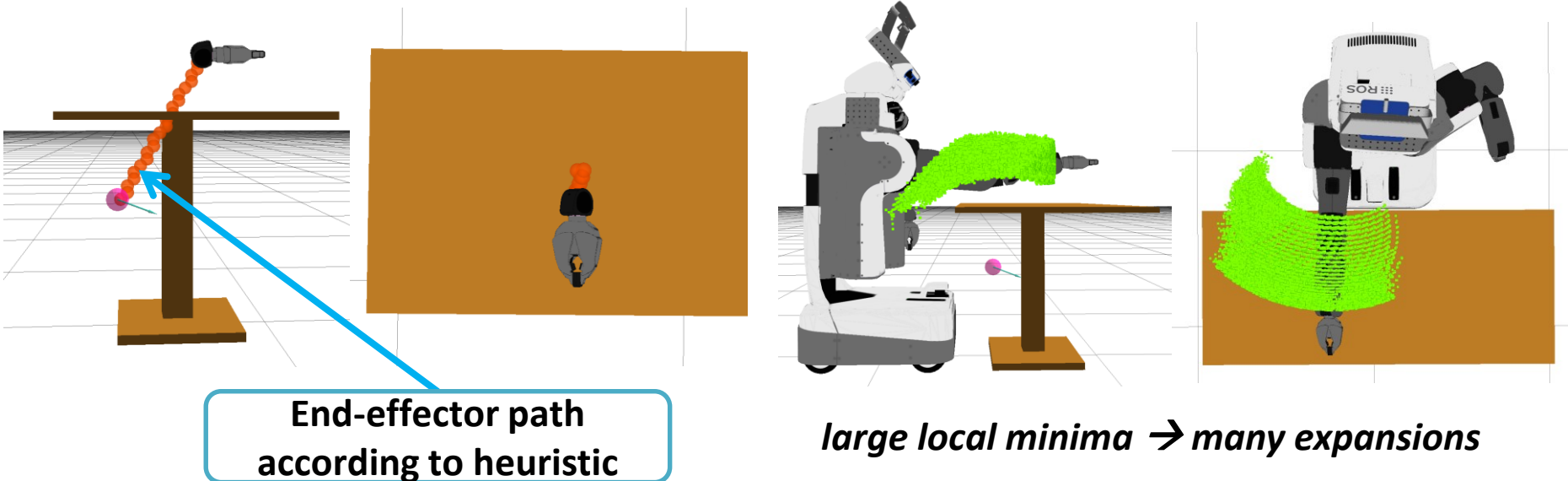


*Any ideas?*

# Informative Heuristics for Arm Planning [Cohen et al., '13]

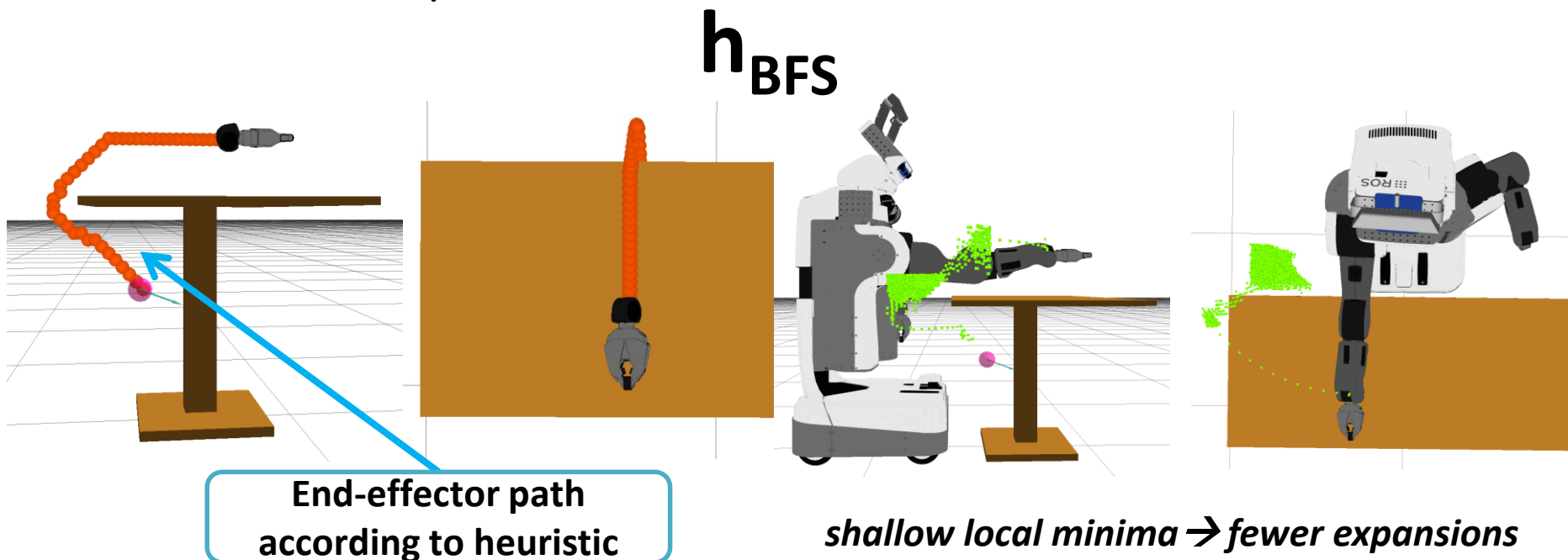
- Euclidean distance for the end-effector?
  - **deep local minima!**

