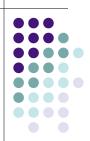


### Topic Models, Latent Space Models, Sparse Coding, and All That

A systematic understanding of probabilistic semantic extraction in large corpora





Eric Xing Carnegie Mellon University

Acknowledgement: Amr Ahmed, Qirong Ho, and Jun Zhu

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## We are inundated with data ...





from images.google.cn

- Humans cannot afford to deal with (e.g., search, browse, or measure similarity) a huge number of text and media documents
- We need computers to help out ...

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# To get started on intelligent systems for automated processing and management of large text or media corpora ...



- Here are some important elements to consider before you start:
  - Task
    - Embedding (visualization)? Classification? Clustering? Topic extraction? ...
  - Data representation:
    - Input and output (e.g., continuous, binary, counts, ...)
  - Model:
    - Latent Semantic Indexing? Bayesian Network? Markov Random Fields? Regression? SVM?
  - Inference:
    - MCMC? Variational? Spectrum Analysis?
  - Learning:
    - MLE? MCLE? Max margin?
  - Computation:
    - Desktop? Hadoop? MPI?
  - Evaluation:
    - Visualization? Human interpretability? Perperlexity? Predictive accuracy?
- It is better to consider one element at a time!

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- -

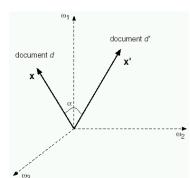
### Tasks:



• Say, we want to have a mapping ..., so that

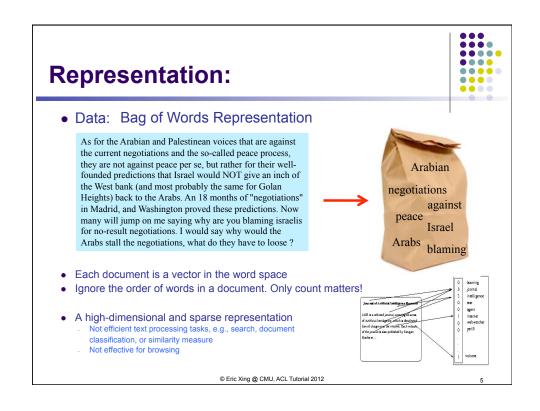


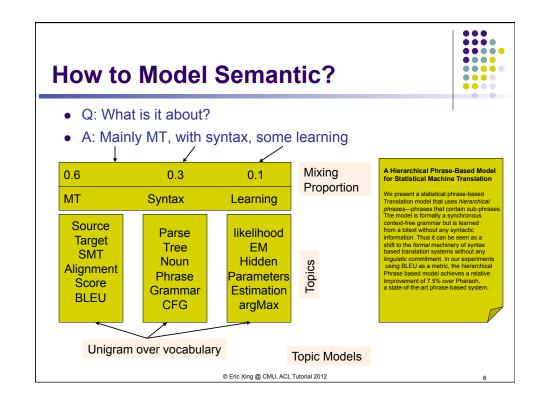


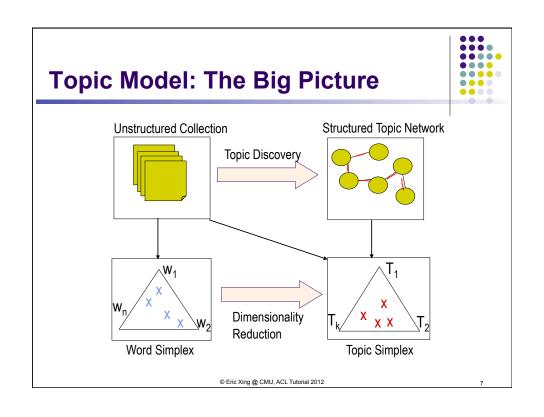


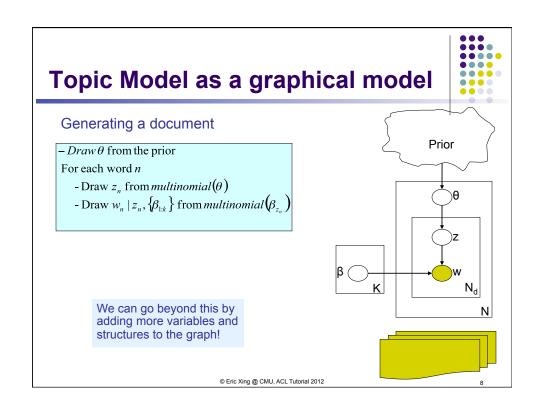
- Compare similarity
- Classify contents
- Cluster/group/categorize docs
- Distill semantics and perspectives
- .

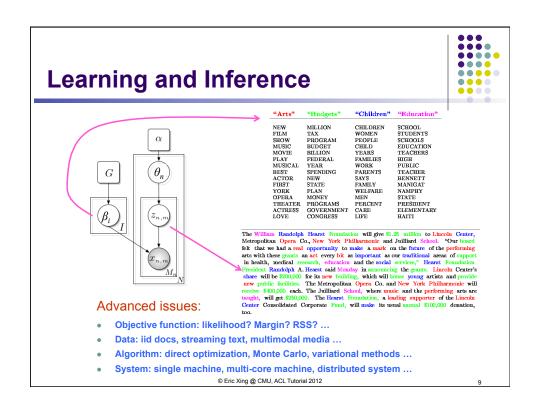
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### **Questions:**



- What is the mathematical and computational basis of all these?
- How to do it right, modular, fast, and real time?
- How to build other related applications on topic models?
- How to scale up?

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..

### Plan of this tutorial



- 1. Overview of basic topic models
- 2. Computational challenges and two classical algorithmic paths
- □ 3. Scenario I: Multimodal data
- 4. Scenario II: When supervision is available
- □ 5. Scenario III: What if I don't know the total number of topics
- □ 6. Scenario IV: Topic evolution in streaming corpus.
- □ 7: Advanced subject I: Sparsity in topic modeling (see EMNLP talk)
- 8: Advanced subject II: Scalability, complexity, and fast algorithms (optional)
- 9: Other applications (optional)

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### 1. Overview of topic models



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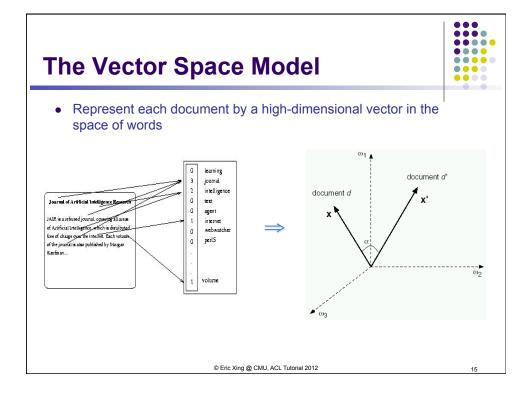
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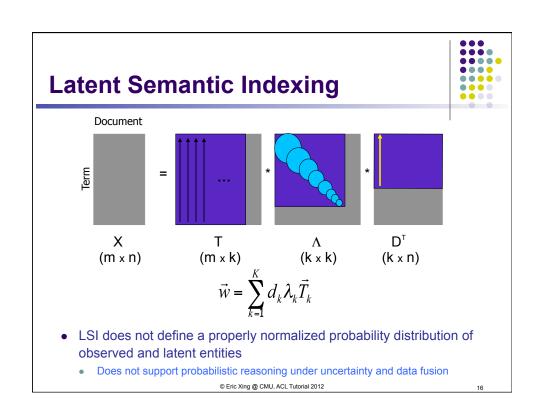
### **Understanding document corpora**

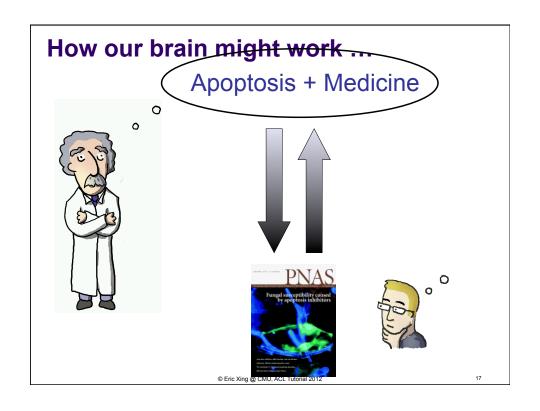


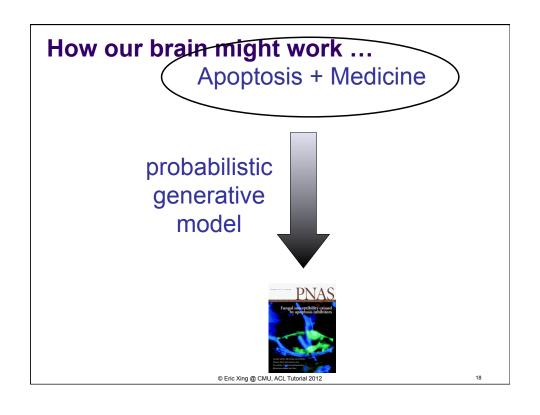
- A document collection is a dataset where each data point is itself a collection of simpler data.
  - Text documents are collections of words.
  - Segmented images are collections of regions.
  - User histories are collections of purchased items.
- Many modern problems ask questions on such data.
  - What topics do these documents "span"?
  - Is this text document relevant to my query?
  - Which category is this text/image in?
  - How have topics changed over time?
  - Who wrote this specific document?
  - What will author X write about?
  - and so on.....

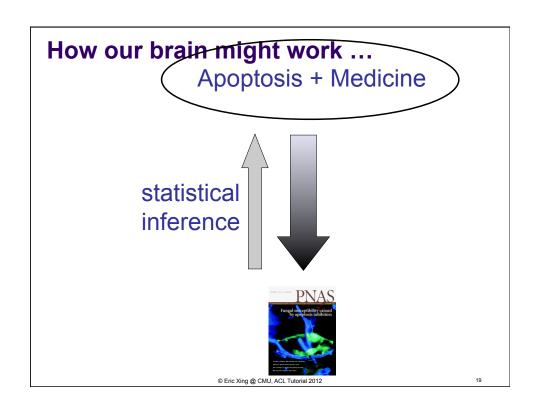
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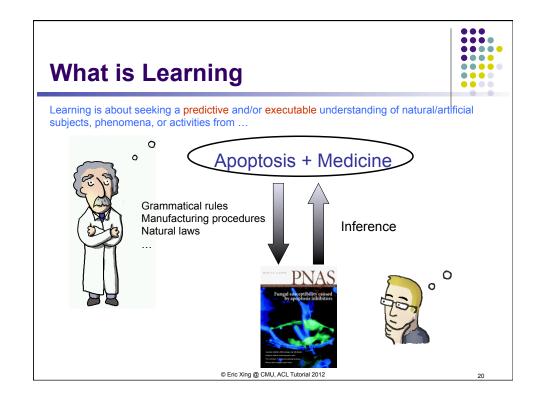


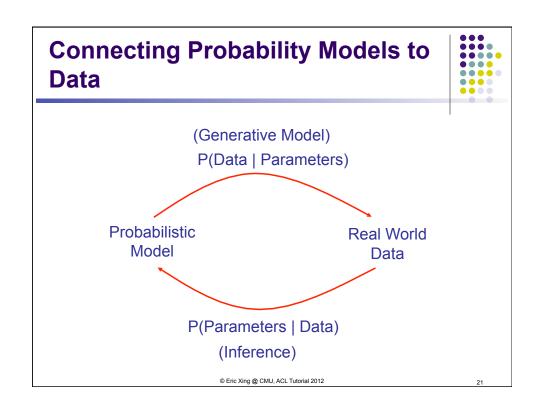


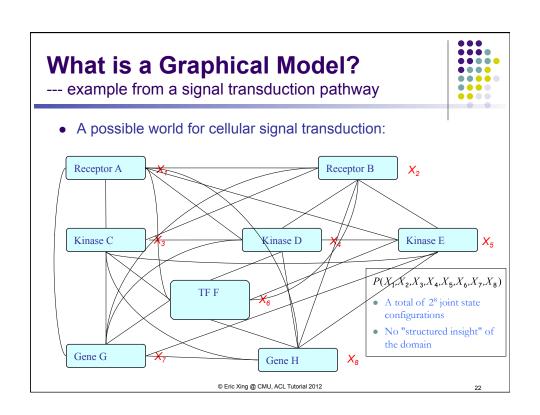












### **Recap of Basic Prob. Concepts**



 Representation: what is the joint probability dist. on multiple variables?

$$P(X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8,)$$

- How many state configurations in total? --- 28
- Are they all needed to be represented?
- Do we get any scientific/medical insight?
- Learning: where do we get all this probabilities?
  - Maximal-likelihood estimation? but how much data do we need?
  - Where do we put domain knowledge in terms of plausible relationships between variables, and plausible values of the probabilities?
- Inference: If not all variables are observable, how to compute the conditional distribution of latent variables given evidence?

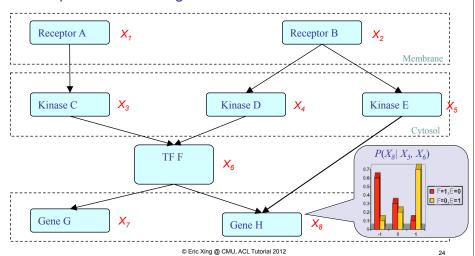
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# **GM:** Structure Simplifies Representation



Dependencies among variables



### **Probabilistic Graphical Models**



- Represent dependency structure with a graph
  - Node <-> random variable
  - Edges encode dependencies
    - Absence of edge -> conditional independence
  - Directed and undirected versions
- Why is this useful?
  - A language for communication
  - A language for computation
  - A language for development
- Origins:
  - Wright 1920's
  - Independently developed by Spiegelhalter and Lauritzen in statistics and Pearl in computer science in the late 1980's

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# Probabilistic Graphical Models, con'd



 $\Box$  If  $X_i$ 's are conditionally independent (as described by a PGM), the joint can be factored to a product of simpler terms, e.g.,



 $P(X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8)$ 

 $= P(X_1) P(X_2) P(X_3|X_1) P(X_4|X_2) P(X_5|X_2)$  $P(X_6|X_3, X_4) P(X_7|X_6) P(X_8|X_5, X_6)$ 

- Why we may favor a PGM?
  - Representation cost: how many probability statements are needed?

2+2+4+4+4+8+4+8=36, an 8-fold reduction from 28!

- Algorithms for systematic and efficient inference/learning computation
  - Exploring the graph structure and probabilistic (e.g., Bayesian, Markovian) semantics
- Incorporation of domain knowledge and causal (logical) structures

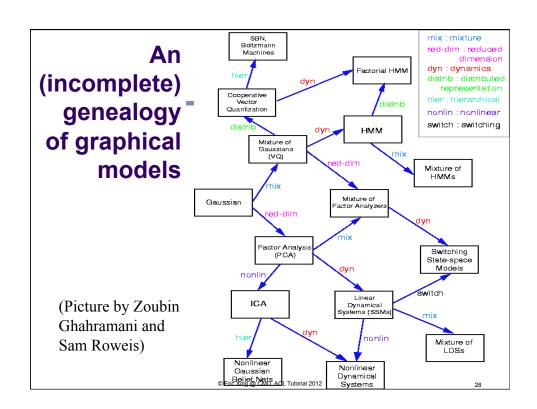
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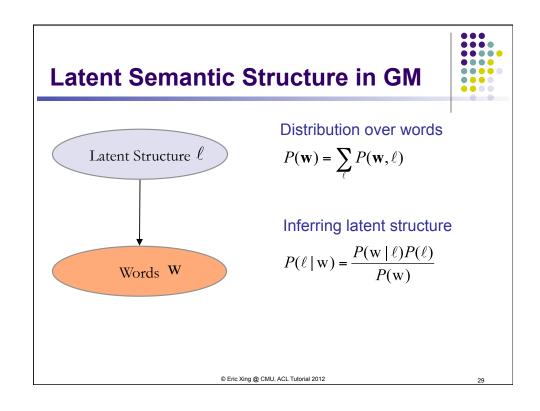
### **Probabilistic Inference**

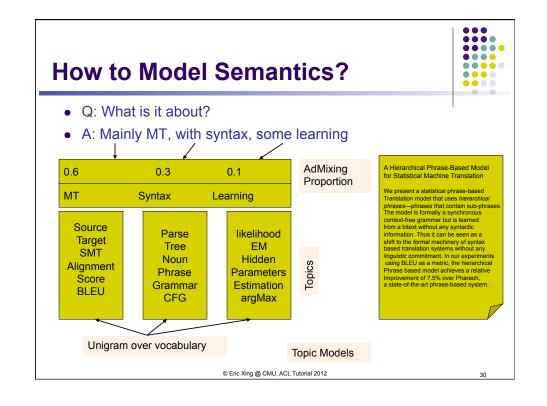


- Computing statistical queries regarding the network, e.g.:
  - Is node X independent on node Y given nodes Z,W?
  - What is the probability of X=true if (Y=false and Z=true)?
  - What is the joint distribution of (X,Y) if Z=false?
  - What is the likelihood of some full assignment?
  - What is the most likely assignment of values to all or a subset the nodes of the network?
- General purpose algorithms exist to fully automate such computation
  - Computational cost depends on the topology of the network
  - Exact inference:
    - The junction tree algorithm
  - Approximate inference;
    - Loopy belief propagation, variational inference, Monte Carlo sampling

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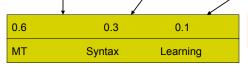




### Why this is Useful?



- Q: What is it about?
- A: Mainly MT, with syntax, some learning



AdMixing Proportion

- Q: give me similar document?
  - Structured way of browsing the collection
- Other tasks
  - Dimensionality reduction
    - TF-IDF vs. topic mixing proportion
    - Classification, clustering, and more ...

A Hierarchical Phrase-Based Model for Statistical Machine Translation

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### **Words in Contexts**



"It was a nice **shot**."









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## **Words in Contexts (con'd)**



• the opposition Labor **Party** fared even worse, with a predicted 35 **Seats**, seven less than last **election**.





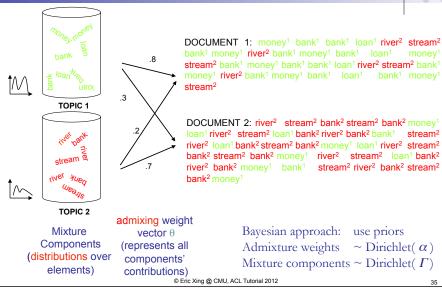
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# "Words" in Contexts (con'd) | Contexts | Con'd | Con'





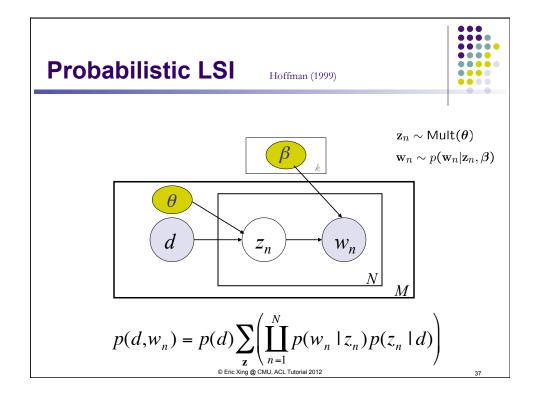


### **Method One:**



Hierarchical Bayesian Admixture (a.k.a. probabilistic Topic Models)

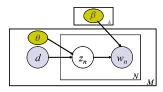
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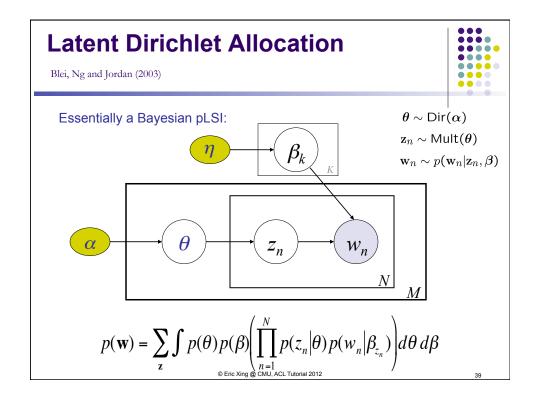
### **Probabilistic LSI**



- A "generative" model
- Models each word in a document as a sample from a mixture model.
- Each word is generated from a single topic, different words in the document may be generated from different topics.
- A topic is characterized by a distribution over words.
- Each document is represented as a list of admixing proportions for the components (i.e. topic vector  $\theta$  ).



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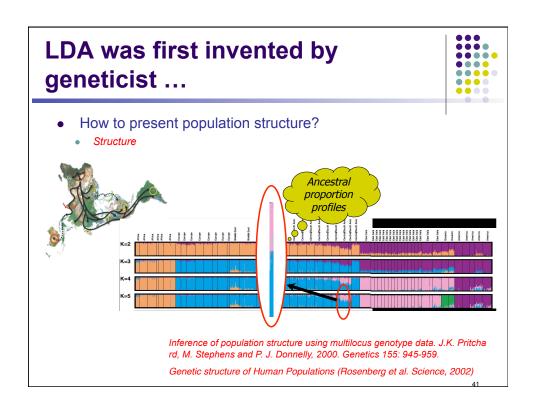
### **LDA**

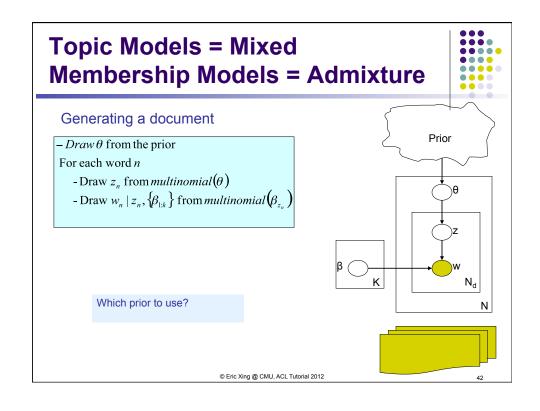


- Generative model
- Models each word in a document as a sample from a mixture model.
- Each word is generated from a single topic, different words in the document may be generated from different topics.
- A topic is characterized by a distribution over words.
- Each document is represented as a list of admixing proportions for the components (i.e. topic vector).
- The topic vectors and the word rates each follows a Dirichlet prior --- essentially a Bayesian pLSI

 $\theta$   $z_n$   $w_n$ 

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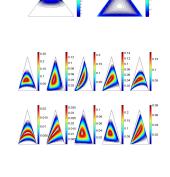


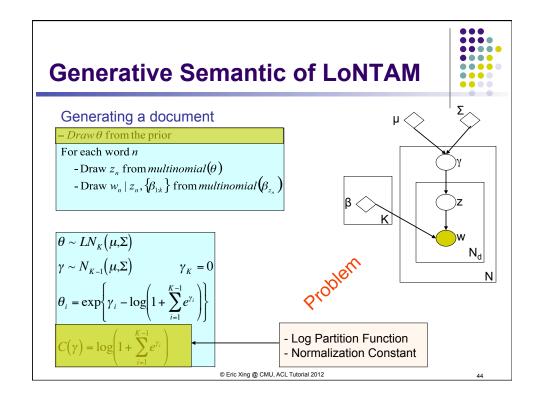


### **Choices of Priors**

- Dirichlet (LDA) (Blei et al. 2003)
  - Conjugate prior means efficient inference
  - Can only capture variations in each topic's intensity independently
- Logistic Normal (CTM=LoNTAM) (Blei & Lafferty 2005, Ahmed & Xing 2006)
  - Capture the intuition that some topics are highly correlated and can rise up in intensity together
  - Not a conjugate prior implies hard inference
- Nested CRP (Blei et al 2005)
  - Defines hierarchy on topics
  - ...

