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## 15-826: Multimedia Databases and Data Mining

*Spatial Access Methods - V*  
*Metric trees, knn methods*  
C. Faloutsos

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## Outline

Goal: 'Find similar / interesting things'

- Intro to DB
- ➔ • Indexing - similarity search
- Data Mining

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## Indexing - Detailed outline

- primary key indexing
- secondary key / multi-key indexing
- spatial access methods
  - problem defn
  - z-ordering
  - R-trees
  - misc
- ➔ • fractals
- text

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## SAMs - Detailed outline

- spatial access methods
  - problem defn
  - z-ordering
  - R-trees
  - misc topics
    - grid files
    - dimensionality curse; dim. reduction
    - metric trees
    - other nn methods
- fractals
- text, ...

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## Metric trees

- What if we only have a distance function  $d(o_1, o_2)$ ?
- (Applications?)

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## Metric trees

- (assumption:  $d()$  is a metric: positive; symmetric; triangle inequality)
- then, we can use some variation of ‘Vantage Point’ trees [Yannilos]
- many variations (GNAT trees [Brin95], MVP-trees [Ozsoyoglu+] ...)

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### Metric trees

- Finally: M-trees [Ciaccia, Patella, Zezula, vldb 97]
- M-trees = 'ball-trees': groups in spheres



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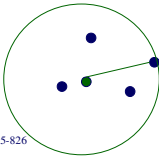
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### Metric trees

- Finally: M-trees [Ciaccia, Patella, Zezula, vldb 97]
- M-trees = 'ball-trees': Minimum Bounding spheres



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### Metric trees

- Search (range and k-nn): like R-trees
- Split?

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## Metric trees

- Search (range and k-nn): like R-trees
- Split? Several criteria:
  - minimize max radius (or sum radii)
  - (even: random!)
- Algorithm?

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## Metric trees

- Search (range and k-nn): like R-trees
- Split? Several criteria:
  - minimize max radius (or sum radii)
  - (even: random!)
- Algorithm?
- eg., similar to the quadratic split of Guttman

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## Metric trees - variations

- Slim trees [Traina+, EDBT2000]
- OMNI tree [Filho+, ICDE2001]

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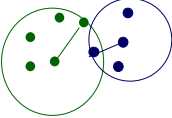
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### Metric trees - Slim trees

- How to improve the structure?

BEFORE



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### Metric trees - Slim trees

- Idea: give-away contents, if it decreases the radius - eg:

BEFORE      AFTER



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### Metric trees - Slim trees

- How to accelerate the splitting time ( $O(N^2)$ , currently)?



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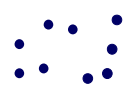
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### Metric trees - Slim trees

- Split using Minimum Spanning Tree (drop longest edge)



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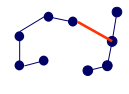
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### Metric trees - Slim trees

- Split using Minimum Spanning Tree (drop longest edge)



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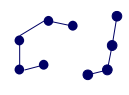
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### Metric trees - Slim trees

- Split using Minimum Spanning Tree (drop longest edge)



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## Metric trees - Slim trees

- result: at least as fast as M-trees for search
- MST: significantly faster for split, with tiny performance penalty

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## SAMs - Detailed outline

- spatial access methods
  - problem defn
  - z-ordering
  - R-trees
  - misc topics
    - grid files
    - dimensionality curse; dim. reduction
    - metric trees
    - other nn methods
- fractals
- text, ...

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## Metric trees - OMNI trees

- How to turn objects into vectors?
- (assume that distance computations are expensive; we need to answer range/nn queries quickly)

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### Metric trees - OMNI trees

- How to turn objects into vectors?
- A: pick  $n$  'anchor' objects; record the distance of each object from them  $\rightarrow n$ -d vector



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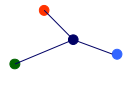
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### Metric trees - OMNI trees

- How to turn objects into vectors?
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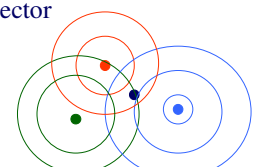
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### Metric trees - OMNI trees

- How to turn objects into vectors?
- A: pick  $n$  'anchor' objects; record the distance of each object from them  $\rightarrow n$ -d vector



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### Metric trees - OMNI trees

- we could put OMNI coordinates in R-tree (or other SAM, or even do seq. scan)
- and still answer range and mn queries! (see [Filho'01] for details)

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### Metric trees - OMNI trees

- Result: faster than M-trees and seq. scanning (especially if distance computations are expensive)

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### Metric trees - OMNI trees

- Q1: how to choose anchors?
- Q2: ... and how many?

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    - other nn methods
- fractals
- text, ...

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## Other nn methods

- Problem#1: vector space
- Problem#2: metric space

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## Other nn methods - vector space

- Solution#1: k-d trees (or R-trees etc)
- Solution#2: Constant time??

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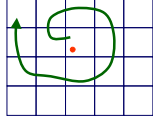
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### Other nn methods - vector space

- Solution#1: k-d trees (or R-trees etc)
- Solution#2: Spiral search - put a grid; spiral out (O(1) on the average, but: exp(?) on dimension) [Bentley+, 80]



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### Other nn methods - vector space

- what if we have no index (grid / kd-tree / R-tree)?

