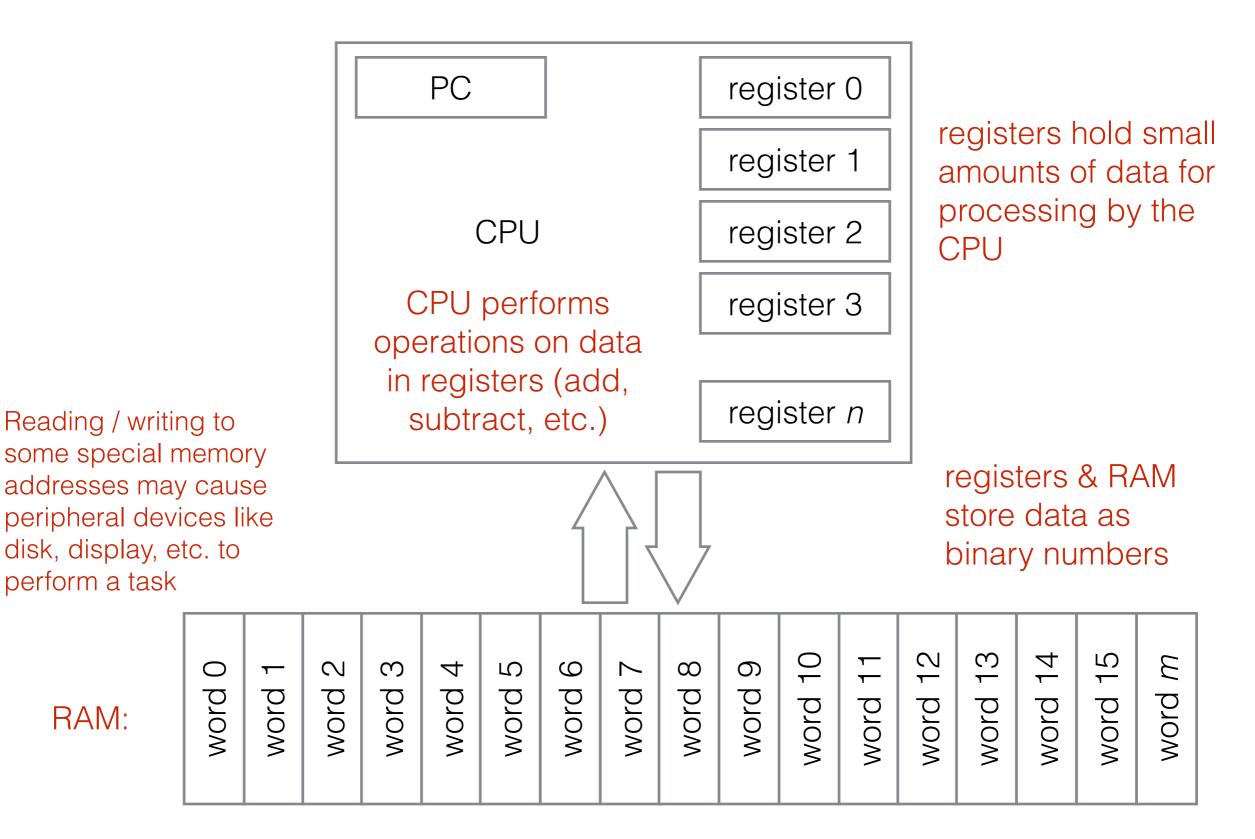
## **Computer Architecture**

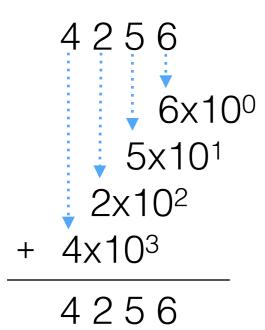
02-201 / 02-601

## The Conceptual Architecture of a Computer



# **Binary Representation**

#### Base 10 (decimal) notation:

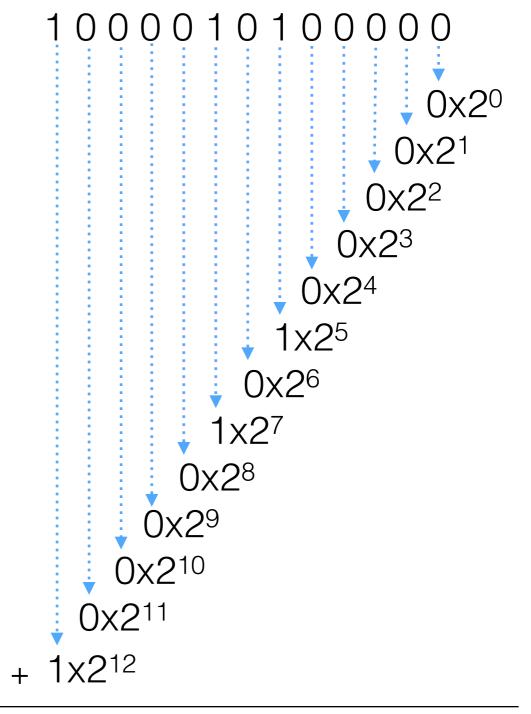


Computers store the numbers in binary because it has transistors that can encode 0 and 1 efficient

Each 0 and 1 is a *bit.* 

Built-in number types each have a maximum number of bits.

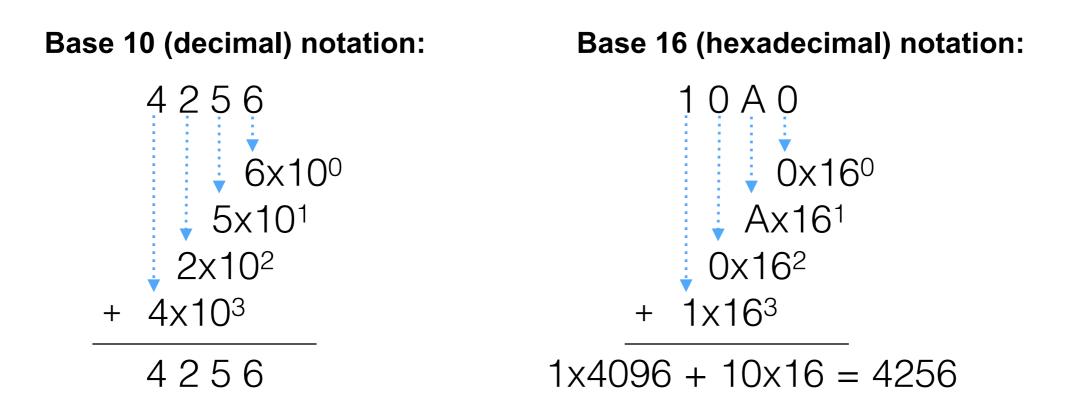
#### **Base 2 (binary) notation:**



4256 = 100001010000

## **Hexadecimal Representation**

Decimal isn't good for computers because they work with bits. But writing everything in binary would be tedious. Hence, we often use base 16, aka "hexadecimal":



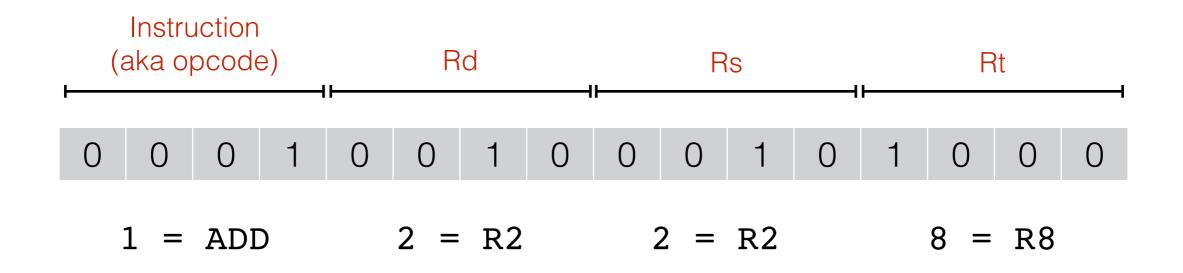
Need 16 different digits, so use 0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F A=10, B=11, C=12, D=13, E=14, F=15

## Add CPU instruction

ADD Rd, Rs, Rt

Set register Rd to Rs + Rt

An instruction is encoded as a sequence of bits:

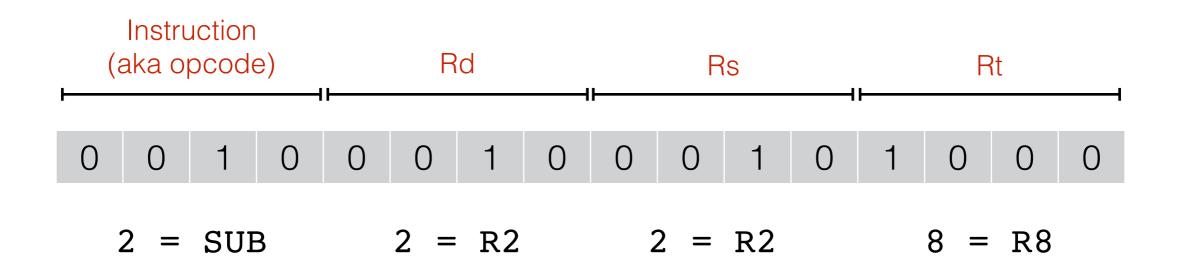


Written as a hexadecimal number: 1228<sub>16</sub>

## **Subtract CPU instruction**

SUB Rd, Rs, Rt Set register Rd to Rs - Rt

The SUB instruction is the same format as ADD, but with a different opcode:



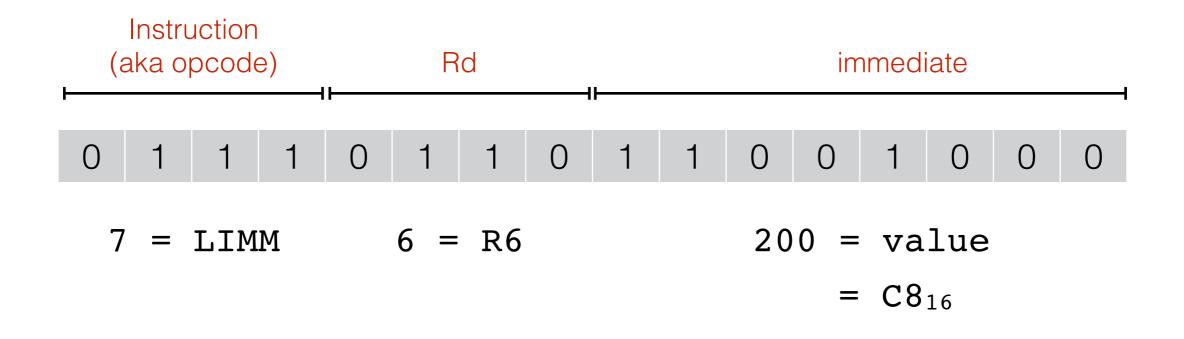
Written as a hexadecimal number: 2228<sub>16</sub>

## Load "Immediate" Instruction

LIMM Rd, value

Set register Rd to value

For LIMM, the last 8 bits give the value to copy into Rd:

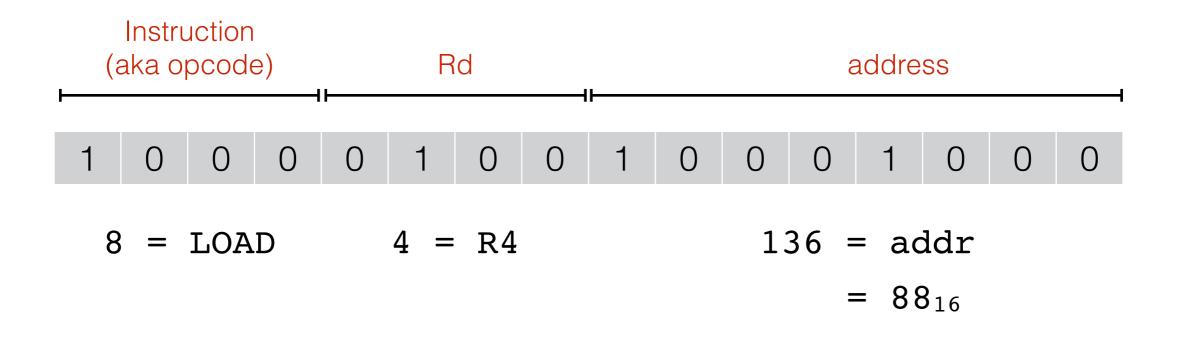


Written as a hexadecimal number: 76C8<sub>16</sub>

## **Load Instruction**

LOAD Rd, addr Set register Rd to ram[addr]

For LOAD, the last 8 bits give the address of the memory cell to copy into Rd:

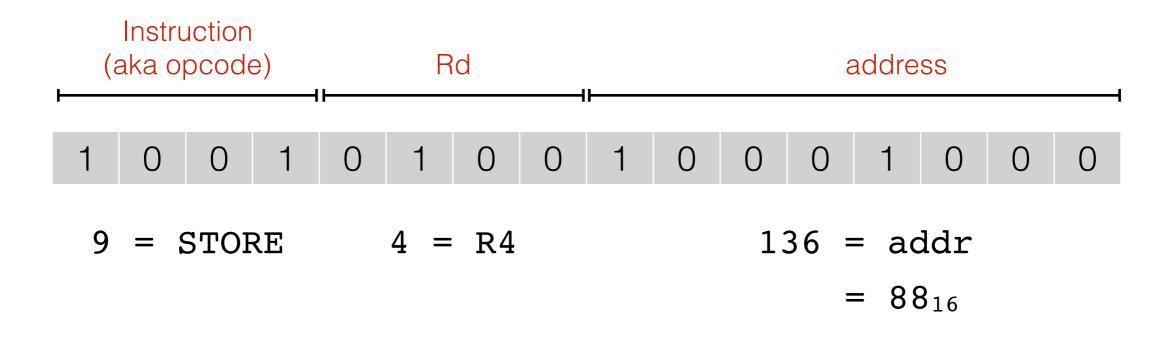


Written as a hexadecimal number: 8488<sub>16</sub>

## **Store Instruction**

STORE Rd, addr Set register ram[addr] to Rd

For LOAD, the last 8 bits give the address of the memory cell to copy into Rd:



Written as a hexadecimal number: 9488<sub>16</sub>

#### An Example Program

LIMM R1, 64 // R1 = 200 LIMM R2, 1E // R2 = 30 ADD R2, R1, R2 // R2 = R1 + R2 STORE R2, 46 // ram[70] = R2

What does this program do?

### An Example Program

LIMM R1, 64 // R1 = 200 LIMM R2, 1E // R2 = 30 ADD R2, R1, R2 // R2 = R1 + R2 STORE R2, 46 // ram[70] = R2

What does this program do? Stores 200 + 30 into memory location 70

#### Similar to the following Go program:

var r1 int = 200
var r2 int = 30
r2 = r1 + r2
var ram70 int = r2

Go manages the registers and memory locations for you.

It may keep a variable in a register, memory, or both.

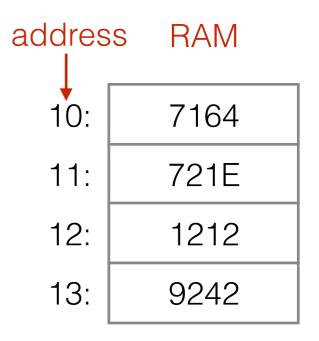
The program is just a sequence of integers that encode for instructions.

LIMM R1, 64	// R1 = 200	; 7164
LIMM R2, 1E	// R2 = 30	; 721E
ADD R2, R1, R2	// R2 = R1 + R2	; 1212
STORE R2, 46	// ram[70] = R2	; 9246

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These integers are stored in the same RAM used for variables:

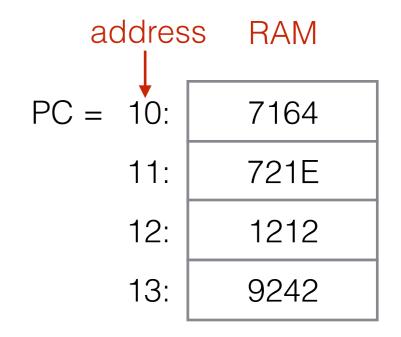


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These integers are stored in the same RAM used for variables:

The CPU has a special register called PC ("program counter") that contains the address of the current instruction.

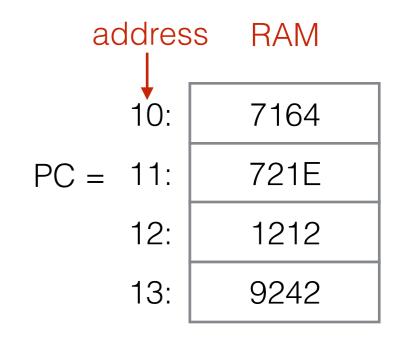


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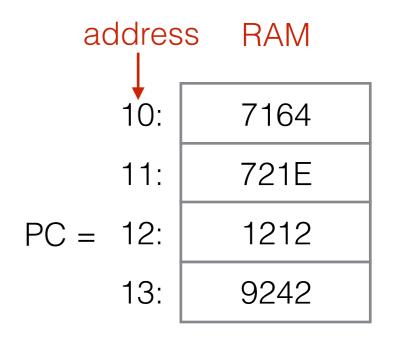


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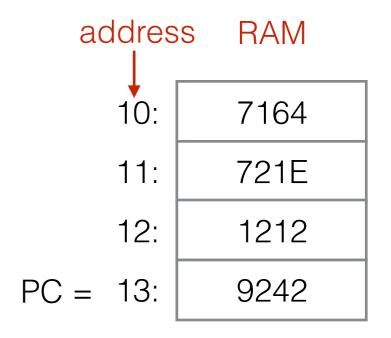


