Abstract—An accurate optical sensing system has been
developed to measure the position and orientation of a laser
beam in two dimensions. The system is useful for evaluation of
the accuracy of hand-held laser microsurgical instruments.
The apparatus uses a lens and a beam-splitter to receive the
incoming laser beam. Two position sensitive detectors placed
at different distances from the beam splitter make it possible to
rapidly and accurately calculate the position and orientation of
the axis of the laser.

Keywords—Microsurgery, accuracy, optical sensing,
position sensitive detector, angular measurement, tremor

I. INTRODUCTION

The need to improve accuracy in microsurgery has led
efforts to enhance accuracy using teleoperation [1,2], the
“steady-hand” approach in which surgeon and robot hold the
same tool [3], and, most recently, a fully hand-held
instrument developed in our laboratory to perform active
tremor compensation [4]. Plans for this active instrument
(known as “Micron”)[5] include a prototype for hand-held
laser microsurgery. To test this design, there is a need for a
system to track the laser beam during tremor-canceling
experiments.

There are many commercial systems that are commonly
used in tracking surgical instruments, including Optotrak
(Northern Digital, Waterloo, Canada), miniBird (Ascension
Technology Corp., Burlington, Vt.), and Isotrak II
(Polhemus, Colchester, Vt.). These systems offer six-
degree-of-freedom (6-dof) tracking and fast response, but,
although their accuracy is high, it is still insufficient for
microsurgical tremor studies. Given the small size of the
active microsurgical instrument, another drawback is that
they require that sensors be attached to the instrument,
possibly resulting in a significant change in the very
dynamics the experiments are designed to measure.

We have developed an instrument that uses a reflective
approach to track the tip of Micron when fitted with a
mechanical tool tip [6]. However, testing with the laser-
equipped instrument presents a slightly different problem.
A single planar position sensitive detector (PSD), such as
those used in [6], would allow tracking of the beam, but
such a 2-dof sensing approach would not allow rotation to
be distinguished from translation in the results. Actual
localization of the laser axis in space is a 5-dof problem.
However, one parameter can be determined and known by
the design of the tracking instrument itself, leaving four
parameters that must be tracked.

This paper presents the development of MADRID
(Measurement Apparatus to Distinguish Rotational and
Irrotational Displacement), a tracking instrument for laser
microsurgical devices. It also presents initial results from
calibration and testing of the instrument.

II. METHODOLOGY

A. System development

The primary elements in MADRID are optical sensors
to track the laser beam. While CCD cameras could be used,
this option is costly due to the two high-frame-rate and high-
resolution digital cameras and frame grabbers needed. As an
alternative, PSDs offer high accuracy, high frequency
response, and lower cost. They provide analog output, thus
avoiding issues of pixel resolution, and are best suited to
tracking a single light spot, such as in this application.

MADRID uses two PSDs to track the laser beam. A
bandpass optical filter (10LF20-670, Newport, Irvine, CA)
is used to block ambient light. The wavelength of the laser
diode matches with the filter CWL (center wavelength). The
bandwidth (FWHM) is 19.4 nm. The laser is split in two
beams by a Tech Spec™ Standard Cube Beam splitter
(NT45-111, Edmund Optics, Barrington, NJ). The size of
the cube is 12.5 mm on each side. After the split, each beam
is received by a PSD (DL 100-7PCBA, Pacific Silicon
Sensor Inc., Westlake Village, CA). The DL 100-7PCBA is
a duolateral position sensing module composed of a 1-cm-
square PSD and an associated amplifier circuit. It senses the
position of a laser spot on the surface of the photodiode and
gives analog current outputs indicating the centroid of the
spot in x and y, as well as intensity. The circuit converts that
current signal into a voltage signal. In order to increase the
linearity of the sensor, the PSD works in reverse bias, so the
PSDs are powered by ±15 V power supply. Under these
conditions the linearity given by the PSD is ±1 percent of
full scale.

Each sensor gives four outputs, two of which are related
to the distance from the centroid of the light spot to the
center of the PSD along the x-axis, while the other two deal
with the y-axis. Within each output pair, one is proportional
to the distance and the light intensity, while the other is
proportional only to the intensity. By normalizing the x and
y signal they become independent of the total light intensity
and therefore independent of changes in the laser diode
power.
The analog signal is sampled at 1000 Hz with an A/D card (5508, ADAC, Woburn, Mass.). Every signal has an offset that is estimated and subtracted by software. Then the signals are passed through a software lowpass filter to reduce the noise.

