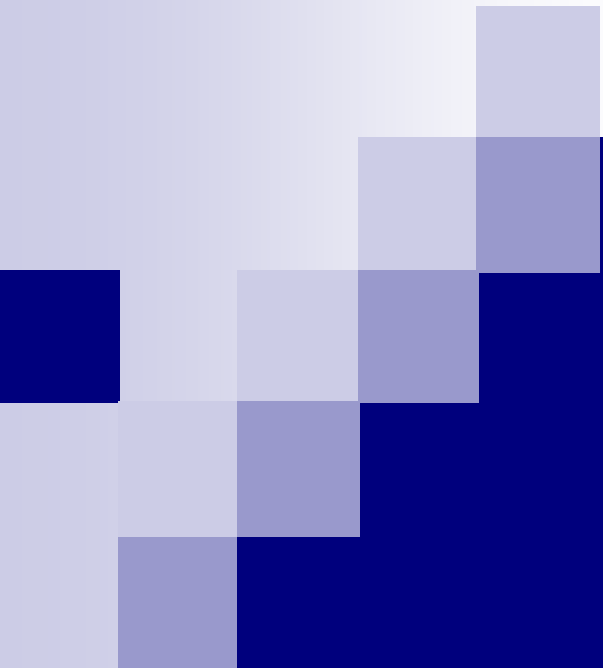


<http://www.cs.cmu.edu/~guestrin/Class/10701/>



What's learning? Point Estimation

Machine Learning – 10701/15781

Carlos Guestrin

Carnegie Mellon University

January 18th, 2005

Growth of Machine Learning



- Machine learning is preferred approach to
 - Speech recognition, Natural language processing
 - Computer vision
 - Medical outcomes analysis
 - Robot control
 - ...
- This trend is accelerating
 - Improved machine learning algorithms
 - Improved data capture, networking, faster computers
 - Software too complex to write by hand
 - New sensors / IO devices
 - Demand for self-customization to user, environment

Syllabus

- Covers a wide range of Machine Learning techniques – from basic to state-of-the-art
- You will learn about the methods you heard about:
 - Naïve Bayes, logistic regression, nearest-neighbor, decision trees, boosting, neural nets, overfitting, regularization, dimensionality reduction, PCA, error bounds, VC dimension, SVMs, kernels, margin bounds, K-means, EM, mixture models, semi-supervised learning, HMMs, graphical models, active learning, reinforcement learning...
- Covers algorithms, theory and applications
- **It's going to be fun and hard work 😊**

Prerequisites



- Probabilities
 - Distributions, densities, marginalization...
- Basic statistics
 - Moments, typical distributions, regression...
- Algorithms
 - Dynamic programming, basic data structures, complexity...
- Programming
 - Mostly your choice of language, but Matlab will be very useful
- We provide some background, but the class will be fast paced
- Ability to deal with “abstract mathematical concepts”

Review Sessions



- Very useful!
 - Review material
 - Present background
 - Answer questions
- Thursdays, 5:00-6:30 in Wean Hall 5409
- First recitation is **tomorrow**
 - Review of probabilities
- Special recitation on Matlab
 - Jan. 25 Wed. 5:00-7:00pm, NSH 3305

Staff



- Four Great TAs: Great resource for learning, interact with them!
 - Anton Chechetka, antonc@cs
 - Stanislav Funiak, sfuniak@cs
 - Andreas Krause, krausea@cs
 - Jure Leskovec, jure@cs

- Course General Czar
 - Terrill L. Frantz, TerrillFrantz@cmu

- Administrative Assistant
 - Monica Hopes, x8-5527, meh@cs

First Point of Contact for HWs



- To facilitate interaction, a TA will be assigned to each homework question – This will be your “first point of contact” for this question
 - But, you can always ask any of us
- For e-mailing instructors, always use:
 - 10701-instructors@cs.cmu.edu
- For announcements, subscribe to:
 - 10701-announce@cs
 - <https://mailman.srv.cs.cmu.edu/mailman/listinfo/10701-announce>

