



10-601 Introduction to Machine Learning

Machine Learning Department
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Decision Trees (Part II)

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Lecture 3
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Q&A

Q: In our medical diagnosis example, suppose two of our doctors (i.e. experts) disagree about whether (+) or not (-) to prescribe. How would the decision tree represent this situation?

A: Today we will define decision trees that predict a single class by a majority vote at the leaf. More generally, the leaf could provide a probability distribution over output classes $p(y|\mathbf{x})$

Q&A

Q: How do these In-Class Polls work?

- A:**
- Sign into **Google Form** (link from Schedule page) using **Andrew Email** (<http://p3.mlcourse.org>)
 - Answer **during lecture** for full credit, or the **same day** (i.e. before 11:59pm) **also for full credit**
 - Avoid the **calamity option** which gives negative points!
 - 8 “free polls” but can’t use more than 3 free polls consecutively
 - Submit a **poll card** if and only if you do not have a smartphone/tablet

Reminders

- **Homework 1: Background**
 - Out: Wed, Aug. 28
 - Due: Wed, Sep. 04 at 11:59pm
 - unique policy for this assignment: we will grant (essentially) any and all extension requests
- **Homework 2: Decision Trees**
 - Out: Wed, Sep. 04
 - Due: Wed, Sep. 18 at 11:59pm

DECISION TREES

Decision Trees

Chalkboard

- Example: Medical Diagnosis
- Does memorization = learning?
- Decision Tree as a hypothesis
- Function approximation for DTs

Tree to Predict C-Section Risk

Learned from medical records of 1000 women (Sims et al., 2000)

Negative examples are C-sections

```
[833+,167-] .83+ .17-
Fetal_Presentation = 1: [822+,116-] .88+ .12-
| Previous_Csection = 0: [767+,81-] .90+ .10-
| | Primiparous = 0: [399+,13-] .97+ .03-
| | Primiparous = 1: [368+,68-] .84+ .16-
| | | Fetal_Distress = 0: [334+,47-] .88+ .12-
| | | | Birth_Weight < 3349: [201+,10.6-] .95+ .05-
| | | | Birth_Weight >= 3349: [133+,36.4-] .78+ .22-
| | | Fetal_Distress = 1: [34+,21-] .62+ .38-
| Previous_Csection = 1: [55+,35-] .61+ .39-
Fetal_Presentation = 2: [3+,29-] .11+ .89-
Fetal_Presentation = 3: [8+,22-] .27+ .73-
```

DECISION TREE LEARNING

Decision Trees

Chalkboard

- An Aside:
 - The Majority Vote Classifier
 - Error Rate
- Decision Tree Learning

Majority Vote Classifier Example

Dataset:

Output Y, Attributes A and B

Y	A	B
-	1	0
-	1	0
+	1	0
+	1	0
+	1	1
+	1	1
+	1	1
+	1	1

In-Class Exercise

What is the **training error** (i.e. *error rate on the training data*) of the **majority vote classifier** on this dataset?

Choose one of:
 $\{0/8, 1/8, 2/8, \dots, 8/8\}$

Decision Tree Learning Example

Dataset:

Output Y, Attributes A, B, C

Y	A	B	C
-	1	0	0
-	1	0	1
-	1	0	0
+	0	0	1
+	1	1	0
+	1	1	1
+	1	1	0
+	1	1	1

In-Class Exercise

Using **error rate** as the splitting criterion, what decision tree would be learned by ID3?

Decision Tree Learning Example

Dataset:

Output Y, Attributes A and B

Y	A	B
-	1	0
-	1	0
+	1	0
+	1	0
+	1	1
+	1	1
+	1	1
+	1	1

In-Class Exercise

Which attribute would **error rate** select for the next split?

1. A
2. B
3. A or B (tie)
4. Neither

Decision Tree Learning Example

Dataset:

Output Y, Attributes A and B

Y	A	B
-	1	0
-	1	0
+	1	0
+	1	0
+	1	1
+	1	1
+	1	1
+	1	1

Information Theory & DTs

Chalkboard

- Information Theory primer
 - Entropy
 - (Specific) Conditional Entropy
 - Conditional Entropy
 - Information Gain / Mutual Information
- Information Gain as DT splitting criterion

Decision Tree Learning Example

Dataset:

Output Y, Attributes A and B

Y	A	B
-	1	0
-	1	0
+	1	0
+	1	0
+	1	1
+	1	1
+	1	1
+	1	1

In-Class Exercise

Which attribute would **mutual information** select for the next split?

