

# Algorithms: Assignment 6

Due date: October 2 (Wednesday)

## Problem 1 (5 points)

Let  $A[1..n]$  be a *sorted* array of  $n$  distinct integer numbers. Write an efficient algorithm  $\text{INDEX-SEARCH}(A, n)$  that finds an index  $i$  such that  $A[i] = i$ . If the array does not have such an element, the algorithm should return 0.

## Problem 2 (5 points)

A  $d$ -ary heap is like a binary heap, but instead of 2 children, nodes have  $d$  children.

- (a) How would you represent a  $d$ -ary heap with  $n$  elements in an array? What are the expressions for determining the parent of a given element,  $\text{PARENT}(i)$ , and a  $j$ -th child of a given element,  $\text{CHILD}(i, j)$ , where  $1 \leq j \leq d$ ?
- (b) Write an efficient implementation of  $\text{HEAPIFY}$  and  $\text{HEAP-INSERT}$  for a  $d$ -ary heap, and give the running time of your algorithms in terms of  $n$  and  $d$ .