$h_{\text{Euclidean}}$

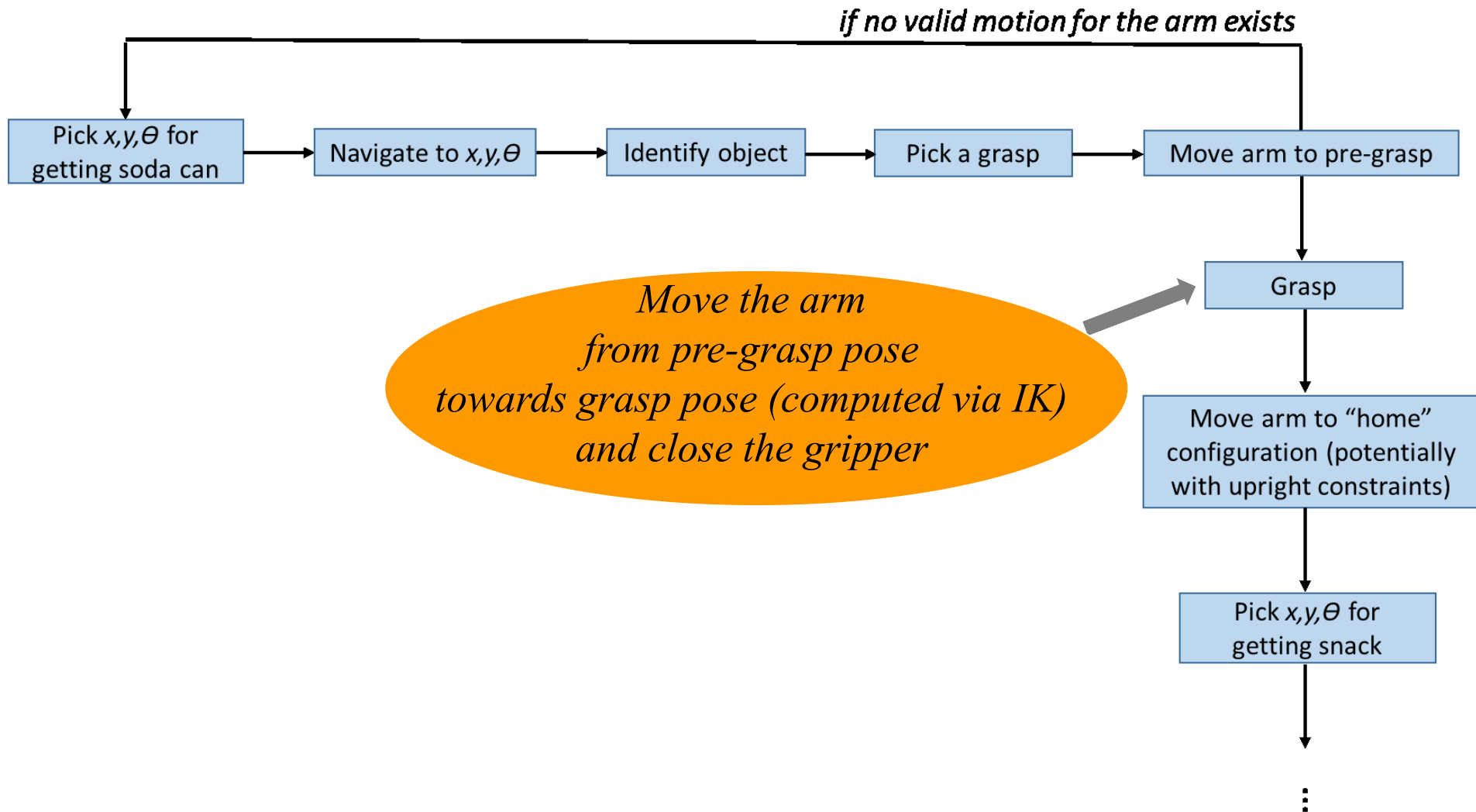


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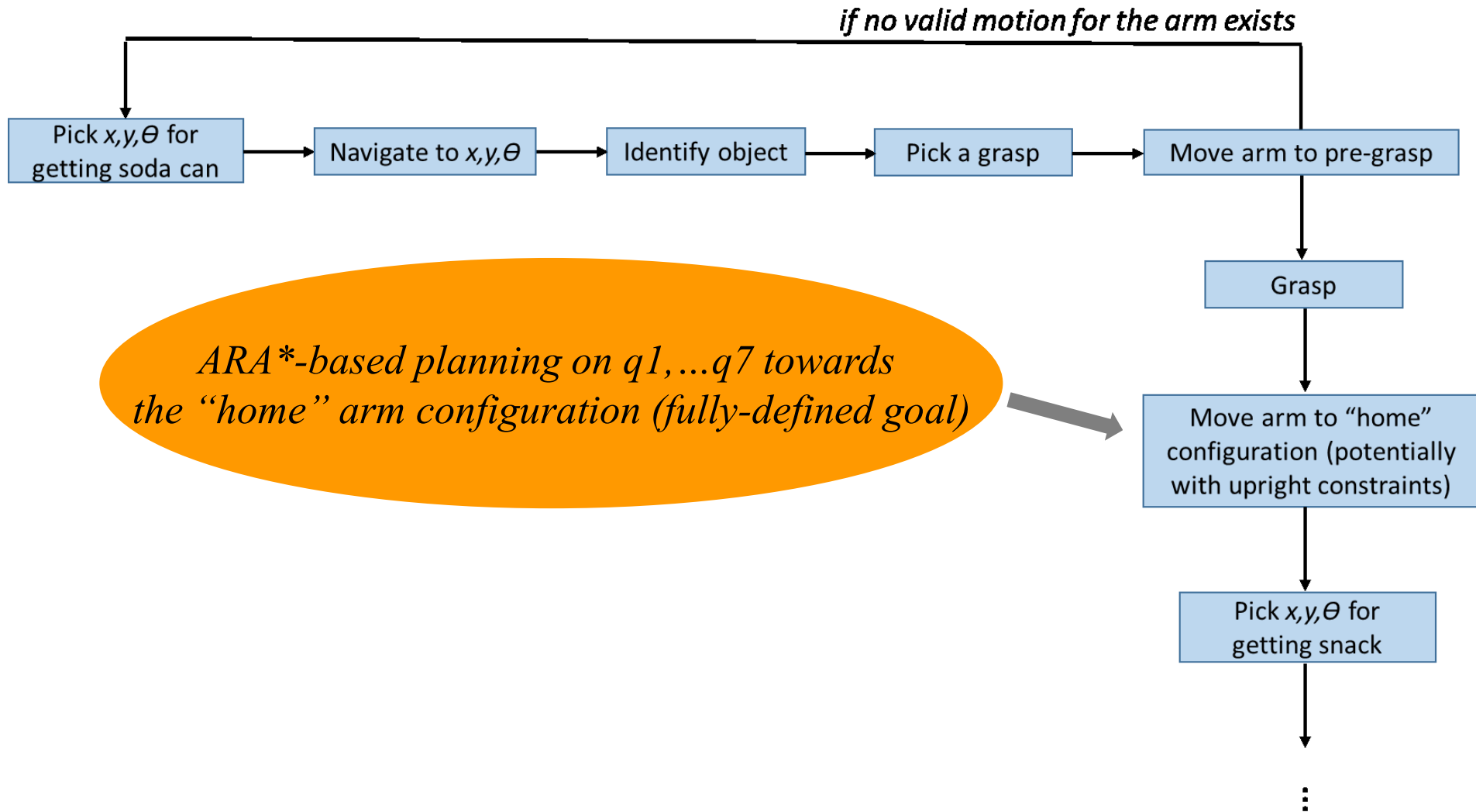
- 3D BFS for end-effector accounting for obstacles
  - computes distances from each  $\langle x, y, z \rangle$  to the goal for the end-effector sphere
  - **dramatically better than Euclidean distance**
  - admissible
  - fast to compute



