

Motivation - Applications
(cont'd)

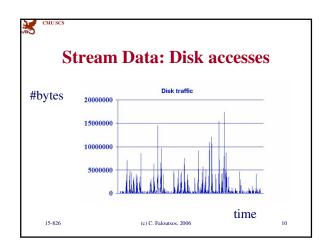
• Computer systems

- 'Active Disks' (buffering, prefetching)

- web servers (ditto)

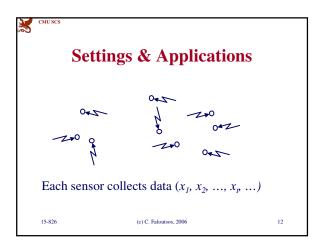
- network traffic monitoring

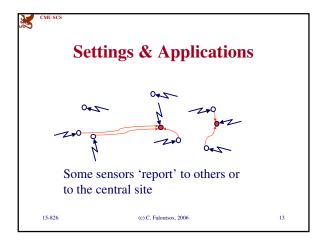
- ...

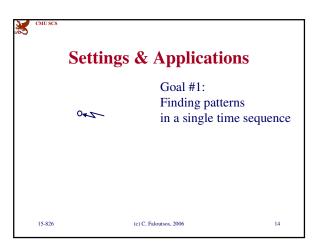


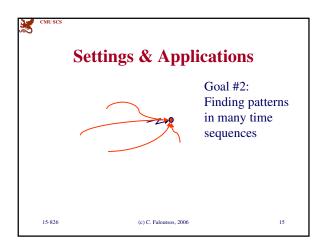
Settings & Applications

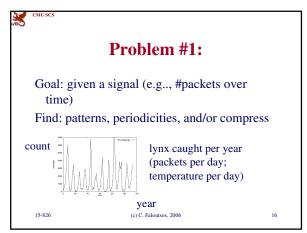
• One or more sensors, collecting time-series data

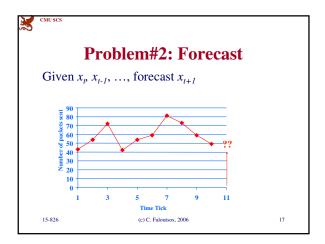


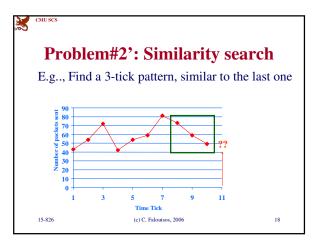


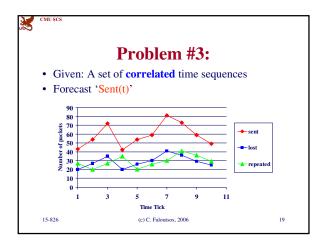


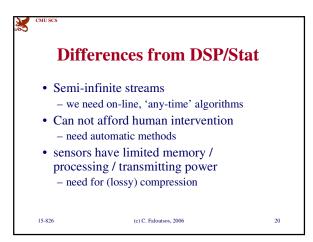












Important observations

Patterns, rules, forecasting and similarity indexing are closely related:

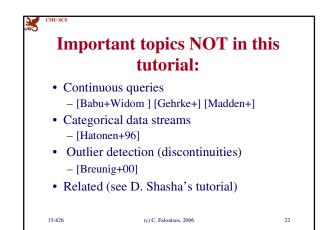
• To do forecasting, we need

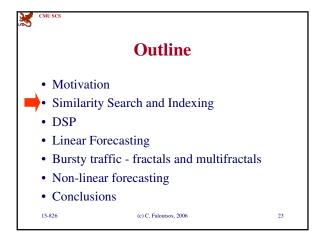
– to find patterns/rules

– to find similar settings in the past

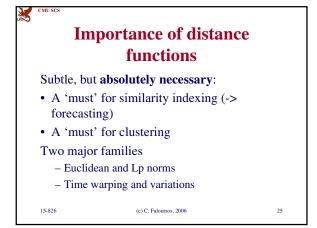
• to find outliers, we need to have forecasts

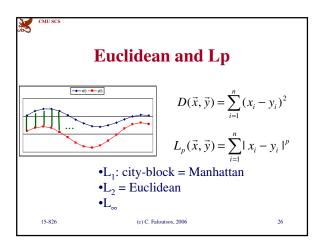
– (outlier = too far away from our forecast)

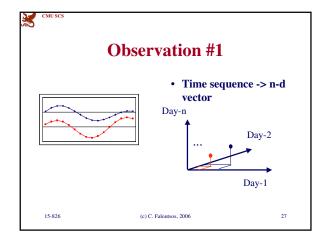


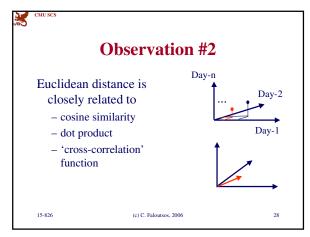


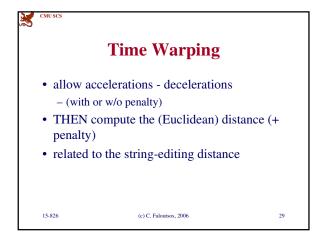


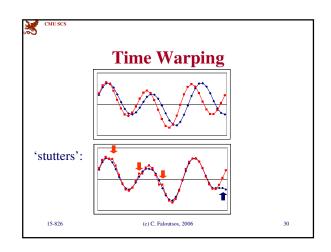














Time warping

Q: how to compute it?

