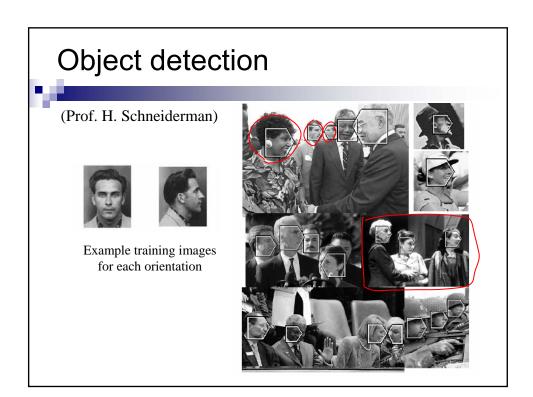


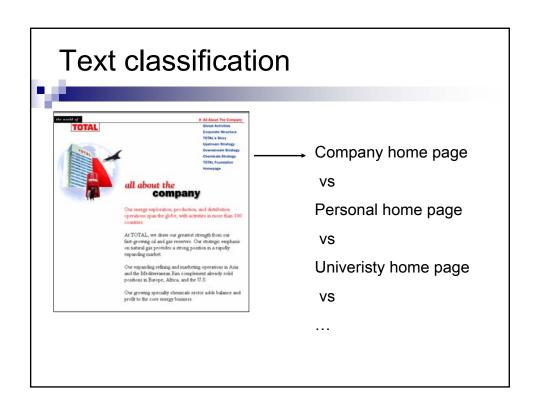
What is Machine Learning?

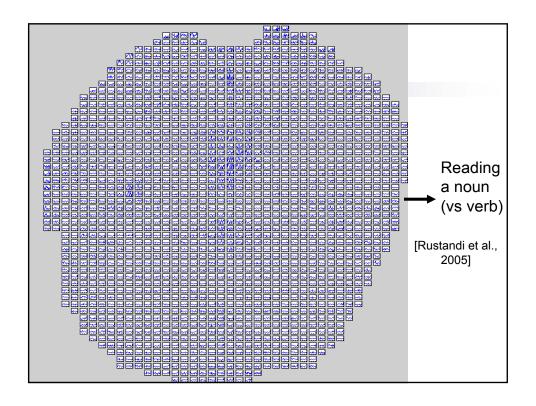
Machine Learning

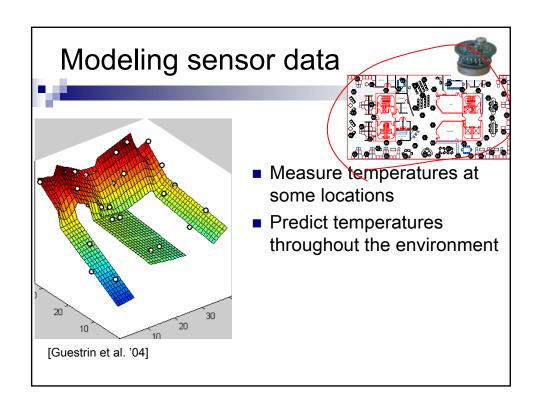


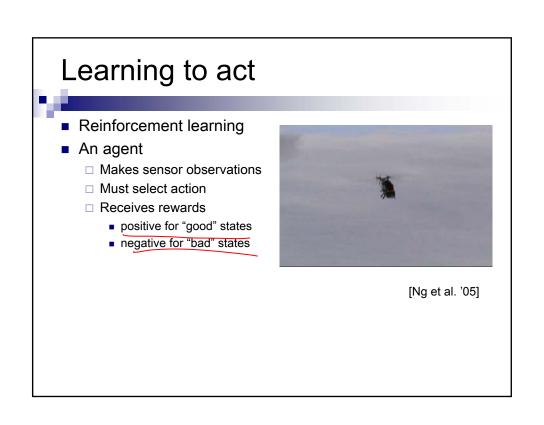
- improve their <u>performance</u>
- at some <u>task</u>
- with <u>experience</u>