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### Outcomes from a topic model



• The "topics"  $\beta$  in a corpus:

-	_		
comp.graphics	T 59	T 104	T 31
	image	ftp	card
	jpeg	pub	monitor
	color	graphics	dos
	file	mail	video
	gif	version	apple
	images	tar	windows
	format	file	drivers
	bit	information	vga
	files	send	cards
	display	server	graphics
	T 30	T 84	T 44
	power	water	sale
	ground	energy	price
sci electronics	power ground wire circuit	air	offer
sci.electronics	circuit	T 30 T 84 ower water round energy wire air ricuit nuclear upply loop oltage hot	shipping
	supply	loop	sell
	voltage	hot	interested
	current		mail
	wiring	cooling	condition
	signal	heat	email
	cable	temperature	ed

_			
	T 42	T 78	T 47
	israel	jews	armenian
	israeli		turkish
politics.mideast	peace		armenians
pontics.mideast	writes	israeli	armenia
	article	arab	turks
	arab	people	genocide
	war	arabs	russian
	lebanese	center	soviet
	lebanon	jew	people
	people	nazi	muslim
	T 44	arab people arabs center jew nazi  T 94 don mail call package writes	T 49
	sale	don	drive
	price	jewish israel israeli arab people arabs center jew nazi T 94 don mail call package	scsi
misc.forsale	offer		disk
misc.iorsaie	shipping	package	hard
	sell	writes	mb
	interested	send	drives
	mail	number	ide
	condition	ve	controller
	email	hotel	floppy
	cd	credit	system

- There is no name for each "topic", you need to name it!
- There is no objective measure of good/bad
- The shown topics are the "good" ones, there are many many trivial ones, meaningless ones, redundant ones, ... you need to manually prune the results
- How many topics? ...

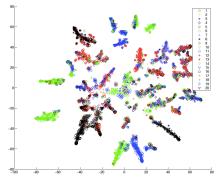
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### Outcomes from a topic model



• The "topic vector"  $\theta$  of each doc



- Create an embedding of docs in a "topic space"
- Their no ground truth of  $\theta$  to measure quality of inference
- But on  $\theta$  it is possible to define an "objective" measure of goodness, such as classification error, retrieval of similar docs, clustering, etc., of documents
- But there is no consensus on whether these tasks bear the true value of topic models ...

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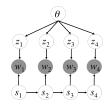
### Outcomes from a topic model



• The per-word topic indicator *z*:

The William Randolph Hearst Foundation will give \$1.25 million to Lincoln Center, Metropolitan Opera Co., New York Philharmonic and Juilliard School. "Our board felt that we had a real opportunity to make a mark on the future of the performing arts with these grants an act every bit as important as our traditional areas of support in health, medical research, education and the social services," Hearst Foundation President Randolph A. Hearst said Monday in announcing the grants. Lincoln Center's share will be \$200,000 for its new building, which will house young artists and provide new public facilities. The Metropolitan Opera Co. and New York Philharmonic will receive \$400,000 each. The Juilliard School, where music and the performing arts are tanght, will get \$250,000. The Hearst Foundation, a leading supporter of the Lincoln Center Consolidated Corporate Fund, will make its usual annual \$100,000 domation, too.

- Not very useful under the bag of word representation, because of loss of ordering
- But it is possible to define simple probabilistic linguistic constraints (e.g, bi-grams) over z and get potentially interesting results [Griffiths, Steyvers, Blei, & Tenenbaum, 2004]

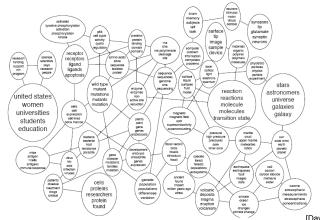


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### Outcomes from a topic model



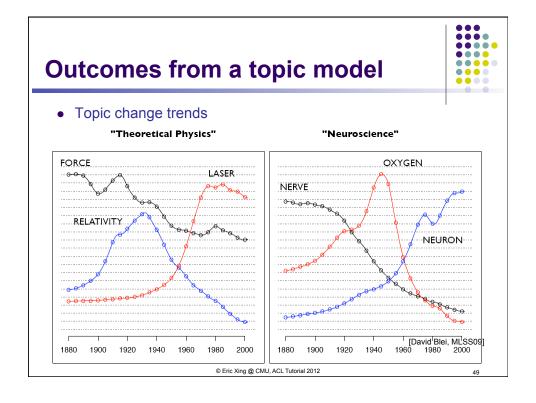
• The topic graph S (when using CTM):



[David Blei, MLSS09]

Kind of interesting for understanding/visualizing large corpora

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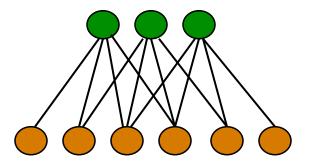


# Method Two: • Layered Boltzmann machines (an undirected Topic Model)

### **The Harmonium**



hidden units



visible units

**Boltzmann machines:** 

$$p(x, h \mid \theta) = \exp \left\{ \sum_{i} \theta_{i} \phi_{i}(x_{i}) + \sum_{j} \theta_{j} \phi_{j}(h_{j}) + \sum_{i,j} \theta_{i,j} \phi_{i,j}(x_{i}, h_{j}) - A(\theta) \right\}$$

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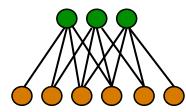
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### **A Binomial Word-count Model**



E.P. Xing, R. Yan and A. G. Hauptmann, UAI 2006

### topics



$$h_j = 3$$
: topic  $j$  has strength  $3$   
 $h_j \in \mathbb{R}$ ,  $\langle h_j \rangle = \sum_i W_{i,j} x_i$ 

$$x_i = n$$
: word i has count n

words counts
$$p(\mathbf{h} \mid \mathbf{x}) = \prod_{j} \text{Normal}_{h_{j}} \left[ \sum_{i} \vec{W}_{ij} \vec{x}_{i}, 1 \right]$$

$$p(\mathbf{x} \mid \mathbf{h}) = \prod_{i} \text{Bi}_{x_{i}} \left[ N, \frac{\exp(\alpha_{j} + \sum_{j} W_{ij} h_{j})}{1 + \exp(\alpha_{j} + \sum_{j} W_{ij} h_{j})} \right]$$

$$\Rightarrow p(\mathbf{x}) \propto \exp\left\{\left(\sum_{i} \alpha_{i} x_{i} - \log \Gamma(x_{i}) - \log \Gamma(N - x_{i})\right) + \frac{1}{2} \sum_{j} \left(\sum_{i} W_{i,j} x_{i}\right)^{2}\right\}$$

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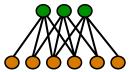
### **The Computational Trade-off**



**Undirected model**: Learning is hard, inference is easy.

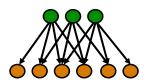
**<u>Directed Model</u>**: Learning is "easier", inference is hard.

Example: Document Retrieval.



topics

words



Retrieval is based on comparing (posterior) topic distributions of documents.

- directed models: inference is slow. Learning is relatively "easy".
- undirected model: inference is fast. Learning is slow but can be done offline.

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### **Method Three:**

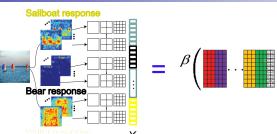


- Sparse topic coding (a non-probabilistic Topic Model)
  - And in this category recently there is also nonnegative matrix factorization (NMF)

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### **Sparse Coding**





- Let X be a signal, e.g., speech, image, etc.
- Let  $\beta$  be a set of normalized "basis vectors"
  - We call it dictionary
- β is "adapted" to x if it can represent it with a few basis vectors
  - There exists a sparse vector  $\theta$  such that  $x \approx \beta \theta$
  - We call  $\theta$  the sparse code

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### **Primer on Sparse Coding**



Sparse Coding with appropriate constraints:
 reconstruction loss sparsity-inducing regularizer

$$\min_{\boldsymbol{\theta}, \boldsymbol{\beta}} \qquad \sum_{d} \ell(\theta_d, \boldsymbol{\beta} | \mathbf{x}_d) + \lambda \Psi(\boldsymbol{\theta})$$

s.t.: 
$$\boldsymbol{\beta} \in \Omega_1; \boldsymbol{\theta} \in \Omega_2.$$

- Reconstruction loss can be:
  - the general log-likelihood loss of an exponential family distribution (Lee et al., 2010)
- Sparisty-inducing regularizer can be:
  - $\bullet \quad \text{the $L_0$ "pseudo-norm":} \quad \|\theta\|_0 := \sum \delta(\theta_i,0)$

NP-hard

• the  $L_1$  norm:  $\|\theta\|_1 := \sum |\theta_i|$ 

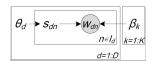
- Convex
- Structured regularizers,  $\dot{\underline{\epsilon}}$ .g., group Lasso (Bengio et al., 2009)  $\|\theta\|_{1/2}:=\sum \| heta_{\mathcal{I}_g}\|_2$
- · Suggests an alternating optimization procedure

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### **Sparse Topical Coding**



- Goal: design a non-probabilistic topic model that is amenable to
  - direct control on the posterior sparsity of inferred representations
  - avoid dealing with normalization constant when considering supervision or rich features
  - seamless integration with a convex loss function (e.g., svm hinge loss)
- We extend sparse coding to hierarchical sparse topical coding
  - word code  $\theta$
  - document code s



reconstruction loss

$$\begin{split} \min_{\left\{\boldsymbol{\theta}_{d}, \mathbf{s}_{d}\right\}, \boldsymbol{\beta}} & \sum_{d, n \in I_{d}} \ell(w_{dn}, \mathbf{s}_{dn}^{\intercal} \boldsymbol{\beta}_{.n}) + \lambda \sum_{d} \lVert \boldsymbol{\theta}_{d} \rVert_{1} + \sum_{d, n \in I_{d}} (\gamma \lVert \mathbf{s}_{dn} - \boldsymbol{\theta}_{d} \rVert_{2}^{2} + \rho \lVert \mathbf{s}_{dn} \rVert_{1}) \\ \text{s.t.} : & \boldsymbol{\theta}_{d} \geq 0, \; \mathbf{s}_{dn} \geq 0, \; \forall d, n \in I_{d}; \; \; \boldsymbol{\beta}_{k} \in \mathcal{P}, \; \forall k, \end{split}$$

truncated aggregation

non-negative codes topical bases

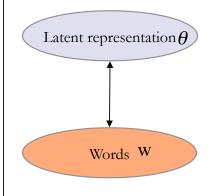
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J. Zhu, & E.P. Xing. UAI, 2011

sparse codes

# **Summary: Latent Sub-space Models**





### The Model:

 $P(\mathbf{w},\theta;\beta)$ 

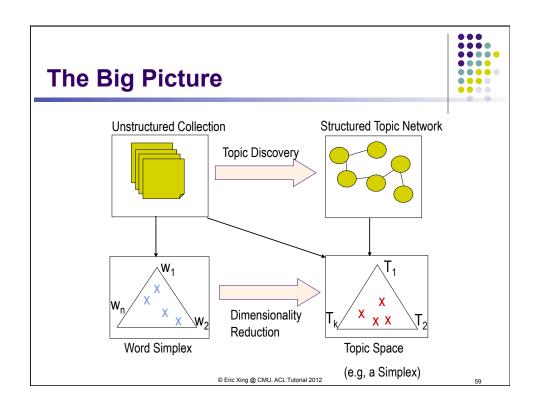
Inferring latent representation:

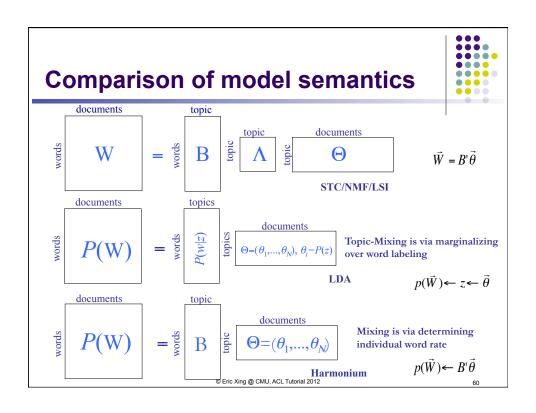
$$P(\theta \mid \mathbf{w}) = \frac{P(\mathbf{w}, \theta)}{P(\mathbf{w})}$$

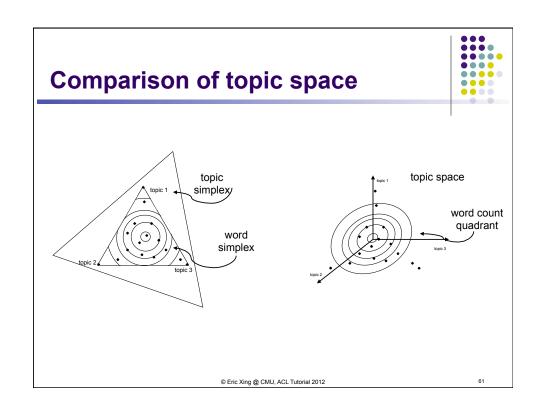
Learning the subspace:

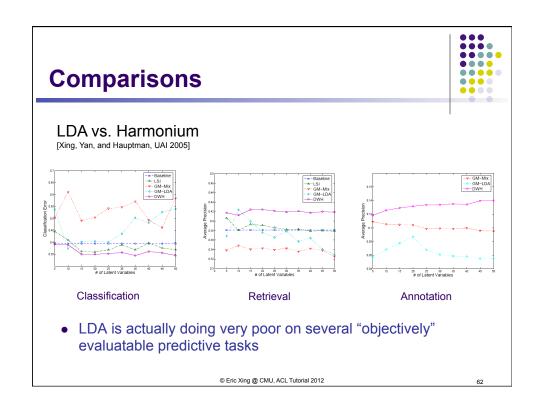
$$\beta = \arg\min f_{\beta}(w,\theta)$$

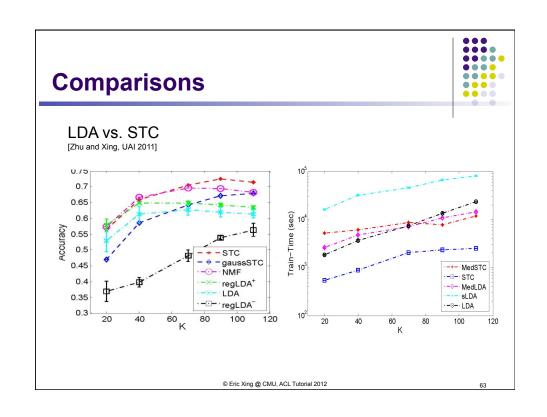
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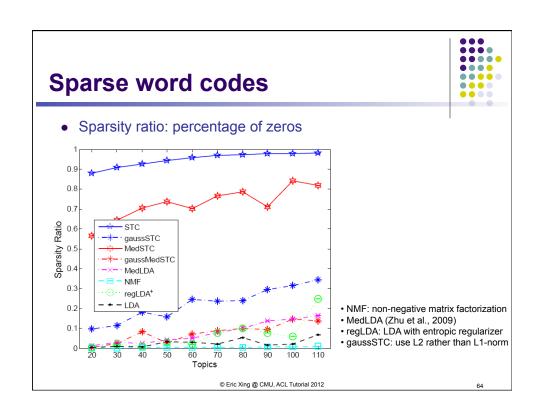












# 2. Computational challenges and three algorithmic paths



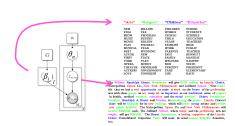
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### **Computation on LDA**



- Inference
  - Given a Document D
    - Posterior:  $P(\Theta \mid \mu, \Sigma, \beta, D)$
    - Evaluation: P(D| μ,Σ, β)



- Learning
  - Given a collection of documents {D<sub>i</sub>}
    - Parameter estimation

$$\underset{(\mu,\Sigma,\beta)}{\operatorname{arg\,max}} \sum \log (P(D_i|\mu,\Sigma,\beta))$$

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### **Exact Bayesian inference on LDA** is intractable



• A possible query:

$$p(\theta_n | D) = ?$$
$$p(z_{n,m} | D) = ?$$

Close form solution?

$$p(\theta_n|D) = \frac{p(\theta_{n_n}, D)}{p(D)}$$

$$= \frac{\sum_{\{z_{n,m}\}} \int \left( \prod_{n} \left( \prod_{m} p(x_{n,m} | \beta_{z_{n}}) p(z_{n,m} | \theta_{n}) \right) p(\theta_{n+} | \alpha) \right) p(\phi | G) d\theta_{n} d\beta}{p(D)}$$

$$= \frac{\sum_{|z_{n,m}|} \int \left( \prod_{n} \left( \prod_{m} p(x_{n,m} | \beta_{z_{n}}) p(z_{n,m} | \theta_{n}) \right) p(\theta_{n} | \alpha) \right) p(\phi | G) d\theta_{n} d\beta}{p(D)}$$

$$p(D) = \sum_{|z_{n,m}|} \int \cdots \int \left( \prod_{n} \left( \prod_{m} p(x_{n,m} | \beta_{z_{n}}) p(z_{n,m} | \theta_{n}) \right) p(\theta_{n} | \alpha) \right) p(\beta | G) d\theta_{1} \cdots d\theta_{N} d\beta$$

Sum in the denominator over  $T^n$  terms, and integrate over n k-dimensional topic

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### **Approximate Inference**



- Variational Inference
  - Mean field approximation (Blei et al)
  - Expectation propagation (Minka et al)
  - Variational 2<sup>nd</sup>-order Taylor approximation (Ahmed and Xing)
- Markov Chain Monte Carlo
  - Gibbs sampling (Griffiths et al)

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### **Collapsed Gibbs sampling**

(Tom Griffiths & Mark Steyvers)



- · Collapsed Gibbs sampling
  - Integrate out  $\theta$

For variables 
$$\mathbf{z} = z_1, z_2, ..., z_n$$
  
Draw  $z_i^{(t+1)}$  from  $P(z_i | \mathbf{z}_{-i}, \mathbf{w})$   
 $\mathbf{z}_{-i} = z_1^{(t+1)}, z_2^{(t+1)}, ..., z_{i-1}^{(t+1)}, z_{i+1}^{(t)}, ..., z_n^{(t)}$ 

$$\{z^{(1)}, z^{(2)}, \dots, z^{(T)}\}$$

$$\theta = \frac{1}{T} \sum_{t} z^{(t)}$$

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### Gibbs sampling

- Need full conditional distributions for variables
- Since we only sample z we need

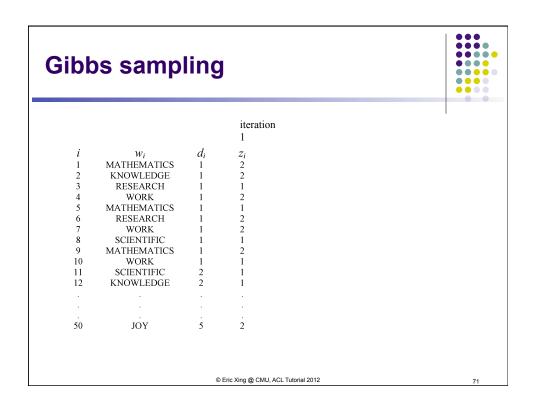
$$P(z_i = j | \mathbf{z}_{-i}, \mathbf{w}) \propto P(w_i | z_i = j, \mathbf{z}_{-i}, \mathbf{w}_{-i}) P(z_i = j | \mathbf{z}_{-i})$$

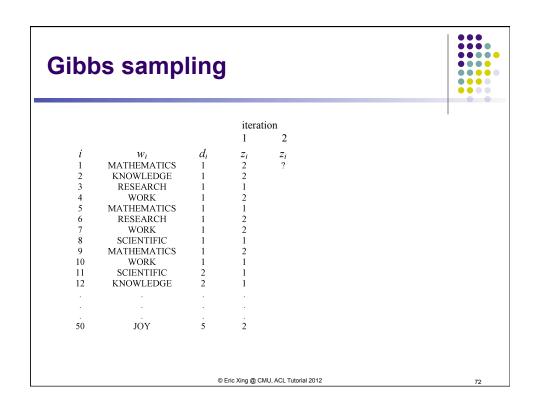
$$= \frac{n_{-i,j}^{(w_i)} + G}{n_{-i,j}^{(\cdot)} + WG} \frac{n_{-i,j}^{(d_i)} + \alpha}{n_{-i,j}^{(d_i)} + T\alpha}$$

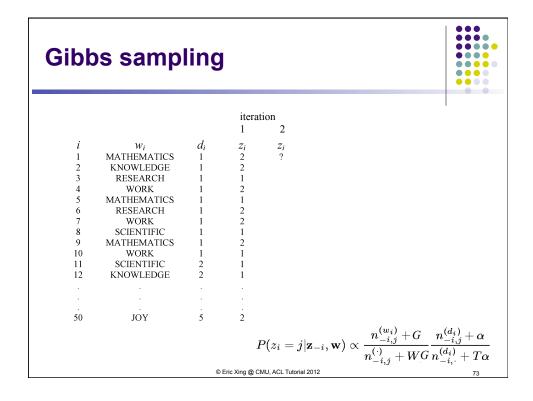
 $n_i^{(w)}$  number of times word w assigned to topic j

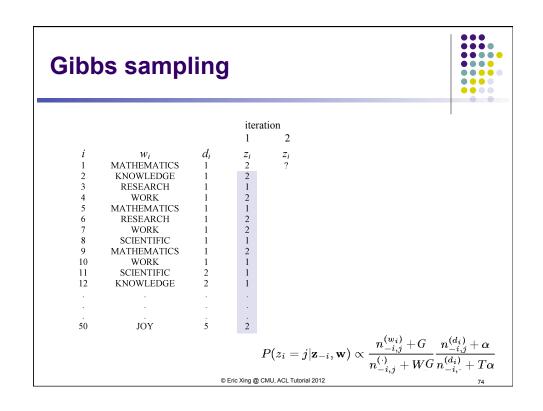
 $n_i^{(d)}$  number of times topic j used in document d

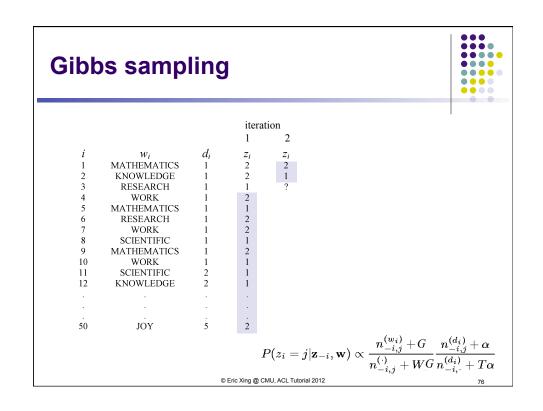
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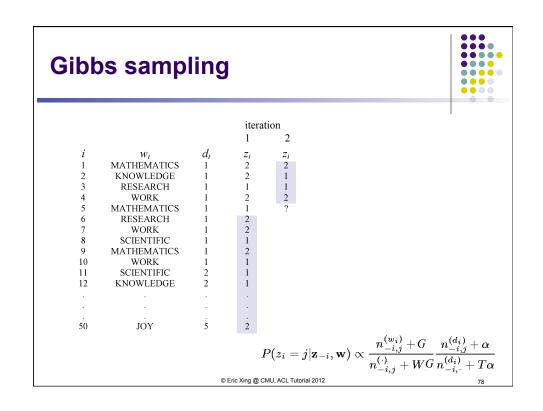












# **Gibbs sampling**



							I
			itera	ition			
			1	2		1000	
i	$w_i$	$d_i$	$z_i$	$Z_i$		$Z_i$	
1	MATHEMATICS	1	2	2		2	
2	KNOWLEDGE	1	2	1		2	
3	RESEARCH	1	1	1		2	
4	WORK	1	2	2		1	
5	MATHEMATICS	1	1	2		2	
6	RESEARCH	1	2	2		2	1
7	WORK	1	2	2		2	$\theta = \frac{1}{2} \sum z^{(t)}$
8	SCIENTIFIC	1	1	1		1	$T \stackrel{\sim}{\smile} T$
9	MATHEMATICS	1	2	2		2	t
10	WORK	1	1	2		2	
11	SCIENTIFIC	2	1	1		2	
12	KNOWLEDGE	2	1	2		2	
50	JOY	5	2	1		1	
				$P(z_i=j $	$(\mathbf{z}_{-i},\mathbf{w}) \propto$	$rac{n_{-i,j}^{(w_i)}+G}{n^{(\cdot)}}$	$rac{n_{-i,j}^{(d_i)}+lpha}{n_{-i,j}^{(d_i)}+Tlpha}$
						-i,j	-i, $-i$

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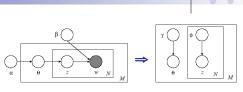
## **Variational Inference**



(e.g., MF, Jordan et al 1999, GMF, Xing et al 2004)

Variational approximation

$$\begin{aligned} q(\theta, z) &= q_{\theta}(\theta) q_{z}(z) \\ &= \operatorname{Dir} \left( \theta \mid \gamma = f(\alpha, \langle z \rangle) \right) \\ & \operatorname{Multi} \left( z \mid \phi = f(\beta_{w}, \langle \ln \theta \rangle) \right) \end{aligned}$$



 $\begin{array}{lcl} \phi_{ni} & \propto & \beta_{iw_n} \exp \left\{ \mathbb{E}_q[\log(\theta_i) \, | \, \gamma] \right\} \\ \gamma_i & = & \alpha_i + \sum_{n=1}^N \phi_{ni}. \end{array}$ 

- Data set:
  - 15,000 documents
  - 90,000 terms
  - 2.1 million words
- Model:
  - 100 factors
  - 9 million parameters
- On a single machine MCMC could converge too slowly for this problem, but ...