A: dynamic programming

D(i, j) = cost to match

prefix of length i of first sequence x with prefix of length j of second sequence y

15-826

(c) C. Faloutsos, 2006

CMU SO

Time warping

Thus, with no penalty for stutter, for sequences

$$x_1, x_2, ..., x_{i,:}$$
 $y_1, y_2, ..., y_i$

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$$D(i,j) = \|x[i] - y[j]\| + \min \begin{cases} D(i-1,j-1) & \text{no stutter} \\ D(i,j-1) & \text{x-stutter} \\ D(i-1,j) & \text{y-stutter} \end{cases}$$

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CMU:

Time warping

VERY SIMILAR to the string-editing distance

$$D(i, j) = \|x[i] - y[j]\| + \min \begin{cases} D(i-1, j-1) & \text{no stutter} \\ D(i, j-1) & \text{x-stutter} \\ D(i-1, j) & \text{y-stutter} \end{cases}$$

15-826 (c) C. Faloutsos, 2006



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Time warping

- Complexity: O(M*N) quadratic on the length of the strings
- Many variations (penalty for stutters; limit on the number/percentage of stutters; ...)
- popular in voice processing [Rabiner+Juang]

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MU SCS

Other Distance functions

- piece-wise linear/flat approx.; compare pieces [Keogh+01] [Faloutsos+97]
- 'cepstrum' (for voice [Rabiner+Juang])
 do DFT; take log of amplitude; do DFT again!
- Allow for small gaps [Agrawal+95] See tutorial by [Gunopulos Das, SIGMOD01]

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(c) C. Faloutsos, 2006

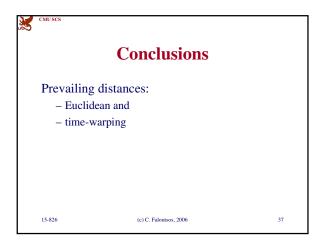
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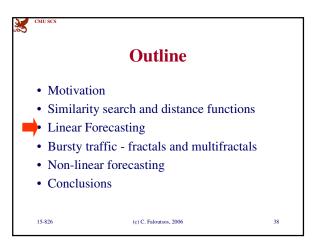
Other Distance functions

• recently: parameter-free, MDL based [Keogh, KDD'04]

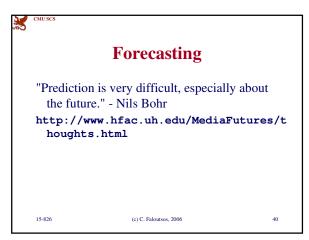
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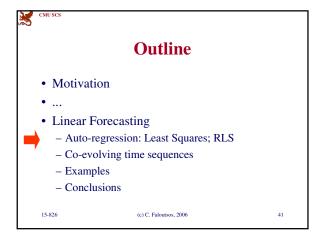
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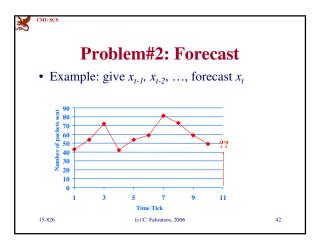