All Text Books are Optional, *but very useful*

- *Machine Learning*, Tom Mitchell
- *Pattern Classification (2nd Edition)*, Duda, Hart and Stork
- *Neural Networks for Pattern Recognition*, Chris Bishop

Grading



- 5 homeworks (30%)
 - First one goes out 1/23
- Final project (20%)
 - Details out March 1st
- Midterm (20%)
 - March 8th
- Final (30%)
 - TBD by registrar

Homeworks

- Homeworks are hard, start early 😊
- Due in the beginning of class
- 3 late days for the semester
- After late days are used up:
 - Half credit within 48 hours
 - Zero credit after 48 hours
- All homeworks **must be handed in**, even for zero credit
- Late homeworks handed in to Monica Hopes, WEH 4616

- Collaboration
 - You may **discuss** the questions
 - Each student writes their own answers
 - Write on your homework anyone with whom you collaborate

Enjoy!



- ML is becoming ubiquitous in science, engineering and beyond
- This class should give you the basic foundation for applying ML and developing new methods
- The fun begins...



What is Machine Learning ?

Machine Learning



Study of algorithms that

- improve their performance
- at some task
- with experience

Object detection

(Prof. H. Schneiderman)



Example training images
for each orientation



Text classification

the world of



all about the
company

Our energy exploration, production, and distribution operations span the globe, with activities in more than 100 countries.

At TOTAL, we draw our greatest strength from our fast-growing oil and gas reserves. Our strategic emphasis on natural gas provides a strong position in a rapidly expanding market.

Our expanding refining and marketing operations in Asia and the Mediterranean Rim complement already solid positions in Europe, Africa, and the U.S.

Our growing specialty chemicals sector adds balance and profit to the core energy business.

► All About The Company

- Global Activities
- Corporate Structure
- TOTAL's Story
- Upstream Strategy
- Downstream Strategy
- Chemicals Strategy
- TOTAL Foundation
- Homepage