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# **Learning a TM**



• Maximum likelihood estimation:

$$\{\beta_1, \beta_2, \dots, \beta_K\}, \alpha = \underset{(\alpha, \beta)}{\operatorname{arg max}} \sum \log(P(D_i | \alpha, \beta))$$

- Need statistics on topic-specific word assignment (due to z), topic vector distribution (due to  $\theta$ ), etc.
  - E.g., this is the formula for topic *k*:

$$\beta_k = \frac{1}{\sum_d N_d} \sum_{d=1}^{D} \sum_{d_n=1}^{N_d} \delta(z_{d,d_n}, k) w_{d,d_n}$$

- These are hidden variables, therefore need an EM algorithm (also known as data augmentation, or DA, in Monte Carlo paradigm)
- This is a "reduce" step in parallel implementation

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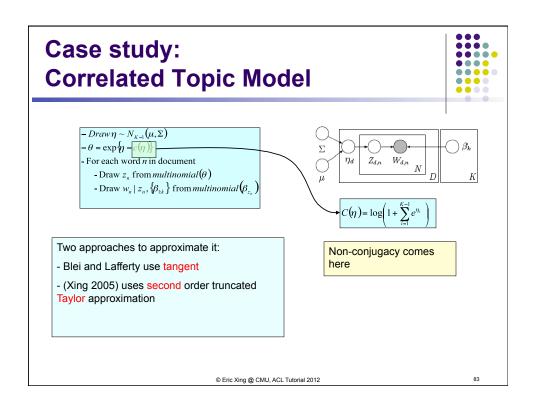
81

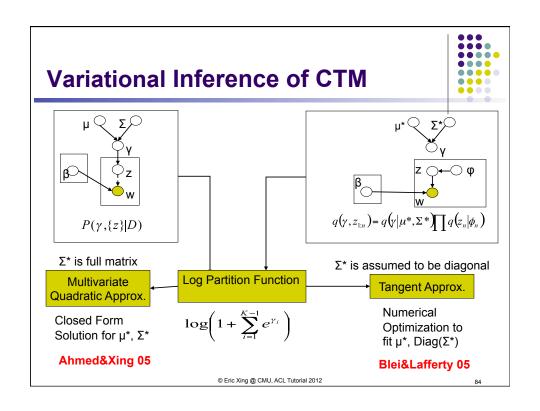
# How to evaluate inference/learning algorithm?



- Empirical performance on, say, clustering, classification, topic saliency, perplexity ...?
- There is no ground truth, poor/good performance may come from model, data, algorithm, parameter tuning ...
- In simulation you know the ground, thus you can exclusively compare the difference caused by inference/learning algorithm!

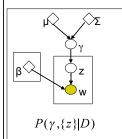
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#### **Variational Inference With no Tears**





Iterate until Convergence

- Pretend you know E[Z<sub>1:n</sub>]
  - $P(\gamma|E[z_{1:n}], \mu, \Sigma)$
- Now you know E[y]
  - $P(z_{1:n}|E[\gamma], w_{1:n}, \beta_{1:k})$

• More Formally:

$$q*(X_C) = P(X_C | \langle S_Y \rangle_{q_y} : \forall y \in X_{MB})$$

Message Passing Scheme (GMF)

Equivalent to previous method (Xing et. al.2003)

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## **LoNTAM Variations Inference**



• Fully Factored Distribution

$$q(y,z_{1:n}) = q(y) \prod q(z_n)$$

• Two clusters:  $\lambda$  and  $Z_{1:n}$ 

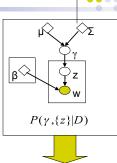
$$q*(X_C) = P(X_C | \langle S_Y \rangle_{q_y} : \forall y \in X_{MB})$$

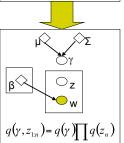
Fixed Point Equations

$$q_{\gamma} * (\gamma) = P(\gamma | \langle S_z \rangle_{q_z}, \mu, \Sigma)$$

$$q_z * (z) = P(z|\langle S_{\gamma} \rangle_{q\gamma}, \beta_{1:k})$$

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$$q_{\lambda} * (\gamma) = P(\langle |\langle S_z \rangle_{q_z}, \mu, \Sigma \rangle)$$
  
 $\propto P(\gamma, \mu, \Sigma) P(\langle S_z \rangle_{q_z} | \gamma)$ 

Now what is  $\langle S_z \rangle_q$ ?

$$S_z = m = \left[ \sum_n I(z_n = 1), ..., \sum_n I(z_n = k) \right]$$

$$\propto N(\gamma, \mu, \Sigma) \exp \left\{ \langle m \rangle_{q_z} \gamma - N \times C(\gamma) \right\}$$

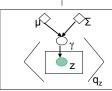
$$\propto N(\gamma, \mu, \Sigma) \exp \left\{ \langle m \rangle_{q_z} \gamma - N \times C(\gamma) \right\}$$

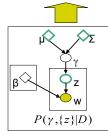
$$\propto \exp\left\{-\frac{1}{2}\gamma'\Sigma^{-1}\gamma + \gamma\Sigma^{-1}\mu + \langle m \rangle_{q_z}\gamma - N \times C(\gamma)\right\}$$

$$C(\gamma) = C(\gamma_{\wedge}) + g'_{\lambda} (\gamma - \gamma_{\wedge}) + .5 (\lambda - \gamma_{\wedge}) H (\gamma - \gamma_{\wedge})$$

$$q_{\lambda}^{*}(\gamma) = N\left(\mu_{\gamma}, \Sigma_{\gamma}\right) \qquad \sum_{\gamma = inv} \left(\Sigma^{-1} + NH\right)$$

$$\mu_{\gamma} = \sum_{\gamma} \left(\Sigma^{-1} \mu + NH \gamma_{\wedge} + \langle m \rangle - Ng\right)$$
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## Variational Z

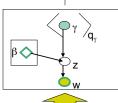


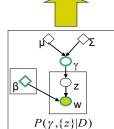
$$q_{z} *(z) = P\left(z \middle| \langle S_{\gamma} \rangle_{q\gamma}, \beta, w\right)$$

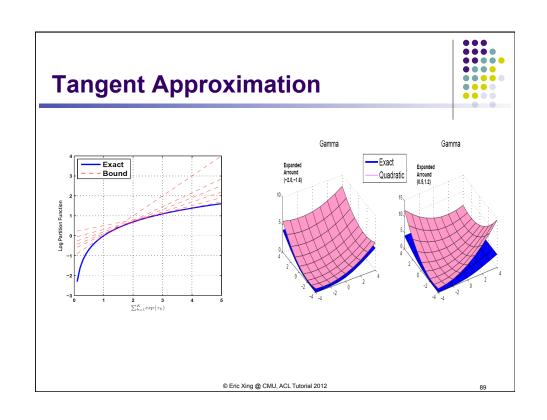
$$\propto P\left(z^{k} \middle| \langle S_{\gamma} \rangle_{q\gamma}\right) P\left(w^{j} \middle| z^{k}, \beta\right)$$

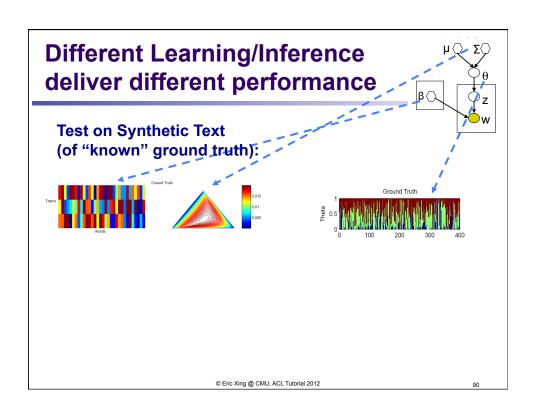
$$\propto P\left(z^{k} \middle| \langle \gamma \rangle_{q\gamma}\right) \beta_{kj}$$

$$\propto \exp\left\{u_{\gamma,k}\right\} \beta_{kj}$$









# Comparison: accuracy and speed L2 error in topic vector est. and # of iterations • Varying Num. of Topics • Varying Voc. Size • Varying Num. Words Per Document • Varying Num. Words Per Document

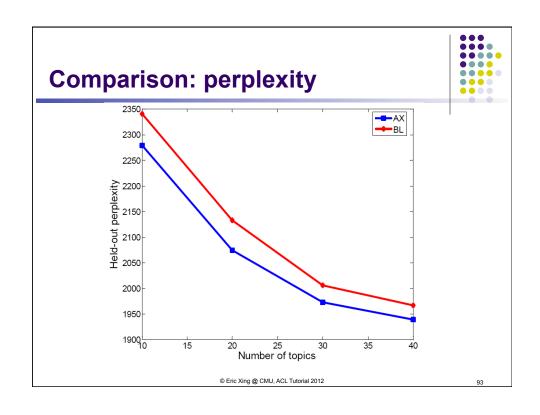
#### **Result on NIPS collection**



- NIPS proceeding from 1988-2003
- 14036 words
- 2484 docs
- 80% for training and 20% for testing
- Fit both models with 10,20,30,40 topics
- Compare perplexity on held out data
  - The perplexity of a language model with respect to text x is the reciprocal of the geometric average of the probabilities of the predictions in text x. So, if text x has k words, then the perplexity of the language model with respect to that text is

**Pr(x)** -1/k

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# **Classification Result on PNAS** collection



- PNAS abstracts from 1997-2002
  - 2500 documents
  - Average of 170 words per document
- Fitted 40-topics model using both approaches
- Use low dimensional representation to predict the abstract category
  - Use SVM classifier
  - 85% for training and 15% for testing

#### **Classification Accuracy**

Total   146   64.3   72.6	Category Genetics Biochemistry Immunology Biophysics	Doc 21 86 24 15	BL 61.9 65.1 70.8 53.3	AX 61.9 77.9 66.6 66.6	-Notable Difference -Examine the low dimensional representations below
	Total	146	64.3	72.6	

# Computation on undirected TM [Welling et al NIPS 04, Xing et al, UAI 05]



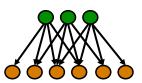
**Undirected model**: Learning is hard, inference is easy.

**<u>Directed Model</u>**: Learning is "easier", inference is hard.

Example: Document Retrieval.



topics



Retrieval is based on comparing (posterior) topic distributions of documents.

- directed models: inference is slow. Learning is relatively "easy".
- undirected model: inference is fast. Learning is slow but can be done offline.

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# **Properties of Directed Networks**



 $h \sim p(h)$ 

- · Factors are marginally independent.
- Factors are conditionally dependent given observations on the visible nodes.

$$P(\ell \mid \mathbf{w}) = \frac{P(\mathbf{w} \mid \ell)P(\ell)}{P(\mathbf{w})}$$

- Easy ancestral sampling.
  - $p_{\theta}(h|v)$
- Learning with (variational) EM



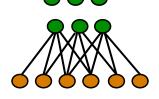
# **Properties of Harmoniums**

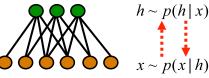


- Factors are marginally dependent.
- Factors are conditionally independent given observations on the visible nodes.

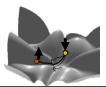
$$P(\ell \mid \mathbf{w}) = \mathsf{j} \mathsf{C}_i P(\ell_i \mid \mathbf{w})$$

Iterative Gibbs sampling.





Learning with contrastive divergence



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# **Learning and Inference**



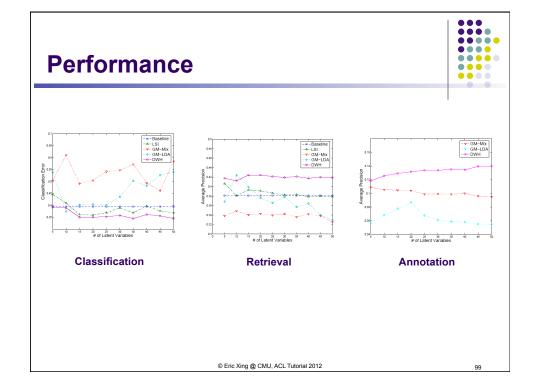
• Maximal likelihood learning based on gradient ascent.

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$$\delta\theta_i \propto \langle f_i(x_i) \rangle_{\text{data}} - \langle f_i(x_i) \rangle_{p}$$

- gradient computation requires model distribution p(.)
- p(.) is intractable
- Contrastive Divergence
  - approximate p(.) with Gibbs sampling
- Variational approximation
  - GMF approximation

$$q(\mathbf{x}, \mathbf{z}, \mathbf{h}) = \prod_{i} q(x_i \mid \mathbf{v}_i) \prod_{k} q(z_k \mid \boldsymbol{\mu}_k, \boldsymbol{\sigma}_k) \prod_{j} q(\boldsymbol{h}_j \mid \boldsymbol{\gamma}_j)$$
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# **Computation on STC**

[Zhu and Xing, UAI 11]



- Hierarchical sparse coding
  - for each document

$$\min_{\boldsymbol{\theta},\mathbf{s}} \qquad \sum_{n \in I} \ell(w_n, \mathbf{s}_n^{\top} \boldsymbol{\beta}_n) + \lambda \|\boldsymbol{\theta}\|_1 + \sum_{n \in I} (\gamma \|\mathbf{s}_n - \boldsymbol{\theta}\|_2^2 + \rho \|\mathbf{s}_n\|_1))$$

s.t.: 
$$\theta \ge 0$$
;  $\mathbf{s}_n \ge 0$ ,  $\forall n \in I$ ,

Word code

$$s_{nk} = \max(0, \nu_k)$$

where 
$$2\gamma\beta_{kn}\nu_k^2 + (2\gamma\mu + \beta_{kn}\eta)\nu_k + \mu\eta - w_n\beta_{kn} = 0$$

• Document code (truncated averaging)

$$\theta_k = \max(0, \bar{s}_k - \frac{\lambda}{2\gamma |I|}) \text{ where } \bar{s}_k = \frac{1}{|I|} \sum_{n \in I} s_{nk}$$

- Dictionary learning
  - projected gradient descent
  - any faster alternative method can be used

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## **Opt. Algorithm for Sparse Coding**



- Much research has been done for optimizing a convex, but non-smooth objective (may subject to some constraints, e.g., non-negativity)
- Greedy algorithm for the non-convex  $L_0$  "pseudo-norm":
  - select the element with maximum correlation with the residual
  - known as "matching pursuit" (Mallat & Zhang, 1993)
- For the convex L<sub>1</sub> norm, many algorithms:
  - Soft-thresholding with coordinate descent (Friedman et al., 2007; Fu, 1998; Zhu & Xing, 2011)
  - Proximal methods (Nesterov, 2007; Jenatton et al., 2010)
  - Active-set methods (Roth & Fischer, 2008)
  - Iterative Re-weighted Least Squares (Daubechies et al., 2008)
  - LARS (Efron et al., 2004) solves for regularization path
  - Online/stochastic variants
  - . . .

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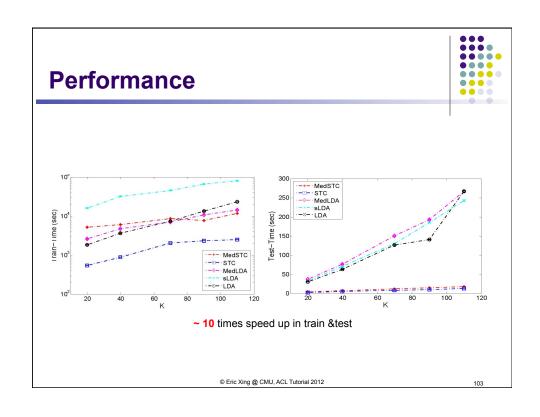
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# Opt. Algorithm for Dictionary Learning

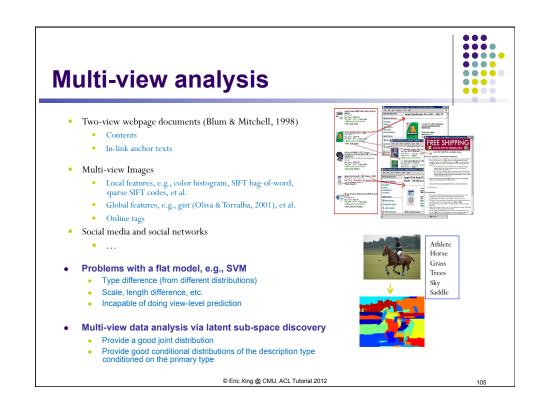


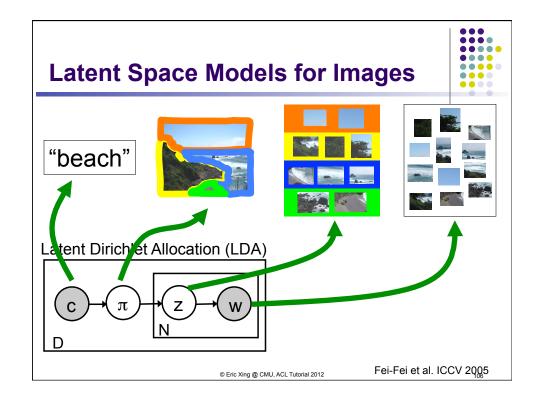
- Optimize a convex and usually smooth objective w/o (convex) constraints
- General optimization procedure can be applied, less research has been done for this step
  - Projected gradient descent
  - Block-wise coordinate descent
  - ..
- A recent progress is made on online/stochastic optimization method (Mairal et al., 2010)

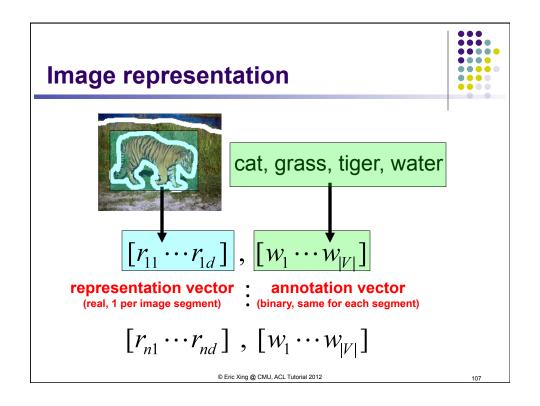
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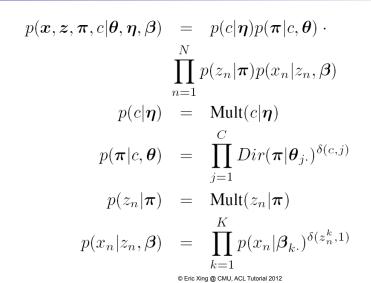
# 3. Scenario I: Multimodal data

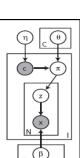






# To Generate an Image ...





# **Annotated images**





{9.32, 2.44, 0.02, 3.23} {4.35, 3.12, -0.23, 9.41}  $\{6.65, 2.11, 1.02, 2.31\}$ 

This cozy place is nestled in the heart of the Mission. Easy access to bars, restuarants, and BART.

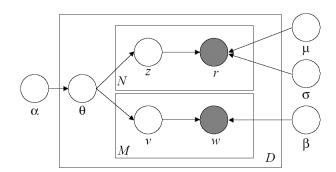
This, cozy, place, is, nestled, in, the, heart, of, the, Mission, Easy, access, to, bars, restuarants, and, BART

- Forsyth et. al. (2001): images as documents where regionspecific feature vectors are like visual words.
- A captioned image can be thought of as annotated data: two documents, one of which describes the other.

