Analysis of Algorithms: Results of Exam 1

number	Х										
of exams	X		X	X			X	X			
	X	X	X	X	X	X	X	X	X		
Х	X	X	X	X	X	X	X	X	X		
X	X	X	X	X	X	X	X	X	X	Х	Х

0-39 40-44 45-49 50-54 55-59 60-64 65-69 70-74 75-79 80-84 85-89 90-100

The histogram shows the distribution of grades, not including the bonus.

Problem 10

A ternary heap is like a binary heap, but instead of two children, nodes have three children.

(a) How would you represent a ternary heap by an array? What are the expressions for determining the parent and children of a given element?

The following expressions determine the parent and children of element i:

$$\begin{aligned} \text{Parent}(i) &= \left\lfloor \frac{i+1}{3} \right\rfloor \\ \text{Left-Child}(i) &= 3i-1 \\ \text{Middle-Child}(i) &= 3i \\ \text{Right-Child}(i) &= 3i+1 \end{aligned}$$

(b) What is the height of a ternary heap of n elements in terms of n?

The height h of a heap is approximately equal to $\log_3 n$. The exact height is

$$h = \lceil \log_3(2n+1) - 1 \rceil$$