Growth of Machine Learning

- Н
- Machine learning is preferred approach to
 - □ Speech recognition, Natural language processing
 - □ Computer vision
 - ☐ Medical outcomes analysis
 - Robot control
 - □ ...
- This trend is accelerating
 - □ Improved machine learning algorithms
 - □ Improved data capture, networking, faster computers
 - □ Software too complex to write by hand
 - □ New sensors / IO devices
 - □ Demand for self-customization to user, environment

Syllabus



- Covers a wide range of Machine Learning techniques — from basic to state-of-the-art
- You will learn about the methods you heard about:
 - Naïve Bayes, logistic regression, nearest-neighbor, decision trees, boosting, neural nets, overfitting, regularization, dimensionality reduction, PCA, error bounds, VC dimension, SVMs, kernels, margin bounds, K-means, EM, mixture models, semi-supervised learning, HMMs, graphical models, active learning, reinforcement learning...
- Covers algorithms, theory and applications
- It's going to be fun and hard work ©

Prerequisites



- Probabilities
 - □ Distributions, densities, marginalization...
- Basic statistics
 - ☐ Moments, typical distributions, regression...
- Algorithms
 - □ Dynamic programming, basic data structures, complexity...
- Programming
 - ☐ Mostly your choice of language, but Matlab will be very useful
- We provide some background, but the class will be fast paced
 - Ability to deal with "abstract mathematical concepts"

Review Sessions



- Very useful!
 - □ Review material
 - □ Present background
 - □ Answer questions
- Thursdays, 5:30-6:50 in Wean Hall 5409
- First recitation is tomorrow
 - □ Review of probabilities
- Special recitation on Matlab
 - □ Jan. 24 Wed. 5:30-6:50pm NSH 1305

Staff



- Four Great TAs: Great resource for learning, interact with them!
 - □ Andy Carlson, acarlson@cs
 - ☐ Jonathan Huang, jch1@cs
 - □ Purna Sarkar, psarkar@cs
 - □ Brian Ziebart, bziebart@cs
- Administrative Assistant
 - ☐ Monica Hopes, x8-5527, meh@cs

First Point of Contact for HWs



- To facilitate interaction, a TA will be assigned to each homework question This will be your "first point of contact" for this question
 - □ But, you can always ask any of us
- For e-mailing instructors, always use:
 - □ 10701-instructors@cs.cmu.edu
- For announcements, subscribe to:
 - □ 10701-announce@cs
 - □ https://mailman.srv.cs.cmu.edu/mailman/listinfo/10701-announce

Text Books



- Required Textbook:
 - □ Pattern Recognition and Machine Learning; Chris Bishop
- Optional Books:
 - □ Machine Learning; Tom Mitchell
 - ☐ The Elements of Statistical Learning: Data Mining, Inference, and Prediction; Trevor Hastie, Robert Tibshirani, Jerome Friedman
 - Information Theory, Inference, and Learning Algorithms; David MacKay

Grading



- 5 homeworks (30%)
 - ☐ First one goes out 1/24
 - Start early, Start early
- Final project (20%)
 - ☑ Details out Feb 26th
- Midterm (20%)
 - ☐ March 7th in class
- Final (30%)
 - □ May 15th, 1-4 p.m.

Homeworks



- Homeworks are hard, start early ©
- Due in the beginning of class
- 3 late days for the semester
- After late days are used up:
 - ☐ Half credit within 48 hours
 - □ Zero credit after 48 hours
- All homeworks must be handed in, even for zero credit
- Late homeworks handed in to Monica Hopes, WEH 4619
- Collaboration
 - You may discuss the questions
 - □ Each student writes their own answers
 - □ Write on your homework anyone with whom you collaborate
 - Don't Look for answers on the web or from last oprevious samesters (lass, etc...

Sitting in & Auditing the Class



- Due to new departmental rules, every student who wants to sit in the class (not take it for credit), must register officially for auditing
- To satisfy the auditing requirement, you must either:
 - Do *two* homeworks, and get at least 75% of the points in each;
 or
 - □ Take the final, and get at least 50% of the points; or
 - □ Do a class project and do *one* homework, and get at least 75% of the points in the homework;
 - Only need to submit project proposal and present poster, and get at least 80% points in the poster.
- Please, send us an email saying that you will be auditing the class and what you plan to do.
- If you are not a student and want to sit in the class, please get authorization from the instructor

Enjoy!



