# Computer Architecture 02-201 / 02-601 

## The Conceptual Architecture of a Computer



## Binary Representation

Base 10 (decimal) notation:


Computers store the numbers in binary because it has transistors that can encode 0 and 1 efficient

Each 0 and 1 is a bit.
Built-in number types each have a maximum number of bits.

Base 2 (binary) notation:
1000010100000
$\div 0 \times 2^{0}$
$0 \times 2^{1}$
$0 \times 2^{2}$
$0 \times 2^{3}$
$0 \times 2^{4}$

- $1 \times 2^{5}$
$0 \times 2^{6}$
$1 \times 2^{7}$
$0 \times 2^{8}$
$0 \times 2^{9}$
$0 \times 2^{10}$
$0 \times 2^{11}$
$+1 \times 2^{12}$


## Hexadecimal Representation

Decimal isn't good for computers because they work with bits.
But writing everything in binary would be tedious. Hence, we often use base 16, aka "hexadecimal":

Base 10 (decimal) notation:


Base 16 (hexadecimal) notation:

$$
\begin{gathered}
10 \mathrm{~A} 0 \\
\hdashline \begin{array}{c}
1 \\
\vdots \\
0 \times 16^{2} \\
A \times 16^{1} \\
0 \times 16^{2}
\end{array} \\
+1 \times 16^{3} \\
\hline 1 \times 4096+10 \times 16=4256
\end{gathered}
$$

Need 16 different digits, so use $0,1,2,3,4,5,6,7,8,9, A, B, C, D, E, F$
$A=10, B=11, C=12, D=13, E=14, F=15$

## Add CPU instruction

ADD Rd, Rs, Rt
Set register Rd to Rs + Rt

An instruction is encoded as a sequence of bits:


Written as a hexadecimal number: 122816

## Subtract CPU instruction

SUB Rd, Rs, Rt
Set register Rd to Rs - Rt

The SUB instruction is the same format as ADD, but with a different opcode:


Written as a hexadecimal number: 222816

## Load "Immediate" Instruction

LIMM Rd, value
Set register Rd to value

For LIMM, the last 8 bits give the value to copy into Rd:


## Load Instruction

LOAD Rd, addr

Set register Rd to ram[addr]

For LOAD, the last 8 bits give the address of the memory cell to copy into Rd:


Written as a hexadecimal number: $8488_{16}$

## Store Instruction

STORE Rd, addr
Set register ram[addr] to Rd

For LOAD, the last 8 bits give the address of the memory cell to copy into Rd:


Written as a hexadecimal number: $9488_{16}$

## An Example Program

$$
\begin{array}{ll}
\text { LIMM R1, } 64 & / / R 1=200 \\
\text { LIMM R2, 1E } & / / R 2=30 \\
\text { ADD R2, R1, R2 } & / / R 2=R 1+R 2 \\
\text { STORE R2, 46 } & / / \operatorname{ram}[70]=R 2
\end{array}
$$

What does this program do?

## An Example Program

```
LIMM R1, 64 // R1 = 200
LIMM R2, 1E // R2 = 30
ADD R2, R1, R2 // R2 = R1 + R2
STORE R2, 46 // ram[70] = R2
```

What does this program do?
Stores $200+30$ into memory location 70

Similar to the following Go program:

```
var r1 int = 200
var r2 int = 30
r2 = r1 + r2
var ram70 int = r2
```

Go manages the registers and memory locations for you.

It may keep a variable in a register, memory, or both.

## Where is the program stored?

The program is just a sequence of integers that encode for instructions.

```
LIMM R1, 64 // R1 = 200 ; 7164
LIMM R2, 1E // R2 = 30 ; 721E
ADD R2, R1, R2 // R2 = R1 + R2 ; 1212
STORE R2, 46 // ram[70] = R2 ; 9246
```


## Where is the program stored?

The program is just a sequence of integers that encode for instructions.

| LIMM R1, 64 | $/ / R 1=200$ | $; 7164$ |
| :--- | :--- | :--- |
| LIMM R2, 1E | // R2 2030 | $; 721 \mathrm{E}$ |
| ADD R2, R1, R2 | // R2 $=$ R1 + R2 | ; 1212 |
| STORE R2, 46 | // ram[70] = R2 | $; 9246$ |

These integers are stored in the same RAM used for variables:


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The CPU has a special register called PC ("program counter") that contains the address of the current instruction.