Company home page

VS

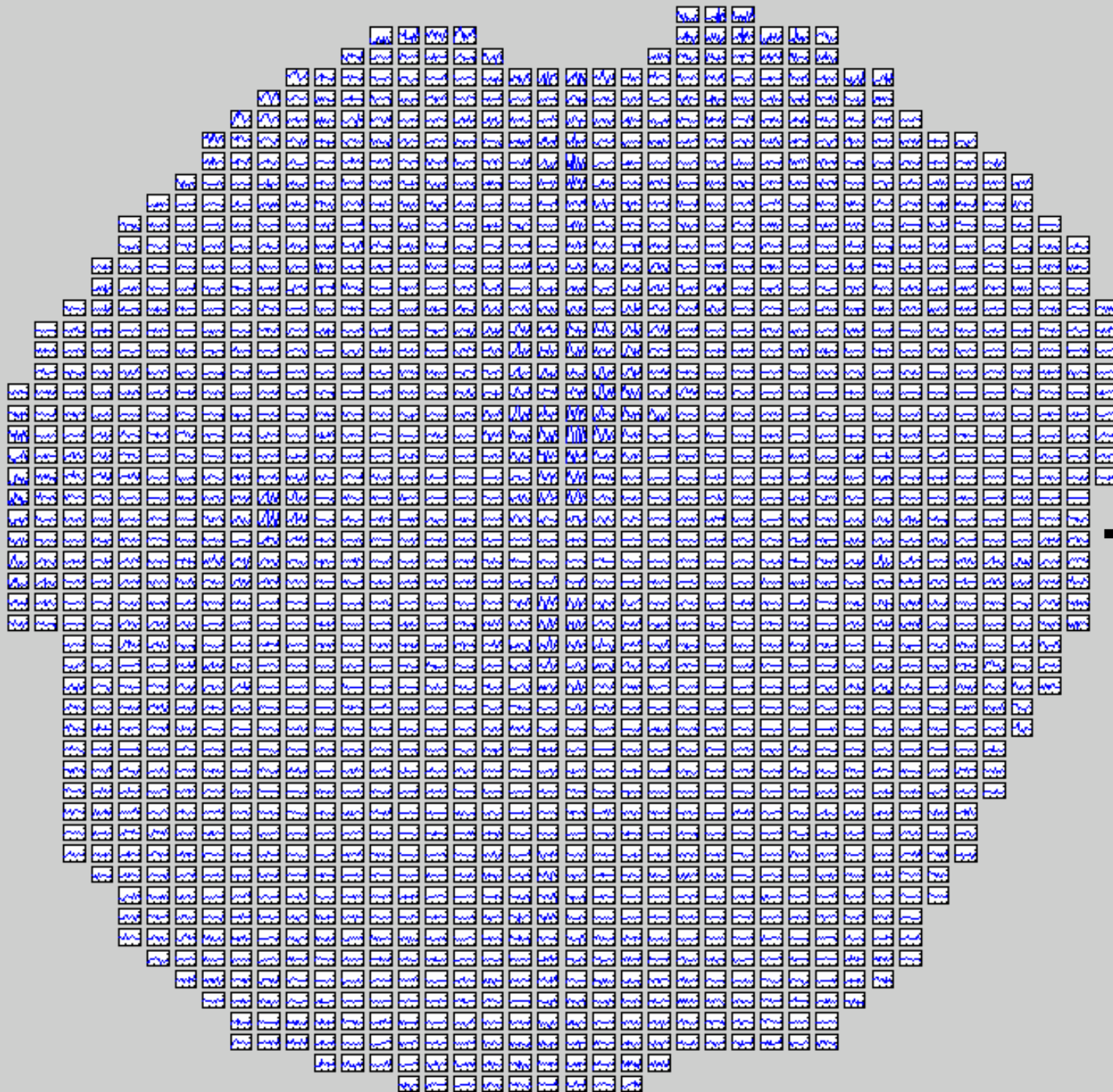
Personal home page

VS

Univeristy home page

VS

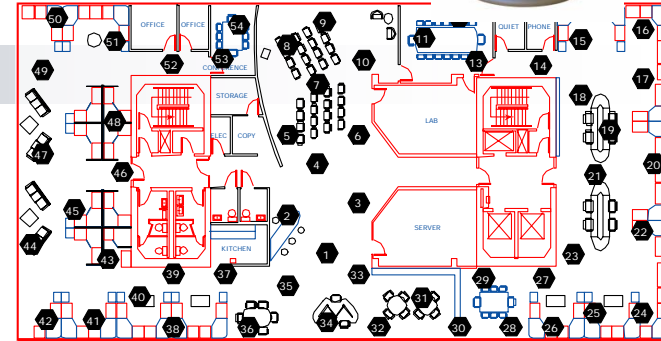
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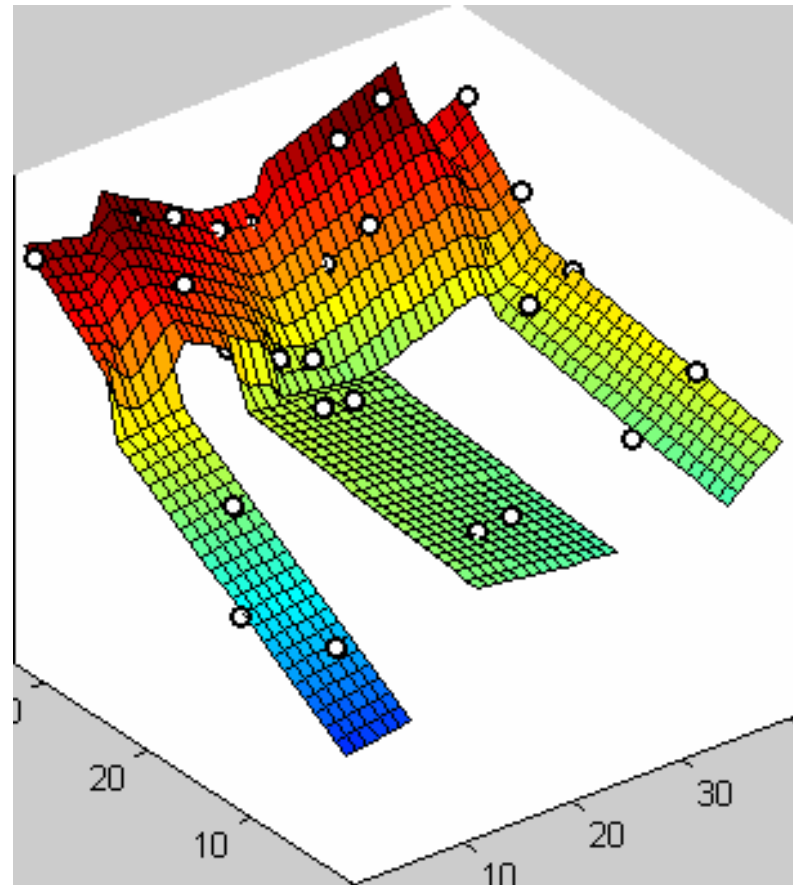
Reading
a noun
(vs verb)

