

CMU SCS

## 15-826: Multimedia Databases and Data Mining

Lecture #22: Multimedia indexing  
*C. Faloutsos*

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## Must-read Material

- [Textbook](#), chapters 7, 8, 9 and 10.
- Myron Flickner, et al:  
[Query by Image and Video Content: the OBIC System](#)  
IEEE Computer 28, 9, Sep. 1995, pp. 23-32.
- [Journal of Intelligent Inf. Systems, 3, 3/4, pp. 231-262, 1994](#) (An earlier, more technical version of the IEEE Computer '95 paper.)
- FastMap: [Textbook](#) chapter 11; Also in: C. Faloutsos and K.I. Lin *FastMap: A Fast Algorithm for Indexing, Data-Mining and Visualization of Traditional and Multimedia Datasets* ACM SIGMOD 95, pp. 163-174.

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## Outline

Goal: 'Find similar / interesting things'

- Intro to DB
- ➔ • Indexing - similarity search
- Data Mining

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## Indexing - Detailed outline

- primary key indexing
- secondary key / multi-key indexing
- spatial access methods
- fractals
- text
- Singular Value Decomposition (SVD)
- ➔ • multimedia
- ...

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## Multimedia - Detailed outline

- multimedia
- ➔ – Motivation / problem definition
- Main idea / time sequences
- images
- sub-pattern matching
- automatic feature extraction / FastMap

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## Problem

Given a large collection of (multimedia) records (eg. stocks)

Allow fast, similarity queries

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## Applications

- time series: financial, marketing (click-streams!), ECGs, sound;
- images: medicine, digital libraries, education, art
- higher-d signals: scientific db (eg., astrophysics), medicine (MRI scans), entertainment (video)

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## Sample queries

- find medical cases similar to Smith's
- Find pairs of stocks that move in sync
- Find pairs of documents that are similar (plagiarism?)
- find faces similar to 'Tiger Woods'

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## Detailed problem defn.:

Problem:

- given a set of multimedia objects,
- find the ones similar to a desirable query object

• for example:

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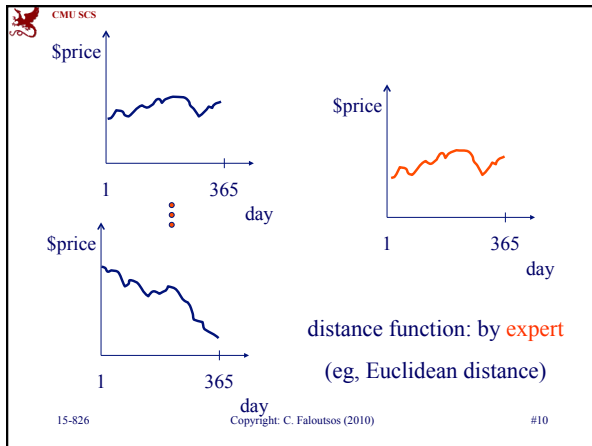
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**Types of queries**

- whole match vs sub-pattern match
- range query vs nearest neighbors
- all-pairs query

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**Design goals**

- Fast (faster than seq. scan)
- ‘correct’ (ie., no false alarms; no false dismissals)

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## Multimedia - Detailed outline

- multimedia
  - Motivation / problem definition
  - ➔ - Main idea / time sequences
  - images
  - sub-pattern matching
  - automatic feature extraction / FastMap

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## Main idea

- Eg., time sequences, 'whole matching', range queries, Euclidean distance

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## Main idea

- Seq. scanning works - how to do faster?

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## Idea: 'GEMINI'

(GEneric Multimedia INdexIng)  
 Extract a few numerical features, for a 'quick and dirty' test

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## 'GEMINI' - Pictorially

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## GEMINI

Solution: 'Quick-and-dirty' filter:

- extract  $n$  features (numbers, eg., avg., etc.)
- map into a point in  $n$ -d feature space
- organize points with off-the-shelf spatial access method ('SAM')
- discard false alarms

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## GEMINI

Important: Q: how to guarantee no false dismissals?