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## Gaussian-multinomial LDA [Bliei et al, JMLR 05]

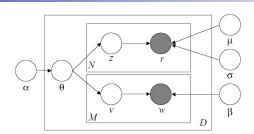




- A natural next step is to glue two LDA models together.
- Bottom: a traditional LDA model on captions
- Top: a Gaussian-LDA model on images
  - each region is a multivariate Gaussian
- Does not work well

# **Exchangeability**





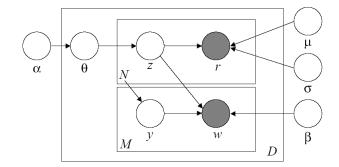
- Like LDA, GM-LDA implicitly makes an exchangeability assumption about words and regions, and their corresponding topics.
- The order in which words and regions are generated does not matter.
- But this is goes against the way we're thinking about the data!
- The words are chosen to describe the image.
- The implicit exchangeability assumptions in the model should reflect this. In other words, we want to model partial exchangeability

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#### **Corr-LDA**

[Bliei et al, JMLR 05]





- Since, w is conditioned on z, the image must be generated first.
- Unlike GM-LDA, the caption is guaranteed to be generated by a subset of the same hidden factors which generated the image.
- The model enforces a correspondence between the latent space associated with images and the latent space associated with captions. © Eric Xing @ CMU, ACL Tutorial 2012

## **Automatic annotation**





True caption
birds tree
Corr-LDA
birds nest leaves branch tree

**GM-LDA** water birds nest tree sky

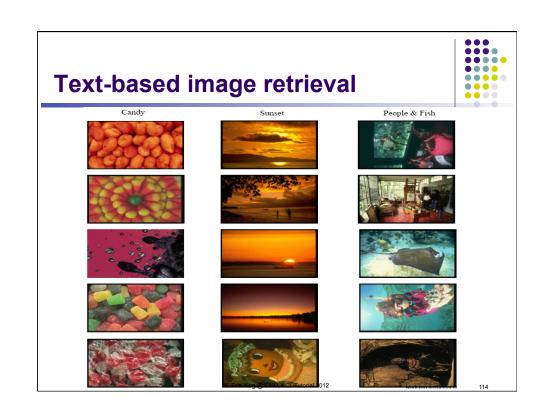
**GM-Mixture** tree ocean fungus mushrooms coral

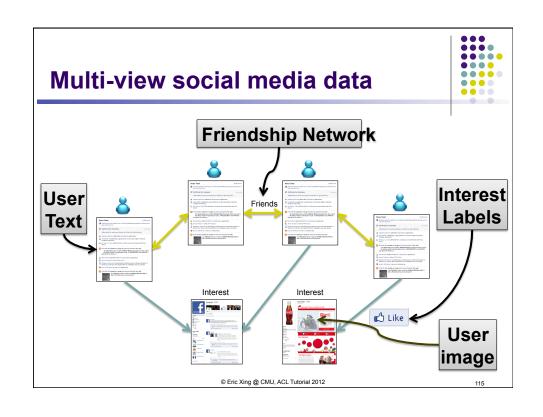
True caption
fish reefs water
Corr-LDA
fish water ocean tree coral

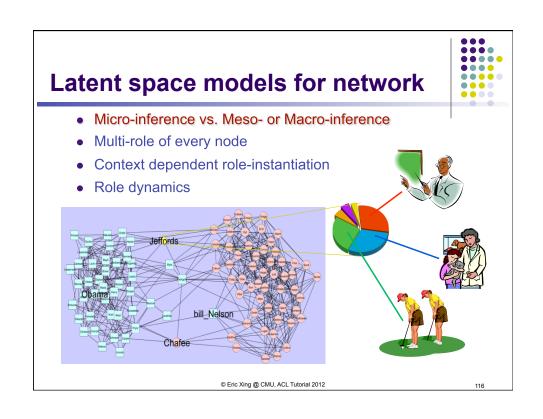
**GM-LDA** water sky vegetables tree people

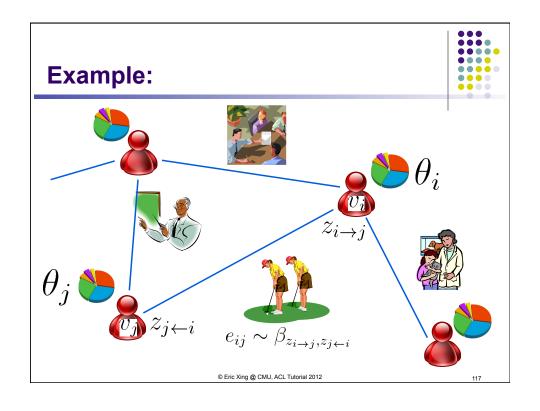
**GM-Mixture** fungus mushrooms tree flowers leaves

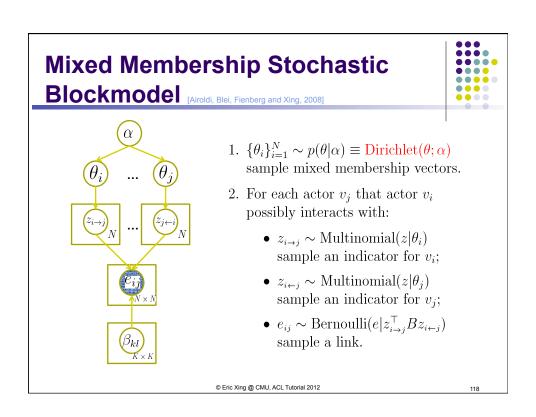
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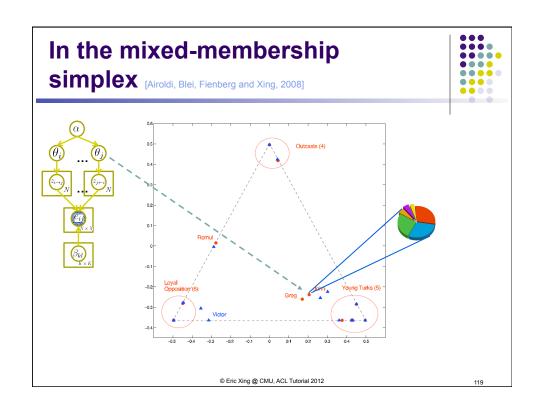


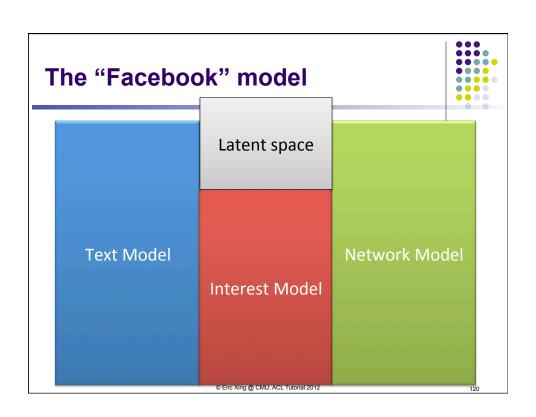


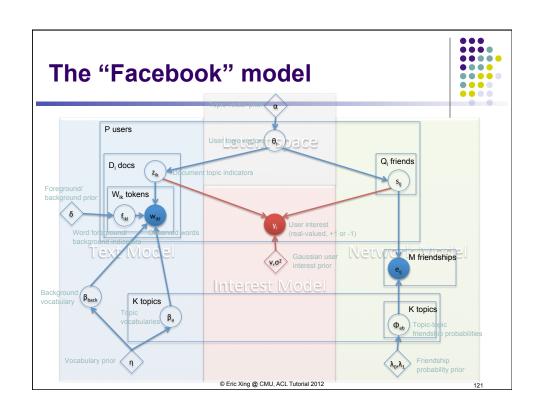


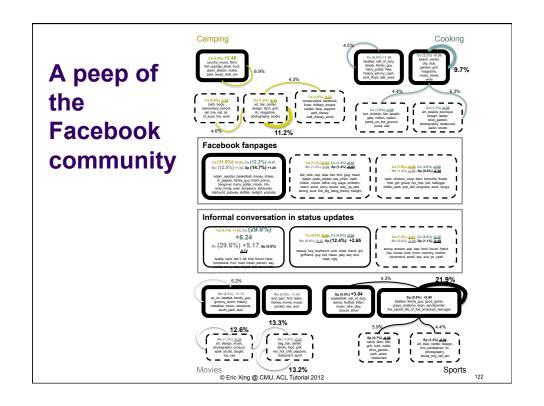


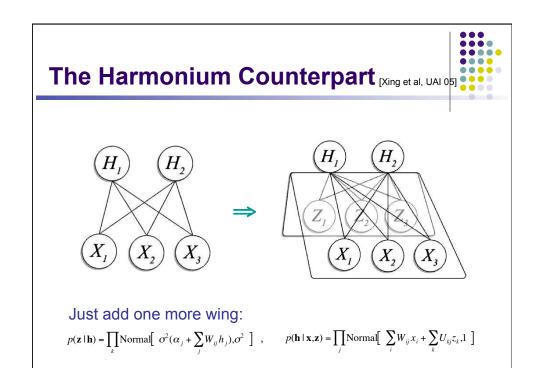


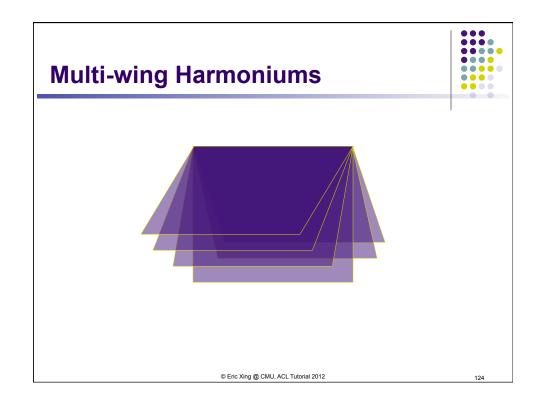










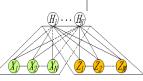






An simple undirected GM with conditional inder

$$\begin{split} p(\mathbf{x}, \mathbf{z}, \mathbf{h}) &\propto \exp \Big\{ \sum_{i} \boldsymbol{\theta}_{i}^{\top} \boldsymbol{\phi}(x_{i}, x_{i+1}) + \sum_{j} \boldsymbol{\eta}_{j}^{\top} \boldsymbol{\psi}(z_{j}, z_{j+1}) + \sum_{k} \boldsymbol{\lambda}_{k}^{\top} \boldsymbol{\varphi}(h_{k}) \\ &+ \sum_{ik} \boldsymbol{\phi}(x_{i}, x_{i+1})^{\top} \mathbf{W}_{i}^{k} \boldsymbol{\varphi}(h_{k}) + \sum_{jk} \boldsymbol{\psi}(z_{j}, z_{j+1})^{\top} \mathbf{U}_{j}^{k} \boldsymbol{\varphi}(h_{k}) \Big\}. \end{split}$$



Local conditional Markov networks (CRFs conditioned on latent H):

$$\begin{split} p(\mathbf{x}|\mathbf{h}) &= \exp \left\{ \sum_{i} \hat{\boldsymbol{\theta}}_{i}^{\top} \phi(x_{i}, x_{i+1}) - A(\hat{\boldsymbol{\theta}}) \right\}, \text{ where } \hat{\boldsymbol{\theta}}_{i} = \boldsymbol{\theta}_{i} + \sum_{k} \mathbf{W}_{i}^{k} \varphi(h_{k}); \\ p(\mathbf{z}|\mathbf{h}) &= \exp \left\{ \sum_{i} \hat{\boldsymbol{\eta}}_{j}^{\top} \psi(z_{j}, z_{j+1}) - B(\hat{\boldsymbol{\eta}}) \right\}, \text{ where } \hat{\boldsymbol{\eta}}_{j} = \boldsymbol{\eta}_{j} + \sum_{k} \mathbf{U}_{j}^{k} \varphi(h_{k}); \end{split}$$

• Conditionally independent latent variables

$$p(\mathbf{h}|\mathbf{x},\mathbf{z}) = \prod_{k} \exp \Big\{ \hat{\lambda}_{k}^{\top} \varphi(h_{k}) - C_{k}(\hat{\lambda}_{k}) \Big\}, \text{ where } \hat{\lambda}_{k} = \lambda_{k} + \sum_{i} \mathbf{W}_{i}^{k} \phi(x_{i},x_{i+1}) + \sum_{j} \mathbf{U}_{j}^{k} \psi(z_{j},z_{j+1})$$

very efficient for fully observed view input data; potentially scale up to large data (e.g., millions of images) (Weston et al, 2010)

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# **Examples of Latent Topics**



storms gulf hawaii low forecast southeast showers  $T_1$ 



rebounds 14 shouting tests guard cut hawks  $T_2$ 



engine flying craft asteroid say hour aerodynamic  $T_3$ 

safe cross red sure dry providing services



losing jersey sixth antonio david york orlando  $T_5$ 

## Are we done?



- What was our task?
  - Embedding (lower dimensional representation): yes,  $Doc \rightarrow \theta$
  - Distillation of semantics: kind of, we've learned "topics" β
  - Classification: is it good?
  - Clustering: is it reasonable?
  - Other predictive tasks?

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# 4. Scenario II: when supervision is available



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# Problem: Discriminative topic models for text classification/scoring



• Democratic or republican?

Movie review/scoring







John McCain



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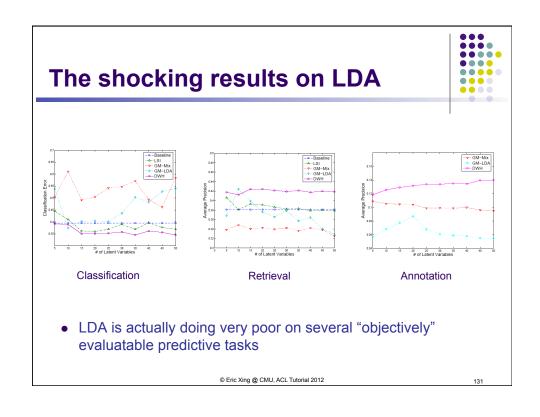
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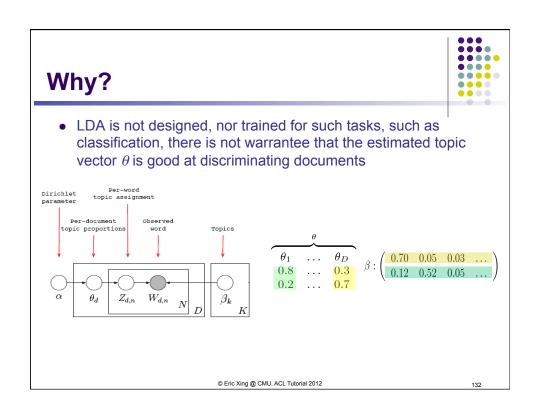
### We want to answer ...



- Are we satisfied with the conventional topic models and the MLE method for PREDICTION?
- Can we learn a PREDICTIVE model better?

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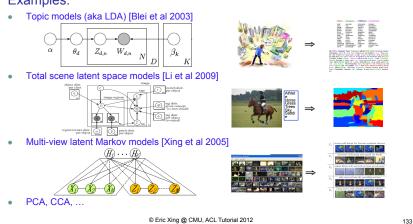




# **Unsupervised Latent Subspace Discovery**



- Finding latent subspace representations (an old topic)
  - Mapping a high-dimensional representation into a latent low-dimensional representation, where each dimension can have some interpretable meaning, e.g., a semantic topic
- Examples:



# **Predictive** Subspace Learning with **Supervision**



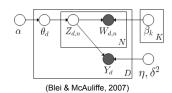
- Unsupervised latent subspace representations are generic but can be sub-optimal for predictions
- Many datasets are available with supervised side information



- Can be noisy, but not random noise (Ames & Naaman, 2007)
  - labels & rating scores are usually assigned based on some intrinsic property of the data
  - helpful to suppress noise and capture the most useful aspects of the data
- Goals:
  - Discover latent subspace representations that are both predictive and interpretable by exploring weak supervision information
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## I. Supervised Topic Model





 How to integrate the max-margin principle into a probabilistic latent variable model?

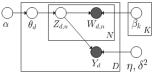
Max-Likelihood Estimation	Max-Margin and Max- Likelihood
sLDA	MedLDA
	(Zhu et al, ICML 2009)

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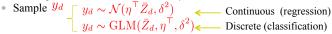
# **Supervised Topic Model**



- LDA ignores documents' side information (e.g., categories or rating score), thus lead to suboptimal topic representation for supervised tasks
- Supervised Topic Models handle such problems, e.g., sLDA (Blei & McAuliffe, 2007) and DiscLDA(Simon et al., 2008)
  - Generative Procedure (sLDA):
    - For each document *d*:
      - Sample a topic proportion  $\theta_d \sim \text{Dir}(\alpha)$
      - For each word:
        - Sample a topic  $Z_{d,n} \sim \operatorname{Mult}(\theta_d)$
        - Sample a word  $W_{d,n} \sim \operatorname{Mult}(\beta_{z_{d,n}})$



(Blei & McAuliffe, 2007



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# **How to train sLDA?**



Maximize

$$P(Y,W)$$
?

Maximize

$$P(Y|W)$$
?

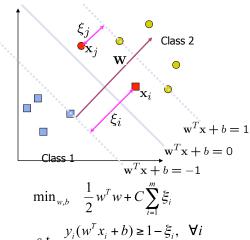
• Support vector machines

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# **Support vector machines**





 $y_i(w \ x_i + b) \ge 1 - \xi_i, \quad \forall i$ 

 $\xi_i \ge 0, \quad \forall i$ 

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# **SVM** using VC-dimension



#### **VC** Theory

(Vapnik, 1982) Given  $x_1, ..., x_n \in \mathbb{R}^d$  iid and  $||x_i||_2 \leq D$ , if  $\mathcal{H}_{\gamma}$  is the hypothesis space of linear classifiers in  $\mathbb{R}^d$  with margin  $\gamma$ ,

$$VC(\mathcal{H}_{\gamma}) \leq \min \left\{ d, \left\lceil rac{4D^2}{\gamma^2} 
ight
ceil 
ight\}.$$

$$error_{true}(h) < error_{train}(h) + \sqrt{\frac{VC(H)(\ln{\frac{2m}{VC(H)}} + 1) + \ln{\frac{4}{\delta}}}{m}}$$

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## **SVM** using VC-dimension



- Thus large-margin → small VC-dim → better generalization bound
- Recall that d+1 is the upper bound for a linear classifier in dspace

$$VC(\mathcal{H}_{\gamma}) \leq \min \left\{ d, \left\lceil rac{4D^2}{\gamma^2} 
ight
ceil 
ight\}.$$

$$error_{true}(h) < error_{train}(h) + \sqrt{\frac{VC(H)(\ln{\frac{2m}{VC(H)}} + 1) + \ln{\frac{4}{\delta}}}{m}}$$

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# MLE versus max-margin learning



- · Likelihood-based estimation
  - Probabilistic (joint/conditional likelihood model)
  - Easy to perform Bayesian learning, and incorporate prior knowledge, latent structures, missing data
  - Bayesian regularization!!
- Max-margin learning
  - Non-probabilistic (concentrate on inputoutput mapping)
  - Not obvious how to perform Bayesian learning or consider prior, and missing data
  - Sound theoretical guarantee with limited samples
- Maximum Entropy Discrimination (MED) (Jaakkola, et al., 1999)
  - Model averaging

 $\hat{y} = \operatorname{sign} \int p(\mathbf{w}) F(x; \mathbf{w}) \, d\mathbf{w}$ 

 $(y \in \{+1, -1\})$ 

The optimization problem (binary classification)

 $\operatorname{MED}_{\mathrm{s.t.}} \operatorname{\substack{KL(p(\Theta)||p_0(\Theta)) \\ \mathrm{Subsumes} \\ \mathrm{s.t.}}} \operatorname{\substack{KL(p(\Theta)||p_0(\Theta)) \\ \mathrm{subsumes} \\ \mathrm{SVM}}} .$ 

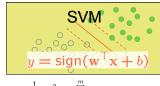
where  $\Theta$  is the parameter  $\mathbf{w}$  when  $\xi$  are kept fixed or the pair  $(\mathbf{w}, \xi)$  when we want to optimize over  $\xi$ 

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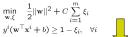
# A road map for max-margin learning



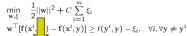


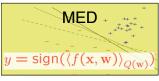












MED-MN? = SMED + "Bayesian" M<sup>3</sup>N

Primal and Dual Sparse!

 $\begin{aligned} & \min_{Q} & \text{KL}(Q||Q_{0}) \\ & y^{i} \langle f(\mathbf{x}^{i}) \rangle_{Q} \geq \xi_{i}, & \forall i \end{aligned}$ 

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# **MaxEnt Discrimination Markov Network**



• Structured MaxEnt Discrimination (SMED):

P1: 
$$\min_{p(\mathbf{w}),\xi} \frac{KL(p(\mathbf{w})||p_0(\mathbf{w})) + U(\xi)}{\text{s.t. } p(\mathbf{w}) \in \mathcal{F}_1, \ \xi_i \geq 0, \forall i.}$$
generalized maximum entropy or regularized KL-divergence

• Feasible subspace of weight distribution:

$$\mathcal{F}_{1} = \{p(\mathbf{w}) : \int p(\mathbf{w})[\Delta F_{i}(\mathbf{y}; \mathbf{w}) - \Delta \ell_{i}(\mathbf{y})] \, d\mathbf{w} \ge -\xi_{i}, \quad \forall i, \forall \mathbf{y} \ne \mathbf{y}^{i} \},$$

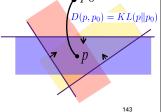
$$expected \text{ margin constraints.}$$

$$D(p, p_{0}) = KL(p||p_{0})$$

Average from distribution of M<sup>3</sup>Ns

$$h_1(\mathbf{x}; p(\mathbf{w})) = \arg\max_{\mathbf{y} \in \mathcal{Y}(\mathbf{x})} \int p(\mathbf{w}) F(\mathbf{x}, \mathbf{y}; \mathbf{w}) d\mathbf{w}$$

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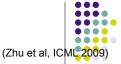
## MedLDA: a max-margin approach



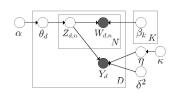
- Big picture of supervised topic models
  - sLDA: optimizes the joint likelihood for regression and classification
  - DiscLDA: optimizes the conditional likelihood for classification ONLY
  - MedLDA: based on max-margin learning for both regression and classification

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#### **MedLDA Regression Model**



Bayesian sLDA:



MED Estimation:

MED Estimation: 
$$\begin{aligned} \text{P1}(\text{MedLDA}^r) : & \min_{q,\alpha,\beta,\delta^2,\xi,\xi^\star} \mathcal{L}(q) + C \sum_{d=1}^D (\xi_d + \xi_d^\star) \\ \text{s.t.} & \forall d : \end{aligned} \end{aligned} \\ \begin{cases} y_d - E[\eta^\top \bar{Z}_d] \leq \epsilon + \xi_d, \ \mu_d \\ -y_d + E[\eta^\top \bar{Z}_d] \leq \epsilon + \xi_d^\star, \ \mu_d^\star \\ \xi_d \geq 0, \ v_d \\ \xi_d^\star \geq 0, \ v_d^\star \end{aligned} \end{aligned} \\ \text{predictive accuracy}$$

• Variational bound  $q(\theta, \mathbf{z}, \eta | \gamma, \phi) \sim p(\theta, \mathbf{z}, \eta | \alpha, \beta, \delta^2, \mathbf{y}, \mathbf{W})$ 

$$\mathcal{L}(q) \triangleq -E[\log p(\theta, \mathbf{z}, \eta, \mathbf{y}, \mathbf{W} | \alpha, \beta, \delta^2)] - \mathcal{H}(q(\mathbf{z}, \theta, \eta)) \geq -\log p(\mathbf{y}, \mathbf{W} | \alpha, \beta, \delta^2)$$

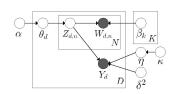
• Predictive Rule:

$$\bar{y} = E[Y|w_{1:N}, \alpha, \beta, \delta^2] = E_{q(Z,\eta)}[\eta^{\top} \bar{Z}|w_{1:N}, \alpha, \beta, \delta^2]$$

#### MedLDA Classification Model (Zhu et al, ICML 2009)



• Bayesian sLDA:



• Multiclass MedLDA Classification Model:

$$P2(MedLDA^{c}): \min_{q,q(\eta),\alpha,\beta,\xi} \mathcal{L}(q) + C \sum_{d=1}^{D} \xi_{d}$$

s.t. 
$$\forall d, \ y \neq y_d : \ E[\eta^{\top} \Delta \mathbf{f}_d(y)] \ge 1 - \xi_d; \ \xi_d \ge 0,$$

• Variational bound  $q(\theta, \mathbf{z}, \eta | \gamma, \phi) \sim p(\theta, \mathbf{z}, \eta | \alpha, \beta, \delta^2, \mathbf{y}, \mathbf{W})$ 

$$\mathcal{L}(q) \triangleq -E[\log p(\theta, \mathbf{z}, \eta, \mathbf{y}, \mathbf{W} | \alpha, \beta, \delta^2)] - \mathcal{H}(q(\mathbf{z}, \theta, \eta)) \geq -\log p(\mathbf{y}, \mathbf{W} | \alpha, \beta, \delta^2)$$

• Predictive Rule:

$$y^* = \arg\max_{y} E[\eta^{\mathsf{T}} \mathbf{f}(y, \bar{Z}) | \alpha, \beta]$$

#### Variational EM Alg.



- **E-step**: infer the posterior distribution of hidden r.v.  $(\theta, \mathbf{z}, \eta)$
- **M-step**: estimate unknown parameters  $(\alpha, \beta, \delta^2)$
- Independence assumption:  $q(\theta, \mathbf{z}, \eta | \gamma, \phi) = q(\eta) \prod_{d=1}^D q(\theta_d | \gamma_d) \prod_{n=1}^N q(z_{dn} | \phi_{dn})$   $L(\gamma, \phi, q(\eta), \ \alpha, \beta, \delta^2, \xi, \xi^\star, \mu, \mu^\star, v, v^\star) = \mathcal{L}(q) + C \sum_{d=1}^D (\xi_d + \xi_d^\star) \sum_{d=1}^D \sum_{i=1}^N c_{di} (\sum_{j=1}^K \phi_{dij} 1)$   $\sum_{d=1}^D \mu_d(\epsilon + \xi_d y_d + E[\eta^\top \bar{Z}_d]) \sum_{d=1}^D (\mu_d^\star(\epsilon + \xi_d^\star + y_d E[\eta^\top \bar{Z}_d]) + v_d \xi_d + v_d^\star \xi_d^\star)$
- Optimize L over  $\phi$ :

$$\phi_{di} \propto \exp\left(E[\log \theta | \gamma] + E[\log p(w_{di} | \beta)] + \frac{y_d}{N\delta^2} E[\eta] - \frac{2E[\eta^\top \phi_{d,-i}\eta] + E[\eta \circ \eta]}{2N^2\delta^2} + \frac{E[\eta]}{N} (\mu_d - \mu_d^*)\right)$$

- The first two terms are the same as in LDA
- The third and fourth terms are similar to those of sLDA, but in expected version. The variance matters!
- The last term is a regularizer. Only support vectors affect the topic proportions
- Optimize L over other variables. See the paper for details!

