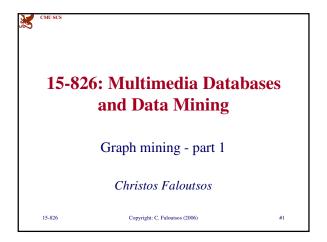
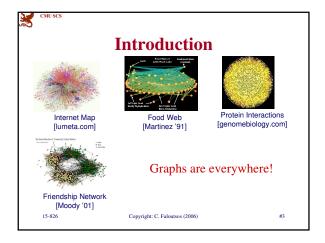
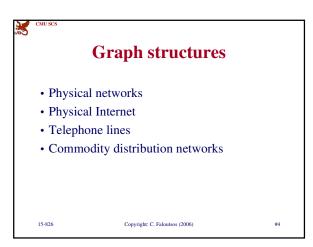
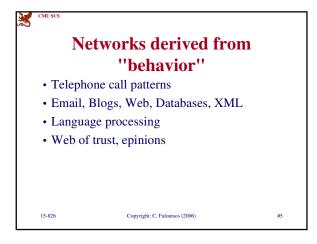
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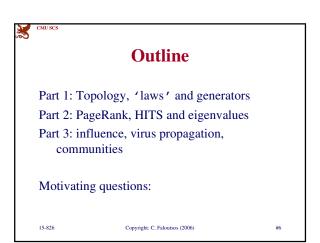












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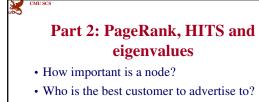


Part 1: Topology and generators

- What do real graphs look like?
- What properties of nodes, edges are important to model?
- What local and global properties are important to measure?
- How to model and generate realistic graphs?

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Part 3: influence and communities

- How do nodes influence their neighbors?
- How do viruses propagate?

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PART 1: Topology, laws and generators

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Outline

Part 1: Topology, 'laws' and generators

- · 'Laws' and patterns
- Generators
- Tools

Part 2: PageRank, HITS and eigenvalues

Part 3: Influence, viruses, communities

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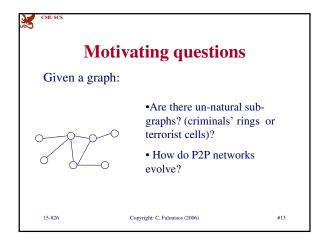


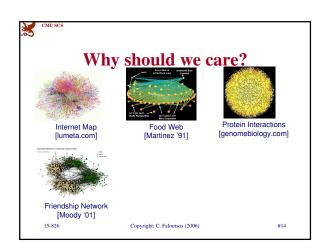
Motivating questions

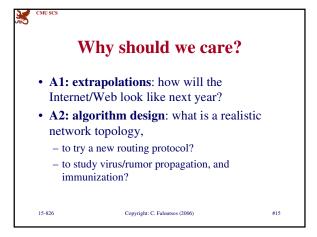
- What do real graphs look like?
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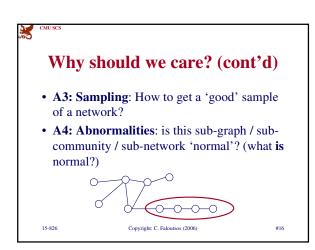
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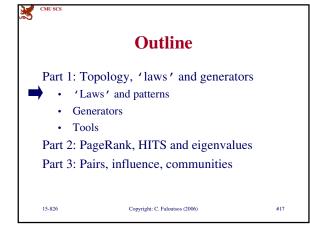
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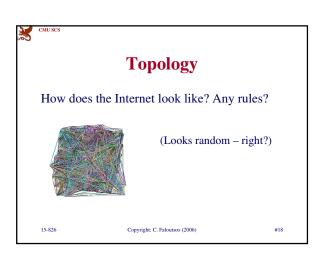