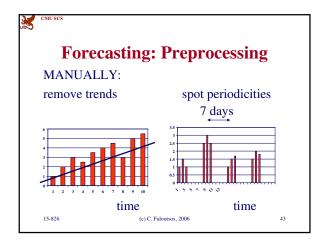


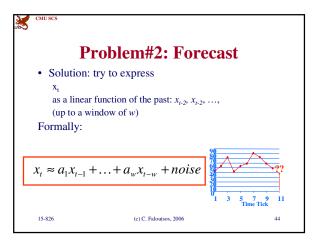


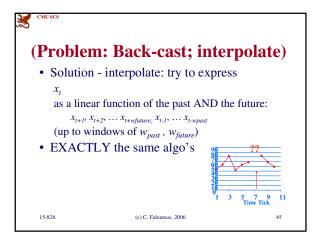


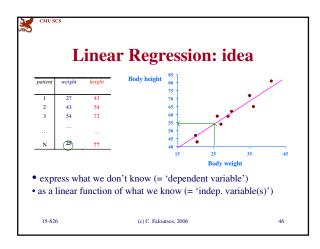


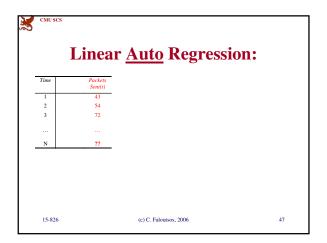


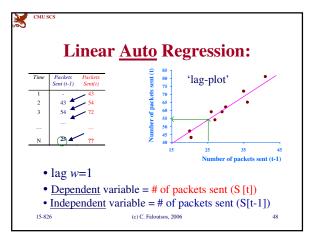




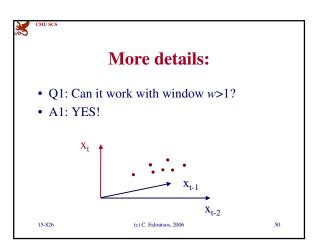




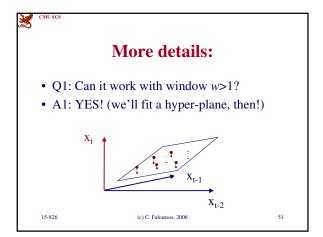


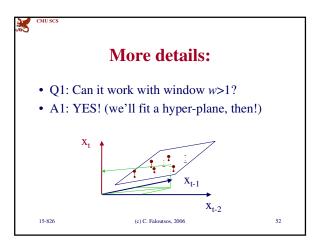


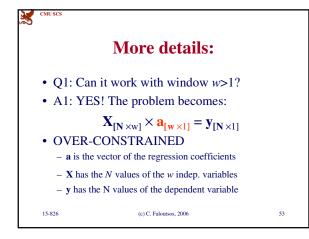


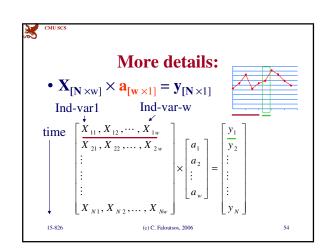


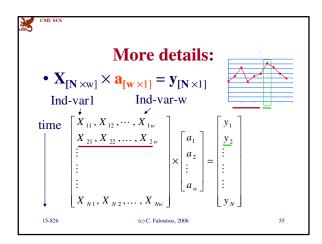
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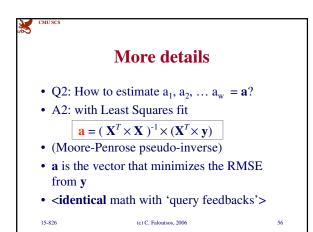


