

Machine Learning



- improve their <u>performance</u>
- at some <u>task</u>
- with <u>experience</u>

Object detection

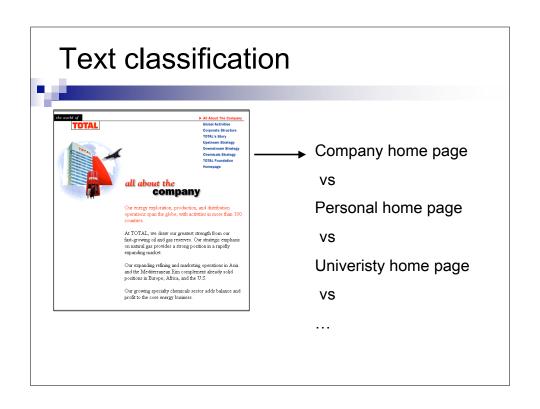
(Prof. H. Schneiderman)

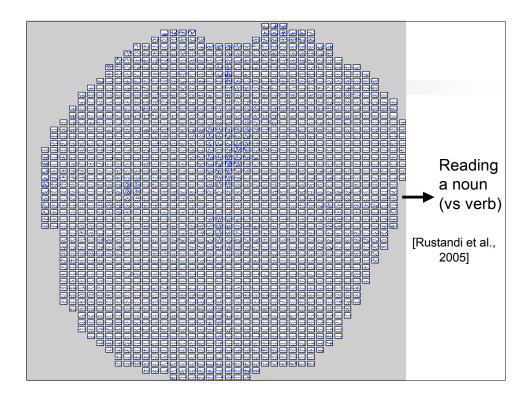


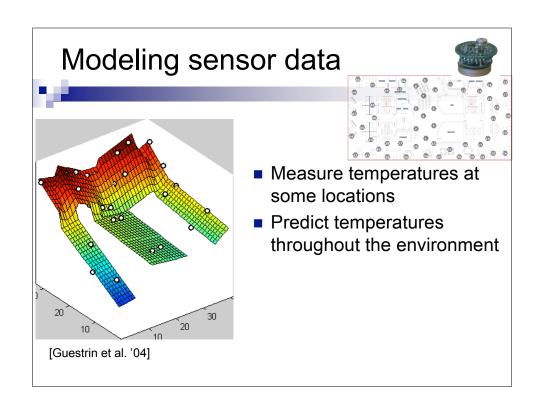


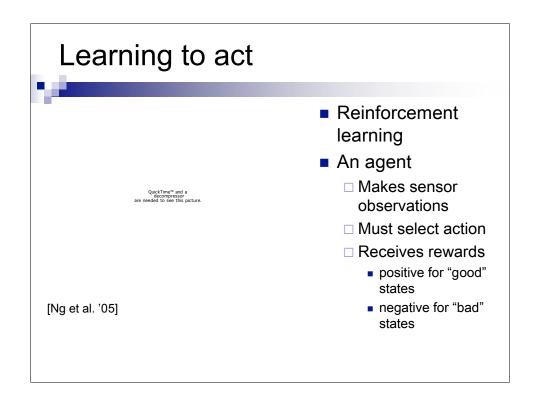
Example training images for each orientation











Growth of Machine Learning

- Machine learning is preferred approach to
 - □ Speech recognition, Natural language processing
 - □ Computer vision
 - □ Medical outcomes analysis
 - Robot control
 - ----
- This trend is accelerating
 - □ Improved machine learning algorithms
 - □ Improved data capture, networking, faster computers
 - □ Software too complex to write by hand
 - □ New sensors / IO devices
 - □ Demand for self-customization to user, environment

Syllabus

- - Covers a wide range of Machine Learning techniques – from basic to state-of-the-art
 - You will learn about the methods you heard about:
 - □ Naïve Bayes, logistic regression, nearest-neighbor, decision trees, boosting, neural nets, overfitting, regularization, dimensionality reduction, PCA, error bounds, VC dimension, SVMs, kernels, margin bounds, K-means, EM, mixture models, semi-supervised learning, HMMs, graphical models, active learning, reinforcement learning...
 - Covers algorithms, theory and applications
 - It's going to be fun and hard work ©

Prerequisites

- - Probabilities
 - □ Distributions, densities, marginalization...
- Basic statistics
 - □ Moments, typical distributions, regression...
- Algorithms
 - □ Dynamic programming, basic data structures, complexity...
- Programming
 - □ Mostly your choice of language, but Matlab will be very useful
- We provide some background, but the class will be fast paced
- Ability to deal with "abstract mathematical concepts"

Review Sessions



- Very useful!
 - □ Review material
 - □ Present background
 - □ Answer questions
- Thursdays, 5:30-6:50 in Wean Hall 5409
- First recitation is tomorrow
 - □ Review of probabilities
- Special recitation on Matlab
 - ☐ Jan. 24 Wed. 5:30-6:50pm NSH 1305

