

Automata Theory: Assignment 3

Due date: September 13 (Thursday)

Problem 1 (6 points)

Consider the following two languages on the alphabet $\Sigma = \{a, b\}$:

$$L_1 = \{a^n : n \geq 1\}$$

$$L_2 = \{b^n : n \geq 1\}$$

Describe the languages below, using either the set notation or precise definitions in English:

$$L_3 = L_1^*$$

$$L_4 = \overline{L_1}$$

$$L_5 = L_1 \cup L_2$$

$$L_6 = L_1 L_2$$

$$L_7 = (L_1^2)(L_2^2)(L_1^2)$$

$$L_8 = (L_1 \cup L_2)^*$$

$$L_9 = (L_1 L_2)^*$$

Problem 2 (4 points)

Consider the alphabet $\Sigma = \{a, b\}$. Is there any language L on this alphabet for which $(\overline{L})^* = \overline{L^*}$? If yes, give an example of such a language; if no, explain why.