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#### MedTM: a general framework



- MedLDA can be generalized to arbitrary topic models:
- Unsupervised or supervised
  - Generative or undirected random fields (e.g., Harmoniums)
- MED Topic Model (MedTM):

$$\begin{split} \mathbf{P}(\mathbf{MedTM}) : \min_{\substack{q(H), q(\Upsilon), \Psi, \xi \\ \text{s.t. } expected \\ \text{model fitting}}} \underbrace{\mathcal{L}(q(H)) + \underbrace{KL(q(\Upsilon) || p_0(\Upsilon)) + U(\xi)}_{\text{predictive accuracy}} \end{split}$$

- ullet H: hidden r.v.s in the underlying topic model, e.g.,  $( heta,\mathbf{z})$  in LDA
- $\Upsilon$ : parameters in predictive model, e.g.,  $\eta$  in sLDA
- ullet  $\Psi$ : parameters of the topic model, e.g., lpha in LDA
- $m{\mathcal{L}}$ : an variational upper bound of the log-likelihood
- U: a convex function over slack variables

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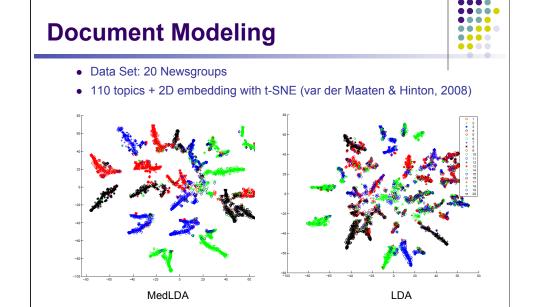
#### **Experiments**

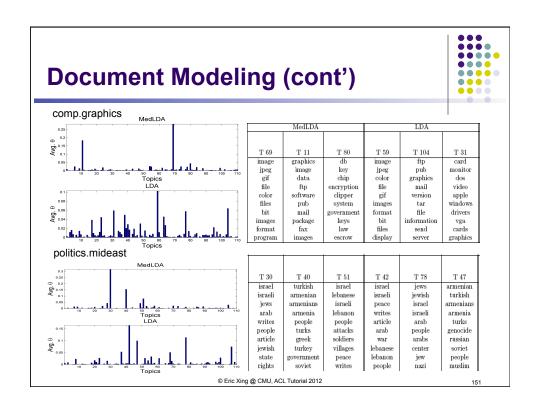


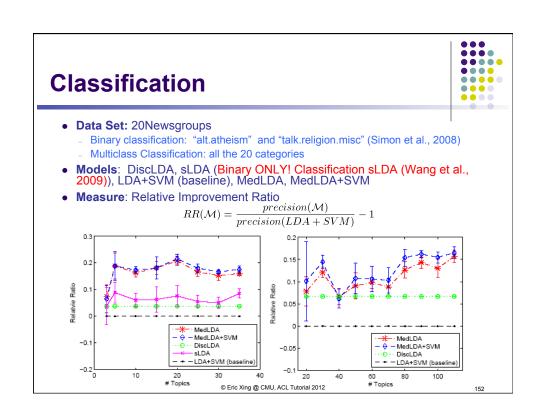
- Goal:
  - To qualitatively and quantitatively evaluate how the max-margin estimates of MedLDA affect its topic discovering procedure
- Data Sets:
  - 20 Newsgroups (classification)
    - Documents from 20 categories
    - ~ 20,000 documents in each group
    - Remove stop word as listed in UMASS Mallet
  - Movie Review (regression)
    - 5006 documents, and 1.6M words
    - Dictionary: 5000 terms selected by tf-idf
    - Preprocessing to make the response approximately normal (Blei & McAuliffe, 2007)

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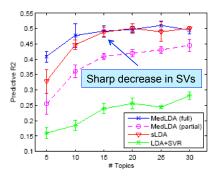


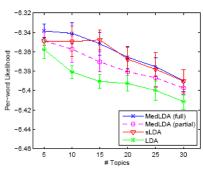
#### Regression



- Data Set: Movie Review (Blei & McAuliffe, 2007)
- Models: MedLDA(partial), MedLDA(full), sLDA, LDA+SVR
- Measure: predictive R2 and per-word log-likelihood

$$pR^{2} = 1 - \frac{\sum_{d} (y_{d} - \hat{y}_{d})^{2}}{\sum_{d} (y_{d} - \bar{y}_{d})^{2}}$$





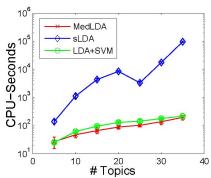
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#### **Time Efficiency**



• Binary Classification



- Multiclass:
  - MedLDA is comparable with LDA+SVM
- Regression:
  - MedLDA is comparable with sLDA

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#### **II. Supervised Multi-view MNs**



 A probabilistic method with an additional view of response variables Y

$$p(y|\mathbf{h}) = \frac{\exp{\{\mathbf{V}^{\top}\mathbf{f}(\mathbf{h}, y)\}}}{Z(V, \mathbf{h})}$$

- Parameters can be learned with maximum likelihood estimation, e.g., special supervised Harmonium (Yang et al., 2007)
  - contrastive divergence is the commonly used approximation method in learning undirected latent variable models (Welling et al., 2004; Salakhutdinov & Murray, 2008).

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#### **Max-margin learning of MNs**



• Expected discriminant function:

$$F(y; V) \triangleq \mathbb{E}_{H}[F(y, H; V)], \text{ where } F(y, H; V) = V_{y}^{\top}H$$

Prediction rule:

$$y^* = \arg\max_{y} \mathbb{E}_{\mathbf{H}}[F(y, H; V)]$$

Hinge loss:

$$\mathcal{R}_{hinge}(V) = \frac{1}{D} \sum_{d} \max_{y} [\Delta \ell_d(y) - V^{\top} \mathbb{E}_{H}[\Delta f_d(y)]],$$

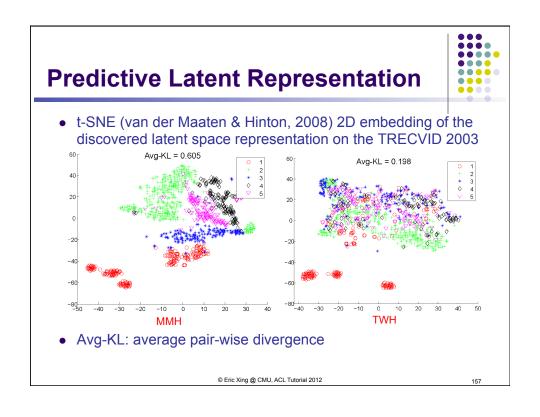
• Joint max-margin and max-likelihood estimation:

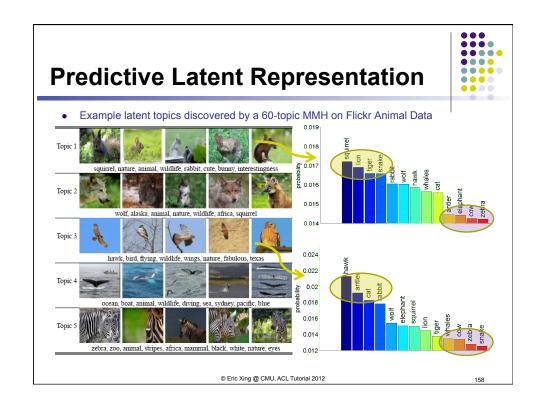
$$\min_{\Theta, V} -L(\Theta) + \frac{1}{2}C_1 ||V||_2^2 + C_2 \mathcal{R}_{hinge}(V)$$

- where  $L(\Theta) := \sum \log p(x_d, z_d)$  is data likelihood
- The rationale is: we want to find a latent representation and a prediction model, which on one hand tend to predict as accurate as possible on training data, while on the other hand tend to explain the data well.

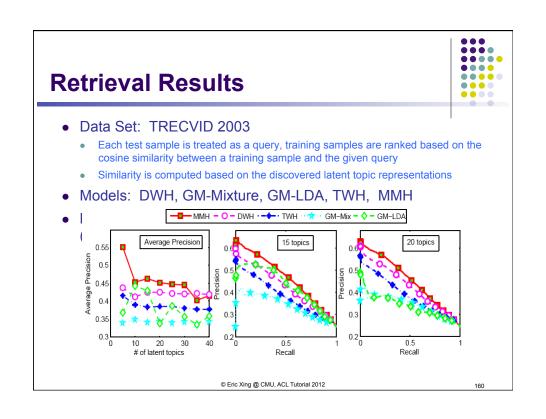
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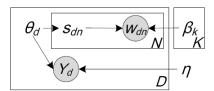


#### **Classification Results** Data Sets: • (Left) TRECVID 2003: (text + image features) (Right) Flickr 13 Animal: (sift + image features) Models: baseline(SVM),DWH+SVM, GM-Mixture+SVM, GM-LDA+SVM, TWH, MedLDA - O - DWH DWH TWH 0.75 MMH(SIFT) MEDLDA(SIFT) GM-Mix 0.55 classification accuracy classification accuracy 0.7 - 🗆 - SVM 0.5 0.6 0.4 0.55 0.5 10 # of latent topics # of latent topics Flickr TRECVID © Eric Xing @ CMU, ACL Tutorial 2012



#### **III. Supervised STC**





• Joint loss minimization

$$\begin{split} \min_{\{\theta_d\}, \{\mathbf{s}_d\}, \beta, \eta} & \quad f(\{\theta_d\}, \{\mathbf{s}_d\}, \beta) + C\mathcal{R}_h(\{\theta_d\}, \eta) + \frac{1}{2} \|\eta\|_2^2 \\ \text{s.t.} : & \quad \theta_d \geq 0, \ \forall d; \ \mathbf{s}_{dn} \geq 0, \ \forall d, n \in I_d; \ \beta_k \in \mathcal{P}, \ \forall k, \end{split}$$

- coordinate descent alg. applies with closed-form update rules
- No sum-exp function; seamless integration with non-probabilistic large-margin principle

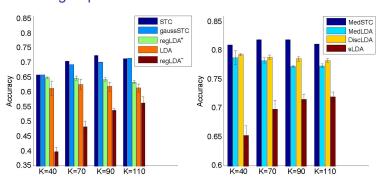
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#### **Classification accuracy**



• 20 newsgroup data:



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# • training & testing time • training & testing time • No calls of digamma function • Converge faster with one additional dimension of freedom

#### **Summary**



- Max-margin, instead of max-likelihood learning of supervised topic models (MedLDA, MMH, MedSTC)
  - Explicit interpretation of effects by support vectors
  - MedLDA can discover discriminative topic representations that are more suitable for supervised tasks
  - The classification model is efficient and can avoid dealing with the normalization factor of a GLM
- The same principle can be applied to a wide variety of probabilistic (MedTM) and non-probabilistic latent variable models

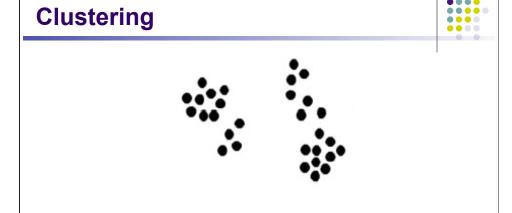
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## 5. Scenario III: what if I don't know the total number of topics?

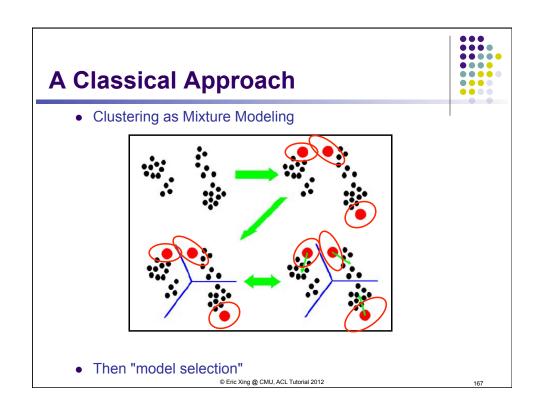


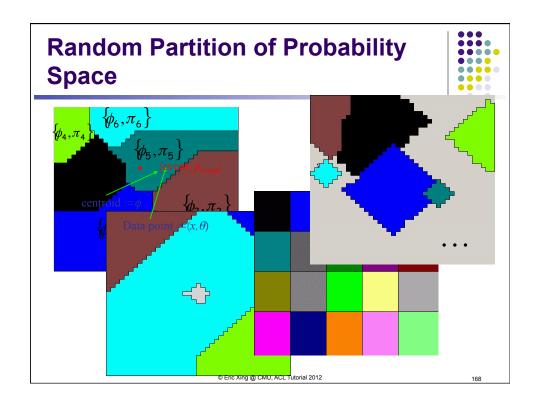
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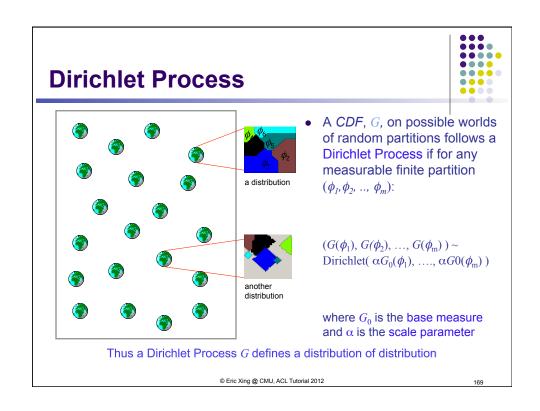
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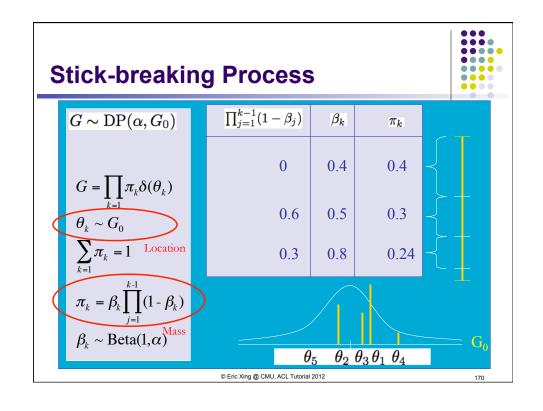


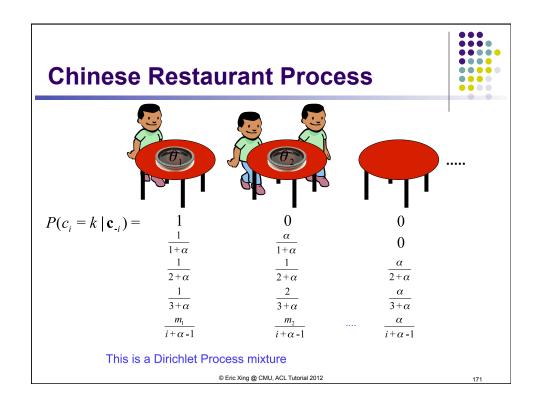
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#### **MCMC** for CRP



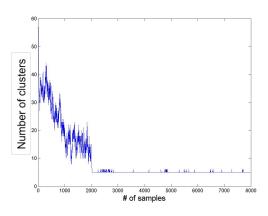
- Gibbs sampling for exploring the posterior distribution under the proposed model
  - Under the CRP metaphor, due to exchangeability, every sample can be treated as the LAST sample!

- $\bullet$  One can also integrate out the parameters such as  $\theta$  and perform collapse Gibbs sampling
- Gibbs sampling algorithm: draw samples of each random variable to be sampled given values of all the remaining variables

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### **Convergence of Ancestral Inference**





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## Variational Inference [Blei & Jordan 2005, Kurihara et al 2007]



- On a single machine Gibbs sampling solution is not efficient enough to scale up to the large scale problems.
- Truncated stick-breaking approximation can be formulated in the space of explicit, non-exchangeable cluster labels.
- Variational inference can now be applied to such a finitedimensional distribution
- Variational Inference:
  - For a complicated  $P(X_1, X_2, ... X_n)$ , approximate it with Q(X):

$$Q(\mathbf{X}) = \prod_{i} Q(\mathbf{X}_{C_i})$$
$$\{Q^*(\mathbf{X}_{C_i})\} = \arg\min KL(Q(\mathbf{X})|P(\mathbf{X}))$$

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#### **Approximations to DP**



- Truncated stick-breaking representation
- Finite symmetric Dirichlet approximation

$$\begin{split} v_i \sim & \mathcal{B}(v_i; 1, \alpha) & i = 1, ..., T-1 \\ v_T = 1 & \\ \pi_i = v_i \prod_{j < i} (1-v_j) & i = 1, ..., T \\ \pi_i = 0 & i > T \end{split}$$

$$oldsymbol{\pi} \sim \mathcal{D}(oldsymbol{\pi}; rac{lpha}{K}, ..., rac{lpha}{K})$$

- expressed as:
- The joint distribution can be The joint distribution can be expressed as:

$$\begin{split} &P(X, \mathbf{z}, \mathbf{v}, \boldsymbol{\eta}) = \\ &\left[ \prod_{n=1}^{N} p(\mathbf{x}_{n} | \eta_{z_{n}}) \; p(z_{n} | \boldsymbol{\pi}(\mathbf{v})) \right] \left[ \prod_{i=1}^{T} p(\eta_{i}) \mathcal{B}(v_{i}; 1, \alpha) \right] \end{split}$$

$$\begin{split} P(X, \mathbf{z}, \mathbf{v}, \boldsymbol{\eta}) &= & P(X, \mathbf{z}, \boldsymbol{\pi}, \boldsymbol{\eta}) = \\ \left[\prod_{n=1}^{N} p(\mathbf{x}_{n} | \eta_{z_{n}}) \, p(z_{n} | \boldsymbol{\pi}(\mathbf{v}))\right] \left[\prod_{i=1}^{T} p(\eta_{i}) \mathcal{B}(v_{i}; \boldsymbol{1}, \boldsymbol{\alpha})\right] & \left[\prod_{n=1}^{N} p(\mathbf{x}_{n} | \eta_{z_{n}}) \, p(z_{n} | \boldsymbol{\pi})\right] \left[\prod_{i=1}^{K} p(\eta_{i})\right] \mathcal{D}(\boldsymbol{\pi}; \frac{\boldsymbol{\alpha}}{K}, ..., \frac{\boldsymbol{\alpha}}{K}) \end{split}$$

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#### **VB** inference



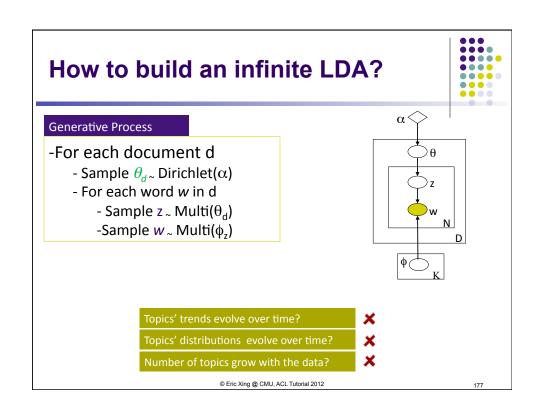
We can then apply the VB inference on the four approximations

$${Q^*(\mathbf{X}_{C_i})} = \arg\min KL(Q(\mathbf{X})|P(\mathbf{X}))$$

The approximated posterior distribution for TSB and FSD are

$$Q_{\mathtt{TSB}}(\mathbf{z}, \boldsymbol{\eta}, \mathbf{v}) = \left[\prod_n^N q(z_n)\right] \left[\prod_{i=1}^T q(\eta_i) q(v_i)\right] \qquad \quad Q_{\mathtt{FSD}}(\mathbf{z}, \boldsymbol{\eta}, \boldsymbol{\pi}) = \left[\prod_n^N q(z_n)\right] \left[\prod_{k=1}^K q(\eta_k)\right] q(\boldsymbol{\pi})$$

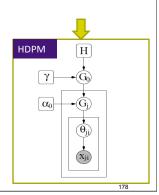
Depending on marginalization or not, v and  $\pi$  may be integrated out.