Staff

- - Four Great TAs: Great resource for learning, interact with them!
 - □ Andy Carlson, acarlson@cs
 - ☐ Jonathan Huang, jch1@cs
 - □ Purna Sarkar, psarkar@cs
 - □ Brian Ziebart, bziebart@cs
 - Administrative Assistant
 - ☐ Monica Hopes, x8-5527, meh@cs

First Point of Contact for HWs

- - To facilitate interaction, a TA will be assigned to each homework question This will be your "first point of contact" for this question
 - $\hfill\square$ But, you can always ask any of us
 - For e-mailing instructors, always use:
 - □ 10701-instructors@cs.cmu.edu
 - For announcements, subscribe to:
 - □ 10701-announce@cs
 - □ https://mailman.srv.cs.cmu.edu/mailman/listinfo/10701-announce

Text Books



- Required Textbook:
 - □ Pattern Recognition and Machine Learning; Chris Bishop
- Optional Books:
 - □ Machine Learning; Tom Mitchell
 - ☐ The Elements of Statistical Learning: Data Mining, Inference, and Prediction; Trevor Hastie, Robert Tibshirani, Jerome Friedman
 - Information Theory, Inference, and Learning Algorithms; David MacKay

Grading



- 5 homeworks (30%)
 - ☐ First one goes out 1/24
 - Start early, Start early
- Final project (20%)
 - □ Details out Feb 26th
- Midterm (20%)
 - ☐ March 7th in class
- Final (30%)
 - □ May 15th, 1-4 p.m.

Homeworks



- Homeworks are hard, start early ©
- Due in the beginning of class
- 3 late days for the semester
- After late days are used up:
 - ☐ Half credit within 48 hours
 - □ Zero credit after 48 hours
- All homeworks must be handed in, even for zero credit
- Late homeworks handed in to Monica Hopes, WEH 4619
- Collaboration
 - ☐ You may discuss the questions
 - □ Each student writes their own answers
 - □ Write on your homework anyone with whom you collaborate

Sitting in & Auditing the Class



- Due to new departmental rules, every student who wants to sit in the class (not take it for credit), must register officially for auditing
- To satisfy the auditing requirement, you must either:
 - □ Do *two* homeworks, and get at least 75% of the points in each; or
 - □ Take the final, and get at least 50% of the points; or
 - Do a class project and do *one* homework, and get at least 75% of the points in the homework;
 - Only need to submit project proposal and present poster, and get at least 80% points in the poster.
- Please, send us an email saying that you will be auditing the class and what you plan to do.
- If you are not a student and want to sit in the class, please get authorization from the instructor

Enjoy!



- ML is becoming ubiquitous in science, engineering and beyond
- This class should give you the basic foundation for applying ML and developing new methods
- The fun begins...

Your first consulting job



- A billionaire from the suburbs of Seattle asks you a question:
 - ☐ He says: I have thumbtack, if I flip it, what's the probability it will fall with the nail up?
 - ☐ You say: Please flip it a few times:
 - ☐ You say: The probability is:
 - □He says: Why???
 - ☐ You say: Because...

Thumbtack - Binomial Distribution

- - P(Heads) = θ , P(Tails) = 1- θ
 - Flips are i.i.d.:
 - □ Independent events
 - ☐ Identically distributed according to Binomial distribution
 - Sequence *D* of α_H Heads and α_T Tails

$$P(\mathcal{D} \mid \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$$

Maximum Likelihood Estimation

- - Data: Observed set D of α_H Heads and α_T Tails
 - Hypothesis: Binomial distribution
 - Learning θ is an optimization problem
 - ☐ What's the objective function?
 - MLE: Choose θ that maximizes the probability of observed data:

$$\widehat{\theta} = \arg \max_{\theta} P(\mathcal{D} \mid \theta)$$

$$= \arg \max_{\theta} \ln P(\mathcal{D} \mid \theta)$$

Your first learning algorithm

$$egin{array}{lll} \widehat{ heta} &=& rg \max_{ heta} & \ln P(\mathcal{D} \mid heta) \ &=& rg \max_{ heta} & \ln heta^{lpha_H} (1- heta)^{lpha_T} \end{array}$$

Set derivative to zero:

$$\frac{d}{d\theta} \ln P(\mathcal{D} \mid \theta) = 0$$

How many flips do I need?



$$\hat{\theta} = \frac{\alpha_H}{\alpha_H + \alpha_T}$$

- Billionaire says: I flipped 3 heads and 2 tails.
- You say: θ = 3/5, I can prove it!
- He says: What if I flipped 30 heads and 20 tails?
- You say: Same answer, I can prove it!
- He says: What's better?
- You say: Humm... The more the merrier???
- He says: Is this why I am paying you the big bucks???