1. A
2. B
3. A or B (tie)
4. Neither

Decision Tree Learning Example

Dataset:

Output Y, Attributes A and B

Y	A	B
-	1	0
-	1	0
+	1	0
+	1	0
+	1	1
+	1	1
+	1	1
+	1	1

Tennis Example

Test your understanding

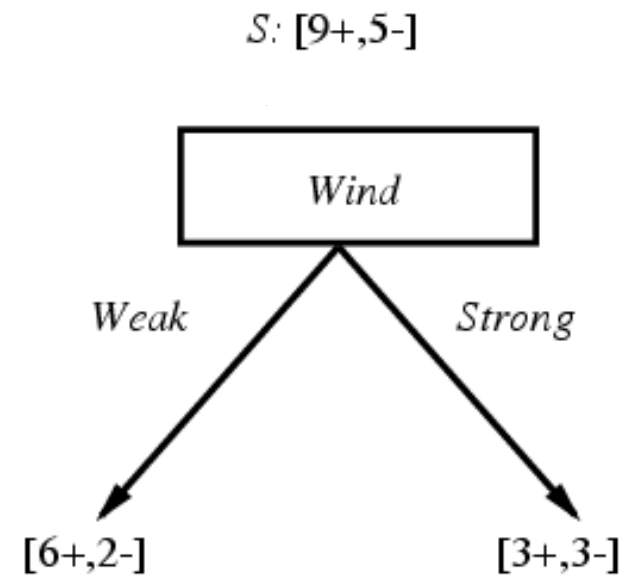
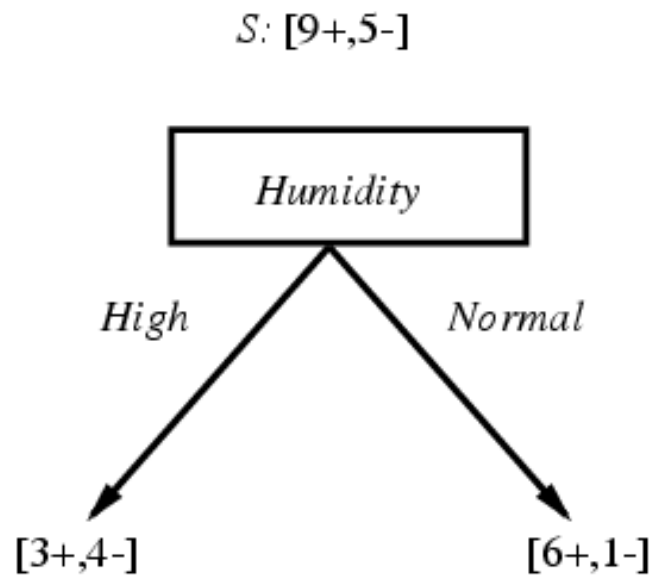
Dataset:

Day	Outlook	Temperature	Humidity	Wind	PlayTennis?
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Tennis Example

Which attribute yields the best classifier?