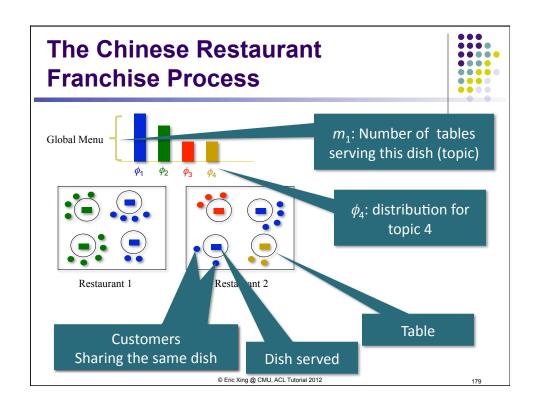
## **The Chinese Restaurant Franchise Process**

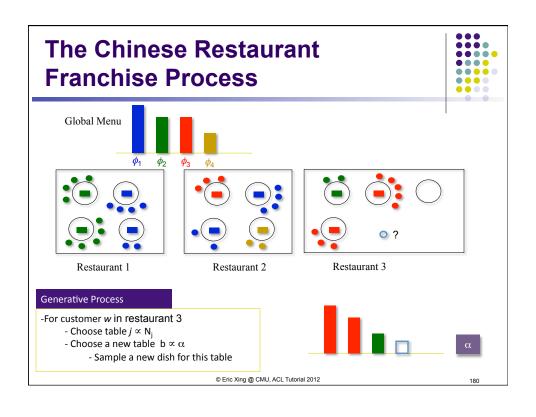


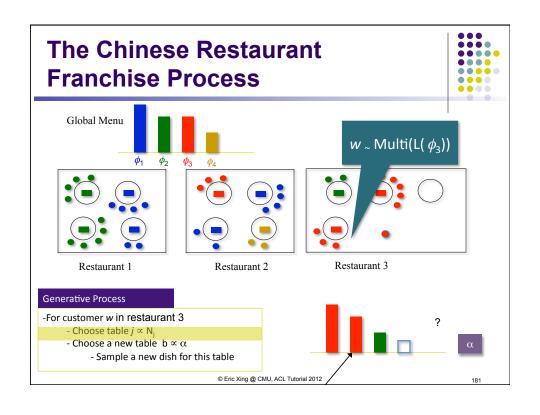
- Hierarchical Dirichlet Process Mixture (HDPM) automatically determines number of topics in LDA
- We will focus on the Chinese Restaurant Franchise process construction
  - A set of restaurants that share a global menu
- Metaphor
  - Restaurant = documents
  - Customer = word
  - Dish = topic
  - Global Menu = Set of topics

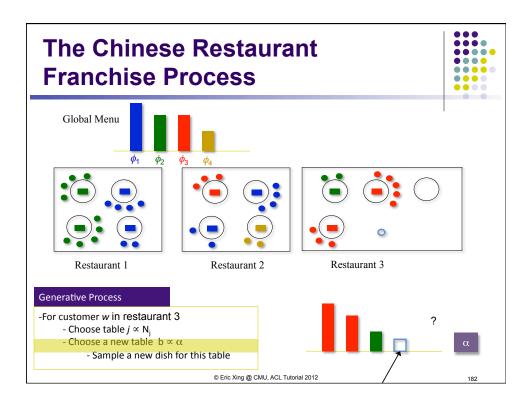


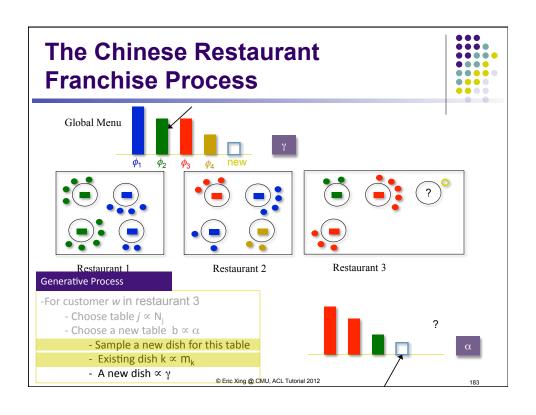
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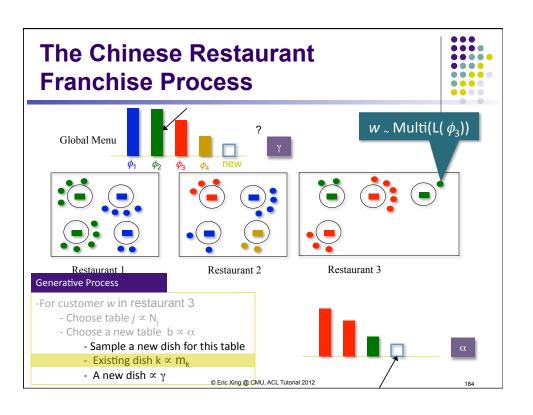


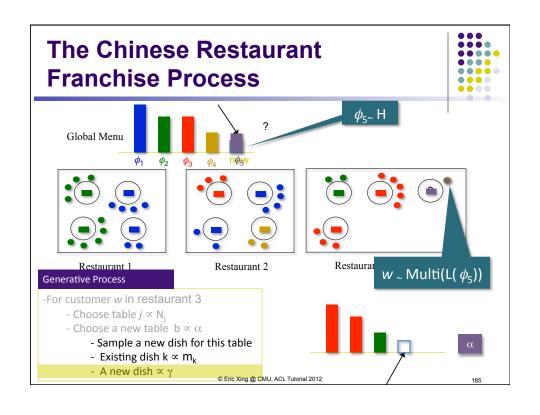


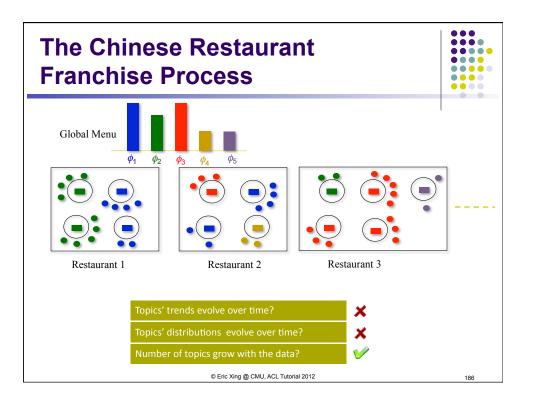


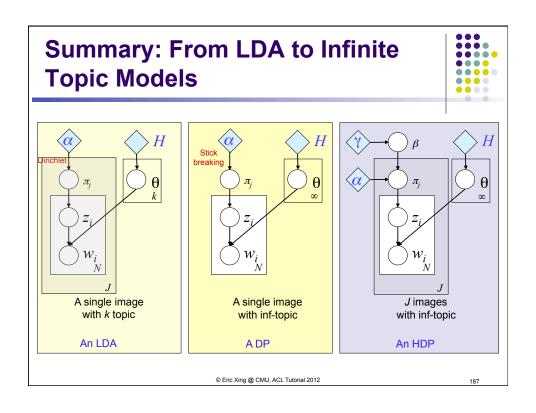




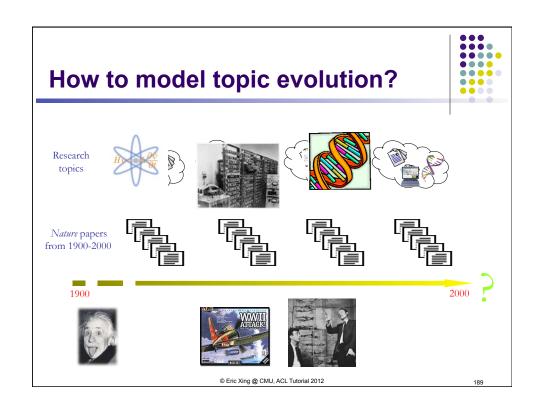


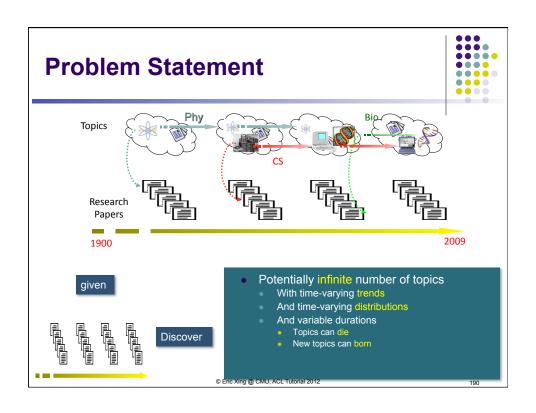


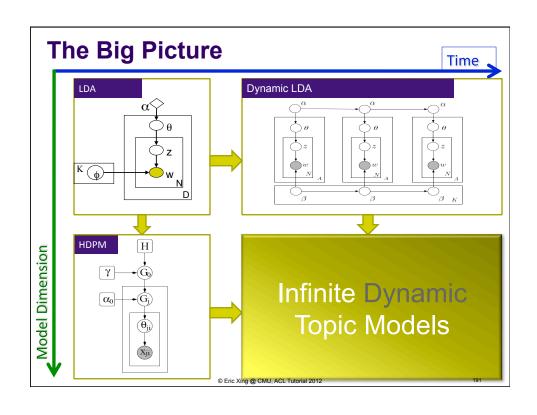


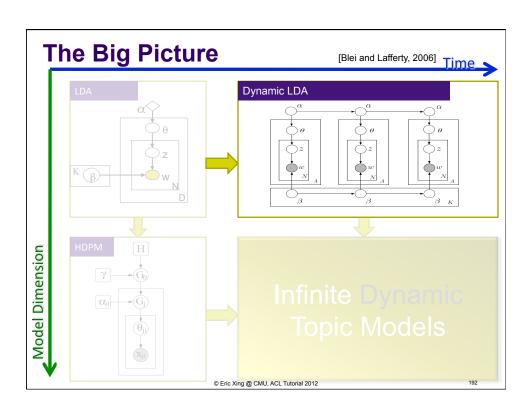


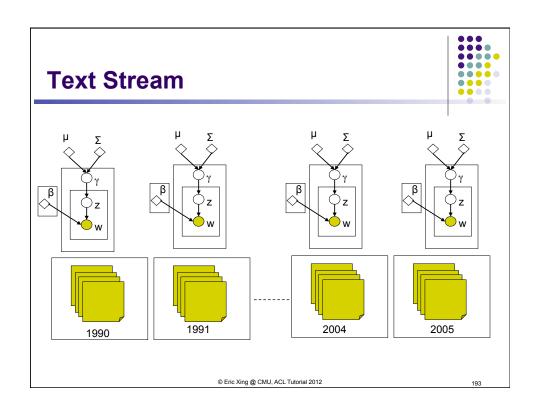
## 6. Scenario IV: Topic evolution in Streaming Corpus

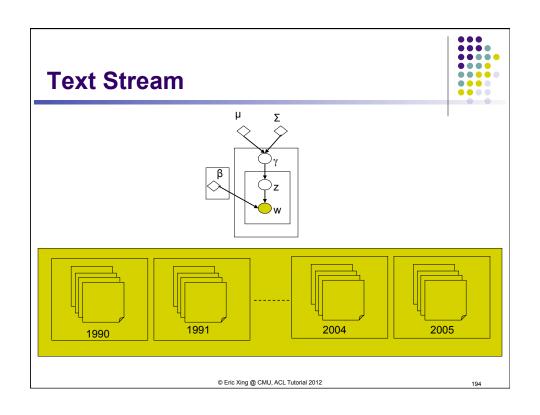


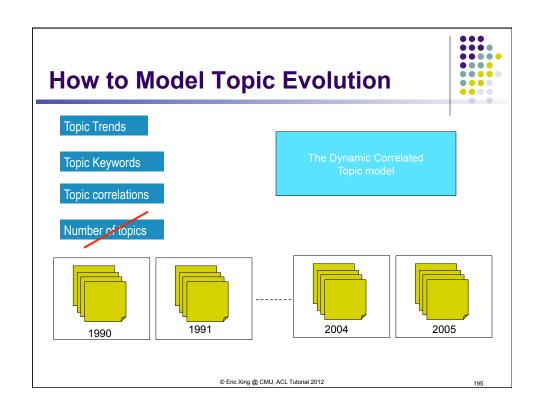


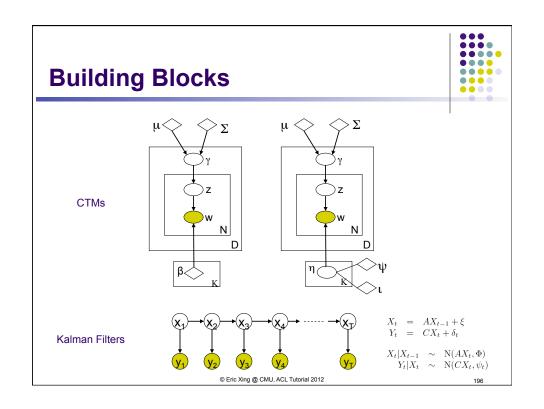


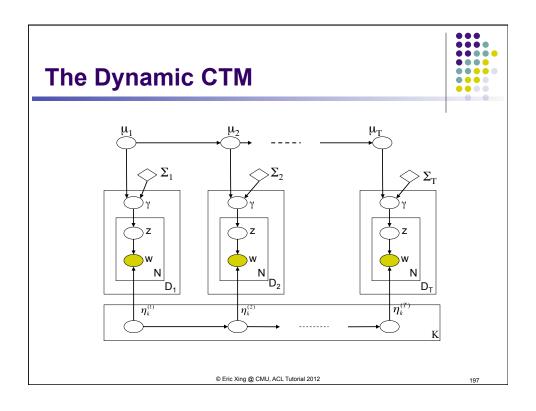


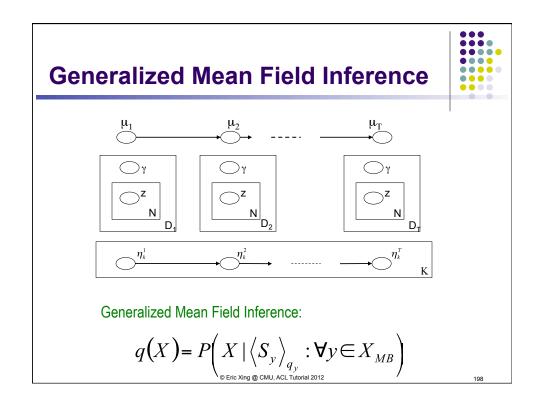










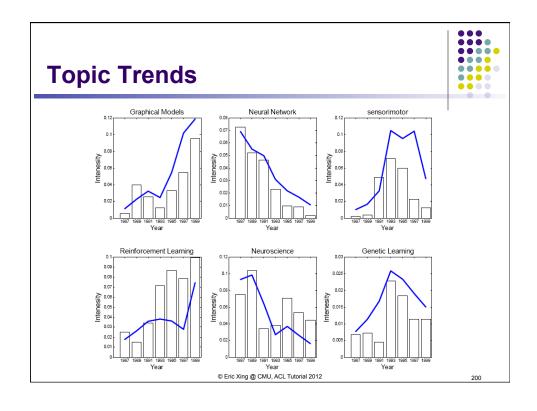


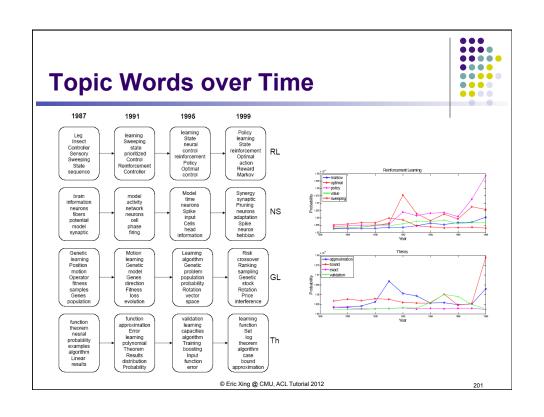
#### **Experimental Results**

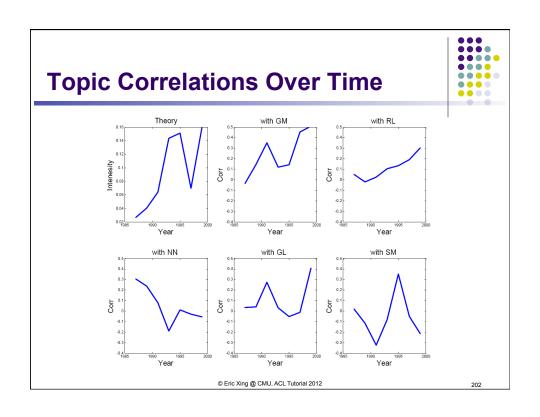


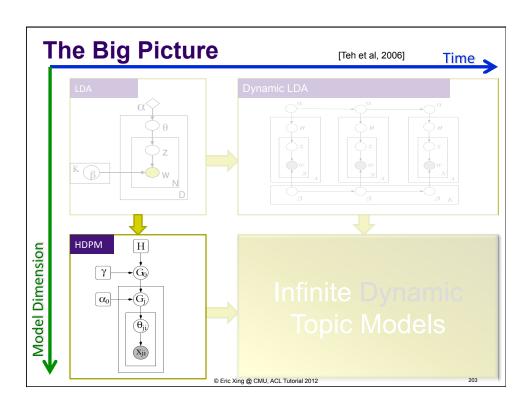
- NIPS data set
  - 12 years
  - 14036 words
  - 2484 docs
  - 90% for training and 10% for testing

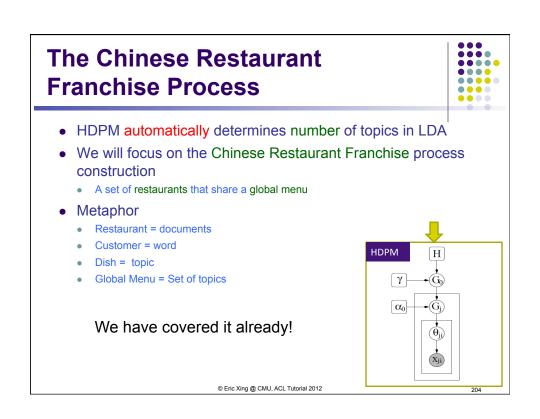
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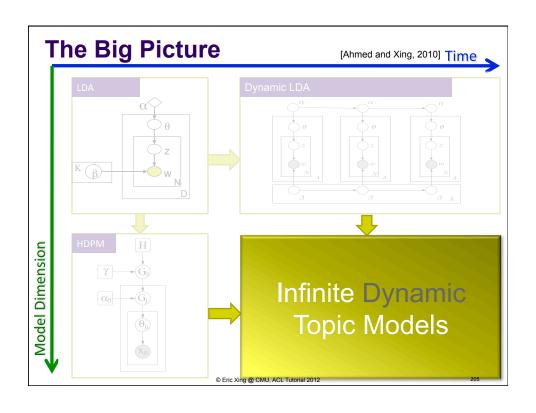