Simple bound (based on Hoeffding's inequality)

For
$$N = \alpha_H + \alpha_T$$
, and $\hat{\theta} = \frac{\alpha_H}{\alpha_H + \alpha_T}$

• Let θ^* be the true parameter, for any ϵ >0:

$$P(|\hat{\theta} - \theta^*| \ge \epsilon) \le 2e^{-2N\epsilon^2}$$

PAC Learning



- PAC: Probably Approximate Correct
- Billionaire says: I want to know the thumbtack parameter θ , within ϵ = 0.1, with probability at least 1- δ = 0.95. How many flips?

$$P(|\hat{\theta} - \theta^*| \ge \epsilon) \le 2e^{-2N\epsilon^2}$$

What about prior



- Billionaire says: Wait, I know that the thumbtack is "close" to 50-50. What can you?
- You say: I can learn it the Bayesian way...
- Rather than estimating a single θ , we obtain a distribution over possible values of θ

Bayesian Learning



Use Bayes rule:

$$P(\theta \mid \mathcal{D}) = \frac{P(\mathcal{D} \mid \theta)P(\theta)}{P(\mathcal{D})}$$

Or equivalently:

$$P(\theta \mid \mathcal{D}) \propto P(\mathcal{D} \mid \theta)P(\theta)$$

Bayesian Learning for Thumbtack

M

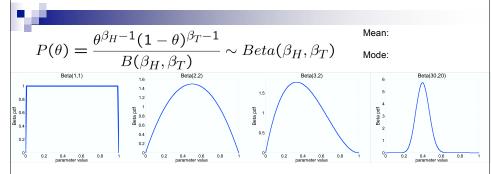
$$P(\theta \mid \mathcal{D}) \propto P(\mathcal{D} \mid \theta)P(\theta)$$

Likelihood function is simply Binomial:

$$P(\mathcal{D} \mid \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$$

- What about prior?
 - □ Represent expert knowledge
 - ☐ Simple posterior form
- Conjugate priors:
 - □ Closed-form representation of posterior
 - ☐ For Binomial, conjugate prior is Beta distribution

Beta prior distribution – $P(\theta)$

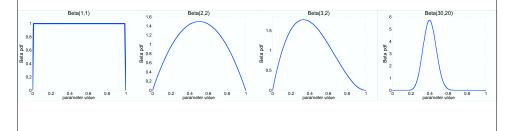


- Likelihood function: $P(\mathcal{D} \mid \theta) = \theta^{\alpha_H} (1 \theta)^{\alpha_T}$
- Posterior: $P(\theta \mid \mathcal{D}) \propto P(\mathcal{D} \mid \theta)P(\theta)$

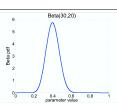
Posterior distribution

- - Prior: $Beta(\beta_H, \beta_T)$
 - \blacksquare Data: $\alpha_{\rm H}$ heads and $\alpha_{\rm T}$ tails
 - Posterior distribution:

$$P(\theta \mid \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$



Using Bayesian posterior



- - Posterior distribution:

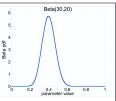
$$P(\theta \mid \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

- Bayesian inference:
 - □ No longer single parameter:

$$E[f(\theta)] = \int_0^1 f(\theta) P(\theta \mid \mathcal{D}) d\theta$$

□ Integral is often hard to compute

MAP: Maximum a posteriori approximation oproximation $P(\theta \mid \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$



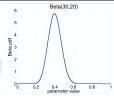
$$P(\theta \mid \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

$$E[f(\theta)] = \int_0^1 f(\theta) P(\theta \mid \mathcal{D}) d\theta$$

- As more data is observed, Beta is more certain
- MAP: use most likely parameter:

$$\hat{\theta} = \arg \max_{\theta} P(\theta \mid \mathcal{D}) \quad E[f(\theta)] \approx f(\hat{\theta})$$

MAP for Beta distribution



$$P(\theta \mid \mathcal{D}) = \frac{\theta^{\beta_H + \alpha_H - 1} (1 - \theta)^{\beta_T + \alpha_T - 1}}{B(\beta_H + \alpha_H, \beta_T + \alpha_T)} \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

MAP: use most likely parameter:

$$\hat{\theta} = \arg \max_{\theta} P(\theta \mid \mathcal{D}) =$$

- Beta prior equivalent to extra thumbtack flips
- As $N \rightarrow \infty$, prior is "forgotten"
- But, for small sample size, prior is important!

What you need to know

- - Go to the recitation on intro to probabilities
 - ☐ And, other recitations too
 - Point estimation:
 - □ MLE
 - □ Bayesian learning
 - □ MAP