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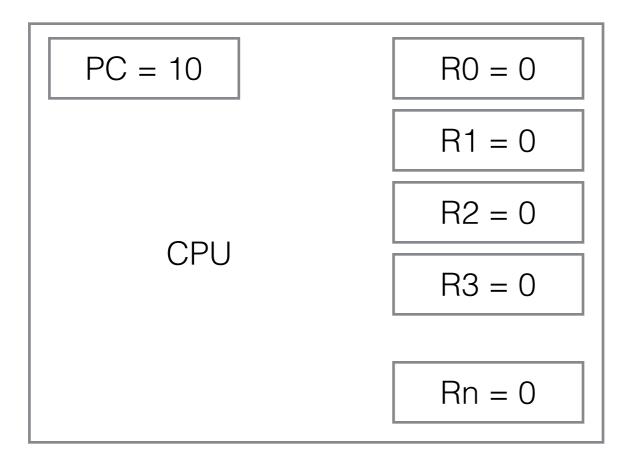
LIMM R1, 64	// R1 = 200	; 7164
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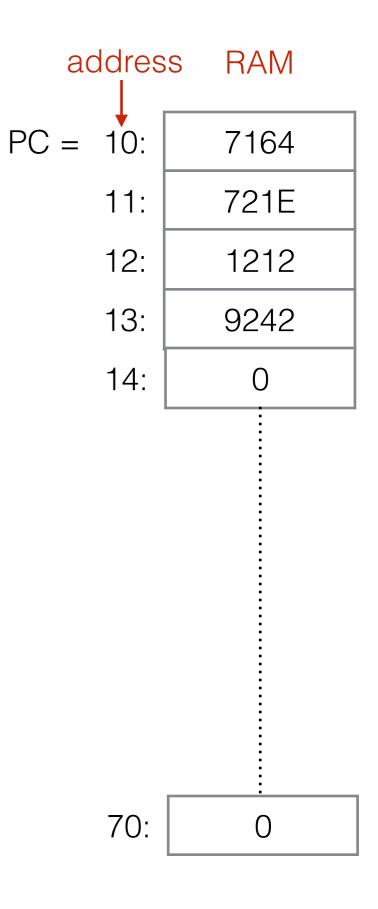
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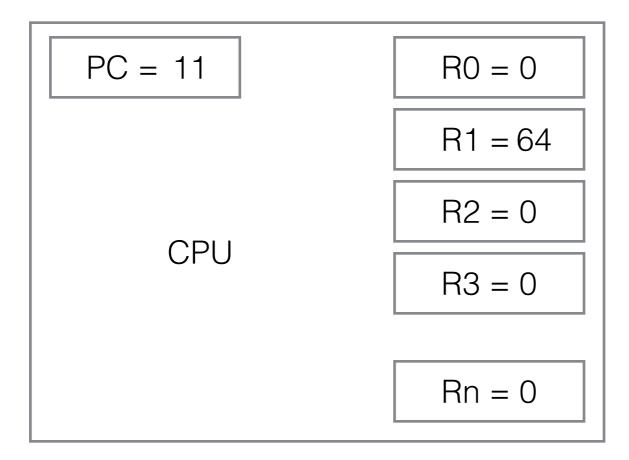


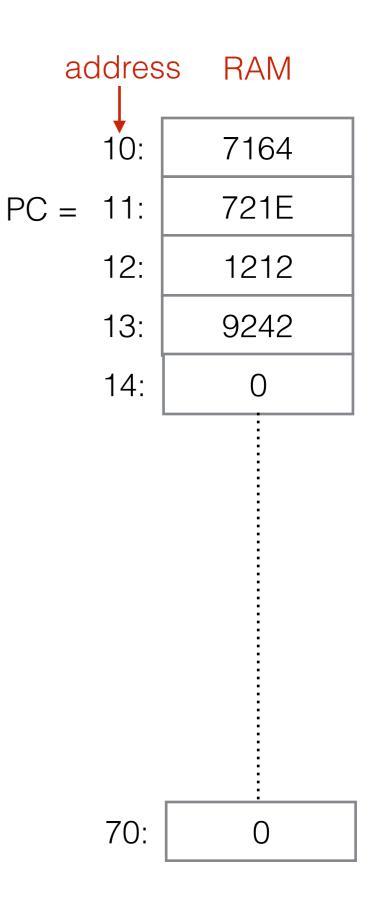
LIMM R1, 64	// R1 = 100	; 7164
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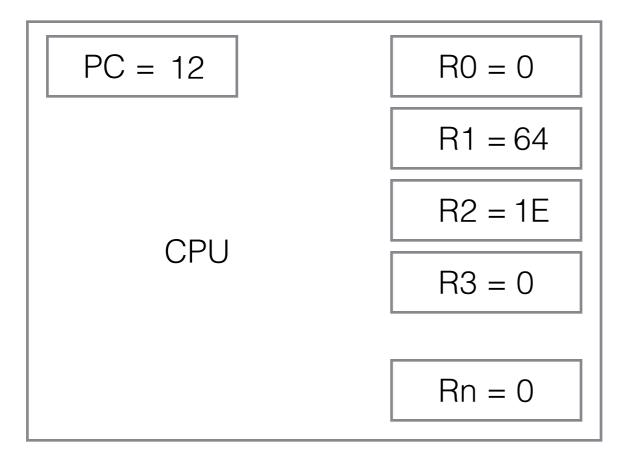


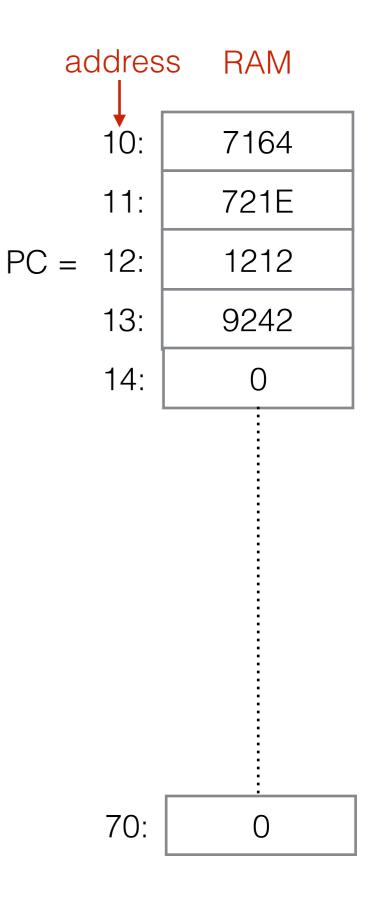
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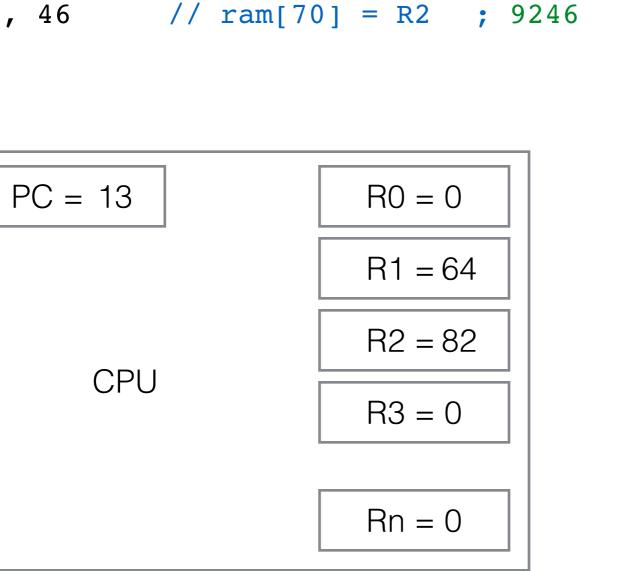


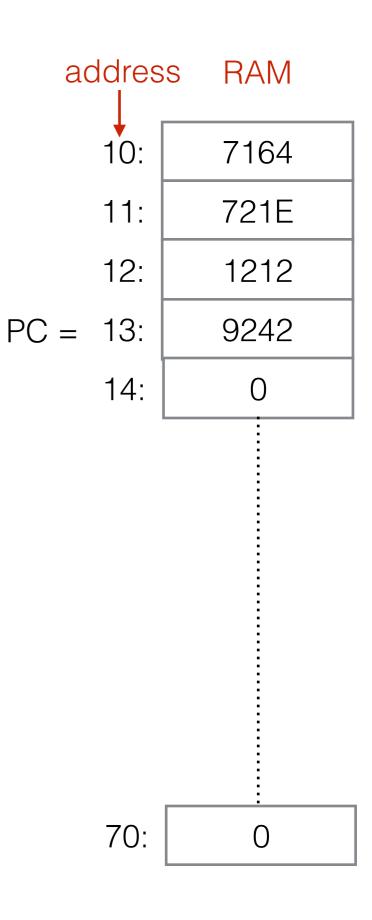
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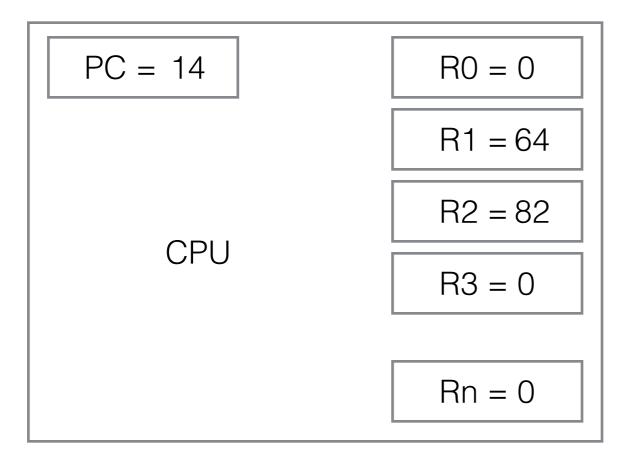


