

# Automata Theory: Solutions 8

[illegible]

### Problem 1

Find simple grammars for the following languages:

(a)  $\{(aa)^nb : n \geq 0\}$

$$\begin{array}{l} S \rightarrow aA \mid b \\ A \rightarrow aS \end{array}$$

(b)  $\{a^n b^n : n \geq 1\}$

$$\begin{aligned} S &\rightarrow aA \\ A &\rightarrow aAB \mid b \\ B &\rightarrow b \end{aligned}$$

**Problem 2**

Simplify the following grammar:

$$\begin{aligned}S &\rightarrow aSa \mid A \mid aC \mid aD \\A &\rightarrow aBa \mid aCa \mid F \\B &\rightarrow aBa \mid \lambda \\C &\rightarrow aC \mid bD \\D &\rightarrow aD \mid bC \\E &\rightarrow aD \mid \lambda \\F &\rightarrow aa \mid aFa\end{aligned}$$

The simplification gives the following result:

$$\begin{aligned}S &\rightarrow aSa \mid aBa \mid aFa \mid aa \\B &\rightarrow aBa \mid aa \\F &\rightarrow aa \mid aFa\end{aligned}$$

Since  $S$ ,  $B$ , and  $F$  give rise to the same strings, we can remove  $B$  and  $F$ :

$$S \rightarrow aSa \mid aa$$