## Algorithms: Solutions 3

## Problem 1

Write an algorithm that combines Insertion-Sort and Merge-Sort.

The following algorithm calls Insertion-Sort for array segments whose length is at most k; the running time of this algorithm is  $\Theta(n \cdot k + n \cdot \lg(n/k))$ .

```
\begin{split} \text{Insertion-Sort}(A,p,r) \\ \text{for } j \leftarrow p+1 \text{ to } r \\ \text{do } key \leftarrow A[j] \\ i \leftarrow j-1 \\ \text{while } i \geq p \text{ and } A[i] > key \\ \text{do } A[i+1] \leftarrow A[i] \\ i \leftarrow i-1 \\ A[i+1] \leftarrow key \\ \\ \text{Combined-Sort}(A,p,r,k) \\ \text{if } r-p < k \\ \text{then Insertion-Sort}(A,p,r) \\ \text{else } q \leftarrow \left\lfloor \frac{p+r}{2} \right\rfloor \\ \text{Combined-Sort}(A,p,q,k) \\ \text{Combined-Sort}(A,p,q,r) \\ \end{split}
```

## Problem 2

Write an algorithm that inputs an integer array A[1..n] and an odd integer number k, and determines whether k can be represented as the sum of two elements of the array.

The following algorithm uses two subroutines, MERGE-SORT (described in class) and BINARY-SEARCH (described in Assignment 1); the running time of this algorithm is  $O(n \cdot \lg n)$ .

```
\begin{array}{ll} \text{Sum-Search}(A,n,k) \\ \text{Merge-Sort}(A,1,n) & \rhd \text{ sort the array } A[1..n] \\ \text{for } i \leftarrow 2 \text{ to } n \\ \text{do if Binary-Search}(A,n,k-A[i]) \neq 0 \\ \text{then return true} & \rhd k \text{ is the sum of two elements of } A[1..n] \\ \text{return false} & \rhd k \text{ is not the sum of any two elements} \end{array}
```