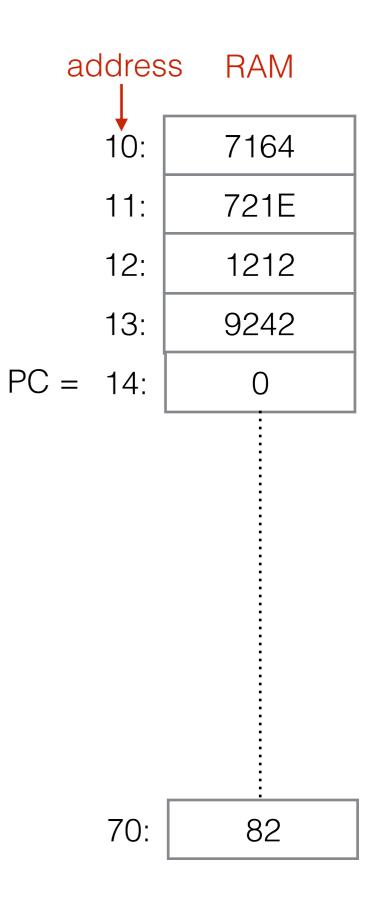
LIMM R1, 64	// R1 = 100	; 7164
LIMM R2, 1E	// R2 = 30	; 721E
ADD R2, R1, R2	// R2 = R1 + R2	; 1212
STORE R2, 46	// ram[70] = R2	; 9246





LIMM R1, 64	// R1 = 100	; 7164
LIMM R2, 1E	// R2 = 30	; 721E
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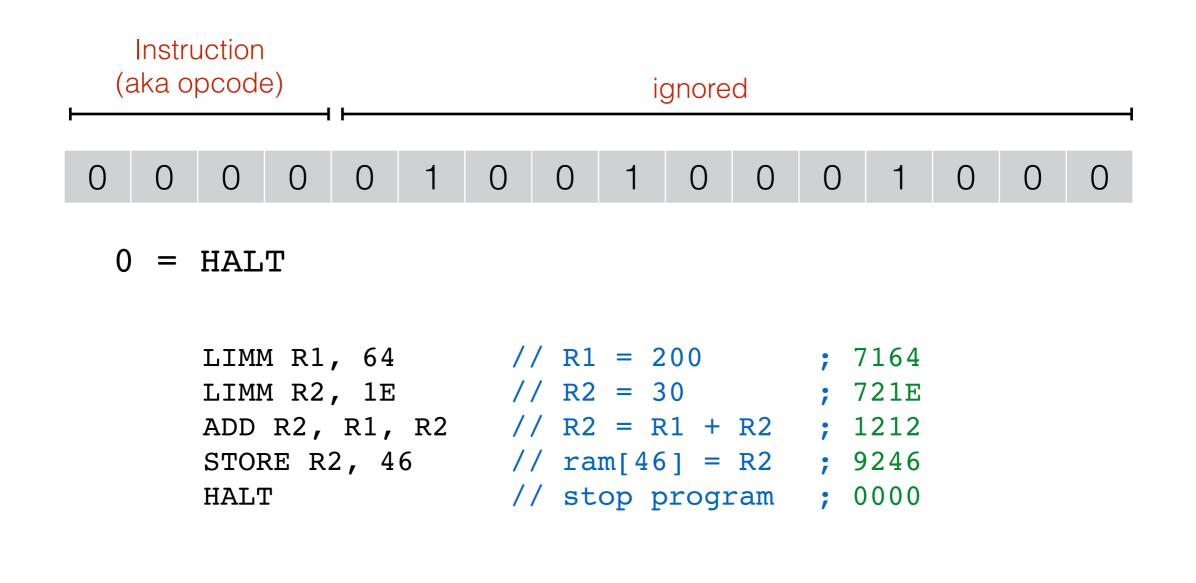




## Ending the program

The computer will keep grabbing an integer, interpreting it as an instruction, and then incrementing PC indefinitely.

To stop this process, you have to add a HALT instruction:



## Input, Output, and 0

Register 0 always has value 0

Stores to memory location FF writes the value to the output

Reads from memory location FF read a value from the input

STORE R3, FF	Write the value R3 to the output
LOAD R4, FF	Read the next input value into R3

#### **Example:**

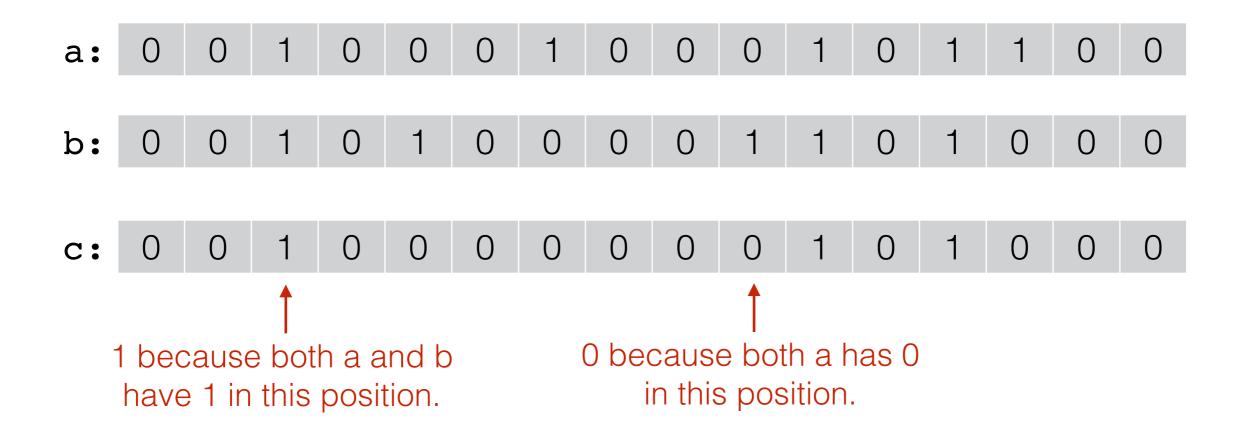
LIMM R1, 64	// R1 = 200	; 7164
LOAD R2, FF	// R2 = input	; 72FF
ADD R2, R1, R2	// R2 = R1 + R2	; 1212
STORE R2, FF	// write R2 to output	; 92FF
HALT	// stop program	; 0000

## **Other Arithmetic Operations: AND**

AND Rd, Rs, Rt

Set register Rd to Rs AND Rt

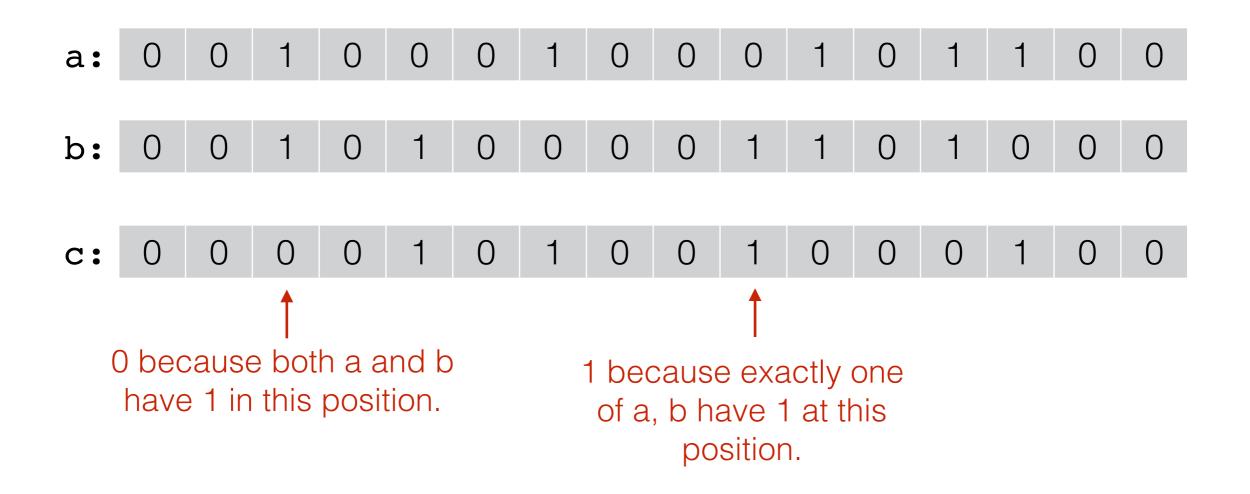
AND takes two binary numbers a and b and creates a binary c number where the ith bit of c is 1 if and only if the ith bits of both a and b are 1:



## **Exclusive Or: XOR**

XOR Rd, Rs, Rt Set register Rd to Rs XOR Rt

XOR takes two binary numbers a and b and creates a binary c number where the ith bit of c is 1 if either a or b but not both have 1 in their ith bit:



## AND and XOR in Go

#### Go has bitwise operators:

- & = AND ^ = XOR
- var r1 int = 200
  var r2 int = 30
  r2 = r1 & r2
  var r3 int
  r3 = r2 ^ r1

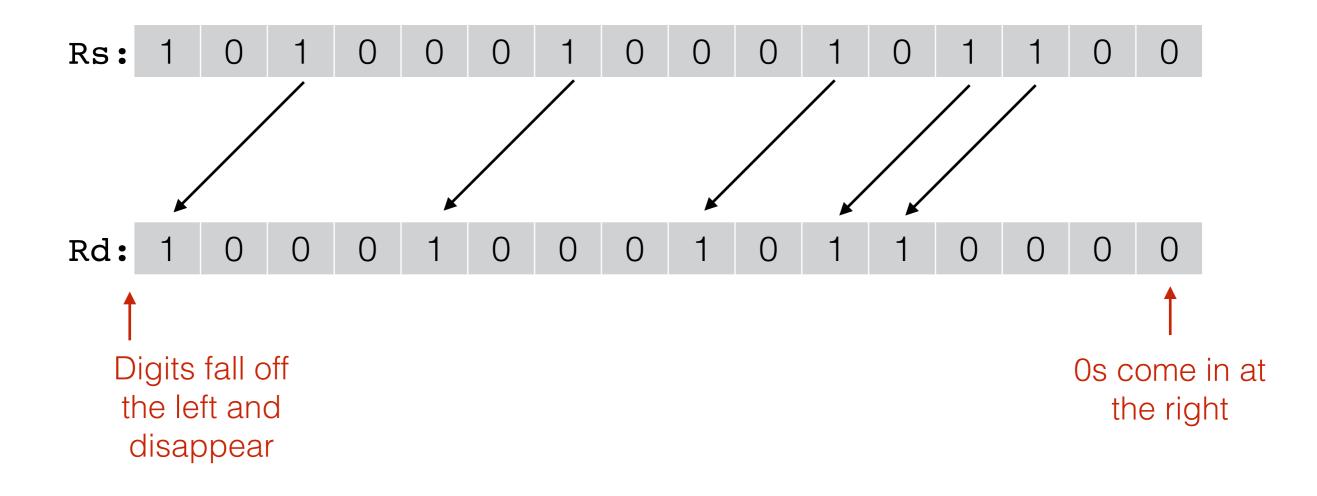
- r1 = 000000011001000
- r2 = 00000000011110
- r2 = 000000000001000

r3 = 000000011000000

# Left and Right Shift

LSHIFT Rd, Rs, Rt

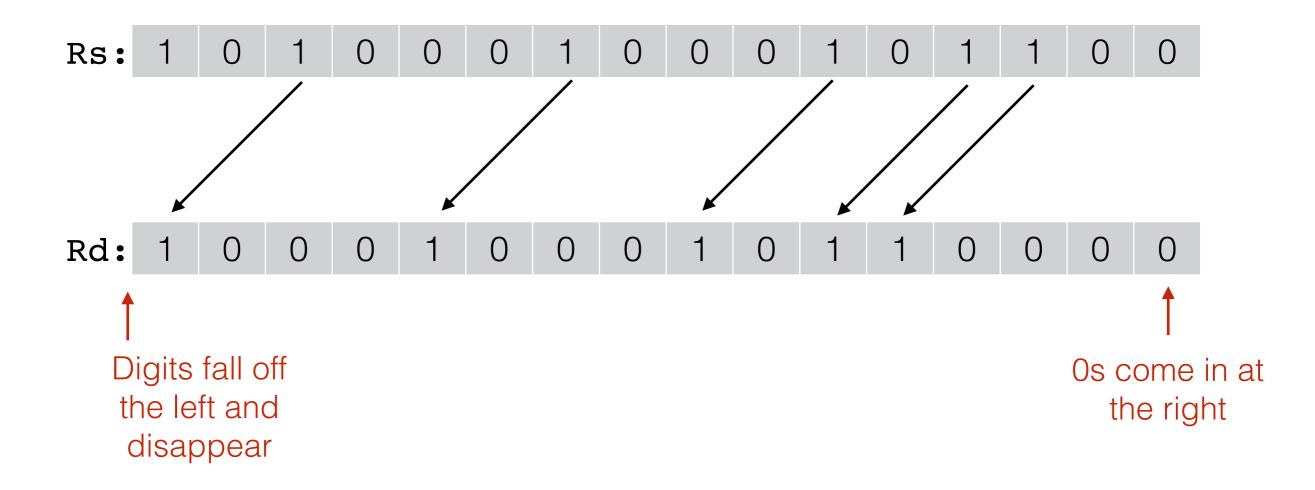
Set register Rd to Rs shifted to the left by Rt digits



# Left and Right Shift

LSHIFT Rd, Rs, Rt

Set register Rd to Rs shifted to the left by Rt digits



RSHIFT is the same except it shifts to the right:

RSHIFT Rd, Rs, Rt

Set register Rd to Rs shifted to the **right** by Rt digits

## AND, XOR, LSHIFT, RSHIFT

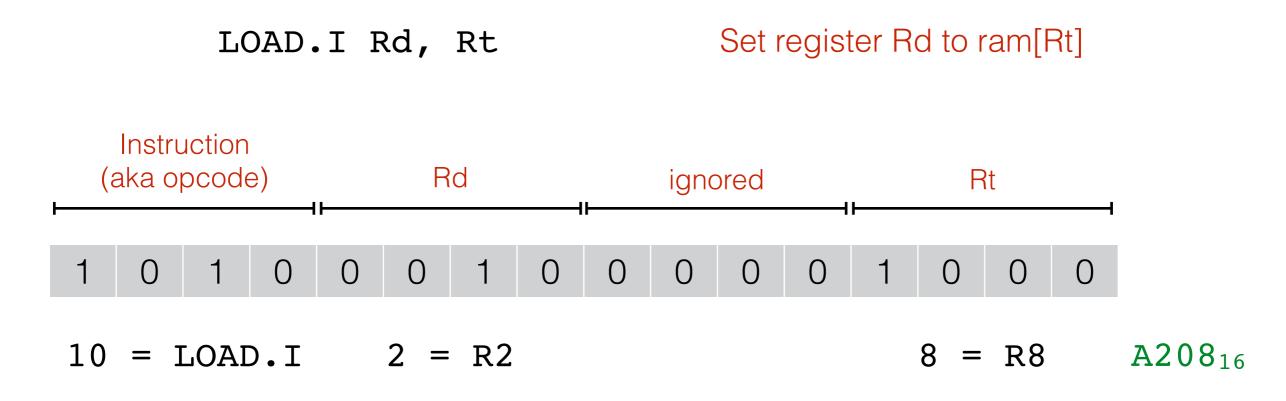
AND Rd, Rs, Rt XOR Rd, Rs, Rt LSHIFT Rd, Rs, Rt RSHIFT Rd, Rs, Rt Set register Rd to Rs AND Rt Set register Rd to Rs XOR Rt Set register Rd to Rs << Rt Set register Rd to Rs >> Rt

#### The instruction format similar to ADD, SUB:

Instruction (aka opcode)	Rd	Rs	Rt	4
0 0 1 1	0 0 1 0	0 0 1 0	1 0 0 0	
3 = AND	2 = R2	2 = R2	8 = R8	$3228_{16}$
4 = XOR	2 = R2	2 = R2	8 = R8	$4228_{16}$
5 = LSHIR		2 = R2	8 = R8	5228 <sub>16</sub>
6 = RSHIR		2 = R2	8 = R8	6228 <sub>16</sub>

## Load Indirect

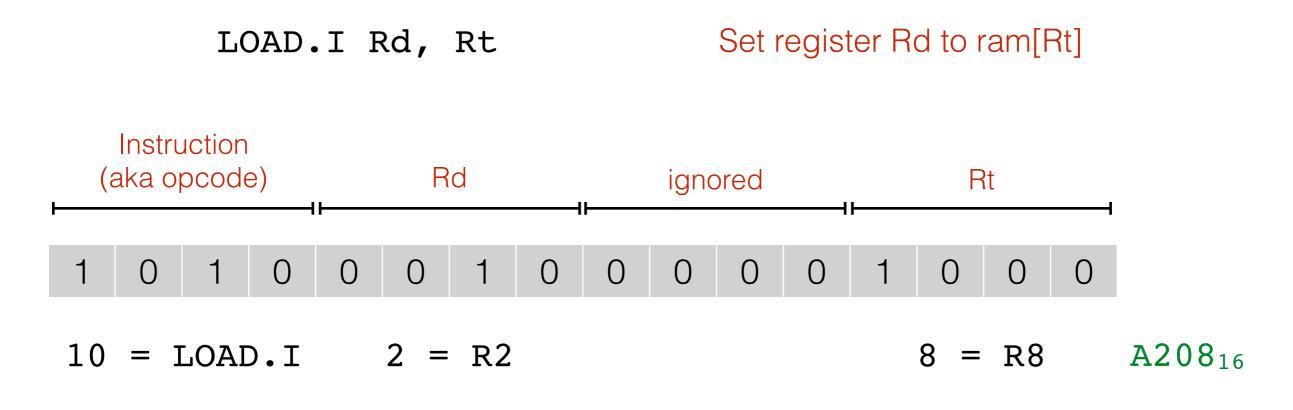
Use the value in a register as an address into RAM to read from:



What's the analog in Go of this operation?