A1: preserve distances (but: difficult /impossible)

A2: Lower-bounding lemma: if the mapping ‘makes things look closer’, then there are no false dismissals

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## GEMINI

Important:

Q: how to extract features?

A: “*if I have only one number to describe my object, what should this be?*”

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## Time sequences

Q: what features?

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## Time sequences

Q: what features?  
 A: Fourier coefficients (we'll see them in detail soon)

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## Time sequences

white noise      brown noise

Fourier spectrum  
 ... in log-log

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## Time sequences

- Eg.:

(a) IBM stock      (b) spectrum (linear scales)      (c) spectrum (log scales)

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## Time sequences

- conclusion: colored noises are well approximated by their first few Fourier coefficients
- colored noises appear in nature:

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## Time sequences

- brown noise: stock prices ( $1/f^2$  energy spectrum)
- pink noise: works of art ( $1/f$  spectrum)
- black noises: water reservoirs ( $1/f^b$ ,  $b > 2$ )
- (slope: related to 'Hurst exponent', for self-similar traffic, like, eg. Ethernet/web [Schroeder], [Leland+])

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## Time sequences - results

- keep the first 2-3 Fourier coefficients
- faster than seq. scan
- NO false dismissals (see book)

The graph plots 'time' on the y-axis against '# coeff. kept' on the x-axis. Three lines are shown: 'total' (top), 'cleanup-time' (middle), and 'r-tree time' (bottom). All three lines show a decreasing trend as the number of coefficients kept increases, with 'total' time being the highest and 'r-tree time' being the lowest.

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## Time sequences - improvements:

- improvements/variations: [Kanellakis+Goldin], [Mendelzon+Rafiei]
- could use Wavelets, or DCT
- could use segment averages [Yi+2000]

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## Multimedia - Detailed outline

- multimedia
  - Motivation / problem definition
  - Main idea / time sequences
  - ➔ – images (color, shapes)
  - sub-pattern matching
  - automatic feature extraction / FastMap

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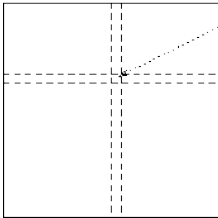
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## Images - color

what is an image?  
A: 2-d array

COLOR IMAGE, eg. 256x256



i-th pixel:  
(r, g, b)

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## Images - color

Color histograms, and distance function

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## Images - color

Mathematically, the distance function is:

$$distance_{histogram}(\vec{x}, \vec{q}) = (\vec{x} - \vec{q}) \begin{bmatrix} a_{RR} & a_{RP} & \dots \\ a_{PR} & a_{PP} & \dots \\ \dots & \dots & \dots \end{bmatrix} (\vec{x} - \vec{q})^t$$

$$\dots = (\vec{x} - \vec{q}) A (\vec{x} - \vec{q})^t$$

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## Images - color

Problem: ‘cross-talk’:

- Features are not orthogonal ->
- SAMs will not work properly
  
- Q: what to do?
- A: feature-extraction question

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## Images - color

possible answers:

- avg red, avg green, avg blue

it turns out that this lower-bounds the histogram distance ->

- no cross-talk
- SAMs are applicable

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## Images - color

performance: time

selectivity

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## Multimedia - Detailed outline

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  - sub-pattern matching
  - automatic feature extraction / FastMap

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### Images - shapes

- distance function: Euclidean, on the area, perimeter, and 20 'moments'
- (Q: how to normalize them?)

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### Images - shapes

- distance function: Euclidean, on the area, perimeter, and 20 'moments'
- (Q: how to normalize them?)
- A: divide by standard deviation)

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### Images - shapes

- distance function: Euclidean, on the area, perimeter, and 20 'moments'
- (Q: other 'features' / distance functions?)