After each instruction, the PC is incremented by 1 .


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These integers are stored in the same RAM used for variables:

The CPU has a special register called PC ("program counter") that contains the address of the current instruction.

After each instruction, the PC is incremented by 1 .


```
LIMM R1, 64 // R1 = 100 ; 7164
LIMM R2, 1E // R2 = 30 ; 721E
ADD R2, R1, R2 // R2 = R1 + R2 ; 1212
STORE R2, 46 // ram[70] = R2 ; 9246
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```
LIMM R1, 64 // R1 = 100 ; 7164
LIMM R2, 1E // R2 = 30 ; 721E
ADD R2, R1, R2 // R2 = R1 + R2 ; 1212
STORE R2, 46 // ram[70] = R2 ; 9246
```

| $\mathrm{PC}=11$ |  |
| :---: | :---: |
|  | $\mathrm{R} 0=0$ |
| $\mathrm{R} 1=64$ |  |
| CPU | $\mathrm{R} 2=0$ |
| $\mathrm{R} 3=0$ |  |
| $\mathrm{Rn}=0$ |  |



```
LIMM R1, 64 // R1 = 100 ; 7164
LIMM R2, 1E // R2 = 30 ; 721E
ADD R2, R1, R2 // R2 = R1 + R2 ; 1212
STORE R2, 46 // ram[70] = R2 ; 9246
```

| $\mathrm{PC}=12$ |  |
| :---: | :---: |
|  | $\mathrm{RO}=0$ |
| $\mathrm{CP} 1=64$ |  |
| $\mathrm{R} 2=1 \mathrm{E}$ |  |
| $\mathrm{R} 3=0$ |  |
| $\mathrm{Rn}=0$ |  |



```
LIMM R1, 64 // R1 = 100 ; 7164
LIMM R2, 1E // R2 = 30 ; 721E
ADD R2, R1, R2 // R2 = R1 + R2 ; 1212
STORE R2, 46 // ram[70] = R2 ; 9246
```

| $\mathrm{PC}=13$ |
| :---: | :---: |
| $\mathrm{RO}=0$ |
| $\mathrm{R} 1=64$ |
| $\mathrm{R} 2=82$ |
| $\mathrm{R} 3=0$ |
| $\mathrm{Rn}=0$ |



```
LIMM R1, 64 // R1 = 100 ; 7164
LIMM R2, 1E // R2 = 30 ; 721E
ADD R2, R1, R2 // R2 = R1 + R2 ; 1212
STORE R2, 46 // ram[70] = R2 ; 9246
```

| $\mathrm{PC}=14$ |  |
| :---: | :---: |
|  | $\mathrm{RO}=0$ |
| $\mathrm{CP} 1=64$ |  |
| $\mathrm{R} 2=82$ |  |
| $\mathrm{R} 3=0$ |  |
| $\mathrm{Rn}=0$ |  |



## Ending the program

The computer will keep grabbing an integer, interpreting it as an instruction, and then incrementing PC indefinitely.

To stop this process, you have to add a HALT instruction:


## Input, Output, and 0

Register 0 always has value 0
Stores to memory location FF writes the value to the output
Reads from memory location FF read a value from the input

| STORE R3, FF | Write the value R3 to the output |
| :--- | :--- |
| LOAD R4, FF | Read the next input value into R3 |

## Example:

| LIMM R1, 64 | $/ / R 1=200$ | $; 7164$ |
| :--- | :--- | :--- |
| LOAD R2, FF | // R2 = input | $; 72 F F$ |
| ADD R2, R1, R2 | // R2 = R1 + R2 | $; 1212$ |
| STORE R2, FF | // write R2 to output | $; 92 F F$ |
| HALT | // stop program | $; 0000$ |

## Other Arithmetic Operations: AND

AND Rd, Rs, Rt Set register Rd to Rs AND Rt

AND takes two binary numbers $a$ and $b$ and creates a binary $c$ number where the ith bit of $c$ is 1 if and only if the ith bits of both $a$ and $b$ are 1 :