[Rustandi et al.,
2005]

Modeling sensor data



- Measure temperatures at some locations
- Predict temperatures throughout the environment



[Guestrin et al. '04]

Learning to act



[Ng et al. '05]

- Reinforcement learning
- An agent
 - Makes sensor observations
 - Must select action
 - Receives rewards
 - positive for “good” states
 - negative for “bad” states

Your first consulting job



- A billionaire from the suburbs of Seattle asks you a question:
 - He says: I have thumbtack, if I flip it, what's the probability it will fall with the nail up?
 - You say: Please flip it a few times:
 - You say: The probability is:
 - **He says: Why???**
 - You say: Because...

Thumbtack – Binomial Distribution

- $P(\text{Heads}) = \theta$, $P(\text{Tails}) = 1 - \theta$

- Flips are i.i.d.:
 - Independent events
 - Identically distributed according to Binomial distribution
- Sequence \mathcal{D} of α_H Heads and α_T Tails

$$P(\mathcal{D} \mid \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$$

Maximum Likelihood Estimation

- **Data:** Observed set D of α_H Heads and α_T Tails
- **Hypothesis:** Binomial distribution
- Learning θ is an optimization problem
 - What's the objective function?
- MLE: Choose θ that maximizes the probability of observed data:

$$\begin{aligned}\hat{\theta} &= \arg \max_{\theta} P(\mathcal{D} | \theta) \\ &= \arg \max_{\theta} \ln P(\mathcal{D} | \theta)\end{aligned}$$

Your first learning algorithm

$$\begin{aligned}\hat{\theta} &= \arg \max_{\theta} \ln P(\mathcal{D} | \theta) \\ &= \arg \max_{\theta} \ln \theta^{\alpha_H} (1 - \theta)^{\alpha_T}\end{aligned}$$

- Set derivative to zero:

$$\frac{d}{d\theta} \ln P(\mathcal{D} | \theta) = 0$$

How many flips do I need?

$$\hat{\theta} = \frac{\alpha_H}{\alpha_H + \alpha_T}$$

- Billionaire says: I flipped 3 heads and 2 tails.
- You say: $\theta = 3/5$, I can prove it!
- He says: What if I flipped 30 heads and 20 tails?
- You say: Same answer, I can prove it!
- **He says: What's better?**
- You say: Humm... The more the merrier???
- He says: Is this why I am paying you the big bucks???

Simple bound (based on Hoeffding's inequality)

- For $N = \alpha_H + \alpha_T$, and $\hat{\theta} = \frac{\alpha_H}{\alpha_H + \alpha_T}$

- Let θ^* be the true parameter, for any $\epsilon > 0$:

$$P(|\hat{\theta} - \theta^*| \geq \epsilon) \leq 2e^{-2N\epsilon^2}$$

PAC Learning

- PAC: Probably Approximate Correct
- Billionaire says: I want to know the thumbtack parameter θ , within $\varepsilon = 0.1$, with probability at least $1 - \delta = 0.95$. How many flips?

$$P(|\hat{\theta} - \theta^*| \geq \epsilon) \leq 2e^{-2N\epsilon^2}$$

What about prior

- Billionaire says: Wait, I know that the thumbtack is “close” to 50-50. What can you?
- **You say: I can learn it the Bayesian way...**
- Rather than estimating a single θ , we obtain a distribution over possible values of θ