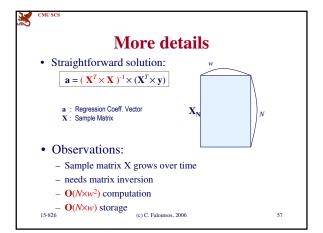


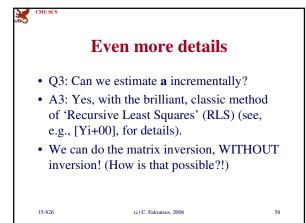


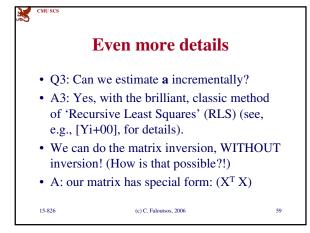


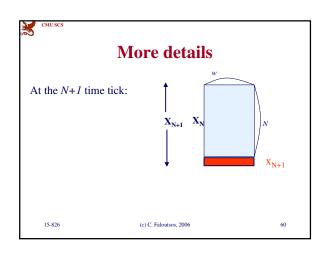


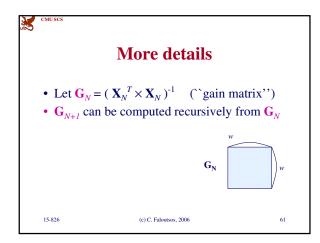


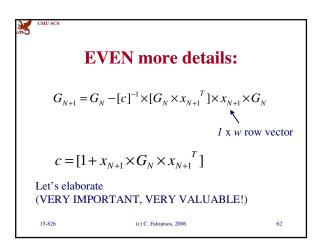


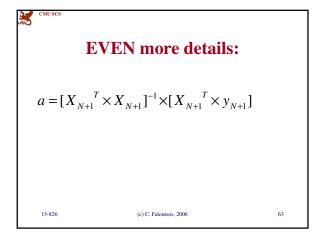


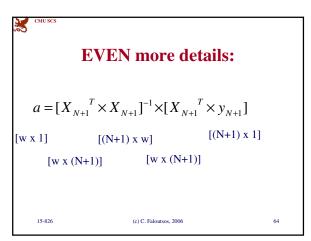


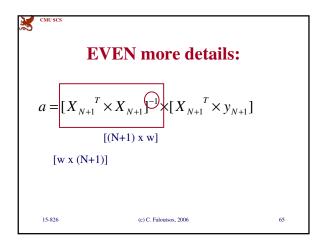


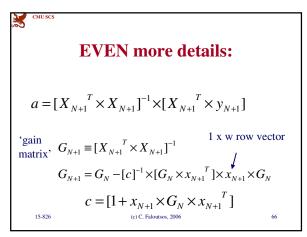


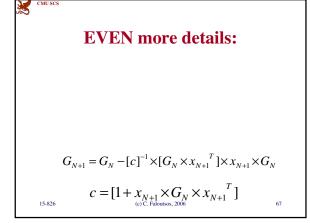


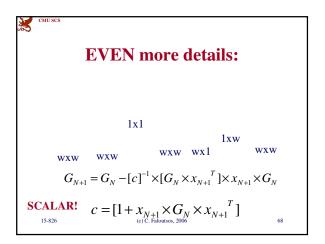


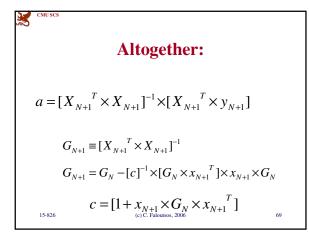


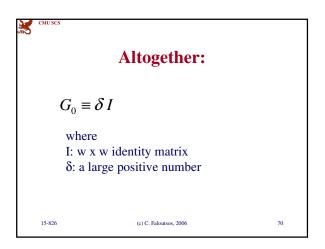


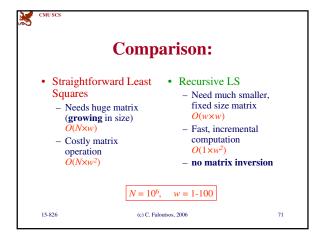


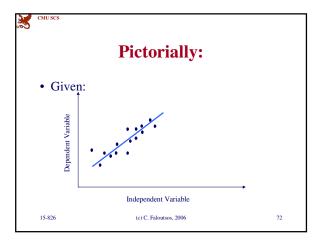


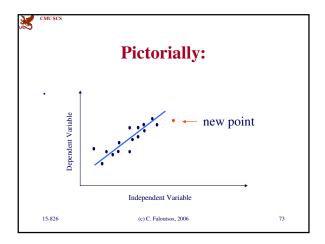


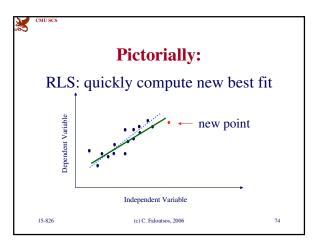


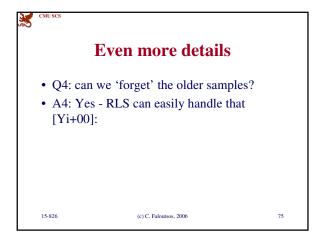


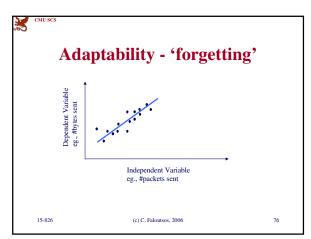


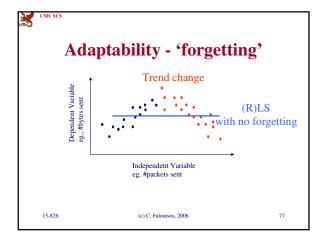


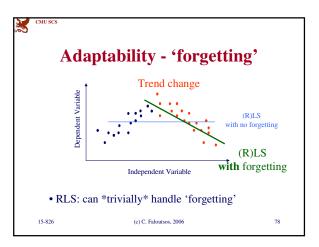


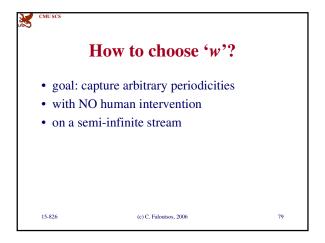


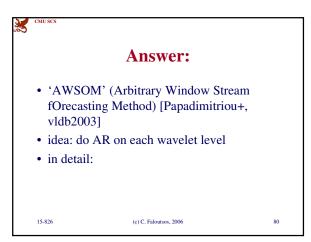


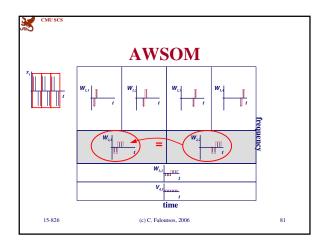


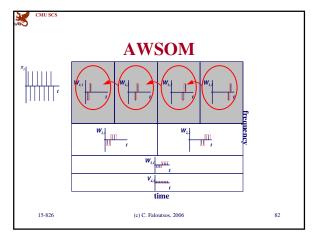


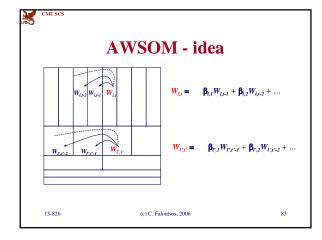