The system is shown in Figure 1. The displacements measured by the two PSDs are the same when the laser beam is translated. If the beam is rotated (except for rotation about its own axis), the readings of the two PSDs will differ as a function of the difference between dimensions $a$ and $d$.

\[
\alpha = \arctan\left(\frac{x_1 - x_2}{a - d}\right) \\
\beta = \arctan\left(\frac{y_1 - y_2}{a - d}\right)
\]

In practice, since the quantity $(a-d)$ is known, the values of $x_1$, $y_1$, $\alpha$, and $\beta$ are sufficient to determine the line that represents the laser beam axis, though the actual distance, $c$, to the laser diode is unknown.

If $c$ is known, the position, $g$, of the laser diode can be calculated as follows.

\[
g_x = x_1 - (d + b + c)\tan \alpha \\
g_y = y_1 - (d + b + c)\tan \beta
\]

The values of $a$, $b$, and $d$ are known to some accuracy, being part of the design, and can be estimated with greater precision during the calibration process. The workspace of the system depends on the size of the PSD (1 cm$^2$, in this system) and on $c$.

### III. RESULTS

![Fig. 2. Results from translational calibration. Circles represent target positions. Measurements from the first PSD are represented by +, and measurements from the second PSD by ×.](image)

Fig. 2 shows the result of translational calibration. Circles represent the target positions. Measurements from the first PSD are represented by +, and measurements from the second PSD by ×.

A. Experimental methods

MADRID has been calibrated, tested for quantification of noise, and then used to track a laser held in the human hand. Precision micrometer stages were used for calibration. Each point used in the calibration was obtained by averaging 4000 points sampled at a rate of 1000 Hz.

Translational calibration was performed with $\alpha$ and $\beta$ held equal to zero. The laser was moved in steps of 1 mm. This first calibration allowed determination of the misalignment in the assembly.

After calibration, a performance test was done with the laser moving in both $x$ and $y$ in steps of 50 $\mu$m for 20 steps, for total travel of 1 mm.

Rotational calibration was then performed. The laser was rotated using rotational stages, without translation. In the first pass, $\alpha$ was changed in steps of 3.82 arc minutes while $\beta$ was held constant. The angle $\beta$ was moved in steps of 6 arc minutes while $\alpha$ was held constant.

Following calibration, the mount for the laser was held motionless and a recording was taken. Using these data, samples of noise in $\alpha$, $\beta$, $g_x$, and $g_y$ were computed. A separate recording was then taken while a human subject attempted to hold the laser motionless in the hand.
Figure 3 shows the results of the performance test. The maximum error in $x$ is 13.8 $\mu$m, and the range measures 1016 $\mu$m. The nonlinearity is 1.36%. The maximum error in $y$ is 7.8 $\mu$m, and the range measures 1000 $\mu$m. The nonlinearity is 0.78%.

Figure 4 presents the results of rotational calibration for $\alpha$. The range of total rotation is 2.56°, maximum error is 0.048°, and error due to nonlinearity is 1.86%.

Fig. 5 presents the results of calibration for $\beta$. The range of total rotation is 2.25°, maximum error is 0.077°, and error due to nonlinearity is 3.44%.

Figs. 6 and 7 present the noise samples recorded with the laser mounted motionless on the bench top. The standard deviation of the noise is represented in Table I.
TABLE I
Noise of the system.

<table>
<thead>
<tr>
<th>DOF</th>
<th>Standard deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha$</td>
<td>0.0022° ≈ 8”</td>
</tr>
<tr>
<td>$\beta$</td>
<td>0.0021° ≈ 8”</td>
</tr>
<tr>
<td>$g_x$</td>
<td>3.66 µm</td>
</tr>
<tr>
<td>$g_y$</td>
<td>3.25 µm</td>
</tr>
</tbody>
</table>

Figure 8 and 9 present the data recorded while a subject tried to hold the laser motionless in the hand.

Figure 8. Rotational data recorded while a subject attempted to hold a laser motionless in the hand, showing rotation in $\alpha$ (top) and $\beta$ (bottom).

Figure 9. Translational data recorded while a subject attempted to hold a laser motionless in the hand, shown movement in $x$ (top) and $y$ (bottom).

IV. DISCUSSION

The results show that the system performs well enough to be used for evaluation of microsurgical instruments that are designed to achieve positioning accuracy of 10 µm. In addition to performance validation of mechatronic or robotic laser microsurgical instruments, the system is also useful for evaluation of the ergonomics of passive instruments, as well as for assessment of surgeons. Furthermore, it allows acquisition of high-precision data to be used in further development of error estimation algorithms such as those used in Micron.

V. CONCLUSION

An optical system to track general motion (rotation and translation) of a laser beam has been developed using position sensitive detectors. The system will be used to validate the performance of hand-held mechatronic tools for laser microsurgery.

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REFERENCES