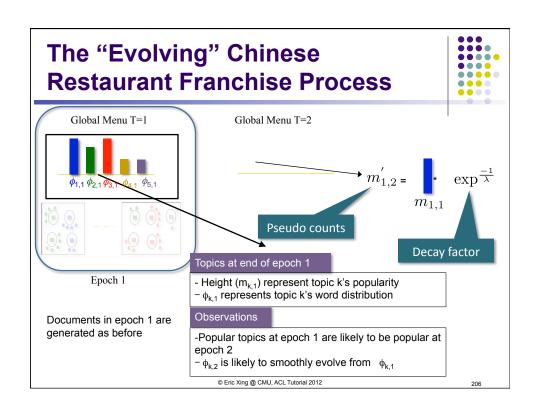


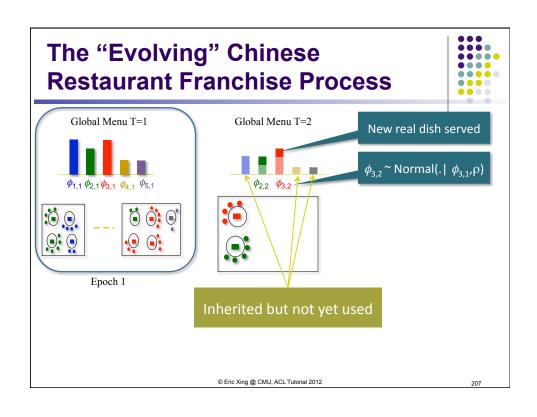


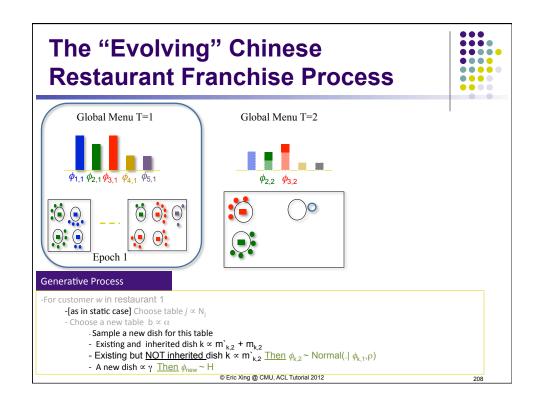


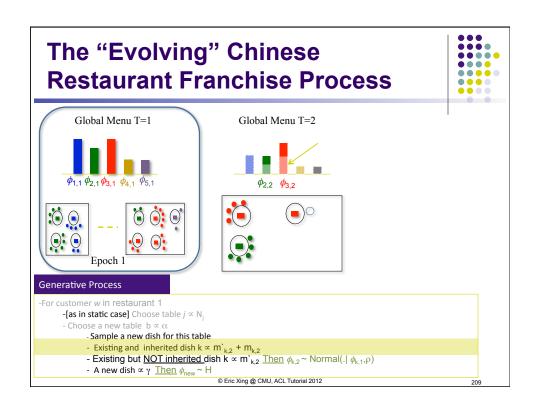


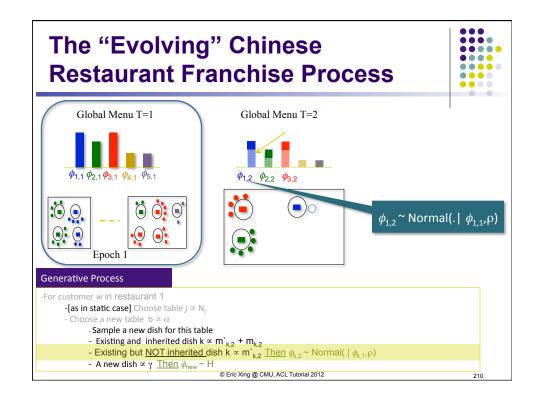


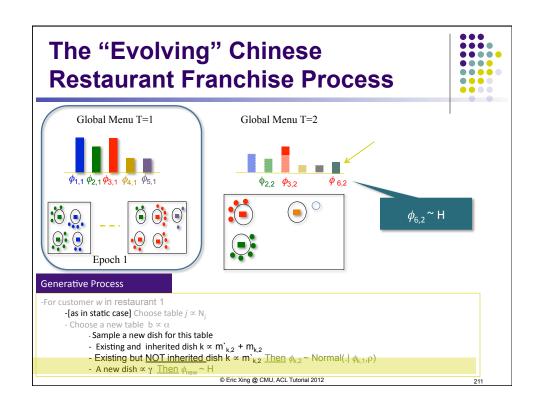


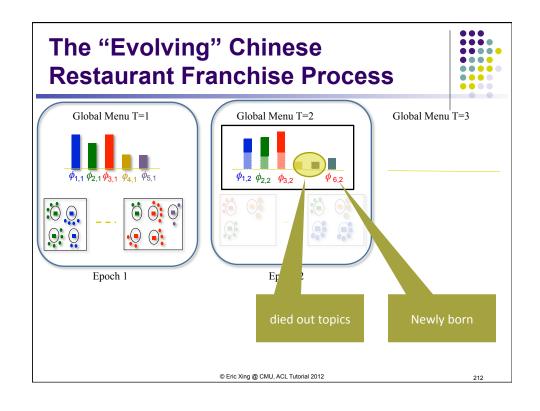


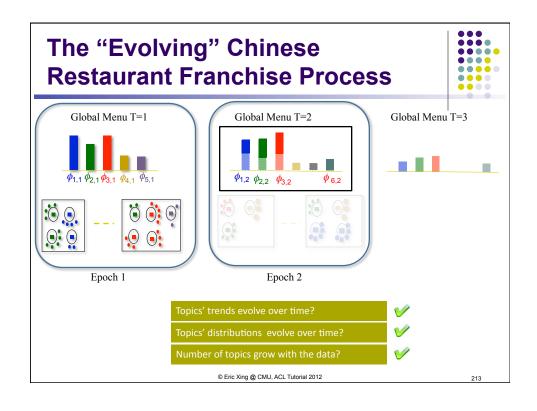


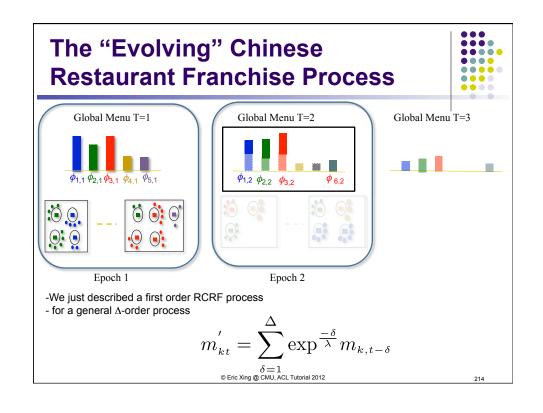










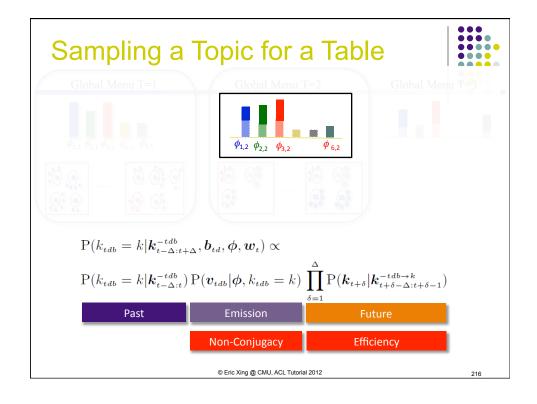


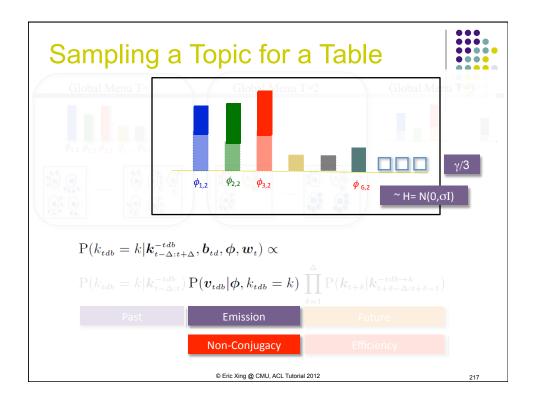
#### **Inference**

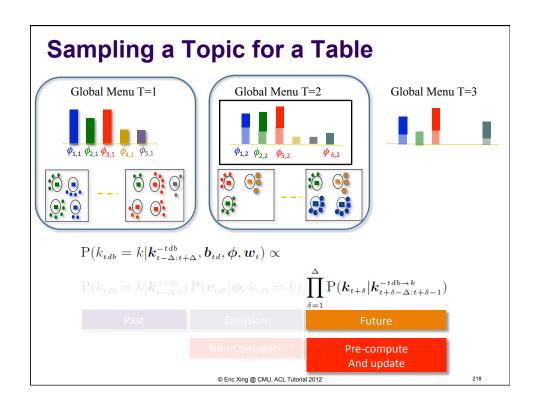


- Gibbs Sampling
  - Sample a table for each word
  - Sample a topic for each table
  - Sample the topic parameter over time
  - Sample hyper-parameters
- How to deal with non-conjugacy
  - Algorithm 8 in Neal's 1998 + Metropolis-Hasting
- Efficiency
  - The Markov blanket contains the previous and following  $\Delta$  epochs

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#### **Sampling Topic Parameters**







- V|φ ~ Mult( Logistic(φ))
- Linear-State space model with non-Gaussian emission
- Use Laplace approximation inside the Forward-Backward algorithm
- Use the resulting distribution as a proposal

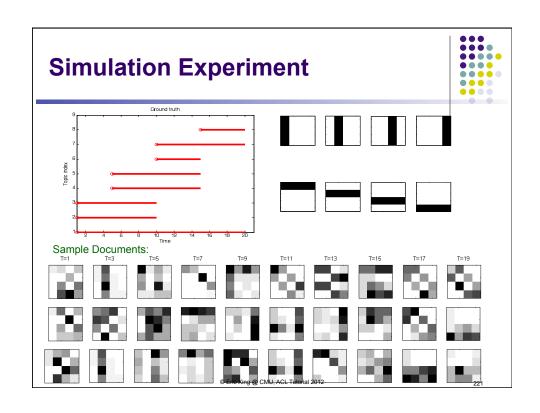
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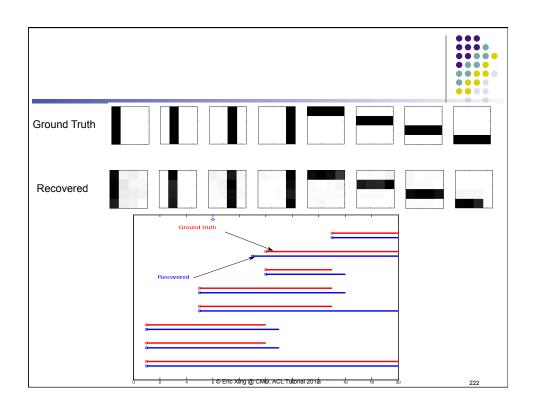
#### **Experiments**

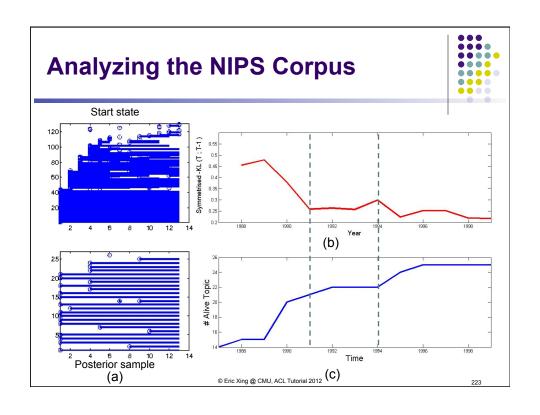


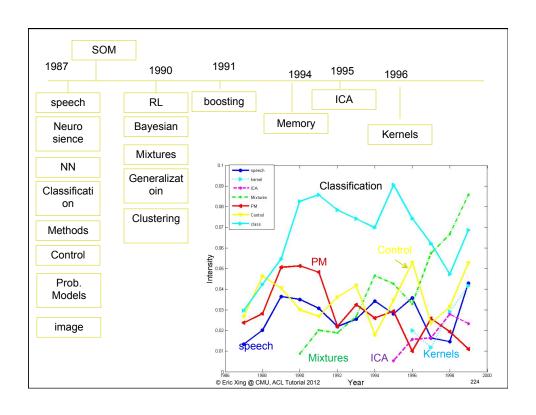
- Simulated data
  - Simulated 20 epochs with 100 data points in each epoch
- Timeline of the NIPS conference
  - 13 years
  - 1740 documents
  - 950 words per document
  - ~3500 vocabulary

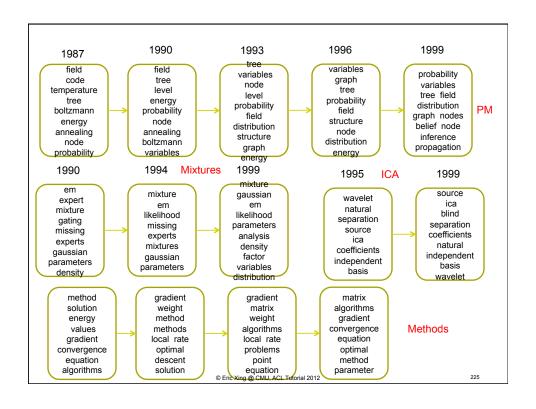
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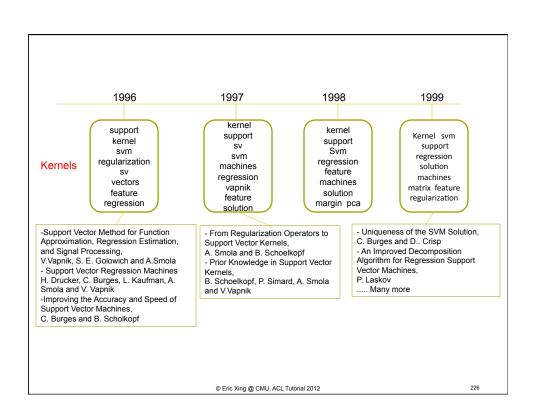


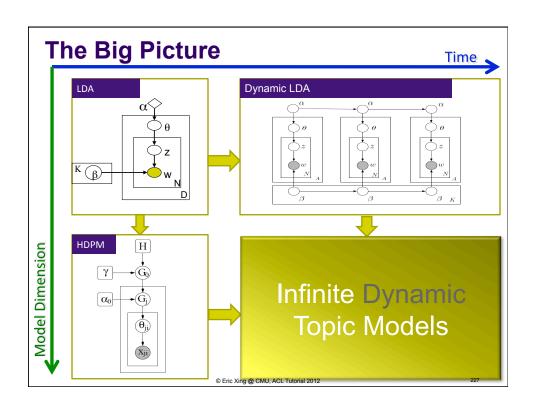


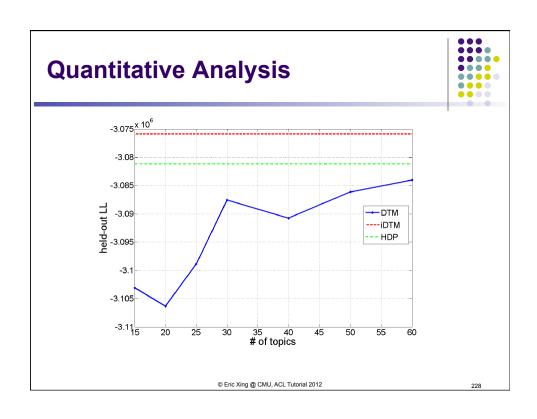


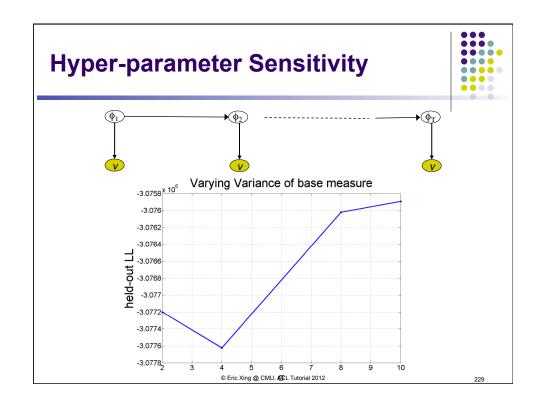


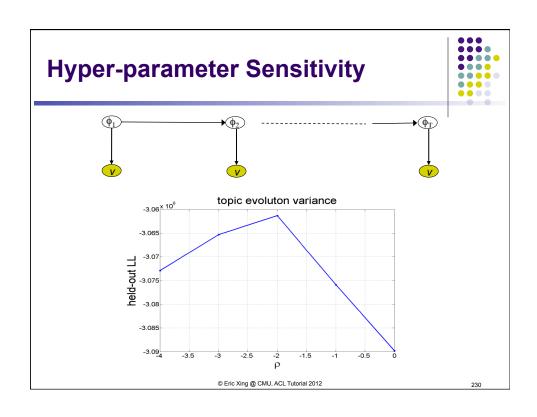


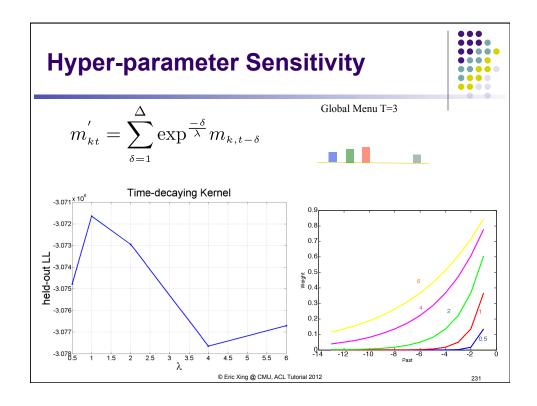


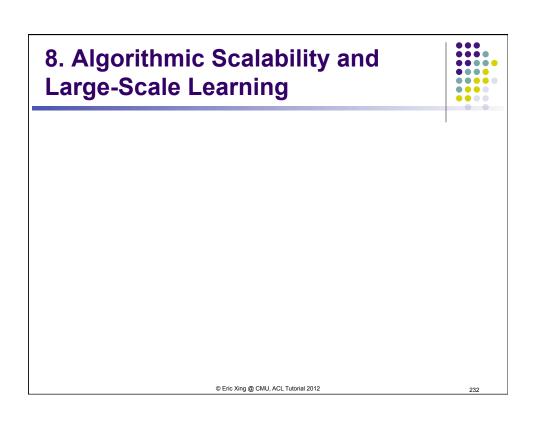












### Scaling topic models to large document collections



- Large-scale corpora have millions, even billions of documents, with vocabulary sizes in the millions
  - Runtime and memory challenges!
- Scaling to such corpora requires techniques such as:
  - 1. Efficient data representations and algorithms
  - 2. Parallelization over multiple CPUs
  - 3. Online inference, to handle incoming documents one-at-a-time

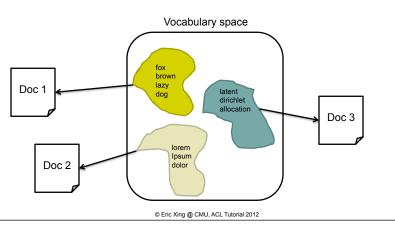
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### Efficient data representations and algorithms



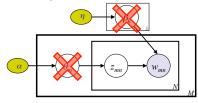
- Key observation: most documents contain just a small fraction of the words in the vocabulary
  - We say that the documents are sparse



## Efficient data representations and algorithms



- Collapsed Gibbs Sampling is a very popular inference algorithm for topic models
  - CGS samples just the word-topic indicators z, without having to sample document topic vectors  $\theta$  or topic vocabularies  $\beta$
  - · CGS requires us to track of two types of counts:
    - Topic-word: For each topic k, # of times it is assigned to vocabulary word v
      - i.e. for all documents m and words n, # of  $z_{mn}$  s.t.  $z_{mn}$  = k and  $w_{mn}$  = v
      - Represents topic vocabularies β
    - Document-topic: In each document m, # of words n assigned to topic k
      - i.e. for all words n in document m, # of  $z_{mn}$  s.t.  $z_{mn}$  = k
      - Represents document topic vectors θ



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### Efficient data representations and algorithms



- Store both word-topic and document-topic counts using a dictionary (key-value) data structure
  - Take advantage of sparsity to save memory!
  - Savings can be very large:
    - e.g. you have 500 topics but each document uses only 5 on average
    - e.g. you have 1 million vocabulary words, but each topic uses only 10,000 on average

Document-topic counts

Topic 1: 5 words Topic 6: 3 words Topic 8: 1 word Topic-word counts for topic k

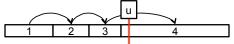
dog: 10 occurrences cat: 15 occurrences mouse: 3 occurrences

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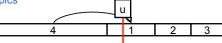
## Efficient data representations and algorithms



- · It's not just about saving memory
- We can speed up Collapsed Gibbs sampling by exploiting sparsity in word-topic and document-topic counts
  - Notice that each word-topic indicator z follows a discrete distribution over K topics
  - We sample z by drawing u ~ Uniform(0,1), and then iterating through each of the K topic choices until the cumulative probability mass exceeds u



 If we consider the topic choices with the largest probability mass first, we'll stop after fewer topics



See Yao, Mimno and McCallum (2009) for details

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### Efficient data representations and algorithms



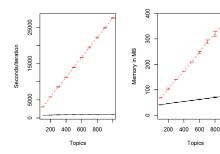


Figure 2: A comparison of time and space efficiency between standard Gibbs sampling (dashed red lines) and the SparseLDA algorithm and data structure presented in this paper (solid black lines). Error bars show the standard deviation over five runs.

Efficient Methods for Topic Model Inference on Streaming Document Collections (Yao, Mimno and McCallum 2009)

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## Efficient data representations and algorithms



- What about variational inference?
- We can apply stochastic gradient descent to speed up variational updates
  - Instead of computing the full gradient, just subsample terms from the gradient!
  - Specifically, we subsample random documents, and then keep gradient terms belonging to those documents
    - This works because the topic model log-likelihood decomposes as a sum over documents!
  - Often, we can obtain good performance with just a small fraction of the terms

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### Parallelization over multiple CPUs



- Efficient data/algorithms can only get you so far on one CPU
- The processor industry is no longer focused on single-CPU performance
  - In 5 years, new processors will not be much faster than today's processors
  - But they will have many more CPU cores for parallel programming!
  - On the other hand, text corpora are growing rapidly
    - English Wikipedia has nearly 4 million articles
    - Blogosphere generates 900 thousand posts per day in 2008, and almost certainly more today (Source: Technorati)
  - We must parallelize both now, and in the future as well

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### Parallelization over multiple CPUs



- Three common strategies for parallel inference:
  - Apply "standard" variational inference (VB) or Gibbs sampling, but distribute the documents over the CPUs
    - Advantages: easy extension to standard variational/MCMC algorithms
    - Drawbacks: convergence no longer guaranteed under some situations, like Collapsed Gibbs sampling
  - Use particle filtering (aka Sequential Monte Carlo sampling) with P particles, and split the particles over the CPUs
    - · Advantages: convergence is always guaranteed; can pick any number of particles P
    - Drawbacks: naïve sampler can lead to very poor results, thus care is needed in designing the sampler
  - Use Auxiliary variables to distribute inference
    - Advantages: Convergence guaranteed, collapsed Gibbs sampling on individual CPUs.
    - Drawbacks: Latency introduced by network if entire data cannot reside on a single machine

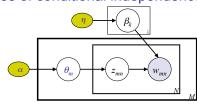
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#### **Distributing documents**



- By distributing documents over CPUs, we can:
  - Infer the word-topic indicators z and document topic vectors in  $\theta$  in parallel (conditioned on the topic vocabularies  $\beta$ )
  - Easily implemented as a map operation
- To infer the topic vocabularies β:
  - Consolidate statistics from the word-topic indicators z into one CPU
  - Have that CPU infer the β's (conditioned on z's)
  - Easily implemented as a map-reduce operation
- Works because of conditional independence in the model!

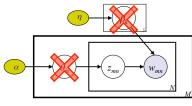


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#### **Distributing documents**



- In Collapsed Gibbs sampling however, the conditional independence assumptions break down
  - Integration of  $\theta$ ,  $\beta$  makes the z's depend on each other
  - MCMC convergence guarantees no longer hold when parallel sampling the z's
- In practice however, parallel CGS sampling does produce good results (Asuncion, Smyth and Welling 2008)
  - Though this may or may not generalize to more complex topic models



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### **Distributing documents**



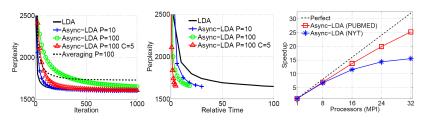


Figure 3: (a) Left: Convergence plot for Async-LDA on KOS, K=16. (b) Middle: Same plot with x-axis as relative time. (c) Right: Speedup results for NYT and PUBMED on a cluster, using Message Passing Interface.

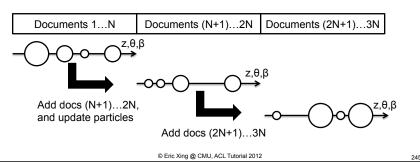
Asynchronous Distributed Learning of Topic Models (Asuncion, Smyth and Welling 2008)

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#### **Sequential Monte Carlo**



- Under SMC (particle filtering), we "evolve" the posterior distribution one set of documents at a time
  - Represent the posterior as a set of weighted samples (called "particles")
    - Within a set of documents, particles are evolved according to some proposal distribution
    - Each particle can be evolved independently in parallel
  - In the illustration below, each circle is a particle. Axis locations represent latent variable values, and sizes represent particle weights.



#### **Sequential Monte Carlo**



Table 1: Details of Yahoo! News dataset and corresponding clustering accuracies of the baseline (LSHC) and our method (Story), K=100.

Sample No.	Sample size	Num Words	Num Entities	Story Acc.	LSHC Acc.
1	111,732	19,218	12,475	0.8289	0.738
2	274,969	29,604	21,797	0.8388	0.791
3	547,057	40,576	32,637	0.8395	0.800

SMC inference performs well on real world datasets

Table 5: Number of particles, sample-1, K = 100.

#I	Particles	4	8	16	32	50
A	ccuracy	0.8101	08289	0.8299	0.8308	0.8358

Increasing the number of particles improves performance

Online Inference for the Infinite Topic-Cluster Model: Storylines from Streaming Text (Ahmed, Ho, Teo, Eisenstein, Smola, Xing 2011)

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#### **Online Inference**



- Often, we want to add new documents to the model incrementally
  - But we can't afford to rerun inference all documents, especially for huge corpora!
  - How can we insert the new documents in a statistically principled manner?
- Online inference allows us to incorporate the influence of new documents
  - Sequential Monte Carlo (already explained)
  - Online variational inference

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#### **Online Variational Inference**



- Key idea: split the set of docs into smaller "minibatches", similar to Sequential Monte Carlo
  - In each minibatch:
    - $\bullet$  Perform variational inference on word-topic indicators z and document topic vectors  $\theta,$  for all docs in the minibatch
    - $\bullet$  Perform gradient steps on the topic vocabularies  $\beta,$  using only terms corresponding to docs in the minibatch
  - The use of minibatches is equivalent to stochastic gradient updates, which are guaranteed to converge (Hoffman, Blei and Bach 2010)
- We can process docs as they arrive, one minibatch at a time

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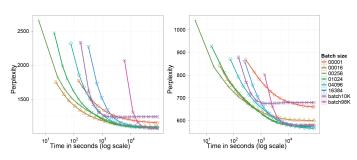


Figure 2: Held-out perplexity obtained on the *Nature* (left) and Wikipedia (right) corpora as a function of CPU time. For moderately large mini-batch sizes, online LDA finds solutions as good as those that the batch LDA finds, but with much less computation. When fit to a 10,000-document subset of the training corpus batch LDA's speed improves, but its performance suffers.