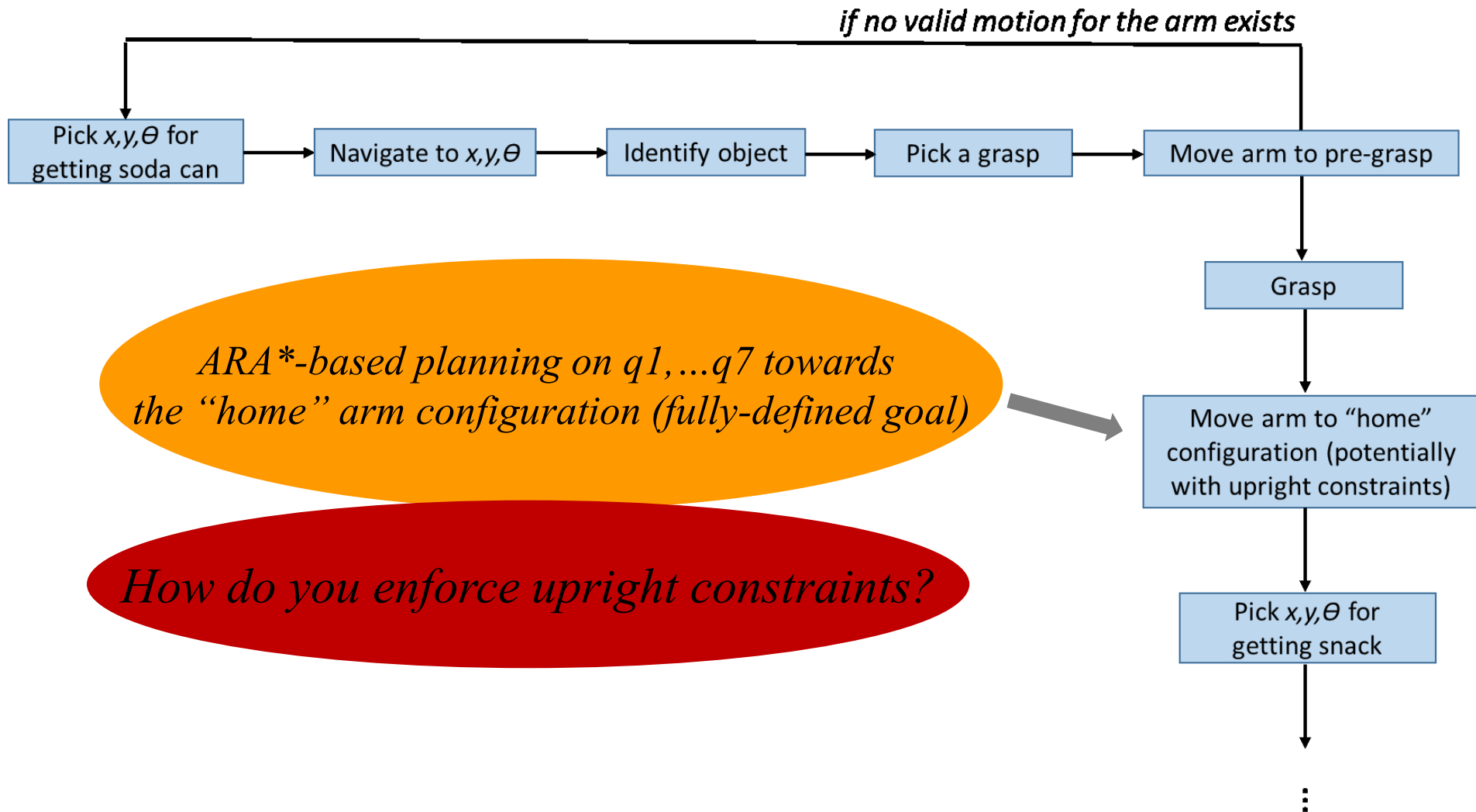
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# Two Examples