## Load Indirect

Use the value in a register as an address into RAM to read from:

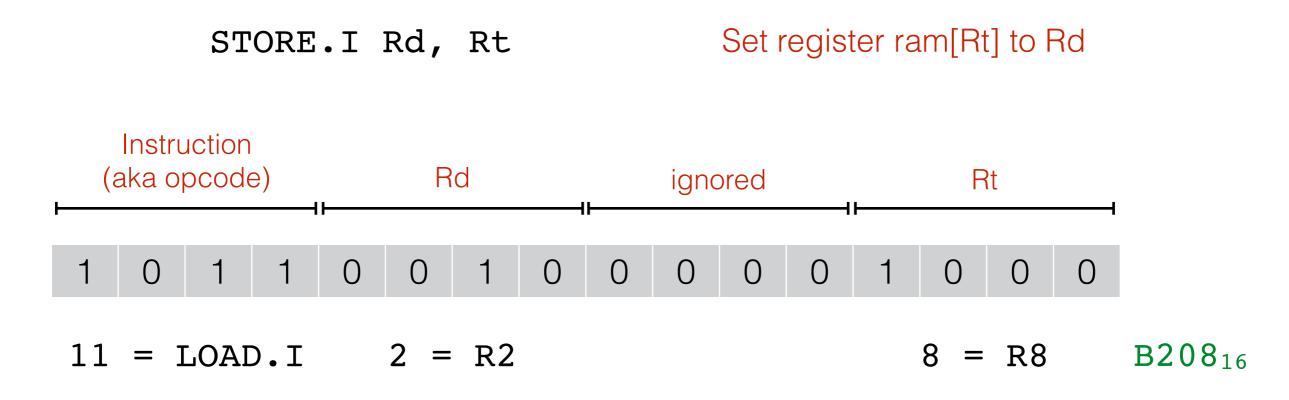


What's the analog in Go of this operation?

Pointer dereferencing with \*:

## **Store Indirect**

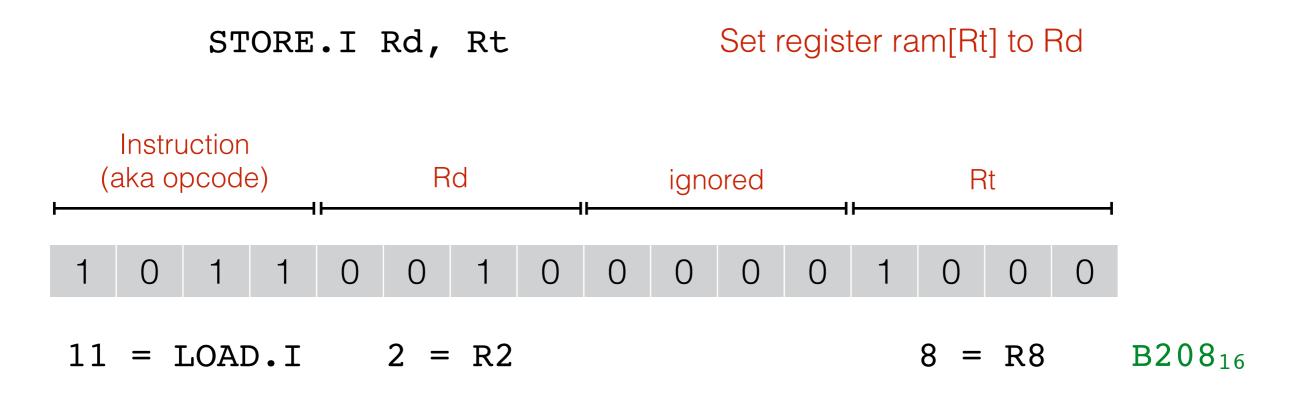
Use the value in a register as an address into RAM to write to:



What's the analog in Go of this operation?

## **Store Indirect**

Use the value in a register as an address into RAM to write to:



What's the analog in Go of this operation?

Pointer dereferencing with \* in an assignment:

var r8 \*int = 70 // not legal in Go
var r2 int
\*r8 = r2 // STORE.I R2 R8

## **Summary So Far**

- Instructions are encoded as integers stored in memory.
- PC incremented after each instruction.
- Can read / write to memory using either an explicit address (immediate), or the contents of another register as the address (indirect)
- Can perform arithmetic operations on registers.
- Input / Output done via reads/writes to special memory locations.

How would we write an **for** loop?

### **Jumps: Manipulating the PC**

JUMP Rd

JMP0 Rd, addr

Set PC to Rd If Rd == 0, set PC to addr

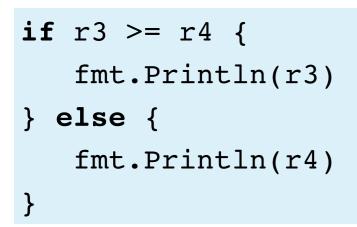
15:	LIMM R1, 1	//	7101
16:	LIMM R5, 18	//	7518
17:	LIMM R6, 0	//	7600
18:	JMP0 R3, 1C	//	C31C
19:	ADD R6, R6, R2	//	1662
1A:	SUB R3, R3, R1	//	2331
1B:	JUMP R5	//	E500
1C:	STORE R6, FF	//	96FF

func mul(r2, r3 int) {
 r1 := 1
 r6 := 0

for r3 != 0 {
 r6 = r6 + r2
 r3 = r3 - r1
 }
 fmt.Print(r2)
}

JMPP Rd, addr

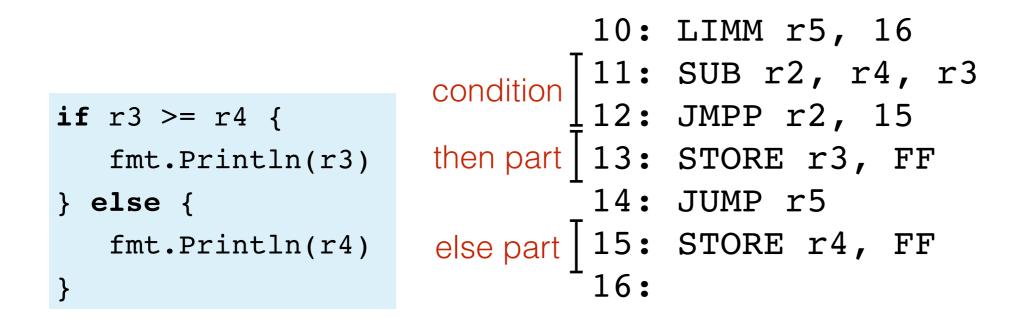
If Rd > 0, set PC to addr



10: LIMM r5, 16
11: SUB r2, r4, r3
12: JMPP r2, 15
13: STORE r3, FF
14: JUMP r5
15: STORE r4, FF
16:

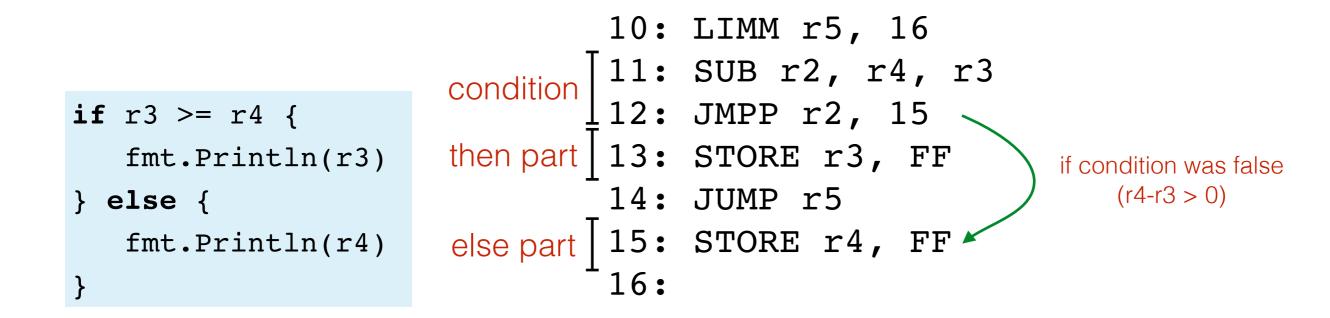
JMPP Rd, addr

If Rd > 0, set PC to addr



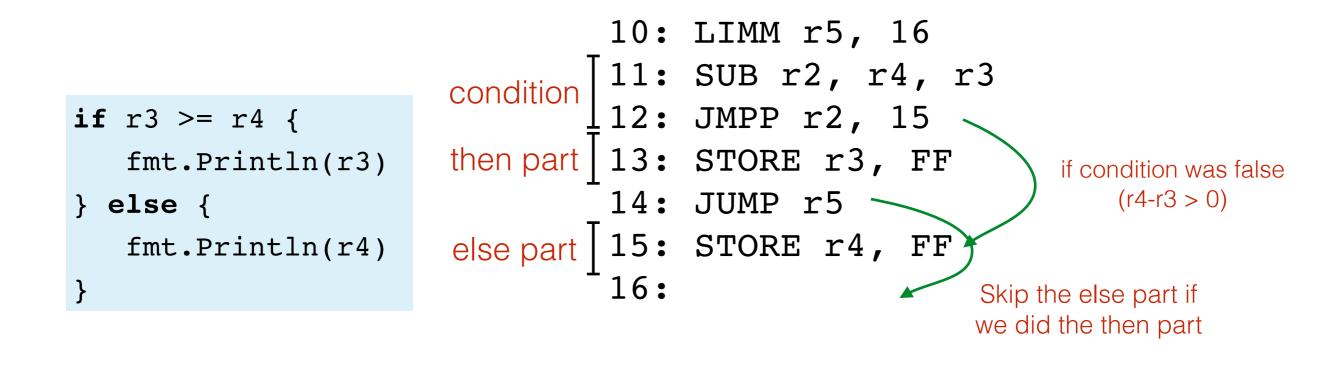
JMPP Rd, addr

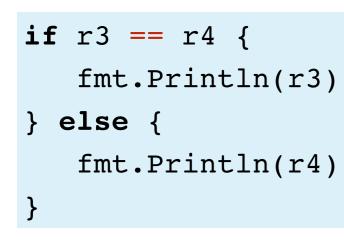
If Rd > 0, set PC to addr



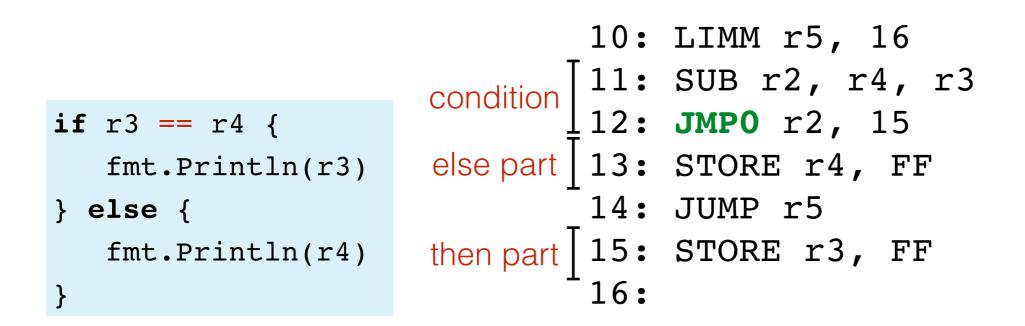
JMPP Rd, addr

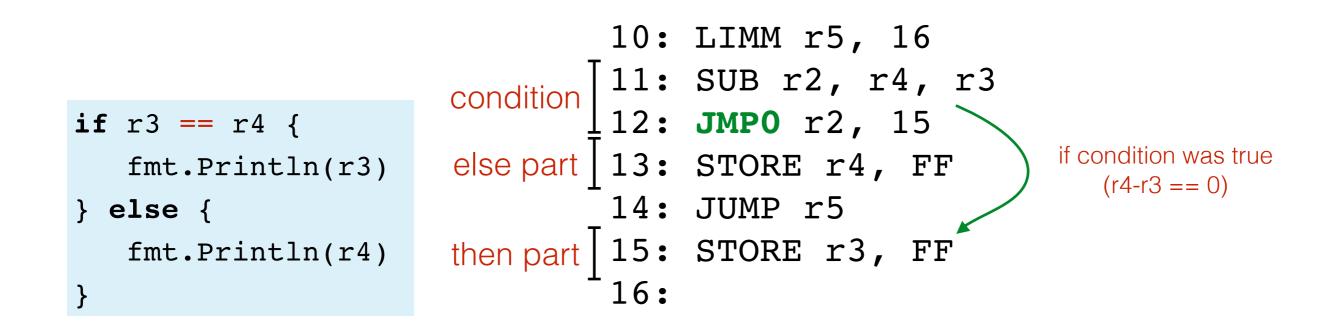
If Rd > 0, set PC to addr

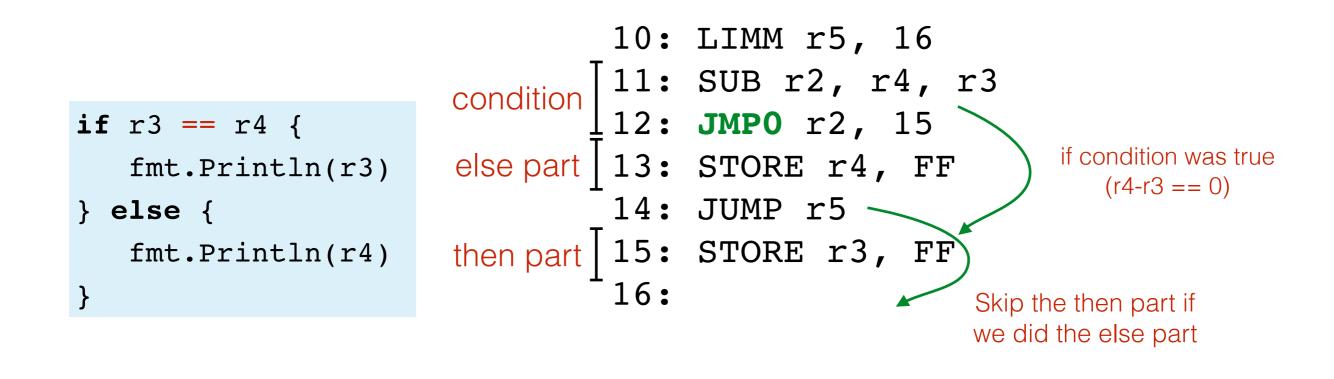




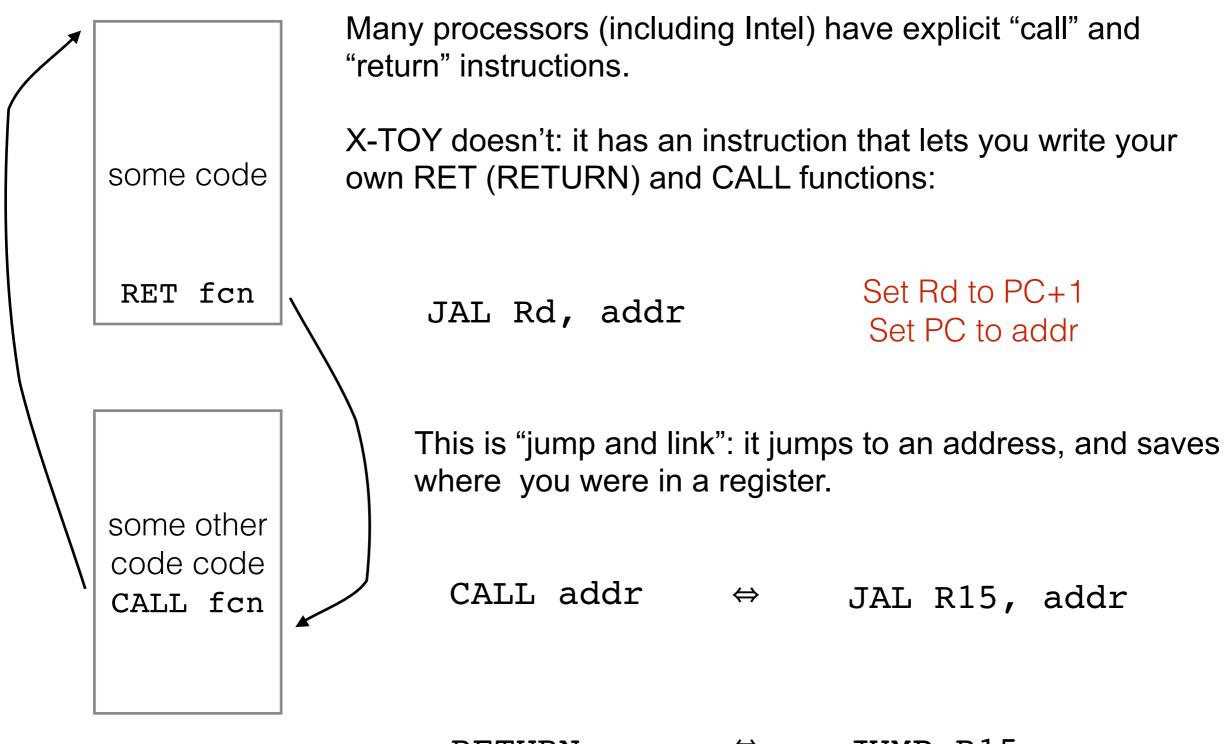
10: LIMM r5, 16
11: SUB r2, r4, r3
12: JMPO r2, 15
13: STORE r4, FF
14: JUMP r5
15: STORE r3, FF
16:







# **Function Calls**



RETURN  $\Leftrightarrow$  JUMP R15

# **Function Call Parameters**

Note: a function is just a block of instructions that we plan to jump into from elsewhere in the program.