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### Images - shapes

- distance function: Euclidean, on the area, perimeter, and 20 ‘moments’
- (Q: other ‘features’ / distance functions?
- A1: turning angle
- A2: dilations/erosions
- A3: ... )

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### Images - shapes

- distance function: Euclidean, on the area, perimeter, and 20 ‘moments’
- Q: how to do dim. reduction?

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### Images - shapes

- distance function: Euclidean, on the area, perimeter, and 20 ‘moments’
- Q: how to do dim. reduction?
- A: Karhunen-Loeve (= centered PCA/SVD)

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## Images - shapes

- Performance: ~10x faster

log(# of I/Os)

# of features kept

← all kept

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## Other shape features?

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## Other shape features

- Morphology (dilations, erosions, openings, closings) [Korn+, VLDB96]

shape

“structuring element”

R=1 ●

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### Other shape features

- Morphology (dilations, erosions, openings, closings) [Korn+, VLDB96]

shape



“structuring element”

R=0.5 ●

R=1 ●

R=2 ●

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### Other shape features

- Morphology (dilations, erosions, openings, closings) [Korn+, VLDB96]

shape



“structuring element”

R=0.5 |

R=1 |

R=2 |

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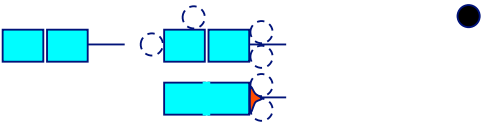
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### Morphology: closing

- fill in small gaps
- very similar to ‘alpha contours’



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### Morphology: closing

- fill in small gaps

'closing',  
with  $R=1$

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### Morphology: opening

- 'closing', for the complement =
- trim small extremities

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### Morphology: opening

- 'closing', for the complement =
- trim small extremities

'opening'  
with  $R=1$

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## Morphology

- Closing: fills in gaps 
- Opening: trims extremities 
- All wrt a structuring element: 

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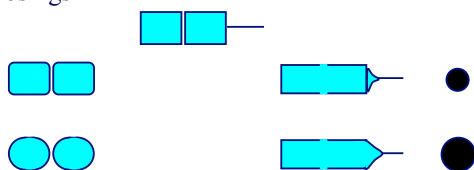
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## Morphology

- Features: areas of openings ( $R=1, 2, \dots$ ) and closings 

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## Multimedia - Detailed outline

- multimedia
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  - images (color; shape)
  - ➔ sub-pattern matching
  - automatic feature extraction / FastMap

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## Sub-pattern matching

- Problem: find **sub**-sequences that match the given query pattern

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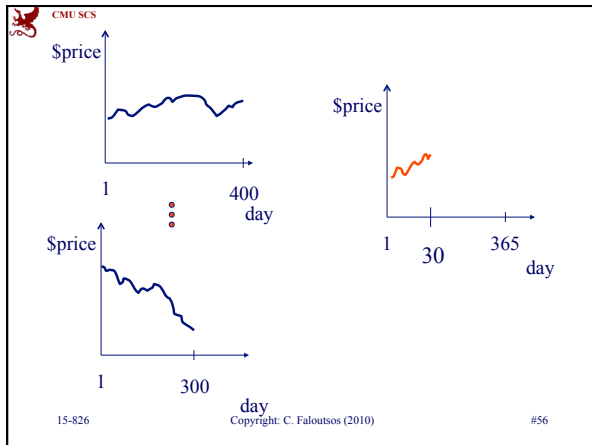
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## Sub-pattern matching

- Q: how to proceed?
- Hint: try to turn it into a 'whole-matching' problem (how?)

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## Sub-pattern matching

- Assume that queries have minimum duration  $w$ ; (eg.,  $w=7$  days)
- divide data sequences into windows of width  $w$  (overlapping, or not?)

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## Sub-pattern matching

- Assume that queries have minimum duration  $w$ ; (eg.,  $w=7$  days)
- divide data sequences into windows of width  $w$  (overlapping, or not?)
- A: sliding, overlapping windows. Thus: trails Pictorially:

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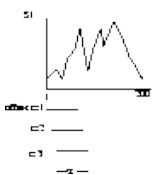

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## Sub-pattern matching

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### Sub-pattern matching

sequences  $\rightarrow$  trails  $\rightarrow$  MBRs in feature space

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### Sub-pattern matching

Q: do we store all points? why not?