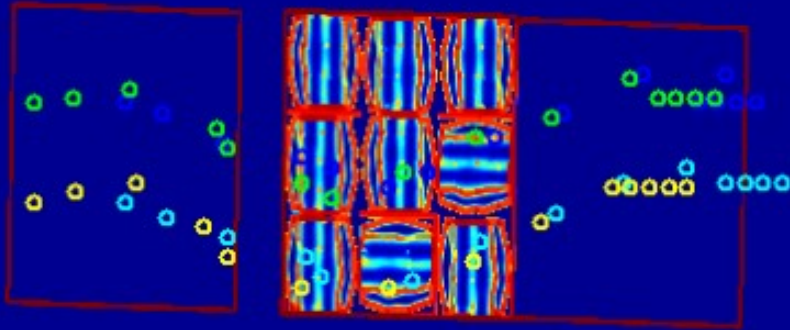
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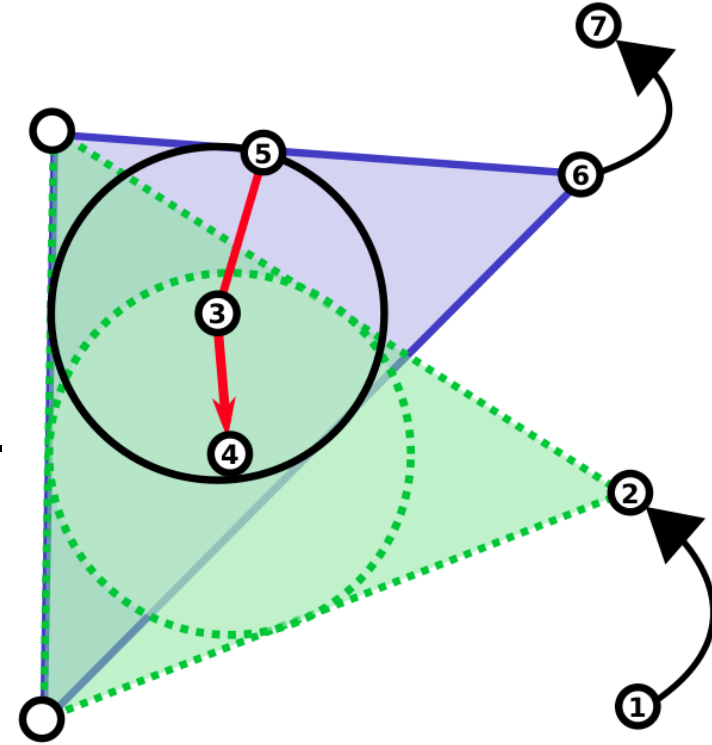
# Little Dog Demo [Vernaza et al., '09]

- Little Dog robot needs to traverse a fully-known terrain
- Planning
  - Plans footsteps first with an anytime variant of A\*
  - Compute COM of the robot afterwards to support execution



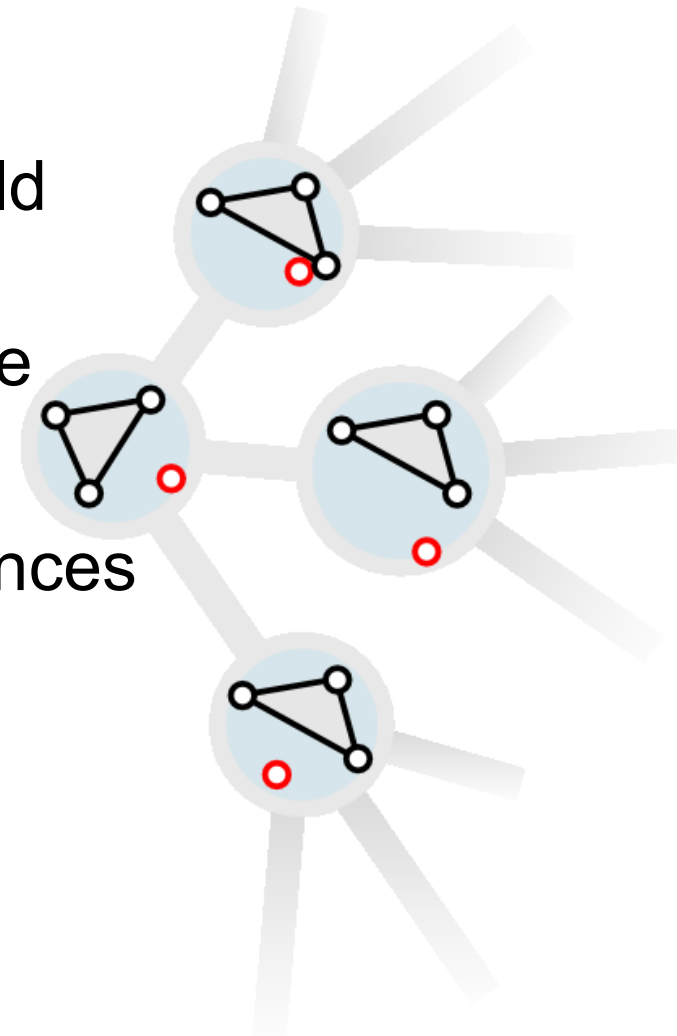
## Assumptions of the planner:

- Only one leg lifted at a time to ensure static stability
- Center of mass shifts during quad-support phase to prevent tipping
- Footholds chosen deliberately to maximize stability

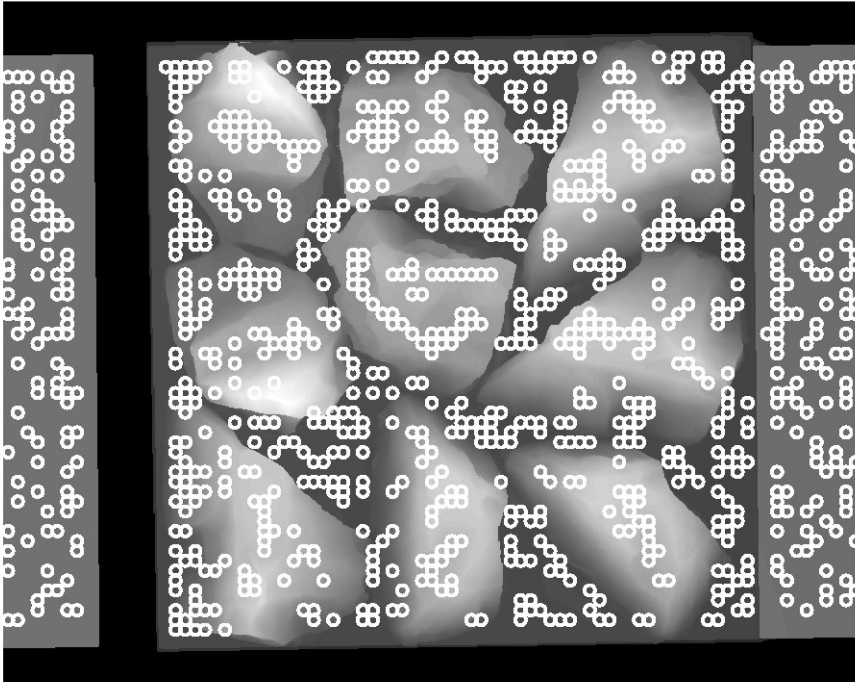


## Planner builds (on-the-fly/implicit) Stance Graph:

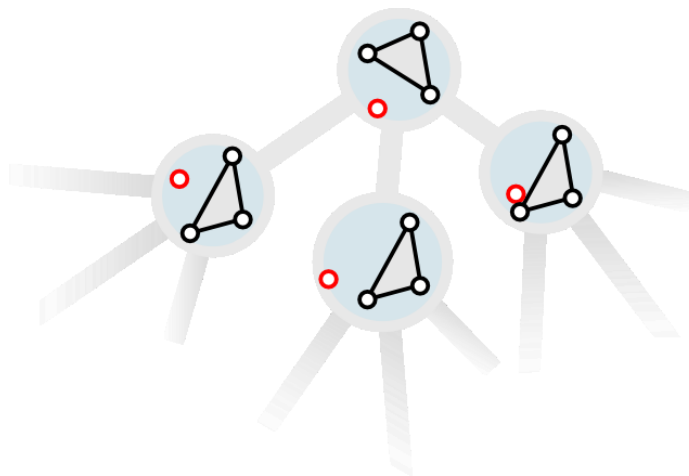
- **Node (stance):** 9-dimensional foothold configuration
  - feet positions and current gait phase
- **Edge:** feasible transition between stances
- **Edge costs** for transitions computed based on risk, anticipated delay