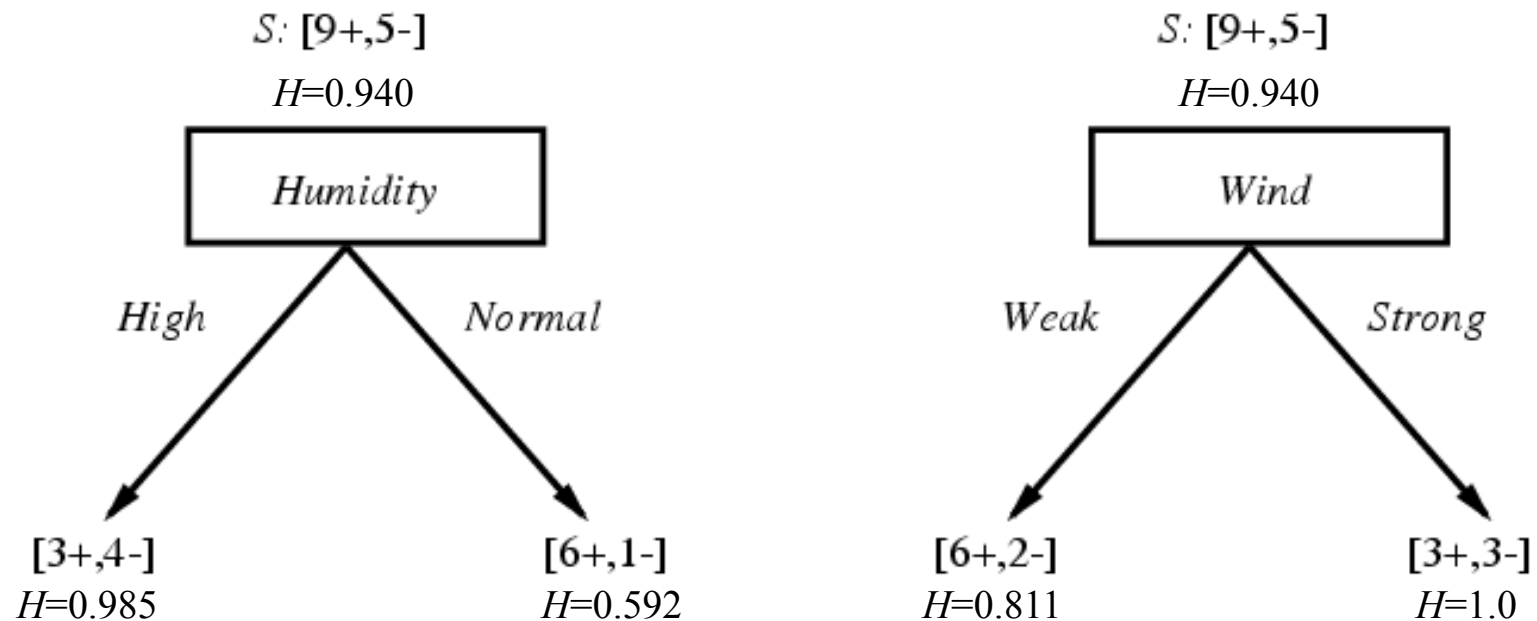
Test your understanding



Tennis Example

Which attribute yields the best classifier?

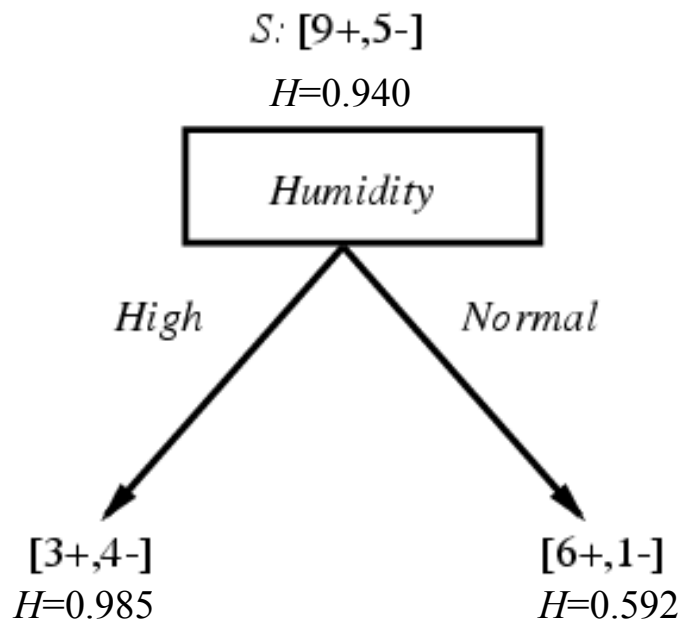
Test your understanding



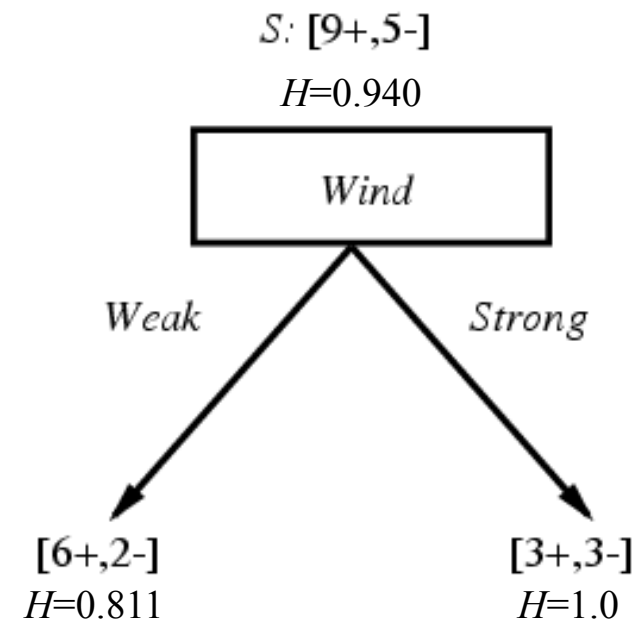
Tennis Example

Which attribute yields the best classifier?