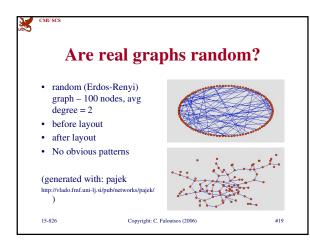


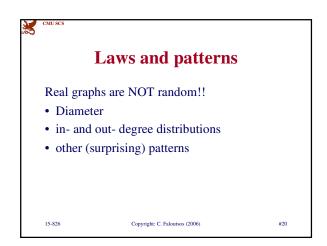


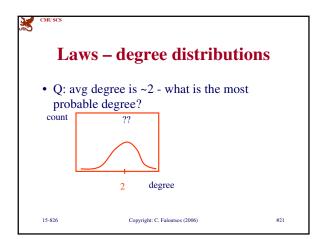


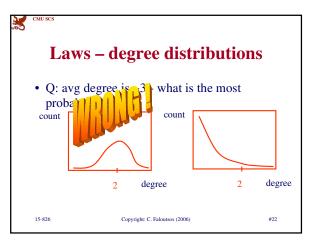


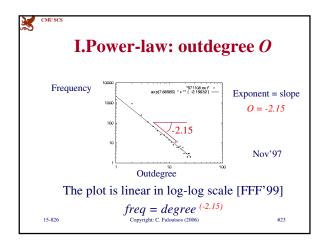
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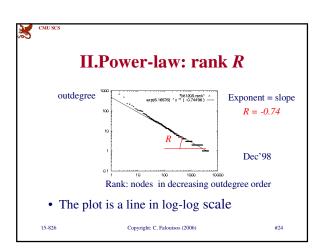


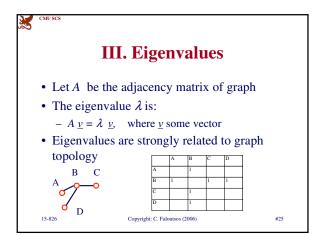


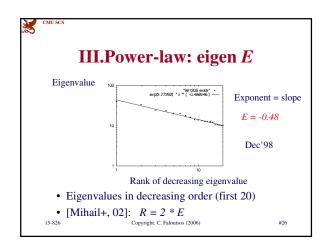












IV. The Node Neighborhood

• N(h) = # of pairs of nodes within h hops

IV. The Node Neighborhood
Q: average degree = 3 - how many neighbors should I expect within 1,2,... h hops?
Potential answer:

1 hop -> 3 neighbors
2 hops -> 3 * 3
...
h hops -> 3h

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IV. The Node Neighborhood

• Q: average degree = 3 - how many neighbors should I expect within 1,2,... h hops?

• Potential answer:

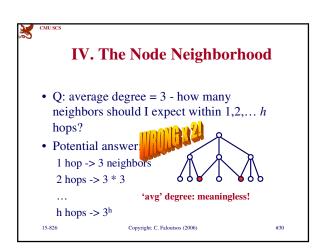
1 hop -> 3 neighbors
2 hops -> 3 * 3
...

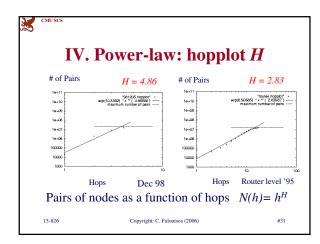
WE HAVE DUPLICATES!
h hops -> 3h

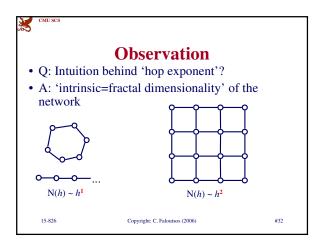
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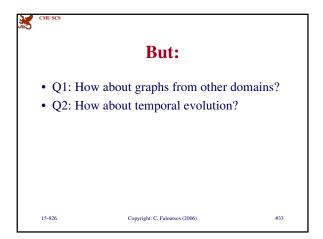
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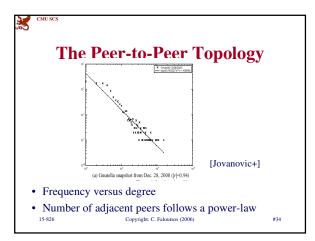
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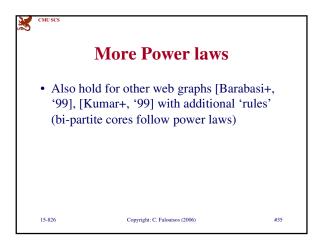


