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Carnegie Mellon Univ.
Dept. of Computer Science
15-415 - Database Applications

Extra Lecture: Data Warehousing / Data Mining
 (R&G, ch 25 and 26)

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Data mining - detailed outline


- Problem
 - Getting the data: Data Warehouses, DataCubes, OLAP
 - Supervised learning: decision trees
 - Unsupervised learning
 - association rules
 - (clustering)


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Problem


Given: multiple data sources
 Find: patterns (classifiers, rules, clusters, outliers...)

NY
 sales(p-id, c-id, date, \$price) →

SF
 customers(c-id, age, income, ...) →

PGH
 ???

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Data Ware-housing


First step: collect the data, in a single place (= Data Warehouse)

How?

How often?

How about discrepancies / non-homogeneities?

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Data Ware-housing


First step: collect the data, in a single place (= Data Warehouse)

How? A: Triggers/Materialized views

How often? A: [Art!]

How about discrepancies / non-homogeneities? A: Wrappers/Mediators

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Data Ware-housing

Step 2: collect counts. (DataCubes/OLAP)

Eg.:

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OLAP

Problem: “is it true that shirts in large sizes sell better in dark colors?”

sales	ci-d	p-id	Size	Color	\$	C / S	S	M	L	TOT
						Red	20	3	5	28
	C10	Shirt	L	Blue	30	Blue	3	3	8	14
	C10	Pants	XL	Red	50	Gray	0	0	5	5
	C20	Shirt	XL	White	20	TOT	23	6	18	47
...										

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DataCubes

‘color’, ‘size’: DIMENSIONS
‘count’: MEASURE

C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

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DataCubes

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C / S	S	M	L	TOT
Red	20	3	5	28
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DataCubes

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DataCubes

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TOT	23	6	18	47

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DataCubes

‘color’, ‘size’: DIMENSIONS
‘count’: MEASURE

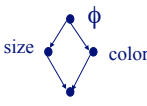
C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

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DataCubes

‘color’, ‘size’: DIMENSIONS
‘count’: MEASURE



C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

DataCube

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DataCubes

SQL query to generate DataCube:

- Naively (and painfully:)

```
select size, color, count(*)
from sales where p-id = 'shirt'
group by size, color
```

```
select size, count(*)
from sales where p-id = 'shirt'
group by size
```

```
...
```

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DataCubes

SQL query to generate DataCube:

- with ‘cube by’ keyword:

```
select size, color, count(*)
from sales
where p-id = 'shirt'
cube by size, color
```

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DataCubes

DataCube issues:

Q1: How to store them (and/or materialize portions on demand)

Q2: Which operations to allow

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DataCubes


DataCube issues:

Q1: How to store them (and/or materialize portions on demand) A: ROLAP/MOLAP

Q2: Which operations to allow A: roll-up, drill down, slice, dice

[More details: book by Han+Kamber]

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DataCubes

Q1: How to store a dataCube?

C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

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DataCubes

Q1: How to store a dataCube?
A1: Relational (R-OLAP)

Color	Size	count	C / S	S	M	L	TOT
'all'	'all'	47	Red	20	3	5	28
Blue	'all'	14	Blue	3	3	8	14
Blue	M	3	Gray	0	0	5	5
...			TOT	23	6	18	47

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DataCubes

Q1: How to store a dataCube?
A2: Multi-dimensional (M-OLAP)
A3: Hybrid (H-OLAP)

C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47


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DataCubes

Pros/Cons:
ROLAP strong points: (DSS, Metacube)

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DataCubes

Pros/Cons:
ROLAP strong points: (DSS, Metacube)

- use existing RDBMS technology
- scale up better with dimensionality

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DataCubes


Pros/Cons:
MOLAP strong points: (EssBase/hyperion.com)

- faster indexing
(careful with: high-dimensionality; sparseness)

HOLAP: (MS SQL server OLAP services)

- detail data in ROLAP; summaries in MOLAP

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DataCubes

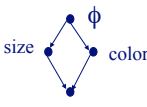
Q1: How to store a dataCube
➡ Q2: What operations should we support?

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DataCubes

Q2: What operations should we support?



C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

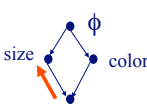
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DataCubes

Q2: What operations should we support?

Roll-up



C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

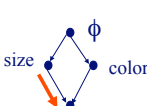
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DataCubes

Q2: What operations should we support?

Drill-down



C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

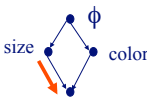
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DataCubes

Q2: What operations should we support?

Slice



color, size

C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

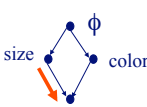
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DataCubes

Q2: What operations should we support?

Dice



color, size

C / S	S	M	L	TOT
Red	20	3	5	28
Blue	3	3	8	14
Gray	0	0	5	5
TOT	23	6	18	47

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DataCubes

Q2: What operations should we support?

