

Carnegie Mellon University
15-415 Database Applications
Spring 2012, Faloutsos
Assignment 6: Schema Refinement
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Solutions

Q1 $XY \rightarrow Z$, $XZ \rightarrow Y$ and $YZ \rightarrow X$ all holds. There are many non-trivial (and related) FDs. Thanks for the hardwork.

Q2.1

It holds:

$CD \rightarrow BD$ (F3, augmentation)

$CD \rightarrow A$ (Above + F2, transitivity)

Q2.2

$BC \rightarrow A$ does not hold. Consider the following counter example with 2 tuples:

a1 b1 c1 d1

a2 b1 c1 d2

Q2.3

It holds:

$AD \rightarrow A$ (reflexivity)

$A \rightarrow B$ (F1 + F3, transitivity)

$AD \rightarrow B$ (above two, transitivity)

Q3.1

{A, D}

Q3.2

{A, B, C, D}

Q3.3

$A \rightarrow D$ and $B \rightarrow CD$

Q3.4

Notice A and B must appear in the candidate key since they do not appear on the right hand side of any dependencies. So the only candidate key is {A, B}.

Q4.1

It is neither loss-less nor dependency-preserving. $AG \rightarrow E$ is not preserved.

Q4.2

It is dependency-preserving, but not lossless.

Q4.3

It is lossless: First we can join {ABCE} and {AEG} lossless-ly, since {AE} is candidate key for {AGE}. Then, {ABCEG} and {BD} can be again joined lossless-ly since {B} is a candidate key for {BD}.

It is also dependency-preserving.

Q5.1

The candidate key is {AC} and {BC}.

Q5.2

R is not in BCNF and not in 3NF. Notice for dependency $B \rightarrow D$, B is not superkey, and D does not appear in the candidate key.

Q5.3

They are two ways to decompose. Notice $BC \rightarrow A$ does not violate BCNF ({BC} is a superkey), so we can start by either $A \rightarrow B$ or $B \rightarrow D$.

Case1: If we start from $A \rightarrow B$, we decompose R to $\{AB, ACD\}$. Notice that now $A \rightarrow D$ holds, so $\{ACD\}$ is not in BCNF, thus it needs to be further decomposed to $\{AC, AD\}$. It is not dependency-preserving since both $BC \rightarrow A$ and $B \rightarrow D$ are lost.

Case2: If we start from $B \rightarrow D$, we decompose R to $\{BD, ABC\}$. Then since $\{ABC\}$ is not in BCNF, it is further split to $\{AB, AC\}$. It is not dependency-preserving since $BC \rightarrow A$ is lost.

Q5.4

Many of you use 3NF synthesis to construct a dependency-preserving 3NF decomposition.

If using the instructions in page 627:

Case1: Starting from $\{AB, AC, AD\}$, which is a lossless 3NF decomposition. Notice that it is not dependency-preserving ($BC \rightarrow A$ and $B \rightarrow D$). So we add another two relations $\{ABC, BD\}$. The result is $\{ABC, BD, AB, AC, AD\}$ (You can eliminate either AB or AC since it is included in $\{ABC\}$).

Case2: Starting from $\{BD, ABC\}$, which is a lossless 3NF decomposition. Notice that it's already dependency-preserving, so it's the final answer.