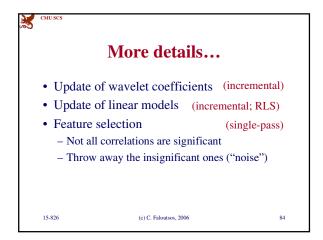


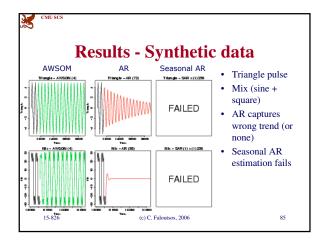


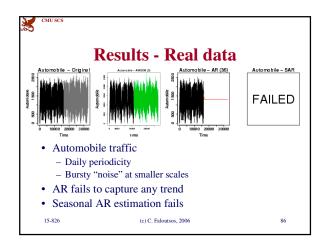


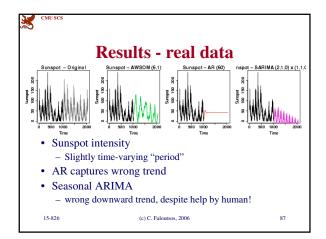


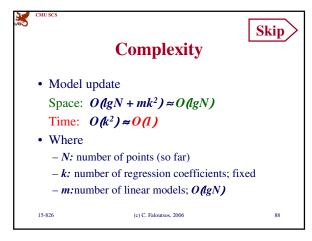


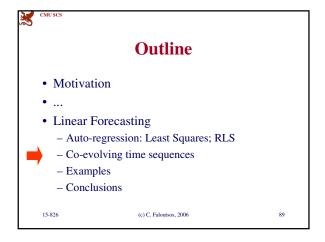


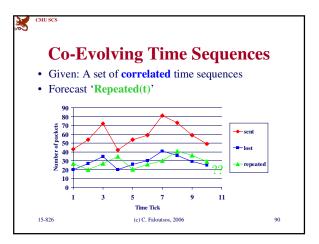


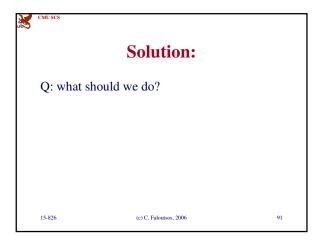


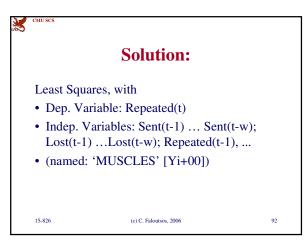


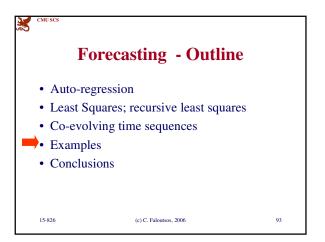


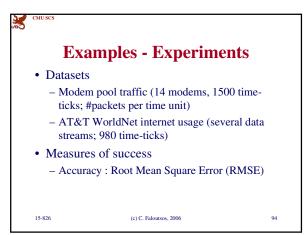


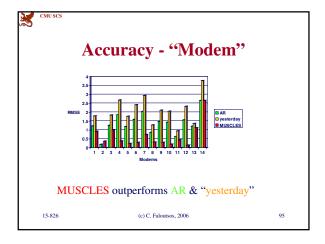


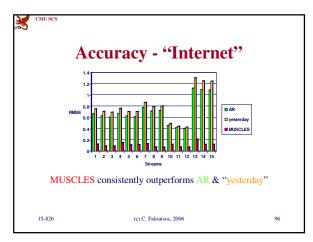


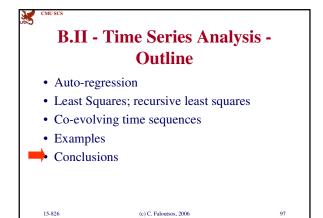










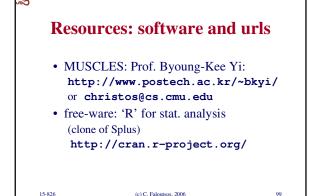


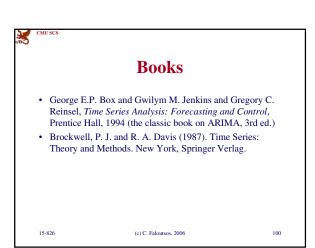


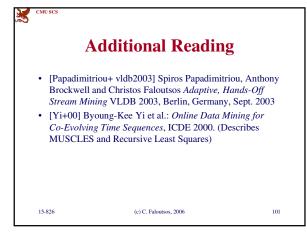
Conclusions - Practitioner's guide

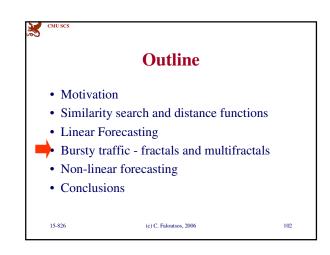
- AR(IMA) methodology: prevailing method for linear forecasting
- Brilliant method of Recursive Least Squares for fast, incremental estimation.
- See [Box-Jenkins]
- very recently: AWSOM (no human intervention)

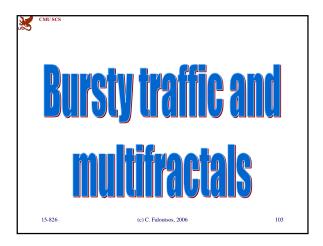
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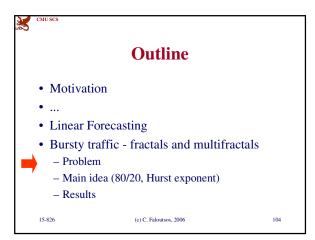