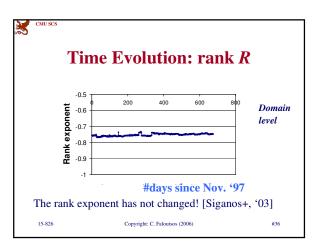


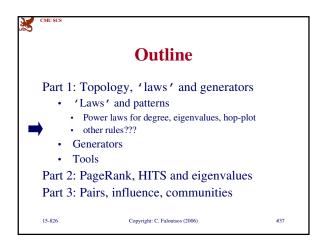


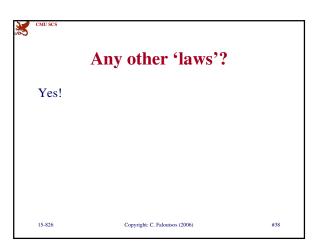


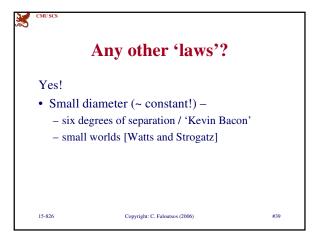


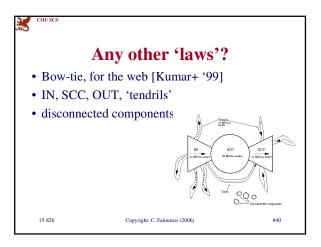


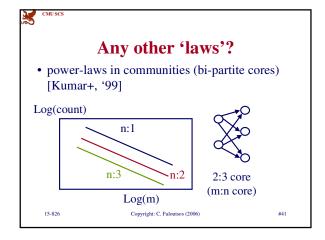


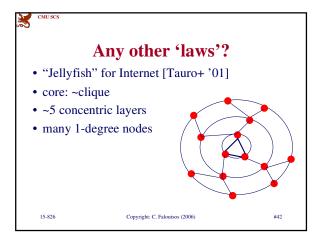


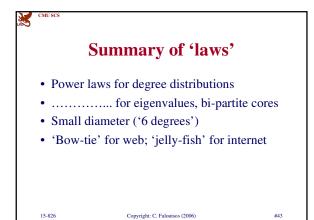


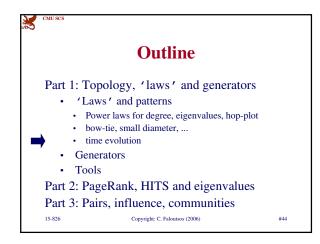


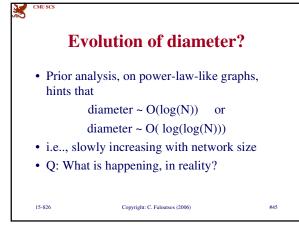


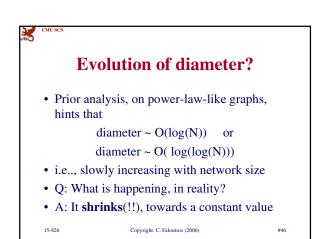


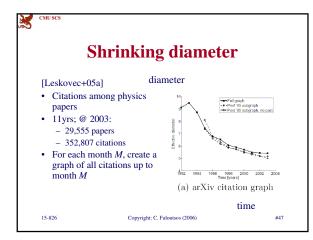


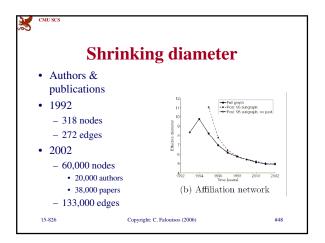


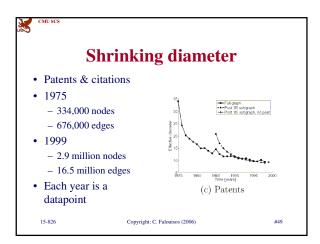


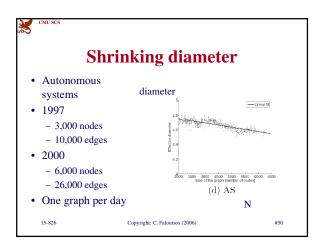


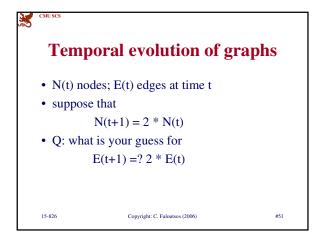


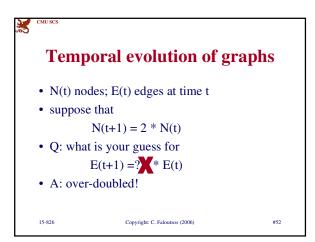


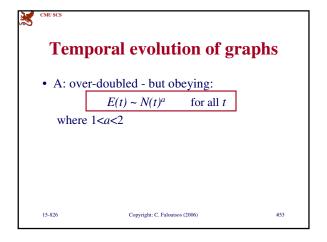


