

# Computer Performance:

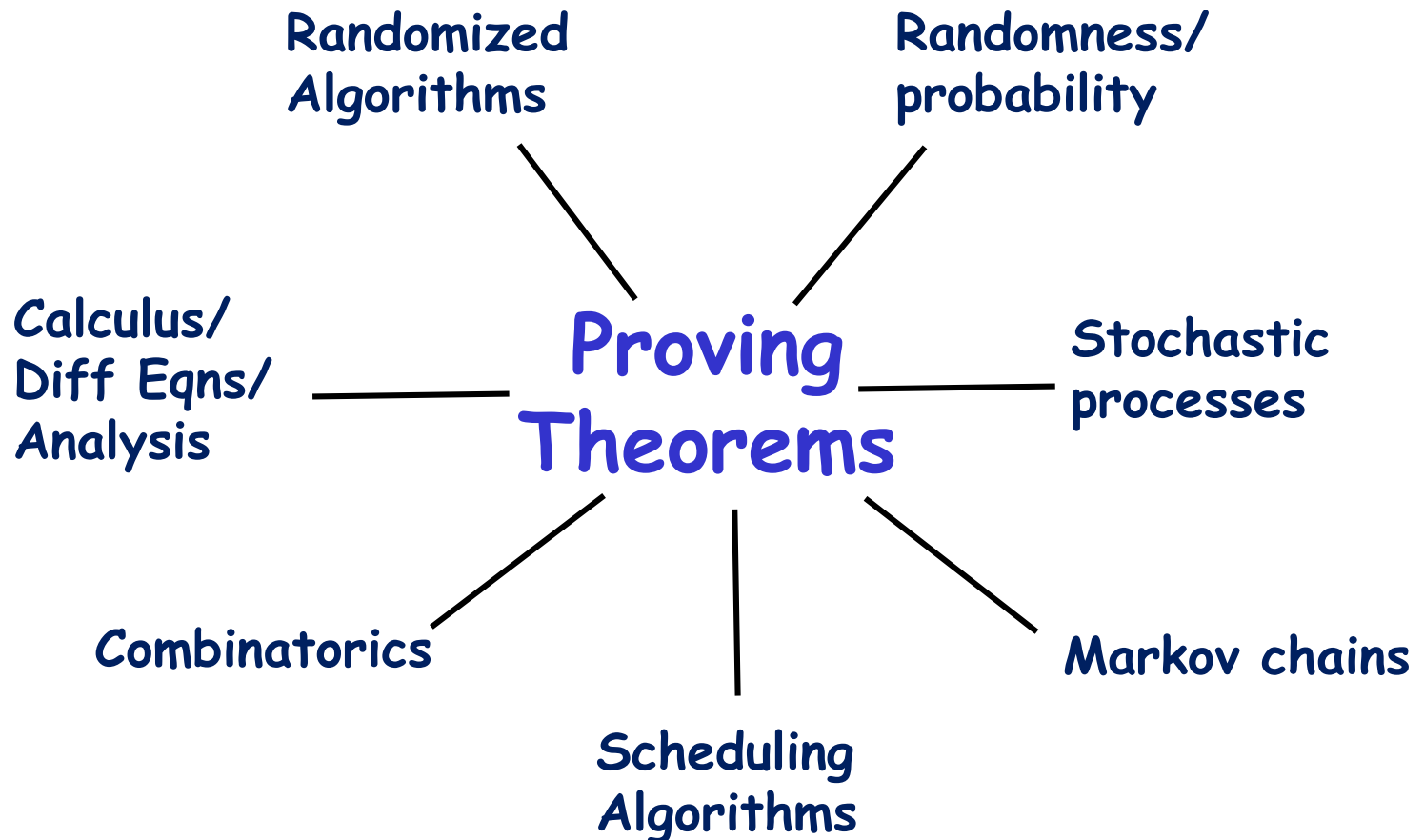


## Queueing and Scheduling

**Mor Harchol-Balter**  
**Computer Science Dept, CMU**

**Accepting new student**

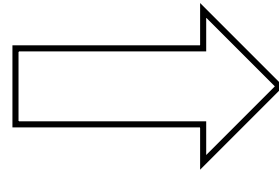
Work with me if you like ...