## Exclusive Or: XOR

XOR Rd, Rs, Rt

Set register Rd to Rs XOR Rt

XOR takes two binary numbers $a$ and $b$ and creates a binary $c$ number where the ith bit of $c$ is 1 if either $a$ or $b$ but not both have 1 in their ith bit:


## AND and XOR in Go

Go has bitwise operators:

$$
\begin{aligned}
& \&=\text { AND } \\
& \wedge=\text { XOR }
\end{aligned}
$$

```
var r1 int = 200
var r2 int = 30
r2 = r1 & r2
var r3 int
r3 = r2 ^ r1
```

$r 1=0000000011001000$
r2 $=0000000000011110$
$r 2=0000000000001000$
$r 3=0000000011000000$

## Left and Right Shift

LSHIFT Rd, Rs, Rt
Set register Rd to Rs shifted to the left by Rt digits


Digits fall off
the left and disappear

Os come in at the right

## Left and Right Shift

LSHIFT Rd, Rs, Rt
Set register Rd to Rs shifted to the left by Rt digits


RSHIFT is the same except it shifts to the right:

Set register Rd to Rs shifted to the right by Rt digits

## AND, XOR, LSHIFT, RSHIFT

AND Rd, Rs, Rt<br>XOR Rd, Rs, Rt<br>LSHIFT Rd, Rs, Rt<br>RSHIFT Rd, Rs, Rt

The instruction format similar to ADD, SUB:

|  | $\begin{aligned} & \text { Instru } \\ & \text { aka } \end{aligned}$ | ction code) |  | Rd |  |  |  |  | Rs |  |  |  | Rt |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 |  |
|  | 3 | AND |  |  |  | R2 |  |  | 2 |  |  |  | 8 |  |  | 322816 |
|  | $4=$ | XOR |  |  | 2 |  |  |  | 2 |  |  |  | 8 |  |  | $4228{ }_{16}$ |
|  | $5=$ | LSH | IFT |  |  | R2 |  |  | = |  |  |  | 8 |  |  | 522816 |
|  | $6=$ | RSH | IFT |  | 2 |  |  |  | = |  |  |  | $8=$ |  |  | 622816 |

## Load Indirect

Use the value in a register as an address into RAM to read from:
LOAD.I Rd, Rt Set register Rd to ram[Rt]


What's the analog in Go of this operation?

## Load Indirect

Use the value in a register as an address into RAM to read from:
LOAD.I Rd, Rt Set register Rd to ram[Rt]

|  | ka | $\mathrm{cod}$ |  | Rd |  |  |  | ignored |  |  |  | Rt |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |  |
| 10 | = | OA |  |  | = | R2 |  |  |  |  |  |  |  | R8 |  | A208 16 |

What's the analog in Go of this operation?

```
var r8 *int = 70 // not legal in Go
var r2 int
```

```
r2 = *r8
```

r2 = *r8
// LOAD.I R2 R8

```
    // LOAD.I R2 R8
```

Pointer dereferencing with *:

## Store Indirect

Use the value in a register as an address into RAM to write to:
STORE.I Rd, Rt Set register ram[Rt] to Rd


What's the analog in Go of this operation?

## Store Indirect

Use the value in a register as an address into RAM to write to:
STORE.I Rd, Rt Set register ram[Rt] to Rd

|  | nstr ka |  |  | Rd |  |  |  | ignored |  |  |  | Rt |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |  |
|  | = |  |  | 2 = R2 |  |  |  |  |  |  |  |  | $8=\mathrm{R} 8$ |  |  | B20816 |

What's the analog in Go of this operation?

Pointer dereferencing with * in an assignment:

```
var r8 *int = 70 // not legal in Go
var r2 int
*r8 = r2 // STORE.I R2 R8
```


## Summary So Far

- Instructions are encoded as integers stored in memory.
- PC incremented after each instruction.
- Can read / write to memory using either an explicit address (immediate), or the contents of another register as the address (indirect)
- Can perform arithmetic operations on registers.
- Input / Output done via reads/writes to special memory locations.

How would we write an for loop?