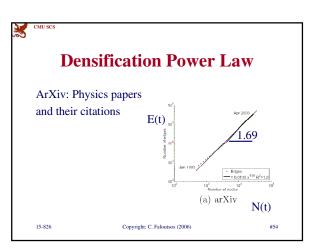


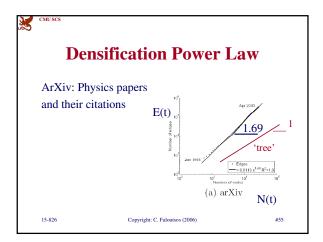


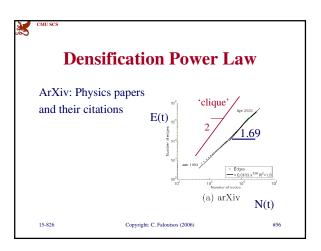


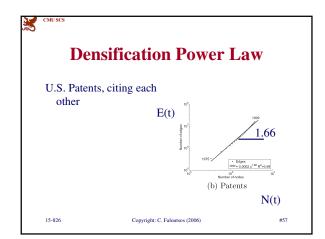


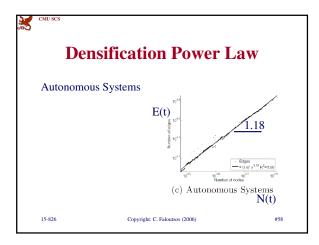


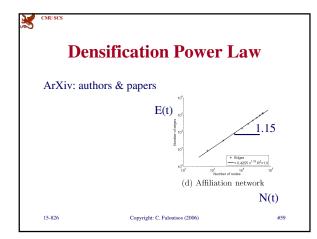


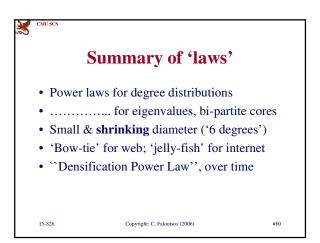


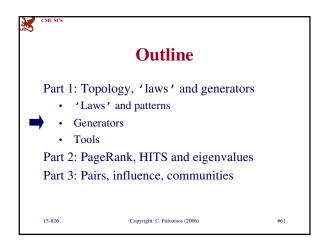


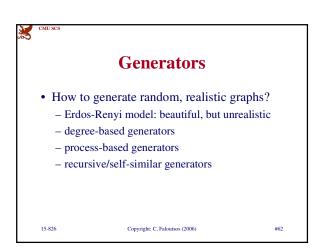


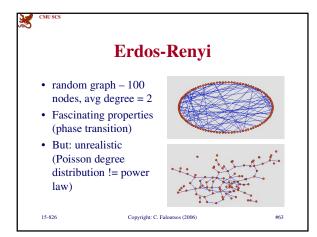


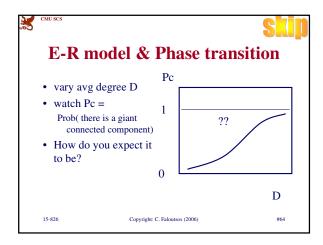


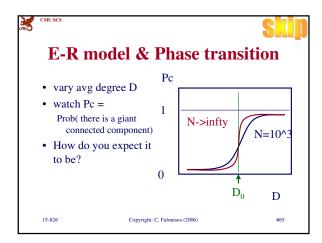


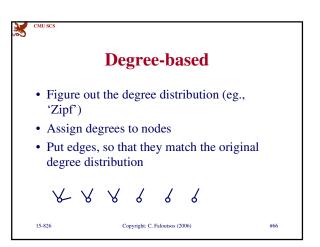






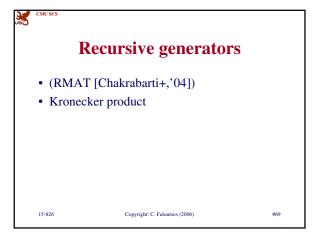




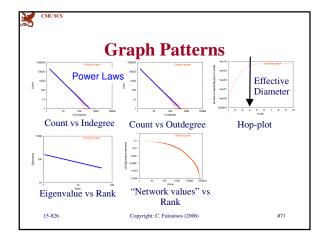






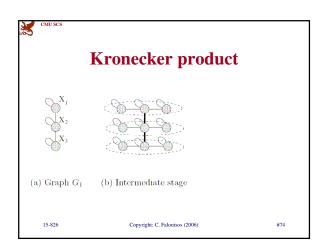


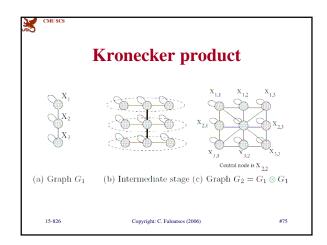


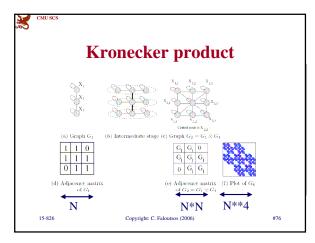