Work with me if you want to do theory that computer systems folks care about ...

### Typical Systems Goals

- ❑ "Reducing tail latency"
- ❑ "Guaranteeing flow fairness"
- ❑ "Combatting transient overload"
- ❑ "Optimally assigning heterogeneous resources to heterogeneous jobs"
- ❑ "Minimizing energy usage while meeting QoS latency goals"
- ❑ "Dynamic capacity provisioning"

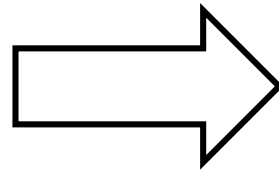


Theory

Work with me if you want to do theory that computer systems folks care about ...

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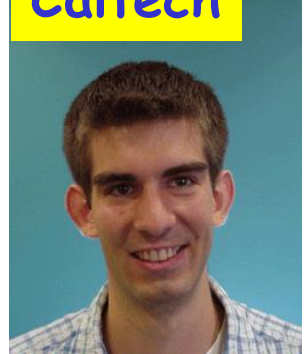
Scheduling  
Theory

# Work with me if you want to end up in academia ...

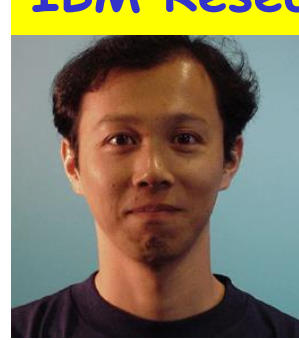
U. Toronto



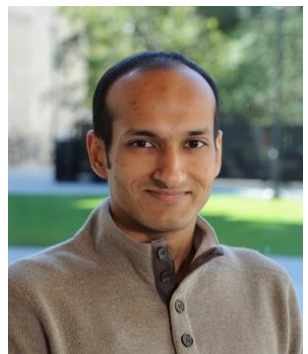
Caltech



IBM Research



StonyBrook



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U. Minnesota



Amherst

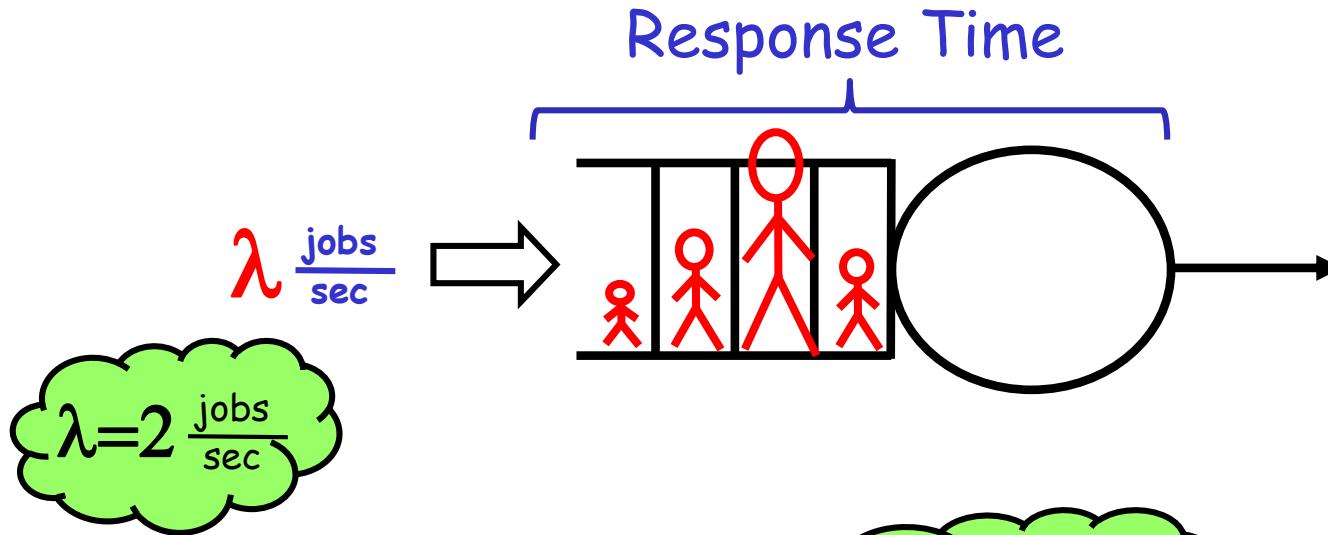


Penn State



- Analysis
- Speaking
- Teaching
- Writing
- Health

# Scheduling 101



$S$  = job size (sec)