- ML is becoming ubiquitous in science, engineering and beyond
- This class should give you the basic foundation for applying ML and developing new methods
- The fun begins...

Your first consulting job



- A billionaire from the suburbs of Seattle asks you a question:
 - ☐ He says: I have thumbtack, if I flip it, what's the probability it will fall with the nail up?
 - ☐ You say: Please flip it a few times:



- □ You say: The probability is: 60%
- ■He says: Why???
- ☐ You say: Because...

Thumbtack - Binomial Distribution

- P(Heads) = θ , P(Tails) = $1-\theta$ [Model] $\int \int \int \nabla \nabla \int \theta = \frac{3}{5}$ P(HH $\tau\tau$ H) = $\theta\theta(1-\theta)(1-\theta)\theta = \theta^3(1-\theta)^2$
 - Flips are i.i.d.:
 - □ Independent events
 - □ Identically distributed according to Binomial distribution
 - Sequence D of α_H Heads and α_T Tails \bigcirc



$$P(\mathcal{D} \mid \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$$

Maximum Likelihood Estimation

- **Data:** Observed set *D* of α_H^3 Heads and α_T^2 Tails
- **Hypothesis:** Binomial distribution
- Learning θ is an optimization problem
 - P(HHTTHIO) ☐ What's the objective function? $P(\mathfrak{I}|\theta)$
- MLE: Choose θ that maximizes the probability of observed data:

$$\widehat{\theta} = \arg \max_{\theta} P(\mathcal{D} \mid \theta)$$

$$= \arg \max_{\theta} \underline{\ln} P(\mathcal{D} \mid \theta)$$

Your first learning algorithm
$$\frac{1}{\ln \alpha^{1} = \ln \alpha + \ln b}{\ln \alpha^{2} = b \ln \alpha}$$

$$\widehat{\theta} = \arg \max_{\theta} \ln P(\mathcal{D} \mid \theta)$$

$$= \arg \max_{\theta} \ln \theta^{\alpha_{H}} (1 - \theta)^{\alpha_{T}}$$

• Set derivative to zero: $\frac{d}{d\theta} \ln P(\mathcal{D} \mid \theta) = 0$

$$\frac{d}{d\theta} \ln P(\mathcal{D} \mid \theta) = 0$$

$$\frac{d}{d\theta} \ln P(\mathcal{$$

How many flips do I need?

$$\hat{\theta}_{\text{rus}} = \frac{\alpha_H}{\alpha_H + \alpha_T}$$

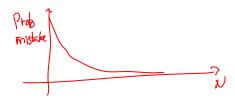
- Billionaire says: I flipped 3 heads and 2 tails.
- You say: θ = 3/5, I can prove it!
- He says: What if I flipped 30 heads and 20 tails?
- You say: Same answer, I can prove it!
- He says: What's better?
- You say: Humm... The more the merrier???
- He says: Is this why I am paying you the big bucks???

Simple bound (based on Hoeffding's inequality)

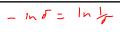
■ For
$$N = \alpha_H + \alpha_T$$
, and $\widehat{\theta}_{ML} = \frac{\alpha_H}{\alpha_H + \alpha_T}$

eg, E=0.01 ■ Let $\underline{\theta}^*$ be the true parameter, for any ε >0:

$$P(||\widehat{\theta} - \theta^*|| \ge \epsilon) \le 2e^{-2N\epsilon^2}$$



PAC Learning





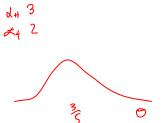
■ Billionaire says: I want to know the thumbtack parameter θ , within ϵ = 0.1, with probability at least $1-\delta = 0.95$. How many flips?