Bayesian Learning

- Use Bayes rule:

$$P(\theta | \mathcal{D}) = \frac{P(\mathcal{D} | \theta)P(\theta)}{P(\mathcal{D})}$$

- Or equivalently:

$$P(\theta | \mathcal{D}) \propto P(\mathcal{D} | \theta)P(\theta)$$

Bayesian Learning for Thumbtack

$$P(\theta | \mathcal{D}) \propto P(\mathcal{D} | \theta)P(\theta)$$

- Likelihood function is simply Binomial:

$$P(\mathcal{D} | \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$$

- What about prior?

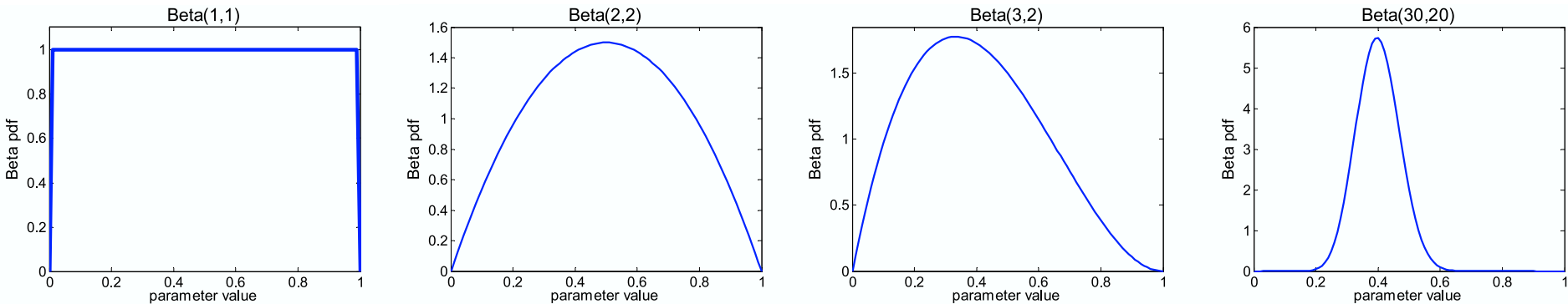
- Represent expert knowledge
- Simple posterior form

- Conjugate priors:

- Closed-form representation of posterior
- For Binomial, conjugate prior is Beta distribution**

Beta prior distribution – $P(\theta)$

$$P(\theta) = \frac{\theta^{\beta_H-1}(1-\theta)^{\beta_T-1}}{B(\beta_H, \beta_T)} \sim \text{Beta}(\beta_H, \beta_T)$$

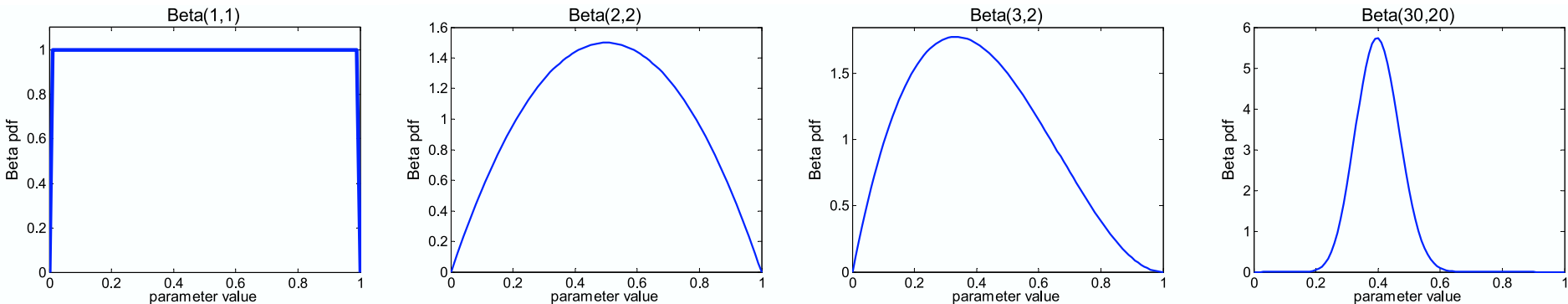


- Likelihood function: $P(\mathcal{D} | \theta) = \theta^{\alpha_H} (1 - \theta)^{\alpha_T}$
- Posterior: $P(\theta | \mathcal{D}) \propto P(\mathcal{D} | \theta) P(\theta)$