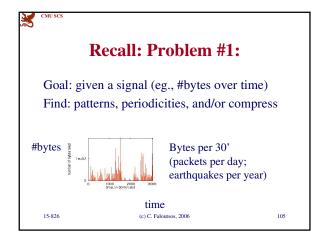


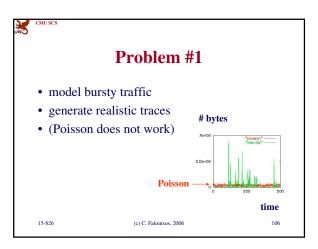


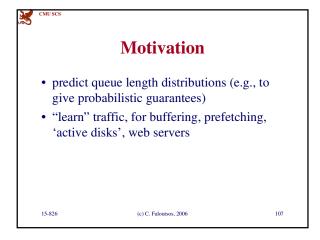


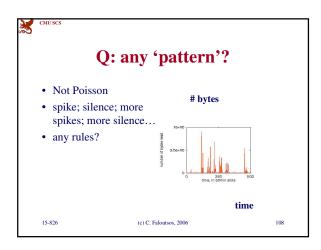


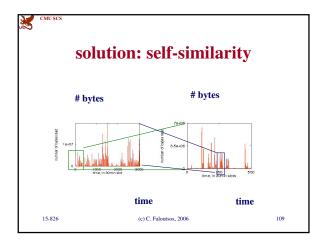


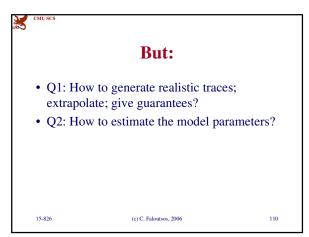


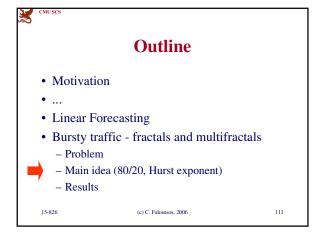


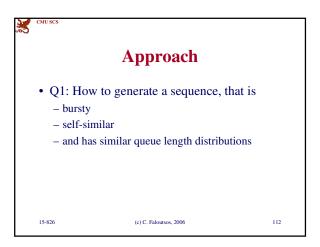


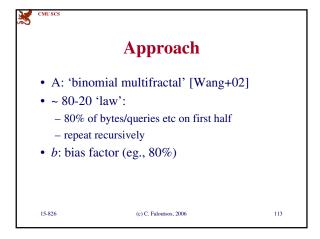


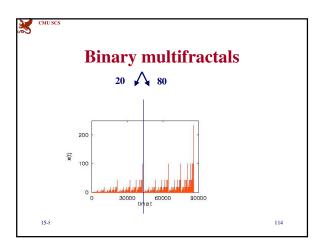


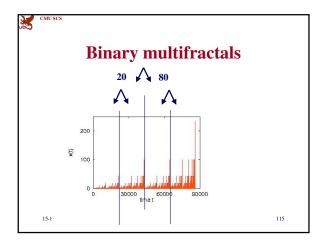


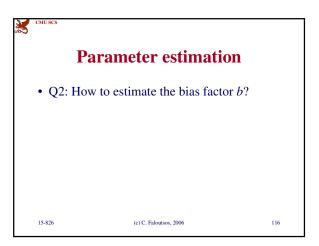












Parameter estimation

• Q2: How to estimate the bias factor b?

• A: MANY ways [Crovella+96]

- Hurst exponent

- variance plot

- even DFT amplitude spectrum! ('periodogram')

- More robust: 'entropy plot' [Wang+02]

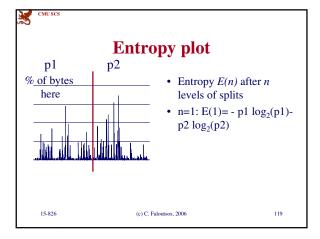
Entropy plot

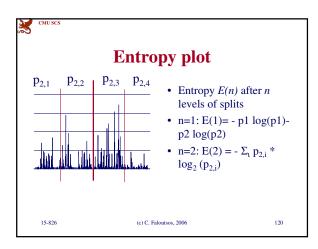
• Rationale:

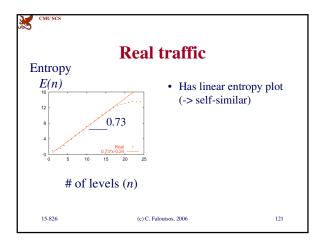
- burstiness: inverse of uniformity

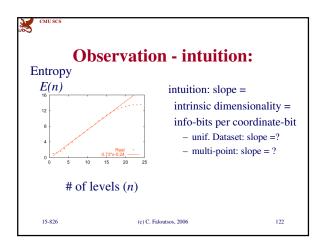
- entropy measures uniformity of a distribution

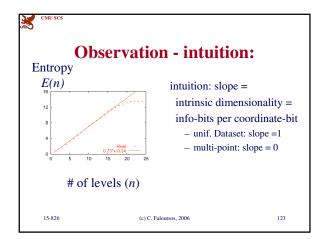
- find entropy at several granularities, to see whether/how our distribution is close to uniform.