# Implementation of *GetSuccessors(s)* Function

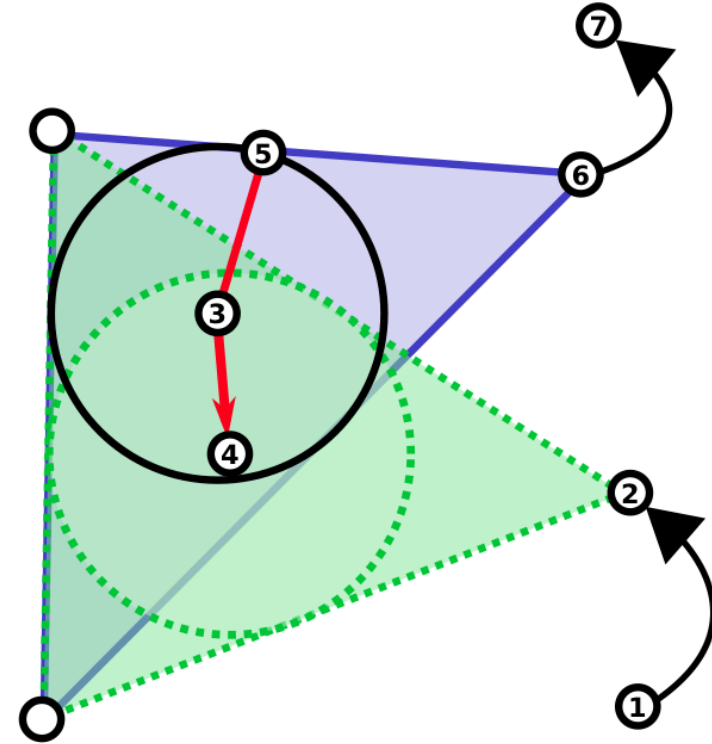


- Finite set of good quality candidate footholds selected prior to planning
- Valid stances are kinematically feasible 4-tuples of candidate footholds
- Successors of a given stance computed by:
  - determining reachable candidate footholds that result in a valid stance



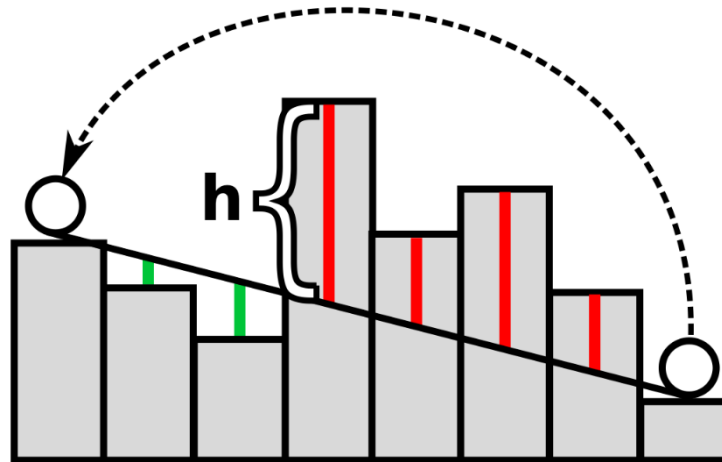
# Implementation of $GetCost(s, s')$ Function

- Edgecosts are weighted sum of:
  - **Overhead**
    - Fixed cost per step
  - **Center of mass travel**
    - Discourages backwards motion of COM
  - **Incircle radius**
    - Farthest distance from interior to exterior of support triangle



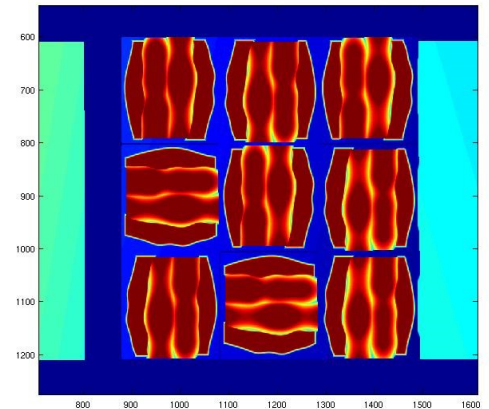
# Implementation of $GetCost(s, s')$ Function

- Edgecosts are weighted sum of:
  - **Collision**
    - Risk of body/foot colliding with terrain
  - **Foot height variance**
    - Encourages robot to stay level



# Implementation of $GetCost(s, s')$ Function

- Edgecosts are weighted sum of:
  - **Reachability**
    - Robot's ability to reach next foothold, switch to next support triangle without dragging feet
  - **Terrain slope**
    - Ensures terrain slope supports direction of motion
  - **Terrain cost**
    - Considers slippage potential given terrain



# Implementation of $GetCost(s, s')$ Function

- Edgecosts are weighted sum of:

- **Reachability**

- Robot's ability to support triangle without falling

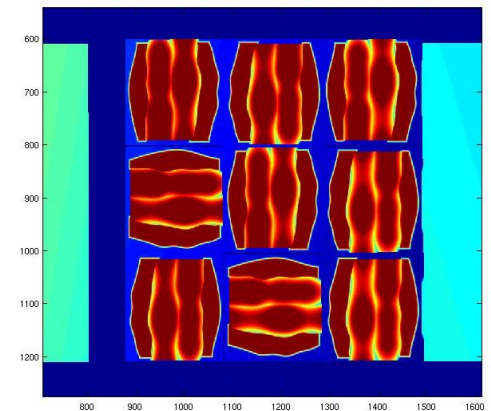
*Lots of features make up the cost function.  
Fine tuning them is not fun ☹*