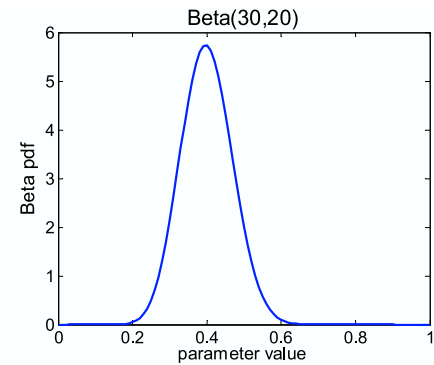
Posterior distribution

- Prior: $Beta(\beta_H, \beta_T)$
- Data: α_H heads and α_T tails
- Posterior distribution:

$$P(\theta | \mathcal{D}) \sim Beta(\beta_H + \alpha_H, \beta_T + \alpha_T)$$



Using Bayesian posterior



- Posterior distribution:

$$P(\theta | \mathcal{D}) \sim \text{Beta}(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

- Bayesian inference:

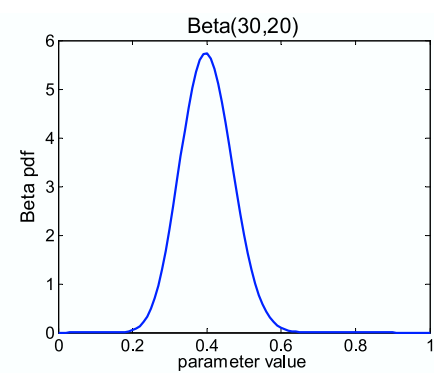
- No longer single parameter:

$$E[f(\theta)] = \int_0^1 f(\theta) P(\theta | \mathcal{D}) d\theta$$

- Integral is often hard to compute

MAP: Maximum a posteriori approximation

$$P(\theta | \mathcal{D}) \sim \text{Beta}(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

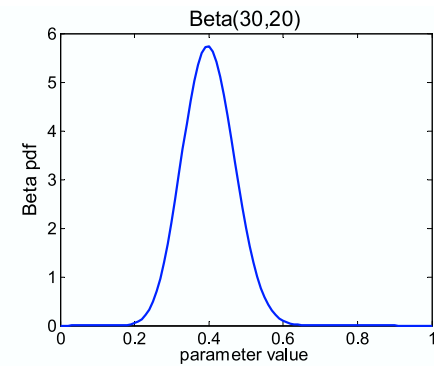


$$E[f(\theta)] = \int_0^1 f(\theta) P(\theta | \mathcal{D}) d\theta$$

- As more data is observed, Beta is more certain
- MAP: use most likely parameter:

$$\hat{\theta} = \arg \max_{\theta} P(\theta | \mathcal{D}) \quad E[f(\theta)] \approx f(\hat{\theta})$$

MAP for Beta distribution



$$P(\theta | \mathcal{D}) = \frac{\theta^{\beta_H + \alpha_H - 1} (1 - \theta)^{\beta_T + \alpha_T - 1}}{B(\beta_H + \alpha_H, \beta_T + \alpha_T)} \sim \text{Beta}(\beta_H + \alpha_H, \beta_T + \alpha_T)$$

- MAP: use most likely parameter:

$$\hat{\theta} = \arg \max_{\theta} P(\theta | \mathcal{D}) =$$

- Beta prior equivalent to extra thumbtack flips
- As $N \rightarrow \infty$, prior is “forgotten”
- **But, for small sample size, prior is important!**

What you need to know



- Go to the recitation on intro to probabilities
 - And, other recitations too
- Point estimation:
 - MLE
 - Bayesian learning
 - MAP