- Roll-up
- Drill-down
- Slice
- Dice
- (Pivot/rotate; drill-across; drill-through)
- top N
- moving averages, etc)

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D/W - OLAP - Conclusions

- D/W: copy (summarized) data + analyze
- OLAP - concepts:
 - DataCube
 - R/M/H-OLAP servers
 - ‘dimensions’; ‘measures’

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Outline

- Problem
- Getting the data: Data Warehouses, DataCubes, OLAP
- ➔ • Supervised learning: decision trees
- Unsupervised learning
 - association rules
 - (clustering)

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Decision trees - Problem

Age	Chol-level	Gender	...	CLASS-ID
30	150	M		+
				...
				-

 ??

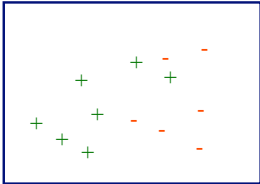
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Decision trees

- Pictorially, we have

num. attr#2
(eg., chol-level)



num. attr#1 (eg., 'age')

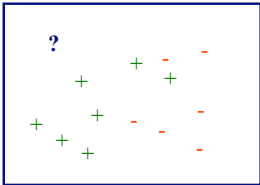
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Decision trees

- and we want to label '?'

num. attr#2
(eg., chol-level)



num. attr#1 (eg., 'age')

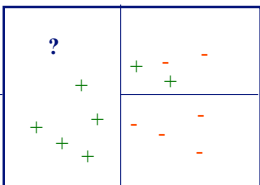
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Decision trees

- so we build a decision tree:

num. attr#2
(eg., chol-level)
40



50
num. attr#1 (eg., 'age')

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Decision trees

- so we build a decision tree:

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Outline

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Decision trees

- Typically, two steps:
 - tree building
 - tree pruning (for over-training/over-fitting)

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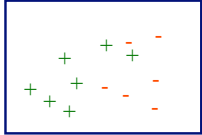
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Tree building

- How?

num. attr#2
(eg., chol-level)



num. attr#1 (eg., 'age')

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Tree building

- How?
- A: Partition, recursively - pseudocode:


```
Partition ( Dataset S)
  if all points in S have same label
  then return
  evaluate splits along each attribute A
  pick best split, to divide S into S1 and S2
  Partition(S1); Partition(S2)
```

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Tree building

- Q1: how to introduce splits along attribute A_i
- Q2: how to evaluate a split?

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Tree building

- Q1: how to introduce splits along attribute A_i
- A1:
 - for num. attributes:
 - binary split, or
 - multiple split
 - for categorical attributes:
 - compute all subsets (expensive!), or
 - use a greedy algo

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Tree building

- Q1: how to introduce splits along attribute A_i
- ➔ • Q2: how to evaluate a split?

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Tree building

- Q1: how to introduce splits along attribute A_i
- ➔ • Q2: how to evaluate a split?
- A: by how close to uniform each subset is - ie., we need a measure of uniformity:

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Tree building

entropy: $H(p_+, p_-)$ Any other measure?

The graph shows a symmetric, inverted U-shaped curve representing the entropy function $H(p_+, p_-)$ over the interval $p_+ \in [0, 1]$. The curve starts at 0 at $p_+ = 0$, reaches its maximum value of 1 at $p_+ = 0.5$, and returns to 0 at $p_+ = 1$. The x-axis is labeled p_+ with ticks at 0, 0.5, and 1. The y-axis has ticks at 0 and 1.

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Tree building

entropy: $H(p_+, p_-)$ 'gini' index: $1 - p_+^2 - p_-^2$

Two graphs are shown side-by-side. Both have p_+ on the x-axis (0 to 1) and a value on the y-axis (0 to 1). The left graph shows the entropy function $H(p_+, p_-)$, which is a symmetric inverted U-shaped curve peaking at 1 when $p_+ = 0.5$. The right graph shows the 'gini' index $1 - p_+^2 - p_-^2$, which is also a symmetric inverted U-shaped curve peaking at 1 when $p_+ = 0.5$.

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Tree building

entropy: $H(p_+, p_-)$ 'gini' index: $1 - p_+^2 - p_-^2$

(How about multiple labels?)

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Tree building

Intuition:

- entropy: #bits to encode the class label
- gini: classification error, if we randomly guess '+' with prob. p_+

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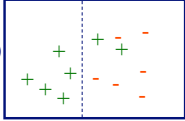

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Tree building


Thus, we choose the split that reduces entropy/classification-error the most: Eg.:

num. attr#2
(eg., chol-level)



num. attr#1 (eg., 'age')

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Tree building

- Before split: we need
 $(n_+ + n_-) * H(p_+, p_-) = (7+6) * H(7/13, 6/13)$
 bits total, to encode all the class labels
- After the split we need:
 - 0 bits for the first half and
 - $(2+6) * H(2/8, 6/8)$ bits for the second half

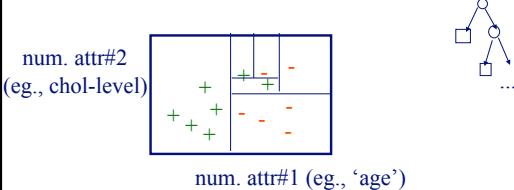
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Tree pruning