How can we pass parameters into a "function"?

## **Function Call Parameters**

Note: a function is just a block of instructions that we plan to jump into from elsewhere in the program.

How can we pass parameters into a "function"?

**Option 1:** The caller and the function just agree about which registers to store the parameters in:

```
// R2 and R3 should contain the
// numbers to multiply; R15 should
// contain the address to return to
15: LIMM R1, 1 // 7101
16: LIMM R5, 18 // 7518
17: LIMM R6, 0 // 7600
18: JMP0 R3, 1C // C31C
19: ADD R6, R6, R2 // 1662
1A: SUB R3, R3, R1 // 2331
1B: JUMP R5 // E500
1C: STORE R6, FF // 96FF
1D: JUMP RF // EF00
```

```
func mul(r2, r3 int) {
  r1 := 1
  r6 := 0

for r3 != 0 {
  r6 = r6 + r2
  r3 = r3 - r1
  }
  fmt.Print(r2)
}
```

### program Mul

# **Example Call in X-TOY**

```
// Input: None
// Output: 8 * 2 = 16 = 0 \times 10
//
10: 7208 R[2] <- 0008
11: 7302 R[3] <- 0002
12: FF15 R[F] <- pc+1; goto 15 (FF15 sets RF to pc+1)
13: 0000 halt
```

### function mul

```
// Input: R2 and R3
// Return address: R15
// Output: to screen
// Temporary variables: R5, R6
15: 7101 R[1] <- 0001
16: 7518 R[5] <- 0018
17: 7600 R[6] <- 0000
18: C31C if (R[3] == 0) goto 1C
19: 1662 R[6] < - R[6] + R[2]
1A: 2331
          R[3] < - R[3] - R[1]
1B: E500 goto R[5]
1C: 96FF write R[6]
1D: EF00
          goto R[F]
```

Notes:

Program starts at address 0x10

You must say the address of every line of code by prefixing it with addr:

# **Option 2: Push Parameters onto the Stack**

Agree that the stack grows from memory address FE downward towards 0

Agree that R14 always holds a pointer to the top of the stack

	LIMM R1, 1
"PUSH R7"	ADD RE, RE, R1
	STORE.I R7 RE

	LOAD.I <mark>R9</mark> RE
"POP <mark>R9</mark> "	LIMM R1, 1
	SUB RE, RE, R1



### **Option 2: Push Parameters onto the Stack**

// The top of the stack should contain the
// two numbers to multiply; R15 should
// contain the address to return to

10:	LOAD.I <mark>R2,</mark> RE	//	A20E	Grab the number at the top of the stack
11:	LIMM R1, 1	//	7101	T "pop": move the top of the stack
12:	SUB RE, RE, R1		2EE1	
13:	LOAD.I R3, RE	11	A30E	Grab the number at the top of the stack
14:	SUB RE, RE, R1	//	2EE1	<ul> <li>move the top of the stack down by 1</li> </ul>
15 <b>:</b>	LIMM R1, 1	//	7101	
16:	LIMM R5, 18	//	7518	
17:	LIMM R6, O	//	7600	
18:	JMP0 R3, 1C	//	C31C	
19:	ADD R6, R6, R2	//	1662	
1A:	SUB R3, R3, R1	//	2331	
1B:	JUMP R5	//	E500	
1C:	STORE R6, FF	//	96FF	
1D:	JUMP RF	//	EF00	

### How many registers are there?

16 in X-TOY This is a typical number (6-32)

Intel processors have 6 general purpose registers in 32-bit mode, plus some others. They have 16 general purpose registers in 64-bit mode.

What if you "run out"?

Yep, that's a problem: you may have to shuffle variables between RAM and registers if you need to use the registers for something.

### **Summary of X-TOY Computer**

#### INSTRUCTION FORMATS

	••••	• • • •	••••	••••	
Format 1:	op	d	s	l t	
Format 2:	op	d	ir	nm	

### ARITHMETIC and LOGICAL operations

1: add	R[d] < - R[s] + R[t]
2: subtract	R[d] <- R[s] - R[t]
3: and	R[d] <- R[s] & R[t]
4: xor	R[d] <- R[s] ^ R[t]
5: shift left	R[d] <- R[s] << R[t]
6: shift right	R[d] <- R[s] >> R[t]

### TRANSFER between registers and memory

7: ]	Load immediate	R[d] < - imm
8: ]	load	R[d] <- mem[imm]
9: s	store	<pre>mem[imm] &lt;- R[d]</pre>
A: ]	load indirect	<pre>R[d] &lt;- mem[R[t]]</pre>
B: s	store indirect	<pre>mem[R[t]] &lt;- R[d]</pre>

#### CONTROL

0: halt halt
C: branch zero if (R[d] == 0) pc <- imm
D: branch pos. if (R[d] > 0) pc <- imm
E: jump register pc <- R[d]
F: jump and link R[d] <- pc; pc <- imm</pre>

R[0] always reads 0. Loads from mem[FF] come from stdin. Stores to mem[FF] go to stdout.

From the X-TOY instructions

## **X-TOY Environment**

	Mul - Vis	ual X-TC	YC
File Edit M	Node Workspace Tools		
	3 🖪 🖶 🗶 🖪 🛅 🤰	C	
1 program		¥ ×	Reference Stdin Stdout Core
2 // Input 3 // Outpu	t: 8 * 2 = 16 = 0x10		Core Save Core Dump
4 //			Program Counter 0010 (0000 0000 0001 0000,
5 10: 7208 6 11: 7302			
7 12: FF15			Current Instruction 7208 (R[2] <- 0008)
8 13: 0000			Registers
9 10 function			
	: R2 and R3		R[0] = 0000 (0000 0000 0000 0000, 0) R[1] = ???? (Uninitialized Value)
	n address: R15		R[2] = ???? (Uninitialized Value)
	it: to screen		R[3] = ???? (Uninitialized Value)
	orary variables: R5, R6		R[4] = ???? (Uninitialized Value)
	R[1] <- 0001		R[5] = ???? (Uninitialized Value)
16 16: 7518 17 17: 1600			R[6] = ???? (Uninitialized Value)
18 18: C310		c	R[7] = ???? (Uninitialized Value)
19 19: 1662	*		R[8] = ???? (Uninitialized Value)
20 1A: 2331	R[3] <- R[3] - R[1]		R[9] = 7777 (Uninitialized Value)
21 1B: E500	<b>V</b>		
22 1C: 96Ff			Memory Save Memory Dump
23 1D: EF00	goto R[F]		<pre>mem[00] = ???? (Uninitialized Value)</pre>
			<pre>mem[01] = ???? (Uninitialized Value)</pre>
	I	_	<pre>mem[02] = ???? (Uninitialized Value)</pre>
			<pre>mem[03] = ???? (Uninitialized Value)</pre>
Steps	0 Step R	un	<pre>mem[04] = ???? (Uninitialized Value)</pre>
			<pre>mem[05] = ???? (Uninitialized Value) mem[05] = 2222 (Uninitialized Value)</pre>
Elapse	0.000 s	rrupt	<pre>mem[06] = ???? (Uninitialized Value) mem[07] = 2222 (Uninitialized Value)</pre>
		Tupt	<pre>mem[07] = ???? (Uninitialized Value) mem[02] = 2222 (Uninitialized Value)</pre>
Refre	1 spr		<pre>mem[08] = ???? (Uninitialized Value) mem[00] = 2222 (Uninitialized Value)</pre>
Target Cleak	100 mc		<pre>mem[09] = ???? (Uninitialized Value)</pre>
Target Clock	100 ms		6

# Intel 8088 Instruction Set

ADD	Add
SUB	Subtraction

AND	Logical AND
XOR	Exclusive OR
SHL	Shift left (unsigned shift left)
SHR	Shift right (unsigned shift right)

JMP	Jump
JCXZ	Jump if CX is zero
JNS	Jump if not negative

INC	Increment by 1
DEC	Decrement by 1

Another motivation for the ++ and -statements in Go (and C, c++, Java..): They correspond directly to a machine instruction.

PUSH	Push data onto stack
POP	Pop data from stack

Has several instructions to push and pop data onto THE stack.

and about 80 others...

http://en.wikipedia.org/wiki/X86\_instruction\_listings#Original\_8086.2F8088\_instructions

# **MacPaint**



http://www.computerhistory.org/atchm/macpaint-and-quickdraw-source-code/