## Algorithms: Assignment 1

Due date: September 7 (Thursday)

## Problem 1 (3 points)

Let A[1..n] be an array of n distinct numbers. If i < j and A[i] > A[j], then the pair (i, j) is called an *inversion*. For example, the array (2, 3, 8, 6, 1) contains five inversions. Write an algorithm Inversions (A, n) that determines the number of inversions in A[1..n].

## Problem 2 (3 points)

Let A[1..n] be a sorted array of n distinct numbers. Write an efficient algorithm BINARY-SEARCH(A, n, k) that finds a given value k in the array A[1..n]. The algorithm should return the index of the found element; for example, if  $A = \langle 1, 3, 4, 6, 9 \rangle$  and k = 6, then the returned index is 4, which means that k = A[4]. If the array does not include the value k, the algorithm should return 0.

## Problem 3 (4 points)

Prove the following equalities:

(a) 
$$1 + x + x^2 + x^3 + ... + x^n = \frac{x^{n+1}-1}{x-1}$$
 (where  $x \neq 1$ ).

**(b)** 
$$(1+2+3+4+...+n)^2 = 1^3+2^3+3^3+4^3...+n^3$$
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