## Jumps: Manipulating the PC

JUMP Rd
JMPO Rd, addr

```
15: LIMM R1, 1
16: LIMM R5, 18
17: LIMM R6, 0
18: JMP0 R3, 1C
19: ADD R6, R6, R2
1A: SUB R3, R3, R1
1B: JUMP R5
1C: STORE R6, FF
```

// 7101
// 7518
// 7600
// C31C
// 1662
// 2331
// E500
// 96FF

## Set PC to Rd

If $R d==0$, set $P C$ to addr

```
func mul(r2, r3 int) {
    r1 := 1
    r6 := 0
    for r3 != 0 {
        r6 = r6 + r2
        r3 = r3 - r1
    }
    fmt.Print(r2)
}
```


## If Statements

```
JMPP Rd, addr
If Rd > 0, set PC to addr
```

```
10: LIMM r5, 16
```

10: LIMM r5, 16
11: SUB r2, r4, r3
11: SUB r2, r4, r3
if r3 >= r4 {
fmt.Println(r3)
} else {
fmt.Println(r4)
}
12: JMPP r2, 15
12: JMPP r2, 15
13: STORE r3, FF
13: STORE r3, FF
14: JUMP r5
14: JUMP r5
15: STORE r4, FF
15: STORE r4, FF
16:

```
16:
```

How would we write a condition $\mathrm{a}==\mathrm{b}$ ?

## If Statements

JMPP Rd, addr
If $R d>0$, set $P C$ to addr


How would we write a condition $\mathrm{a}==\mathrm{b}$ ?

## If Statements

JMPP Rd, addr
If Rd $>0$, set PC to addr


How would we write a condition $\mathrm{a}==\mathrm{b}$ ?

## If Statements

JMPP Rd, addr
If $R d>0$, set $P C$ to addr


How would we write a condition $\mathrm{a}==\mathrm{b}$ ?

## Example If Statement \#2

```
10: LIMM r5, 16
11: SUB r2, r4, r3
if r3 == r4 {
    fmt.Println(r3)
} else {
    fmt.Println(r4)
}
12: JMPO r2, 15
13: STORE r4, FF
14: JUMP r5
15: STORE r3, FF
16:
```


## Example If Statement \#2

```
    10: LIMM r5, 16
if r3 == r4 {
    fmt.Println(r3)
} else {
    fmt.Println(r4)
}
```



## Example If Statement \#2



## Example If Statement \#2



## Function Calls



## Function Call Parameters

Note: a function is just a block of instructions that we plan to jump into from elsewhere in the program.

How can we pass parameters into a "function"?

## Function Call Parameters

Note: a function is just a block of instructions that we plan to jump into from elsewhere in the program.

How can we pass parameters into a "function"?
Option 1: The caller and the function just agree about which registers to store the parameters in:

```
// R2 and R3 should contain the
// numbers to multiply; R15 should
// contain the address to return to
15: LIMM R1, 1 // 7101
16: LIMM R5, 18 // 7518
17: LIMM R6, 0 // 7600
18: JMP0 R3, 1C // C31C
19: ADD R6, R6, R2 // 1662
1A: SUB R3, R3, R1 // 2331
1B: JUMP R5 // E500
1C: STORE R6, FF // 96FF
1D: JUMP RF // EF00
```

```
func mul(r2, r3 int) {
    r1 := 1
    r6 := 0
    for r3 != 0 {
        r6 = r6 + r2
        r3 = r3 - r1
    }
    fmt.Print(r2)
}
```

program Mul
// Input: None
// Output: 8 * $2=16=0 \times 10$
//
10: $7208 \quad \mathrm{R}[2]<-0008$
11: $7302 \mathrm{R}[3]<-0002$
12: FF15 R[F] <- pc+1; goto 15 (FF15 sets RF to pc+1)
13: 0000 halt
function mul
// Input: R2 and R3
// Return address: R15
// Output: to screen
// Temporary variables: R5, R6
15: $7101 \mathrm{R}[1]<-0001$
16: $7518 \quad \mathrm{R}[5]<-0018$
17: 7600 R[6] <- 0000
18: C31C if (R[3] == 0) goto 1C
19: $1662 \mathrm{R}[6]<-\mathrm{R}[6]+\mathrm{R}[2]$
1A: $2331 \quad \mathrm{R}[3]<-\mathrm{R}[3]-\mathrm{R}[1]$
1B: E500 goto R[5]
1C: 96FF write R[6]
1D: EF00 goto R[F]