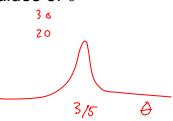
$$P(||\widehat{\theta} - \theta^*| \ge \epsilon) \le 2e^{-2N\epsilon^2}$$

What about prior



- Billionaire says: Wait, I know that the thumbtack is "close" to 50-50. What can you?
- You say: I can learn it the Bayesian way...
- Rather than estimating a single θ, we obtain a distribution over possible values of θ





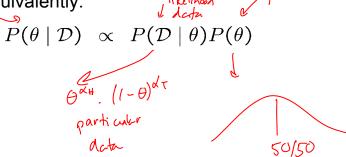
Bayesian Learning



■ Use Bayes rule:

$$P(\theta \mid \mathcal{D}) = \frac{P(\mathcal{D} \mid \theta)P(\theta)}{P(\mathcal{D})}$$

Or equivalently:

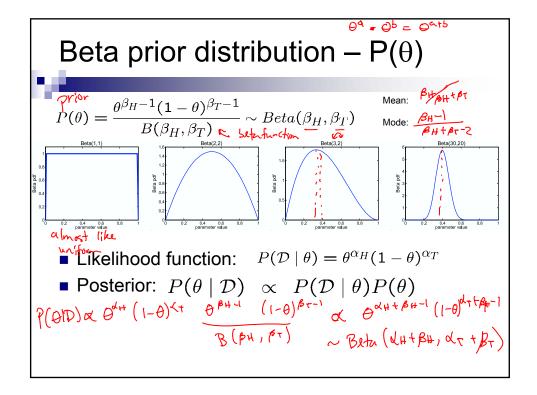


Bayesian Learning for Thumbtack

- Posterior $P(\theta \mid \mathcal{D}) \propto P(\mathcal{D} \mid \theta) P(\theta)$
 - Likelihood function is simply Binomial:

$$P(\mathcal{D} \mid \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$$

- What about prior?
 - □ Represent expert knowledge
 - □ Simple posterior form
- Conjugate priors:
 - □ Closed-form representation of posterior
 - ☐ For Binomial, conjugate prior is Beta distribution



Posterior distribution Prior: $\underline{Beta(\beta_H,\beta_T)}$ Data: α_H heads and α_T tails (binomial)

Posterior distribution:

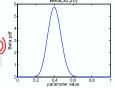
$$P(\theta \mid \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

$$R(\theta) = \text{Beta}(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

$$R(\theta) = \text{Bet$$

Using Bayesian posterior

P(+D) 1



Posterior distribution:

$$P(\theta \mid \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

■ Bayesian inference:

□ No longer single parameter:

$$E[f(\theta)] = \int_0^1 f(\theta) P(\theta \mid \mathcal{D}) d\theta$$

□ Integral is often hard to compute

MAP: Maximum a posteriori

approximation

approximation
$$P(heta \mid \mathcal{D}) \sim Beta(eta_H + lpha_H, eta_T + lpha_T)$$
 $E[f(heta)] = \int_0^1 f(heta) P(heta \mid \mathcal{D}) d heta$

- As more data is observed, Beta is more certain
- MAP: use most likely parameter:

$$\widehat{\theta}_{\text{NAP}} = \underset{\theta}{\text{arg max}} P(\theta \mid \mathcal{D}) \qquad E[f(\theta)] \approx f(\widehat{\theta})$$

$$= \underset{\text{d.h.t.}}{\underbrace{\text{d.h.t.}}} \qquad \underset{\text{d.h.t.}}{\text{like}} \qquad \underset{\text{d.h.t.}}{\text{MLE}_{\text{l.ips}}}$$

$$= \underset{\text{d.h.t.}}{\underbrace{\text{d.h.t.}}} \qquad \underset{\text{d.h.t.}}{\text{like}} \qquad \underset{\text{d.h.t.}}{\text{l.ips}}$$

MAP for Beta distribution

$$P(\theta \mid \mathcal{D}) = rac{ heta^{eta_H + lpha_H - 1}(1 - heta)^{eta_T + lpha_T - 1}}{B(eta_H + lpha_H, eta_T + lpha_T)} \sim Beta(eta_H + lpha_H, eta_T + lpha_T)$$

MAP: use most likely parameter:

$$\widehat{\theta} = \arg\max_{\theta} P(\theta \mid \mathcal{D}) = \frac{\sqrt{1 + \beta \mu^{-1}}}{\sqrt{1 + 1 + \beta \mu^{-2}}}$$

- Beta prior equivalent to extra thumbtack flips
- As $N \rightarrow \infty$, prior is "forgotten"
- But, for small sample size, prior is important!

What you need to know



- Go to the recitation on intro to probabilities
 - ☐ And, other recitations too
- Point estimation:

 - Bayesian learning
 - □ MAP