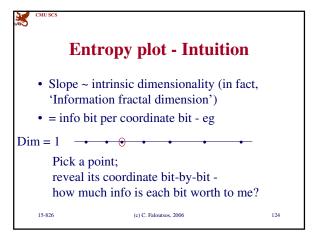


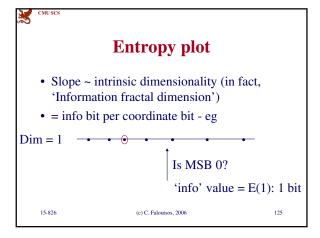


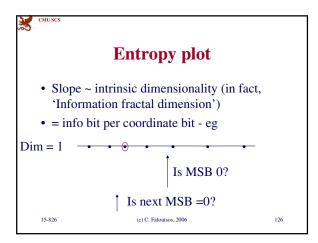


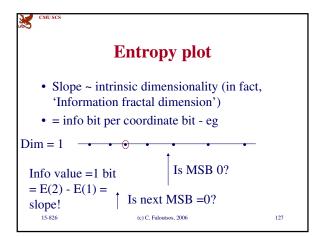


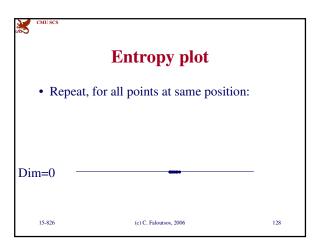


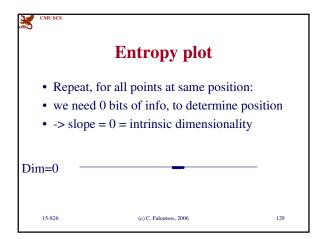


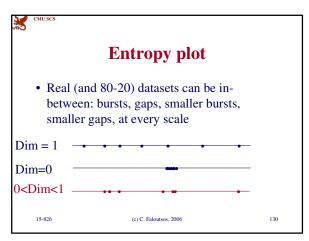






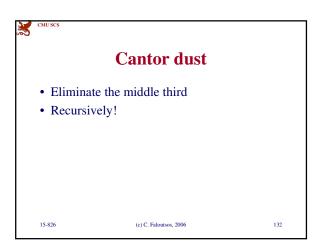


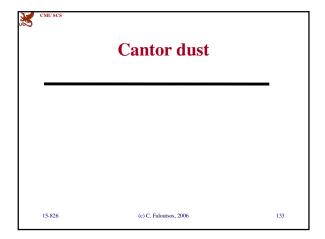


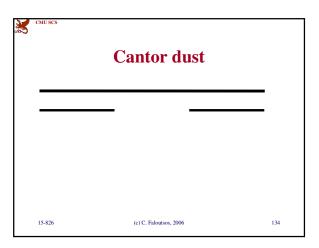


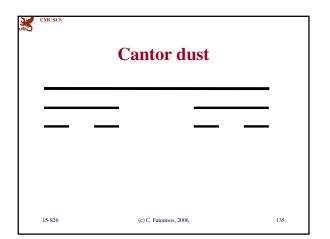
(Fractals, again)

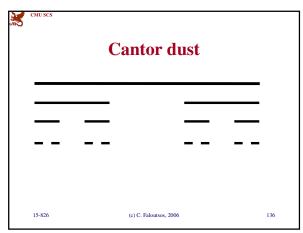
• What set of points could have behavior between point and line?

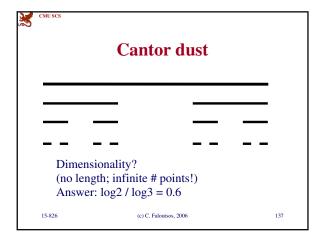


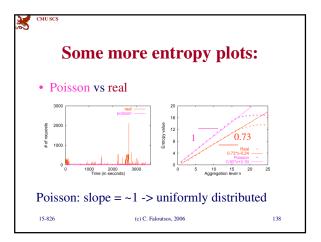


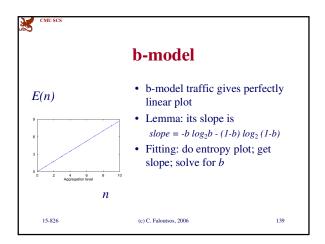


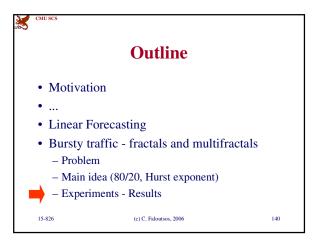










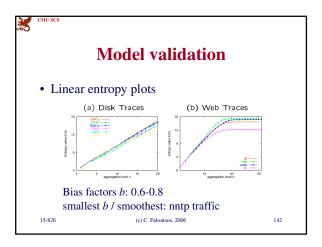


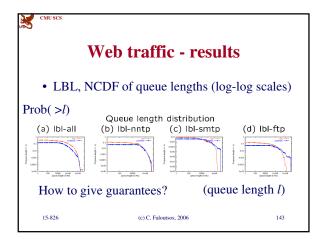
Experimental setup

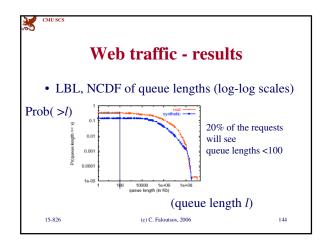
• Disk traces (from HP [Wilkes 93])

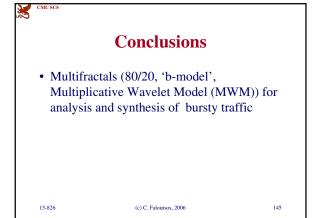
• web traces from LBL

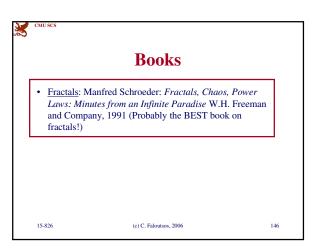
http://repository.cs.vt.edu/
lbl-conn-7.tar.Z







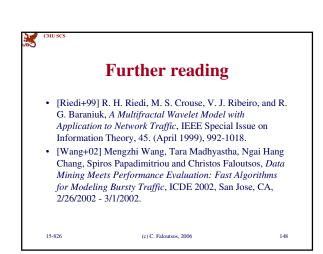


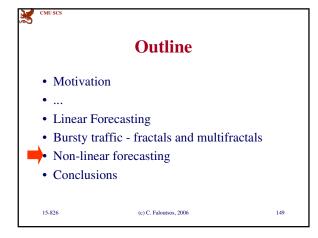


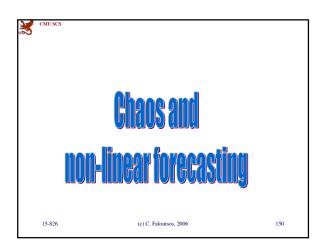
Further reading:

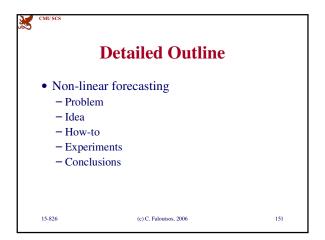
• Crovella, M. and A. Bestavros (1996). Self-Similarity in World Wide Web Traffic, Evidence and Possible Causes. Sigmetrics.

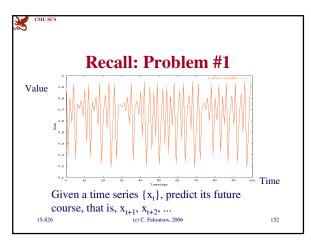
• [ieeeTN94] W. E. Leland, M.S. Taqqu, W. Willinger, D.V. Wilson, On the Self-Similar Nature of Ethernet Traffic, IEEE Transactions on Networking, 2, 1, pp 1-15, Feb. 1994.