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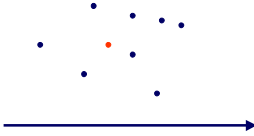
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### Other nn methods - vector space

- what if we have no index (grid / kd-tree / R-tree)?
- Solution#3: [Friedman+75] Project on 1-d & sort



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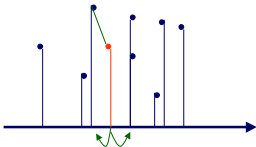
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### Other nn methods - vector space

- what if we have no index (grid / kd-tree / R-tree)?
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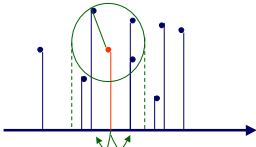
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### Other nn methods - vector space

- what if we have no index (grid / kd-tree / R-tree)?
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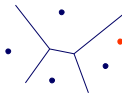
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### Other nn methods - vector space

- Solution#4: Voronoi diagrams (eg., [Aurenhammer '91])



- mainly, in comp. geometry
- tricky for  $\geq 3$  dimensions

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### Other nn methods

- Problem#1: vector space
- ➔ • Problem#2: metric space

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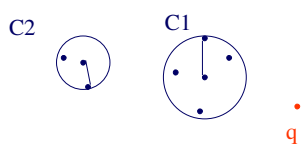
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### Other nn methods - metric space

- Solution#1: Branch+Bound [Fukunaga+, '73]. Very similar to nn in M-trees:



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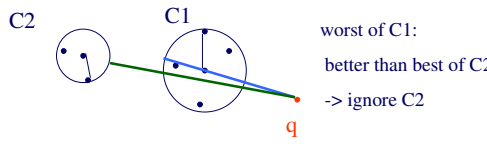
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### Other nn methods - metric space

- Solution#1: Branch+Bound [Fukunaga+, '73]. Identical to nn in M-trees:



worst of C1:  
better than best of C2  
-> ignore C2

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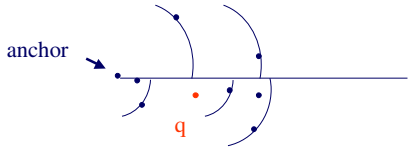
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### Other nn methods - metric space

- Solution#2: Anchor points [Burkhard+, 73]



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### Other nn methods - metric space

- Solution#2: Anchor points [Burkhard+, 73]
- variations: [Shapiro, '77], [Shasha+, '90]
- related to metric trees

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### Conclusions

- Metric trees (= “sphere/ball trees”) for metric spaces
  - M-trees / OMNI-trees
- several clever methods for nn search
  - branch + bound
  - anchors

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## SAMs - Detailed outline

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## Conclusions for SAMs

- z-ordering and R-trees for low-d points and regions
- M-trees & variants for metric datasets
- beware of the 'dimensionality curse'

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## References

- Aurenhammer, F. (Sept. 1991). "Voronoi Diagrams - A Survey of a Fundamental Geometric Data Structure." ACM Computing Surveys 23(3): 345-405.
- Bentley, J. L., B. W. Weide, et al. (Dec. 1980). "Optimal Expected-Time Algorithms for Closest Point Problems." ACM Trans. on Mathematical Software (TOMS) 6(4): 563-580.
- Burkhard, W. A. and R. M. Keller (Apr. 1973). "Some Approaches to Best-Match File Searching." Comm. of the ACM (CACM) 16(4): 230-236.

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## References

- Christian Böhm, Stefan Berchtold, Daniel A. Keim: *Searching in high-dimensional spaces: Index structures for improving the performance of multimedia databases*. ACM Comput. Surv. 33(3): 322-373 (2001)
- Edgar Chávez, Gonzalo Navarro, Ricardo A. Baeza-Yates, José L. Marroquín: *Searching in metric spaces*. ACM Comput. Surv. 33(3): 273-321 (2001)

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## References

- Ciaccia, P., M. Patella, et al. (1997). M-tree: An Efficient Access Method for Similarity Search in Metric Spaces. VLDB.
- Filho, R. F. S., A. Traina, et al. (2001). Similarity search without tears: the OMNI family of all-purpose access methods. ICDE, Heidelberg, Germany.
- Friedman, J. H., F. Baskett, et al. (Oct. 1975). "An Algorithm for Finding Nearest Neighbors." IEEE Trans. on Computers (TOC) C-24: 1000-1006.

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## References

- Fukunaga, K. and P. M. Narendra (July 1975). "A Branch and Bound Algorithm for Computing k-Nearest Neighbors." IEEE Trans. on Computers (TOC) C-24(7): 750-753.
- Shapiro, M. (May 1977). "The Choice of Reference Points in Best-Match File Searching." Comm. of the ACM (CACM) 20(5): 339-343.

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### References

- Shasha, D. and T.-L. Wang (Apr. 1990). "New Techniques for Best-Match Retrieval." ACM TOIS 8(2): 140-158.
- Traina, C., A. J. M. Traina, et al. (2000). Slim-Trees: High Performance Metric Trees Minimizing Overlap Between Nodes. EDBT, Konstanz, Germany.

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