

Carnegie Mellon University

15-415 Database Applications

Spring 2012, Faloutsos

Assignment 6: Schema Refinement

Due: ~~3/27~~ **3/29**, 1:30 pm, in class – **hard copy**

Reminders

- Weight: **5%** of the homework grade.
- The points of this homework add up to **100**.
- Lead TA: Bin Fu (binf@andrew.cmu.edu).
- Please **type** all your answers.
- Rough time-estimates: **2~4 hours**.
- The textbook referred to in the homework is Database Management Systems by Ramakrishnan and Gehrke, 3rd edition.

Question 1: Functional dependency examples [6 points]

Consider the relation shown in the following table:

X	Y	Z
x ₁	y ₁	z ₁
x ₂	y ₁	z ₂
x ₁	y ₂	z ₂
x ₂	y ₁	z ₂

List all the functional dependencies that this relation instances satisfy.

Question 2: Functional dependency deductions [24 points]

Consider the following set S of functional dependencies:

$$A \rightarrow C \text{ (F1)}$$

$$BD \rightarrow A \text{ (F2)}$$

$$C \rightarrow B \text{ (F3)}$$

For each of the following dependencies, if it can be deduced from S, give the rigorous proof; if not, give a counter-example with 3 tuples or less.

[Q2.1] $CD \rightarrow A$ [8 points]

[Q2.2] $BC \rightarrow A$ [8 points]

[Q2.3] $AD \rightarrow B$ [8 points]

Question 3: Related Concepts I [20 points]

Consider the relation schema $R(A, B, C, D)$ with functional dependencies $A \rightarrow D$, $B \rightarrow CD$ and $AC \rightarrow D$.

[Q3.1] Find the attribute closure $\{A\}^+$. [5 points]

[Q3.2] Find the attribute closure $\{A, B\}^+$. [5 points]

[Q3.3] Find the minimum cover (i.e. canonical cover) of the given functional dependencies. [5 points]

[Q3.4] List all the candidate key(s) of R. [5 points]

Question 4: Decompositions [15 points]

Consider the relation schema $R(A, B, C, D, E, G)$ with functional dependencies $F = \{AB \rightarrow C, AG \rightarrow E, B \rightarrow D, E \rightarrow G\}$. Notice F is the minimum cover of itself.

For each of the following decompositions $R(A, B, C, D, E, G)$, determine whether it is (a) dependency-preserving, and (b) lossless.

- i) $\{ABC, CDE, EG\}$ [5 points]
- ii) $\{ABCD, AEG\}$ [5 points]
- iii) $\{ABCE, BD, AEG\}$ [5 points]

Question 5: BCNF and 3NF [35 points]

Consider the relation schema $R(A, B, C, D)$ with functional dependencies $A \rightarrow B, BC \rightarrow A$ and $B \rightarrow D$, which is the minimum cover itself.

[Q5.1] Find all the candidate key(s) of R . [5 points]

[Q5.2] Is relation R in BCNF? Is it in 3NF? Justify your answers. [10 points]

[Q5.3] Decompose the relation $R(A, B, C, D)$ into a collection of BCNF relations, so that the decomposition is lossless. Please follow the instructions on section 19.6.1 of the textbook (R+G, 3rd edition, p622). Is the decomposition dependency-preserving? [10 points]

[Q5.4] Decompose the relation $R(A, B, C, D)$ into a collection of 3NF relations, so that the decomposition is both lossless and dependency-preserving. Please follow the instructions on page 627 of the textbook. [10 points]