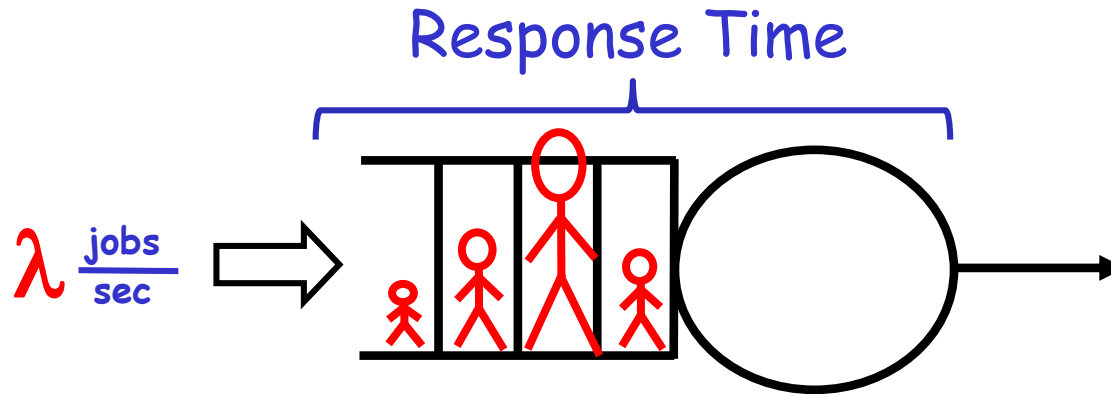
$$E[S] = \frac{1}{3} \text{ sec}$$

$\rho$  = load = Fraction of time server is busy

$$\rho = \lambda E[S] = \frac{2}{3}$$

Q: What scheduling policy minimizes  $E[\text{RespTime}]$ ?

# Scheduling 101



## Non-Preemptive

## Preemptive

**FCFS:** First Come First Served

**LCFS:** Last Come First Served

**Random:** Pick Random Job

**SJF:** Shortest Job First

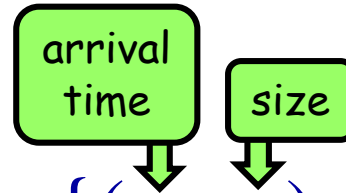
**PS:** Processor Sharing

**SRPT:** Shortest Remaining Processing Time

Q: How do these compare wrt  $E[\text{Resp Time}]$ ?

Q: Is SRPT optimal?

# Optimality of SRPT



Defn: Arrival Sequence  $A = \{(a_1, s_1), (a_2, s_2), (a_3, s_3), \dots\}$

Claim:  $\forall A$ ,  $SRPT(A)$  is optimal for  $E[\text{RespTime}]$

Proof Sketch:



Consider a given  $A$ .

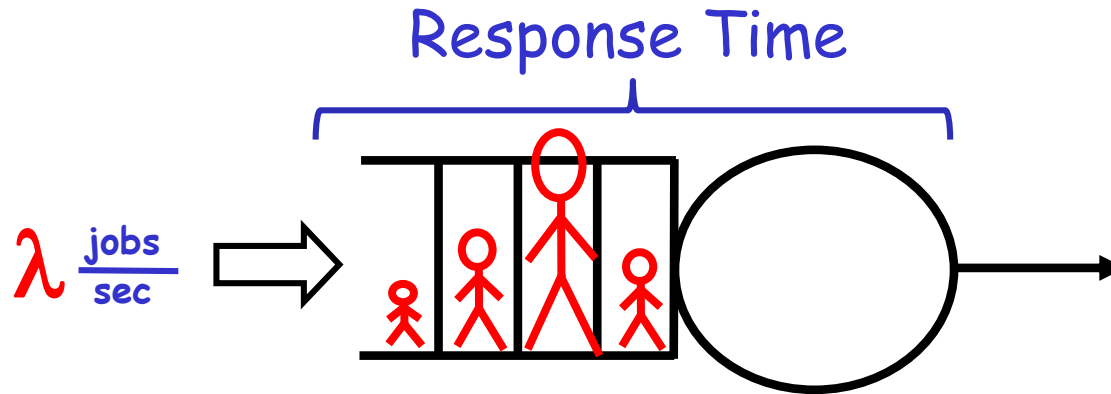
Define  $OPT(A)$  as yielding optimal response time for  $A$ .