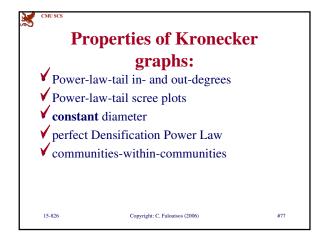


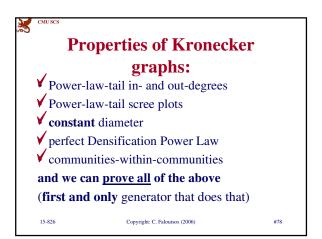


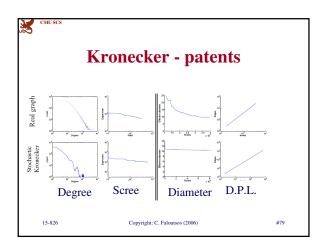


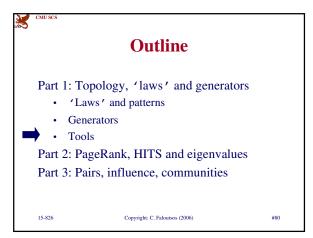


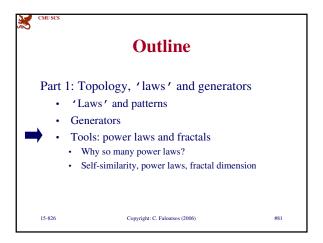


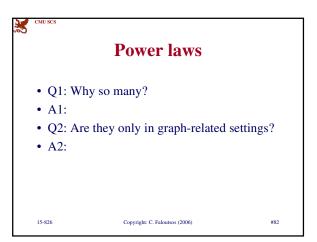


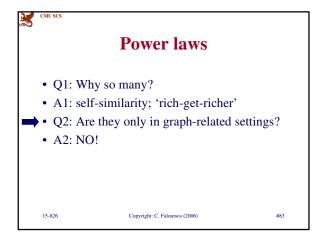


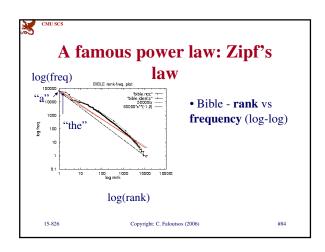


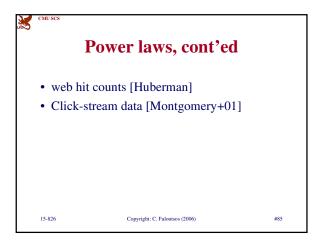


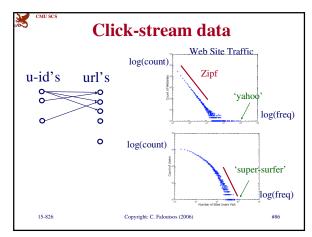


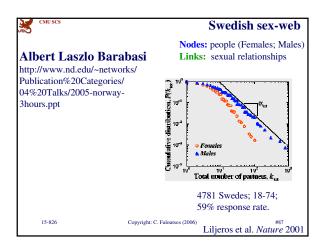


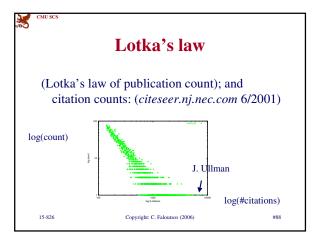


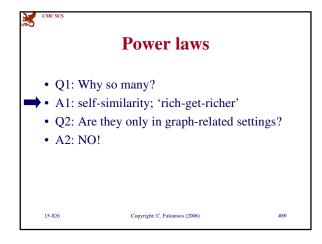


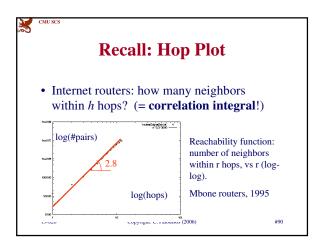


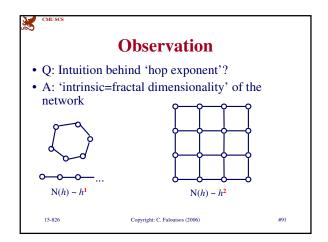


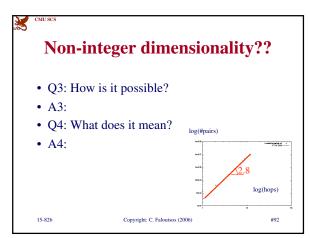












Non-integer dimensionality

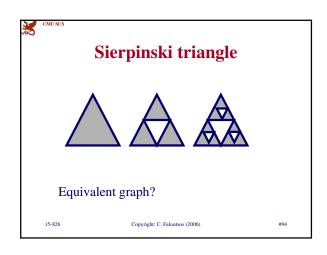
• Q3: How is it possible?