Test your understanding



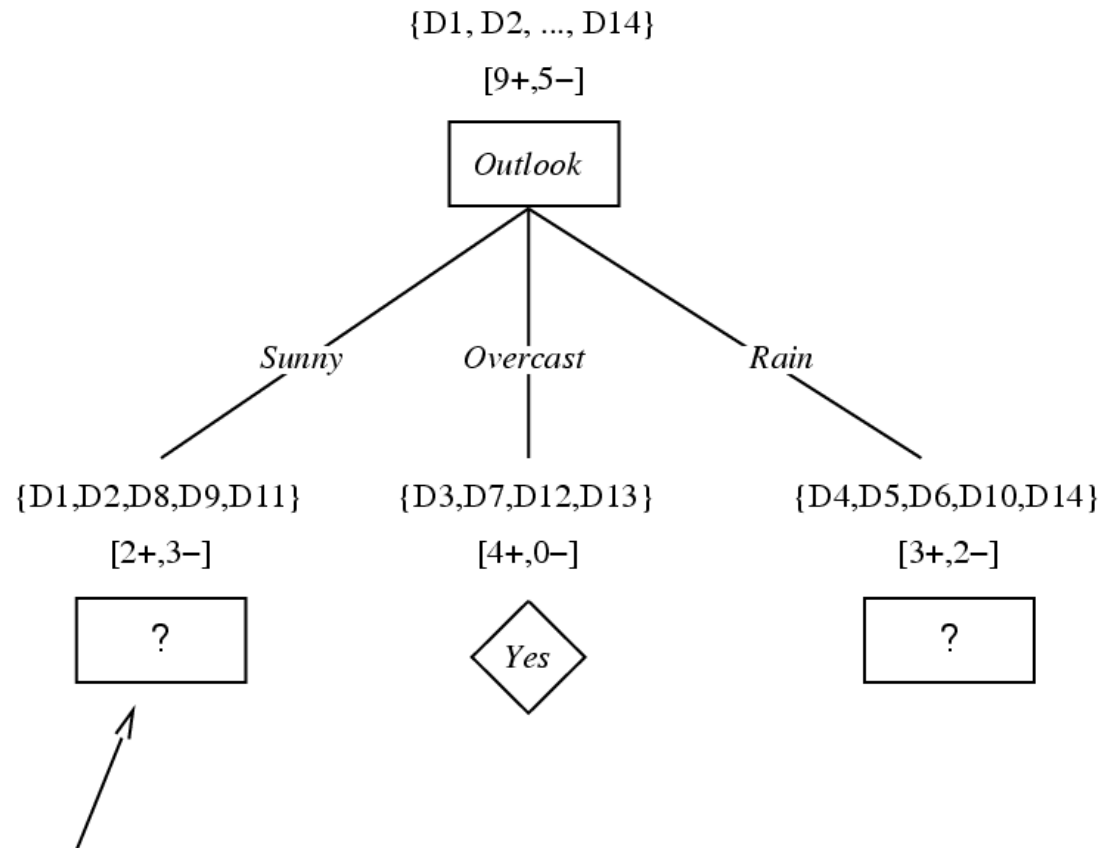
$$\begin{aligned} \text{Gain}(S, \text{Humidity}) &= .940 - (7/14).985 - (7/14).592 \\ &= .151 \end{aligned}$$



$$\begin{aligned} \text{Gain}(S, \text{Wind}) &= .940 - (8/14).811 - (6/14)1.0 \\ &= .048 \end{aligned}$$

Tennis Example

Test your understanding



$$S_{\text{sunny}} = \{D1, D2, D8, D9, D11\}$$

$$\text{Gain}(S_{\text{sunny}}, \text{Humidity}) = .970 - (3/5) 0.0 - (2/5) 0.0 = .970$$

$$\text{Gain}(S_{\text{sunny}}, \text{Temperature}) = .970 - (2/5) 0.0 - (2/5) 1.0 - (1/5) 0.0 = .570$$

$$\text{Gain}(S_{\text{sunny}}, \text{Wind}) = .970 - (2/5) 1.0 - (3/5) .918 = .019$$