- **Terrain slope**

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# Implementation of $GetCost(s, s')$ Function

- Edgecosts are weighted sum of:

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*Lots of features make up the cost function.  
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- **Terrain slope**

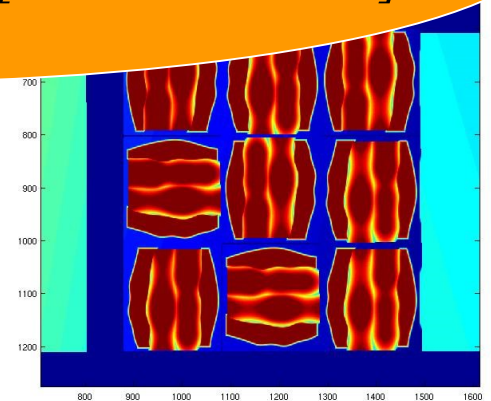
- Ensures terrain slope direction

*Any thoughts on making the process easier?*

*Using Learning Cost (Inverse RL) function we learned before!  
See it being used for LittleDog by [Zucker et al., '09]*

- **Terrain cost**

- Considers slippage potential given terrain



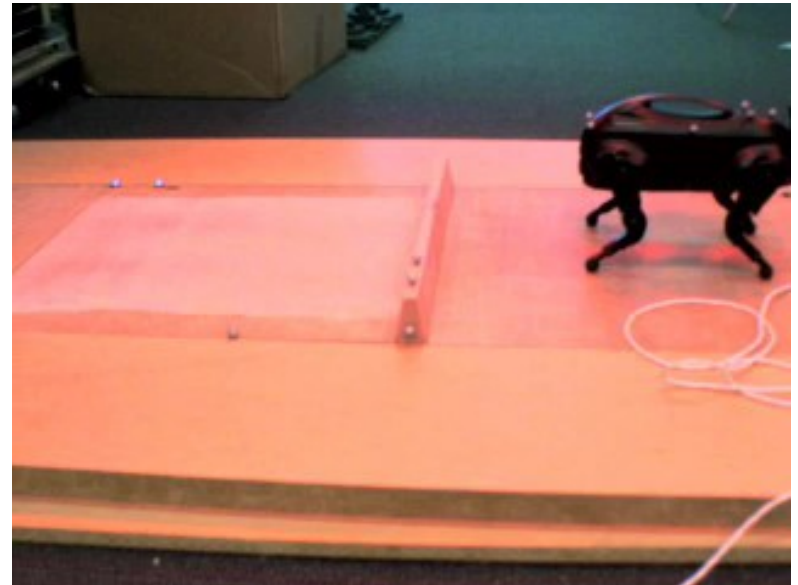
# Sometimes smart but often stupid

## Search-based planning for a legged robot over rough terrain

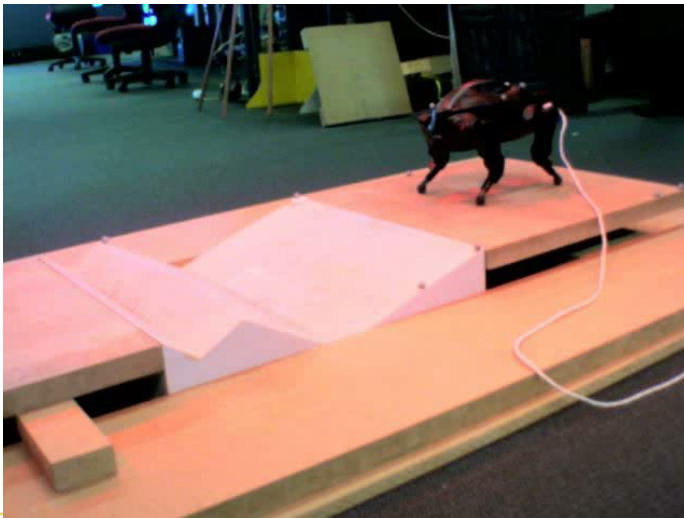
Paul Vernaza, Maxim Likhachev,  
Subhrajit Bhattacharya, Sachin Chitta\*,  
Aleksandr Kushleyev, Daniel D. Lee

GRASP Laboratory  
University of Pennsylvania

\*Willow Garage, Inc.



*no footstep planning*



# Summary

- Multiple planners used for both domains
- Start and goal configurations are often most constrained
  - can be exploited by the planners
- Cost is really complex in planning for articulated robots (e.g., quadrupeds and humanoids)
- Planning is higher-dimensional but can take longer than on ground and aerial vehicles
- Design of proper heuristics is a key to efficiency