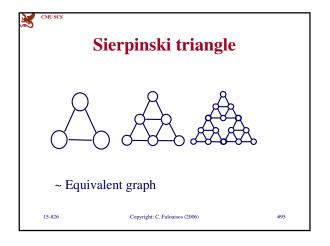
• A3: Through recursion!

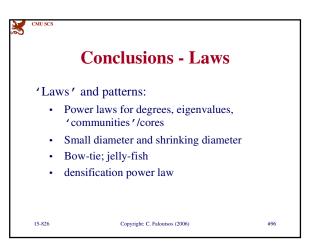
• Q4: What does it mean?

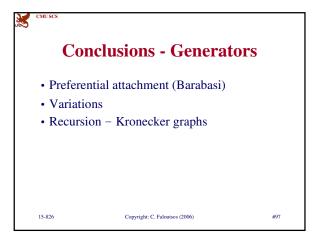
• A4: There are groups (quasi-cliques / communities) in every scale

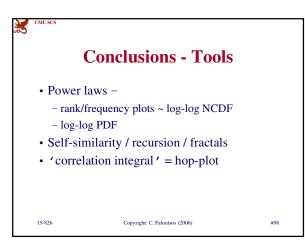
For example, Sierpinski triangle:

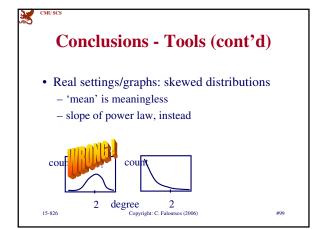


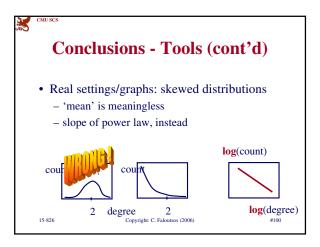


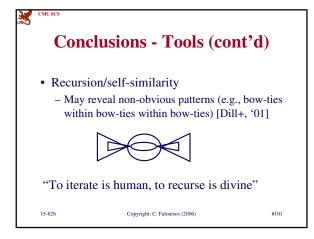


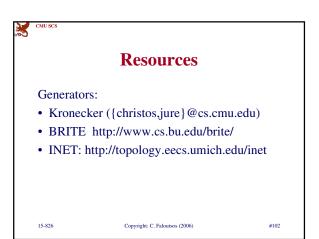












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Other resources

Visualization - graph algo's:

- Graphviz: http://www.graphviz.org/
- pajek: http://vlado.fmf.unilj.si/pub/networks/pajek/

Kevin Bacon web site: http://www.cs.virginia.edu/oracle/

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