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### Sub-pattern matching

Q: how to do range queries of duration  $w$ ?

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### Sub-pattern matching

Q: how to do range queries of duration  $w$ ?  
A: R-tree; find qualifying stocks and intervals

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### Sub-pattern matching

Q: how to do range queries of duration  $w$ ?  
A: R-tree; find qualifying stocks and intervals

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### Sub-pattern matching

Q: how to do range queries of duration  $>w$  (say,  $2*w$ )?

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### Sub-pattern matching

Q: how to do range queries of duration  $>w$  (say,  $2*w$ )?  
 A: Two range queries of radius epsilon and intersect  
 (or two queries of smaller radius and union – see paper)

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### Sub-pattern matching

(improvement [Moon+2001])

- use non-overlapping windows, for data

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### Conclusions

- GEMINI works for any setting (time sequences, images, etc)
- uses a ‘quick and dirty’ filter
- faster than seq. scan
- (but: how to extract features automatically?)

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## Multimedia - Detailed outline

- multimedia
  - Motivation / problem definition
  - Main idea / time sequences
  - images (color; shape)
  - sub-pattern matching
  - ➔ automatic feature extraction / FastMap

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## FastMap

Automatic feature extraction:

- Given a dissimilarity function of objects
- Quickly map the objects to a (k-d) 'feature' space.
- (goals: indexing and/or visualization)

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## FastMap

	O1	O2	O3	O4	O5
O1	0	1	1	100	100
O2	1	0	1	100	100
O3	1	1	0	100	100
O4	100	100	100	0	1
O5	100	100	100	1	0

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## FastMap

- Multi-dimensional scaling (MDS) can do that, but in  $O(N^2)$  time

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## MDS

Multi Dimensional Scaling

The diagram shows a set of points in a 2D space. A point labeled 'T' is shown in two positions: a solid grey dot and an open circle. Arrows indicate distances between various points, including the two positions of 'T'. The text 'Multi Dimensional Scaling' is written to the left of the diagram.

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## Main idea: projections

We want a **linear** algorithm: FastMap [SIGMOD95]

The diagram shows a triangle with vertices  $O_a$ ,  $O_b$ , and  $O_i$ . A vertical dashed line from  $O_i$  to the base  $O_a O_b$  is labeled  $E$ . The distance from  $O_a$  to  $O_i$  is  $d_{ai}$ , and from  $O_b$  to  $O_i$  is  $d_{bi}$ . The distance from  $O_a$  to the projection of  $O_i$  on the base is  $x_i$ . The total distance from  $O_a$  to  $O_b$  is  $d_{ab}$ .

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## FastMap - next iteration

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## Results

Documents /cosine similarity ->  
Euclidean distance (how?)

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## Results

bb reports

recipes

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## Applications: time sequences

- given  $n$  co-evolving time sequences
- visualize them + find rules [ICDE00]

rate

time

GBP

JPY

HKD

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## Applications - financial

- currency exchange rates [ICDE00]

USD(t)

USD(t-5)

FRF

DEM

JPY

GBP

HKD

USD

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## Video Trails

[ACM MM97]

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St. Louis

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## Variations

- Isomap [Tenenbaum, de Silva, Langford, 2000]
- LLE (Local Linear Embedding) [Roweis, Saul, 2000]
- MVE (Minimum Volume Embedding) [Shaw & Jebara, 2007]



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## Variations

- Isomap [Tenenbaum, de Silva, Langford, 2000]
- LLE (Local Linear Embedding) [Roweis, Saul, 2000]
- MVE (Minimum Volume Embedding) [Shaw & Jebara, 2007]



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## Conclusions

- GEMINI works for multiple settings
- FastMap can extract ‘features’ automatically (-> indexing, visual d.m.)

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