Assume that  $SRPT(A) \neq OPT(A)$ .

Prove there's a contradiction.



# Scheduling Optimality



## Non-Preemptive

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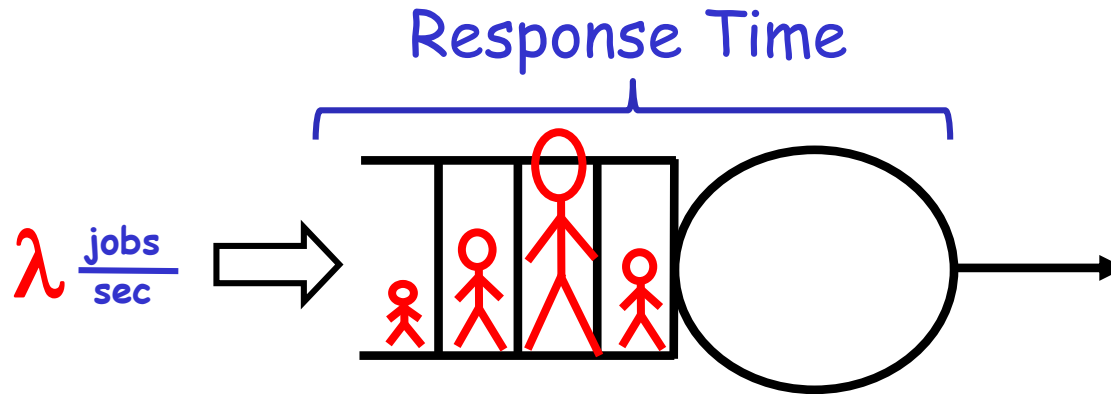
## Preemptive

**PS:** Processor Sharing

**SRPT:** Shortest  
Remaining  
Processing  
Time

Q: Is SRPT  
optimal for  
 $E[\text{Resp Time}]$ ?

# Scheduling Optimality



## Non-Preemptive

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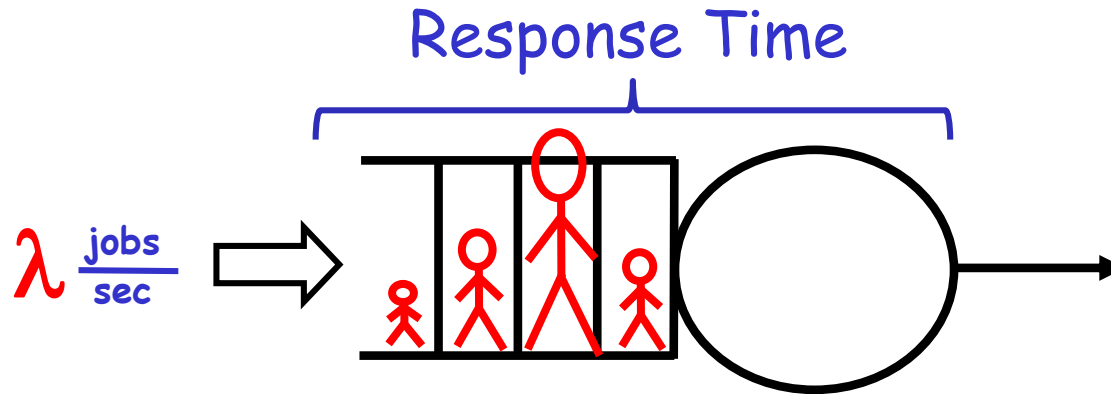
## Preemptive

**PS:** Processor Sharing

**SRPT:** Shortest  
Remaining  
Processing  
Time

Q: Is SRPT  
optimal for  
99<sup>th</sup> %-tile  
Resp Time?