Online Learning for Latent Dirichlet Allocation (Hoffman, Blei and Bach 2009)

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#### **Auxiliary Variable Representation**



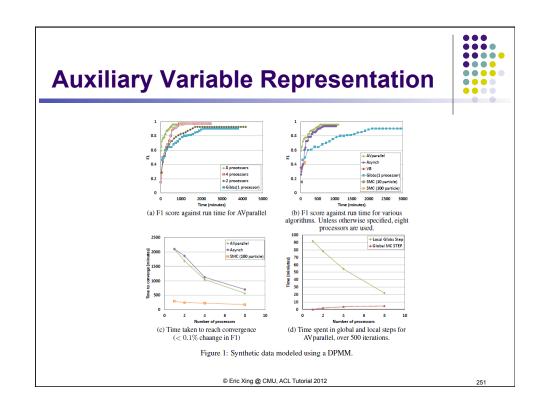
- Key Idea "Dirichlet mixtures of Dirichlet processes are Dirichlet processes"
- We can re-write the generative process of DPMM as:-

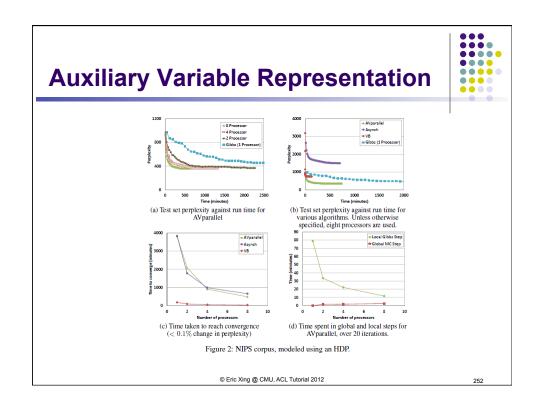
$$D_j \sim DP\left(\frac{\alpha}{P}, H\right), \quad \phi \sim Dirichlet\left(\frac{\alpha}{P}, \dots, \frac{\alpha}{P}\right), \quad \pi_i \sim \phi, \quad \theta_i \sim D_{\pi_i}, \quad x_i \sim f(\theta_i), j = 1, \dots, P \text{ and } i = 1, \dots, N.$$

 By adding additional constrain on the concentration parameter of bottom level DP we can re-write HDP as:-

$$\begin{split} \zeta_{j} \sim \operatorname{Gamma}\left(\frac{\alpha}{P}\right), \quad j = 1, \dots, P & D_{mj} \sim \operatorname{DP}(\zeta_{j}, D_{0j}), \quad m = 1, \dots, M, \quad j = 1, \dots, P \\ D_{0j} \sim \operatorname{DP}\left(\frac{\alpha}{P}\right), \quad j = 1, \dots, P & \theta_{mi} \sim \nu_{m}, \quad m = 1, \dots, M, \quad i = 1, \dots, N_{m} \\ \theta_{mi} \sim D_{m\pi_{mi}} & x_{mi} \sim f(\theta_{mi}) \end{split}$$

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# Algorithmic Scalability and Large-Scale learning



- · Data structures and algorithms matter
  - Dictionaries to exploit vocabulary/topic sparsity
  - Faster sampling by reordering topics
- · Parallelization is great, but one needs to be careful
  - Multiple parallel inference approaches, with their own pros/cons
  - Conditional independence allows us to divide documents among processors
  - Auxiliary variables can provide conditional independence in collapsed samplers
- Online inference is possible
  - For the same reasons that parallelization is possible
  - Use incoming document minibatches to update topic vocabulary distributions

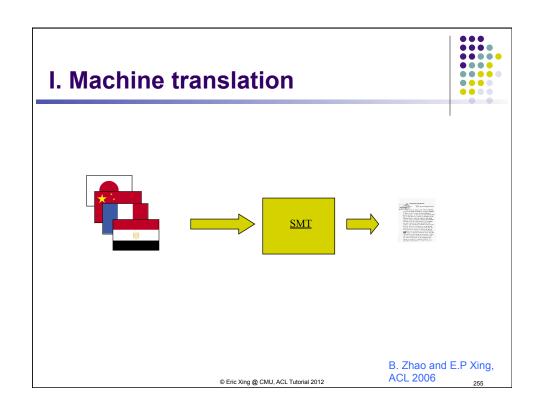
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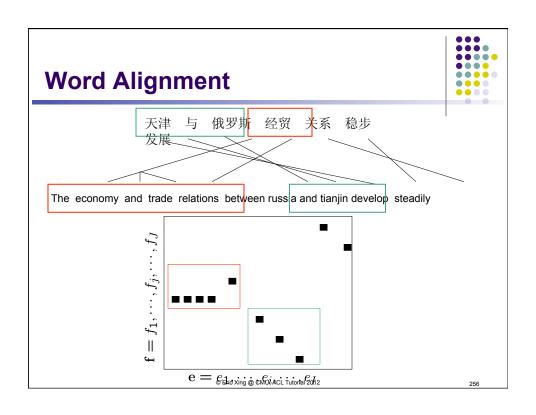
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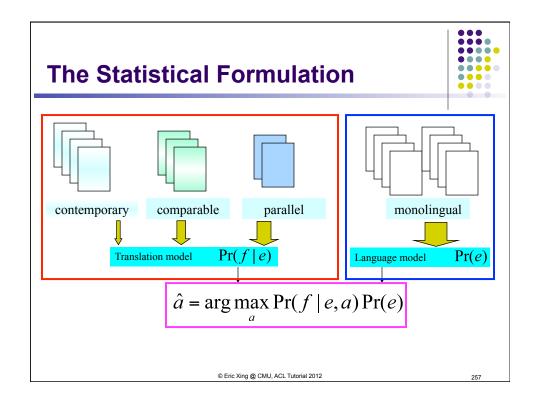
#### 9: Other apps (Optional)



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### BiTAM: From monolingual to bilingual topic models (Zhao & Xing, ACL/Coling 2006)



- Monolingual space, a unigram LM p(w|z)
  - A topic corresponding to a point in the word simplex.
    - AdMixture of unigrams (Blei, et al. 2003)
- Bilingual space, a translation lexicon p(f|e,z)
  - Given a topic z, a word usually has limited translations.
  - Topic-specific translation lexicons are sharper
  - Each topic is a point in the conditional simplex
  - AdMixture of topic-specific translation lexicons (Zhao & Xing, ACL/Coling 2006)
- Example
  - A Chinese word "club", the translations can be:



ogre	war	socialize	interests
0.4	0.5	0.0	0.1
0.0	0.1	0.5	0.4



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#### **BiTAM: A Generative Process**



- Sample topic weights  $\theta$  from a Dirichlet( $\alpha$ )
- Sample a topic z from multinomial ( $\theta$ )
- For each word f in the sentence  $\vec{f}$ 
  - Sample an alignment an alignment model
  - ullet Generate f with word  $e_a^{-}$ m a topic-specific lexicon

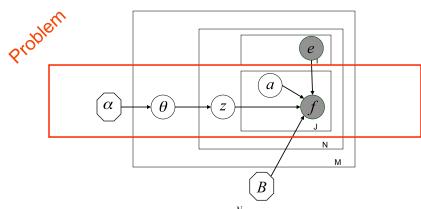
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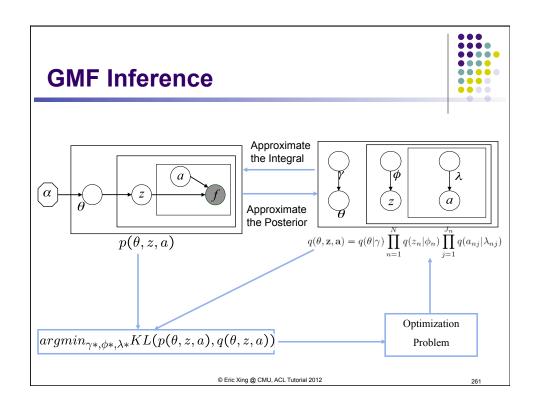
#### **BiTAM Model-1**

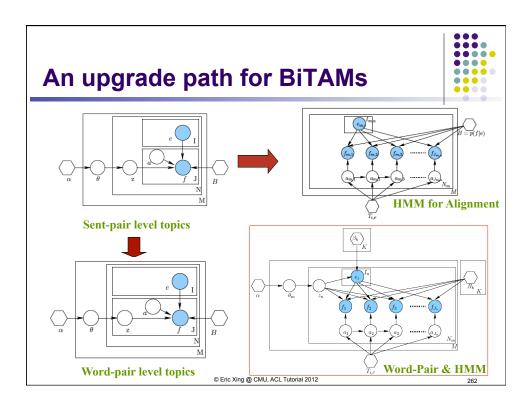


• Graphical Model (a language to encode dependencies)



$$p(F \mid A, E, \alpha, B) = \int_{\theta} p(\theta \mid \alpha) \prod_{\text{@ Eric Xing @ CMU}}^{N} \sum_{\vec{p} \in L \text{ Triffinal 2012}} p(z_n \mid \theta) p(f_n \mid a_n, e_n, B_{z_n}) d\theta$$





#### **Experiments**



- Training data
  - Small: Treebank 316 doc-pairs (133K English words)
  - Large: FBIS-Beijing, Sinorama, XinHuaNews, (15M English words).

Train	#Doc.	#Sent.	#Tokens		
114111		#Sent.	English	Chinese	
Treebank	316	4172	133K	105K	
FBIS.BJ	6,111	105K	4.18M	3.54M	
Sinorama	2,373	103K	3.81M	3.60M	
XinHua	19,140	115K	3.85M	3.93M	
FOUO	15,478	368K	13.14M	11.93M	
Test	95	627	25,500	19,726	

- Word Alignment Accuracy & Translation Quality
  - F-measure
  - BLEU

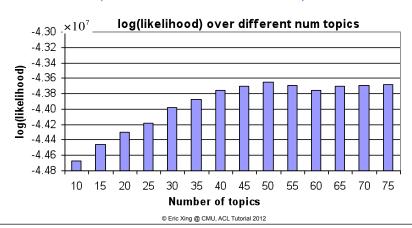
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#### **Model Selection**



- Choosing num-topics K
  - 10-fold cross-validation
  - Number of topics is set to be 50 for 23 million words corpus



### **Topics**



T1	Teams, sports, disabled, games members, people, cause, water, national, handicapped
T2	Shenzhen, singapore, hongkong, stock, national, investment, yuan, options, million, dollar
Т3	Chongqing, company, takeover, shenzhen, tianjin, city, national, government, project, companies
T4	Hongkong, trade, export, import, foreign, tech., high, 1998, year, technology
T5	House, construction, government, employee, living, provinces, macau, anhui, yuan
Т6	Gas, company, energy, usa, russia, france, chongqing, resource, china, economy, oil

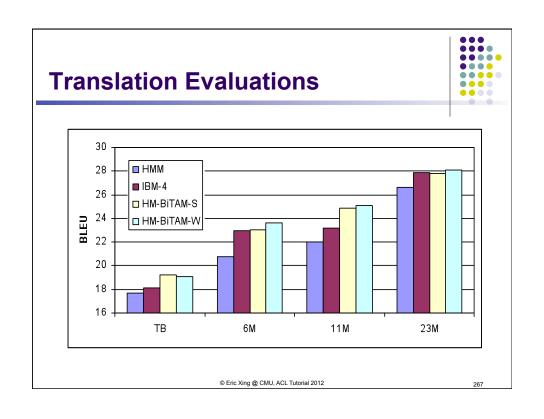
T1	人, 残疾, 体育, 事业, 水, 世界, 区, 新华社, 队员, 记者
T2	深圳,深,新,元,有,股,香港,国有, 外资,新华社
Т3	国家, 重庆, 市, 区, 厂 , 天津, 政府, 项目, 国, 深圳
T4	香港, 贸易, 出口, 外资, 合作, 今年, 项目, 利用, 新, 技术
T5	住房,房,九江,建设,澳门,元,职 工,目前,国家,占,省
T6	公司, 天然气, 两, 国, 美国, 记者, 关系, 俄, 法, 重庆

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#### **HM-BiTAM** versus others 70 ■ HMM **■** IBM-4 65 □ HM-BiTAM ■ HM-BiTAM-W 60 F-Measure 55 50 45 40 ТВ 23M 6M 11M

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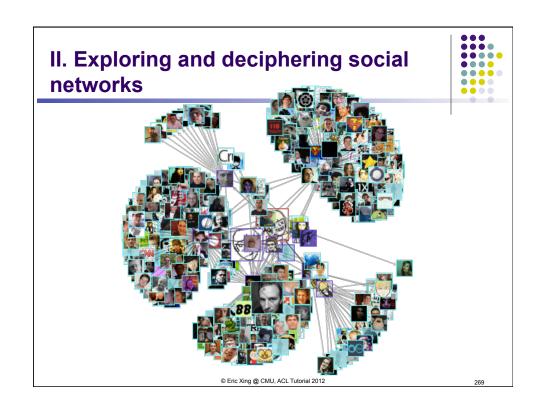


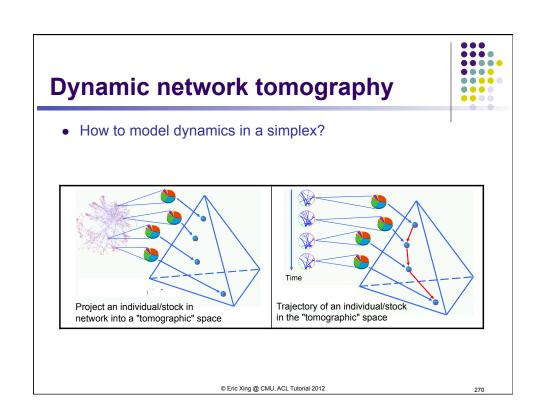
#### **Translation Evaluations**

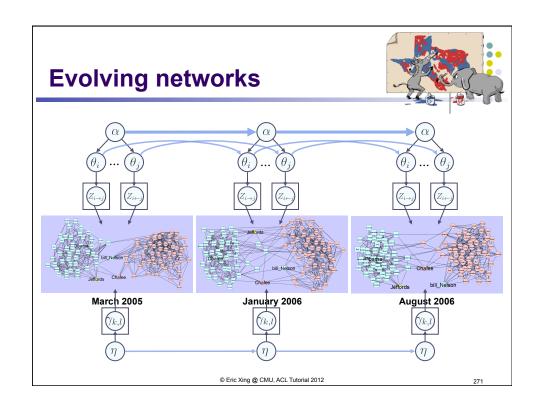


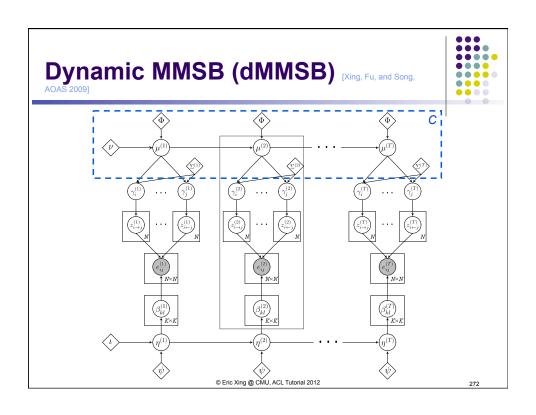
Systems	1-gram	2-gram	3-gram	4-gram	BLEUr4
Hiero Sys.	73.92	40.57	23.21	13.84	30.70
Gale Sys.	75.63	42.71	25.00	14.30	32.78
HM-BiTAM	76.77	42.99	25.42	14.04	33.19
Ground Truth	76.10	43.85	26.70	15.73	34.17

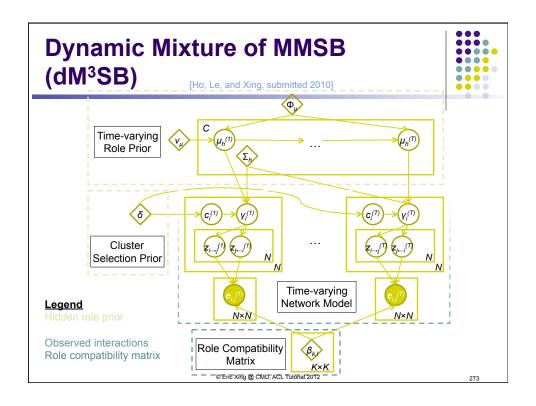
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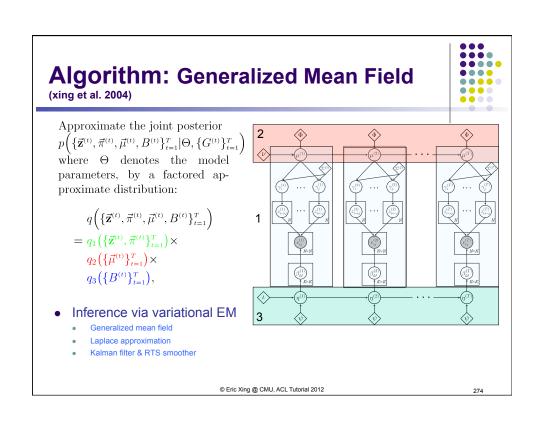


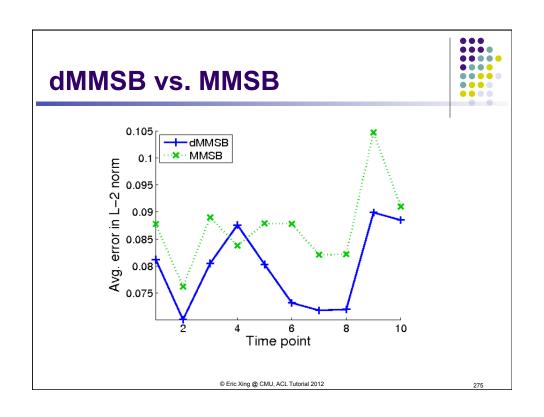


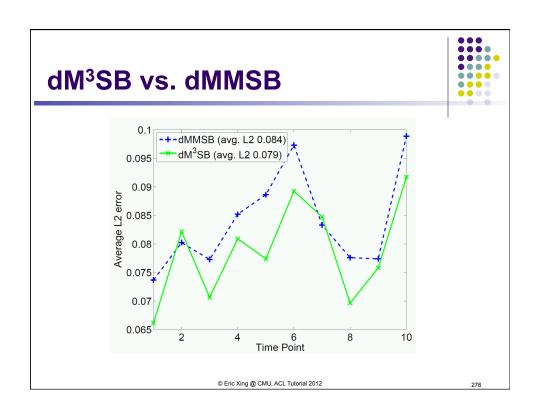


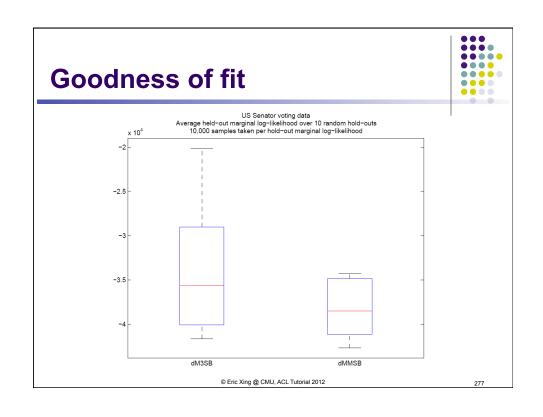


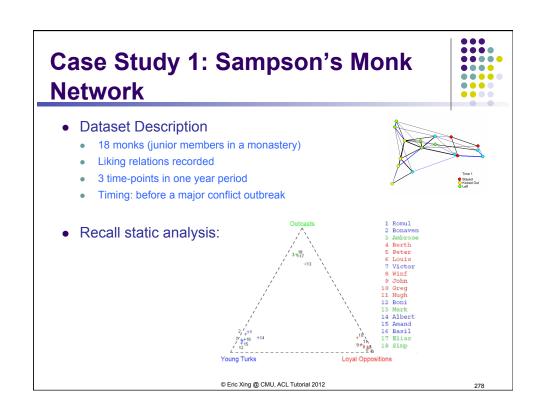








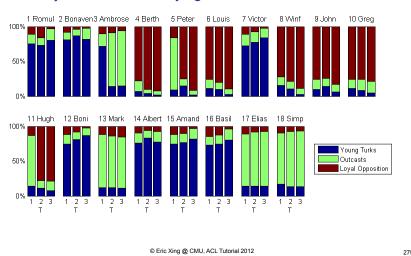


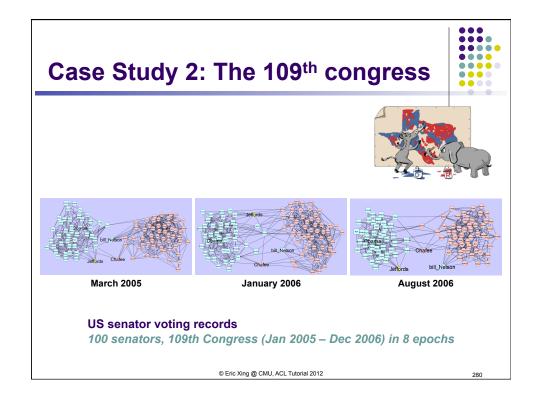


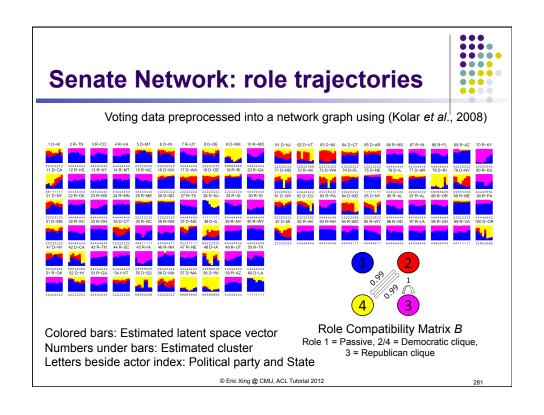
### Sampson's Monk Network: role trajectories

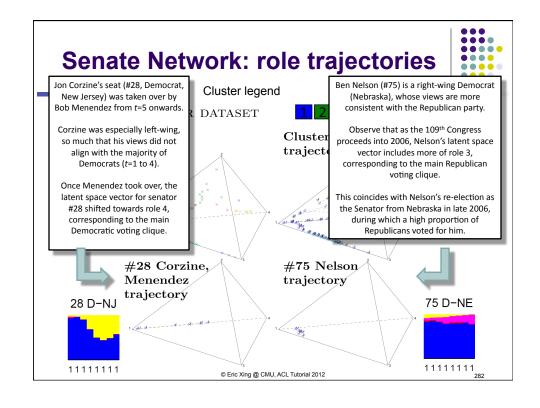


• The trajectories of the varying role-vectors over time









#### **Summary of this tutorial**



- 1. Overview of basic topic models
- 2. Computational challenges and two classical algorithmic paths
- □ 3. Scenario I: Multimodal data
- 4. Scenario II: When supervision is available
- 5. Scenario III: What if I don't know the total number of topics
- □ 6. Scenario IV: Topic evolution in streaming corpus.
- □ 7: Advanced subject I: Sparsity in topic modeling (see EMNLP talk)
- 8: Advanced subject II: Scalability, complexity, and fast algorithms (optional)
- 9: Other applications (optional)

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#### Conclusion



- GM-based topic models are cool
  - Flexible
  - Modular
  - Interactive
- · There are many ways of implementing topic models
  - unsupervised
  - supervised
- Efficient Inference/learning algorithms
  - GMF, with Laplace approx. for non-conjugate dist.
  - MCMC
- Many applications
  - .
  - Word-sense disambiguation
  - Image understanding
  - Network inference

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#### More research questions we ask:



- Event detection/prediction
  - Emergence/disappearance/evolution of perspective, bias, object, theme, etc.
  - Is there going to be a war? When? Can we predict the economy or stock from traditional or internet news?
- Automated summary
  - Describe a scene or arbitrary image
  - From keyword or class-label to story
- Semantic-based browsing and search
  - Ranking/matching based on topic/perspective
  - Video retrieval based on story
- Theoretical properties
  - Does TM have an invariant, unique solution, under what condition it is attainable?
  - How fast we converge to such solution? What requirement data must satisfy?
- Scalable computing
  - Easy, converging, fault tolerant, distributed, and online topical inference/learning
  - Doing all these with Facebook or Twitter or Flickr

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