## Example Call in X-TOY

Notes:
Program starts at address $0 \times 10$
You must say the address of every line of code by prefixing it with addr:

## Option 2: Push Parameters onto the Stack

Agree that the stack grows from memory address FE downward towards 0

Agree that R14 always holds a pointer to the top of the stack
\(\left.$$
\begin{array}{ll}\text { "PUSH R7" } & \begin{array}{l}\text { LIMM R1, } 1 \\
\text { ADD RE, RE, R1 }\end{array}
$$ <br>

STORE.I R7 RE\end{array}\right]\)|  |  |
| :--- | :--- |
| "POP R9" | LOAD.I R9 RE <br>  <br>  <br>  <br>  <br> SUBM RE, RE, R1 |

## Option 2: Push Parameters onto the Stack

| // The top of the stack should contain the// two numbers to multiply; R15 should |  |
| :---: | :---: |
| // contain the address to return to |  |
| 10: LOAD.I R2, RE | // A20E $\longleftarrow$ Grab the number at the top of the stack |
| 11: LIMM R1, 1 | // 7101 T "pop": move the top of the stack |
| 12: SUB RE, RE, R1 | // 2EE1 I down by 1 |
| 13: LOAD.I R3, RE | // A30E $\longleftarrow$ Grab the number at the top of the stack |
| 14: SUB RE, RE, R1 | // 2EE1 $\longleftarrow$ move the top of the stack down by 1 |
| 15: LIMM R1, 1 | // 7101 |
| 16: LIMM R5, 18 | // 7518 |
| 17: LIMM R6, 0 | // 7600 |
| 18: JMP0 R3, 1C | // C31C |
| 19: ADD R6, R6, R2 | // 1662 |
| 1A: SUB R3, R3, R1 | // 2331 |
| 1B: JUMP R5 | // E500 |
| 1C: STORE R6, FF | // 96FF |
| 1D: JUMP RF | // EFOO |

## How many registers are there?

16 in $X$-TOY
This is a typical number (6-32)
Intel processors have 6 general purpose registers in 32-bit mode, plus some others.
They have 16 general purpose registers in 64-bit mode.

What if you "run out"?

Yep, that's a problem: you may have to shuffle variables between RAM and registers if you need to use the registers for something.

## Summary of X-TOY Computer

INSTRUCTION FORMATS


TRANSFER between registers and memory
7: load immediate $\mathrm{R}[\mathrm{d}]<-$ imm
8: load $\quad R[d]<-$ mem[imm]
9: store mem[imm] <- R[d]
A: load indirect $R[d]<-m e m[R[t]]$
$B:$ store indirect mem[R[t]] <- R[d]
CONTROL

| 0: halt | halt |
| :--- | :--- |
| C: branch zero | if $(R[d]==0) \mathrm{pc}<-$ imm |
| D: branch pos. | if $(R[d]>0) \mathrm{pc}<-$ imm |
| E: jump register | $\mathrm{pc}<-\mathrm{R}[\mathrm{d}]$ |
| $\mathrm{F}:$ jump and link | $R[d]<-\mathrm{pc} ; \mathrm{pc}<-$ imm |

R[0] always reads 0 .
Loads from mem[FF] come from stdin.
Stores to mem[FF] go to stdout.
From the X-TOY instructions

## X-TOY Environment



## Intel 8088 Instruction Set

| ADD | Add |
| :--- | :--- |
| SUB | Subtraction |


| INC | Increment by 1 |
| :--- | :--- |
| DEC | Decrement by 1 |


| AND | Logical AND |
| :--- | :--- |
| XOR | Exclusive OR |


| SHL | Shift left (unsigned shift left) |
| :--- | :--- |


| SHR | Shift right (unsigned shift right) |
| :--- | :--- |


| PUSH | Push data onto stack |
| :--- | :--- |
| POP | Pop data from stack |


| JMP | Jump |
| :--- | :--- |
| JCXZ | Jump if CX is zero |
| JNS | Jump if not negative |

Another motivation for the ++ and -statements in Go (and C, C++, Java..): They correspond directly to a machine instruction.

Has several instructions to push and pop data onto THE stack.

## MacPaint


http://www.computerhistory.org/atchm/macpaint-and-quickdraw-source-code/