# Scheduling Optimality



## Non-Preemptive

**FCFS:** First Come First Served

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**Random:** Pick Random Job

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Job First

## Preemptive

**PS:** Processor Sharing

**SRPT:** Shortest  
Remaining  
Processing  
Time

Q: What is optimal for  
Max response  
time?

# Slowdown Metric

$$\text{Slowdown}(\text{job}) = \frac{\text{RespTime}(\text{job})}{\text{Size}(\text{job})}$$

**Q: Does SRPT minimize  $E[\text{Slowdown}]$ ?**

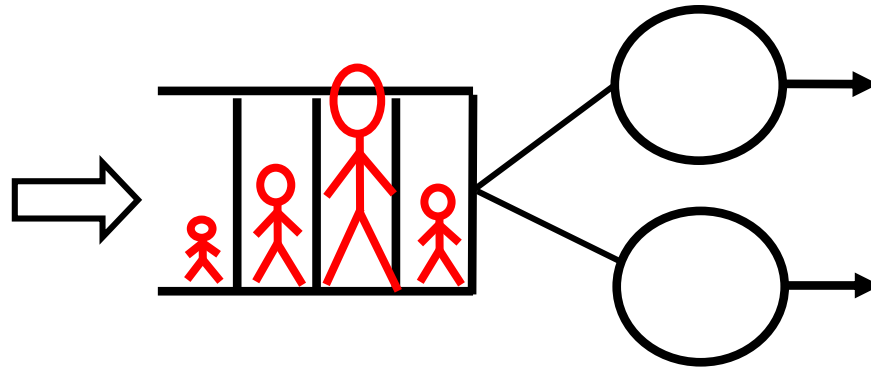
**Yes?**

**Q: Prove it!**

**No?**

**Q: What scheduling policy is optimal for  $E[\text{Slowdown}]$ ?**

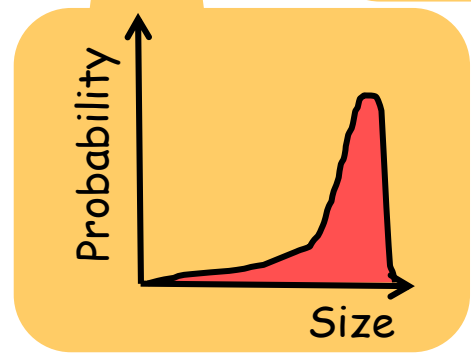
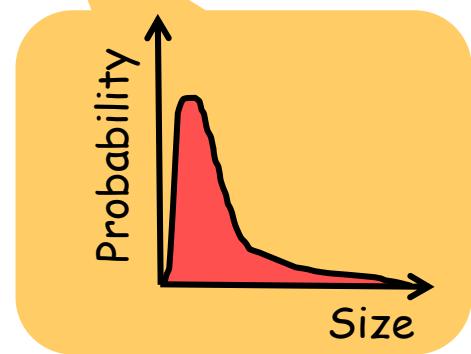
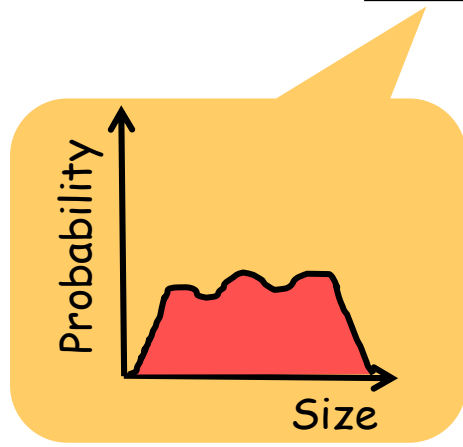
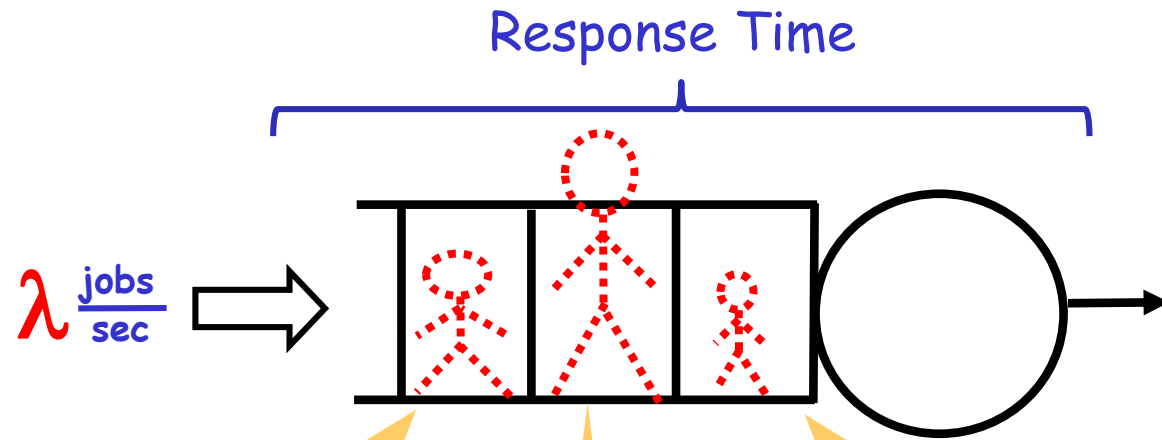
# Minimizing Response Time for 2 Servers