- What for?



num. attr#2
(eg., chol-level)

num. attr#1 (eg., 'age')

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Tree pruning

Shortcut for scalability: DYNAMIC pruning:

- stop expanding the tree, if a node is 'reasonably' homogeneous
 - ad hoc threshold [Agrawal+, vldb92]
 - (Minimum Description Language (MDL) criterion (SLIQ) [Mehta+, edbt96])

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Tree pruning

- Q: How to do it?
- A1: use a 'training' and a 'testing' set - prune nodes that improve classification in the 'testing' set. (Drawbacks?)
- (A2: or, rely on MDL (= Minimum Description Language))

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Scalability enhancements

- Interval Classifier [Agrawal+, vldb92]: dynamic pruning
- SLIQ: dynamic pruning with MDL; vertical partitioning of the file (but label column has to fit in core)
- SPRINT: even more clever partitioning


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Conclusions for classifiers

- Classification through trees
- Building phase - splitting policies
- Pruning phase (to avoid over-fitting)
- For scalability:
 - dynamic pruning
 - clever data partitioning


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Outline

- Problem
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Association rules - idea

[Agrawal+SIGMOD93]

- Consider 'market basket' case:
 - (milk, bread)
 - (milk)
 - (milk, chocolate)
 - (milk, bread)
- Find 'interesting things', eg., rules of the form:
 - milk, bread \rightarrow chocolate | 90%

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Association rules - idea

In general, for a given rule
 $I_j, I_k, \dots, I_m \rightarrow I_x \mid c$
 'c' = 'confidence' (how often people buy I_x , given that they have bought I_j, \dots, I_m)
 's' = support: how often people buy I_j, \dots, I_m, I_x

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Association rules - idea

Problem definition:

- given
 - a set of ‘market baskets’ (=binary matrix, of N rows/ baskets and M columns/products)
 - min-support ‘s’ and
 - min-confidence ‘c’
- find
 - all the rules with higher support and confidence

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Association rules - idea

Closely related concept: “large itemset”
 $I_j, I_k, \dots, I_m, I_x$
 is a ‘large itemset’, if it appears more than ‘min-support’ times

Observation: once we have a ‘large itemset’, we can find out the qualifying rules easily (how?)
 Thus, let’s focus on how to find ‘large itemsets’

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Association rules - idea

Naive solution: scan database once; keep $2^{|I|}$ counters
 Drawback?
 Improvement?

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Association rules - idea

Naive solution: scan database once; keep $2^{|I|}$ counters
 Drawback? 2^{1000} is prohibitive...
 Improvement? scan the db $|I|$ times, looking for 1-, 2-, etc itemsets

Eg., for $|I|=3$ items only (A, B, C), we have

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Association rules - idea

first pass

min-sup:10

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Association rules - idea

first pass

min-sup:10

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Association rules - idea

Anti-monotonicity property:
if an itemset fails to be 'large', so will every superset of it (hence all supersets can be pruned)

Sketch of the (famous!) 'a-priori' algorithm
Let $L(i-1)$ be the set of large itemsets with $i-1$ elements
Let $C(i)$ be the set of candidate itemsets (of size i)

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Association rules - idea

Compute $L(1)$, by scanning the database.
repeat, for $i=2,3,\dots$,
 'join' $L(i-1)$ with itself, to generate $C(i)$
 two itemset can be joined, if they agree on their first $i-2$ elements
 prune the itemsets of $C(i)$ (how?)
 scan the db, finding the counts of the $C(i)$ itemsets - set this to be $L(i)$
 unless $L(i)$ is empty, repeat the loop
(see example 6.1 in [Han+Kamber])

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Association rules - Conclusions

Association rules: a new tool to find patterns

- easy to understand its output
- fine-tuned algorithms exist
- still an active area of research

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Overall Conclusions

- Data Mining: of high commercial interest
- DM = DB+ ML+ Stat
- Data warehousing / OLAP: to get the data
- Tree classifiers (SLIQ, SPRINT)
- Association Rules - 'a-priori' algorithm
- (clustering: BIRCH, CURE, OPTICS)

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Reading material

- Agrawal, R., T. Imielinski, A. Swami, '*Mining Association Rules between Sets of Items in Large Databases*', SIGMOD 1993.
- M. Mehta, R. Agrawal and J. Rissanen, '*SLIQ: A Fast Scalable Classifier for Data Mining*', Proc. of the Fifth Int'l Conference on Extending Database Technology (EDBT), Avignon, France, March 1996

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Additional references

- Agrawal, R., S. Ghosh, et al. (Aug. 23-27, 1992). *An Interval Classifier for Database Mining Applications*. VLDB Conf. Proc., Vancouver, BC, Canada.
- Jiawei Han and Micheline Kamber, *Data Mining*, Morgan Kaufman, 2001, chapters 2.2-2.3, 6.1-6.2, 7.3.5

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