Q: How should we schedule to minimize  $E[\text{Response Time}]$  given 2 servers?  
(assume you can preempt jobs)

Q: Is your policy optimal?

# What if Don't Know Size?



Q: What's the right scheduling policy?

Q: Is your policy optimal?

# Real World Jobs are Multi-Dimensional

“job” = (# servers, duration)

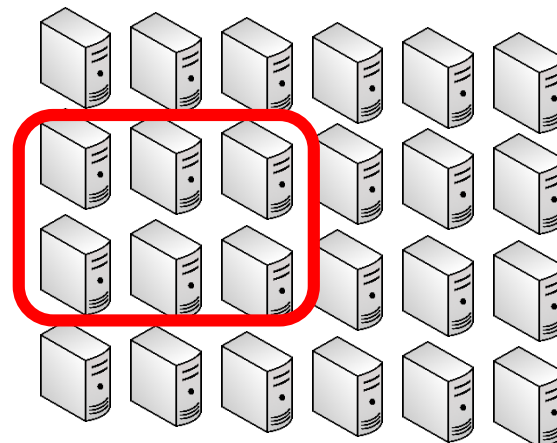
(500srvs, 1hr)

(575srvs, 1min)

(32srvs, 12hrs)

○  
○  
○

1 “cell” at Google  
= 10,000 servers

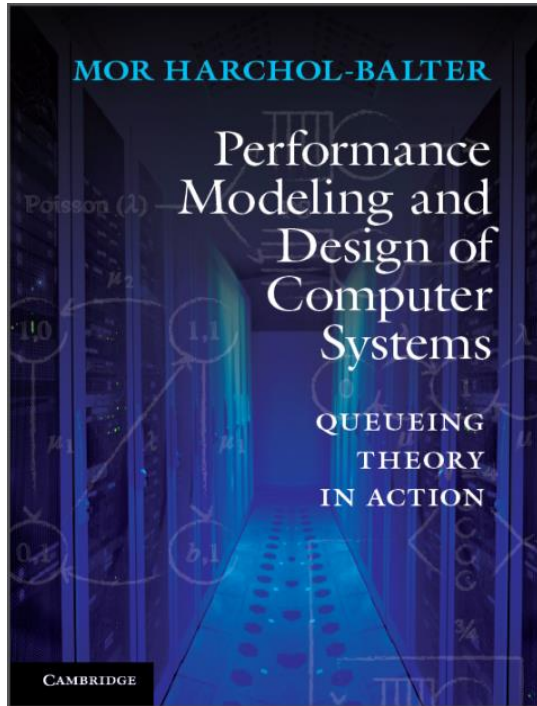


Q: Stability condition?

Q:  $E[\text{Response time}]$ ?

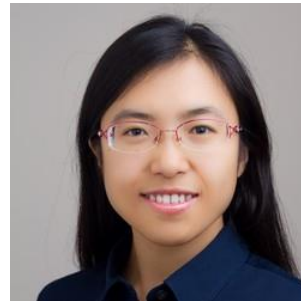
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This Semester: 15-857  
Analytical Performance Modeling  
MWF 1:25 p.m.

co-Instructor:



Awesome TAs:



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