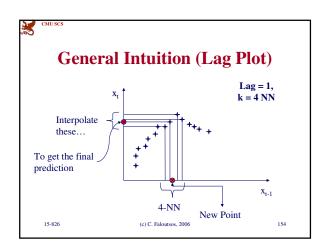




How to forecast?

• ARIMA - but: linearity assumption

• ANSWER: 'Delayed Coordinate Embedding' = Lag Plots [Sauer92]



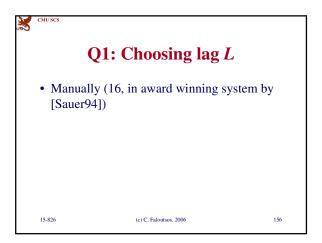
Questions:

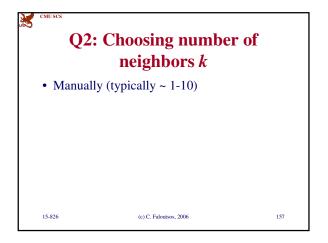
• Q1: How to choose lag L?

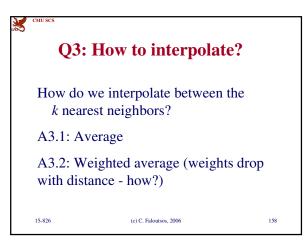
• Q2: How to choose k (the # of NN)?

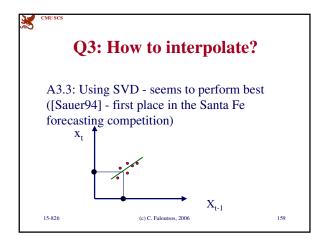
• Q3: How to interpolate?

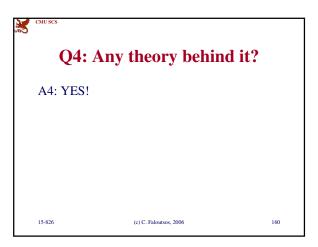
• Q4: why should this work at all?

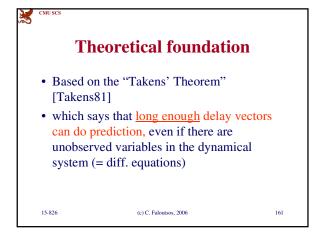


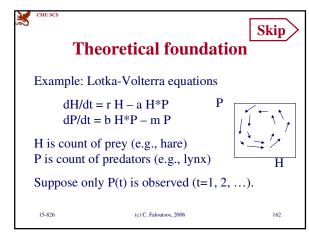


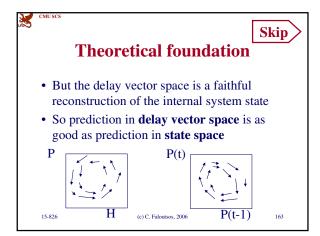


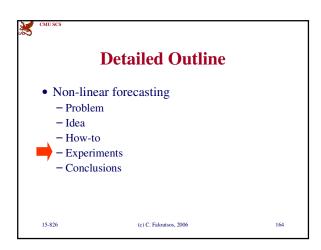


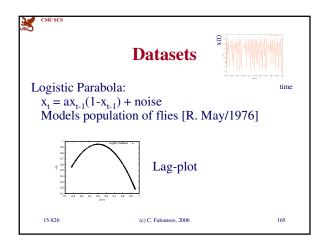


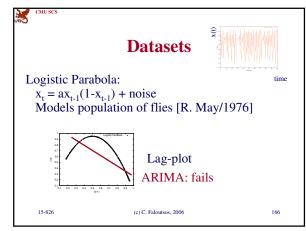


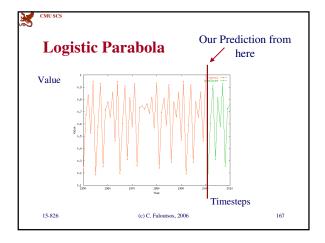


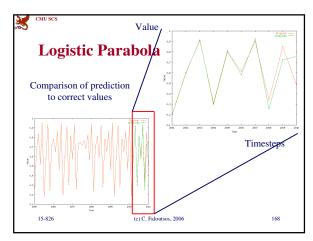


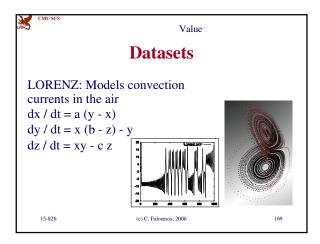


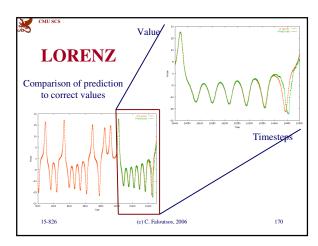


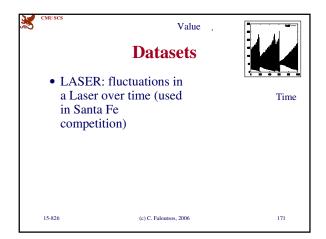


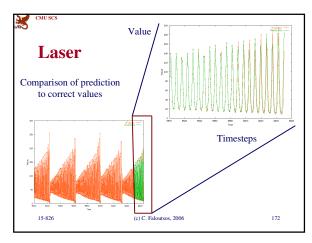










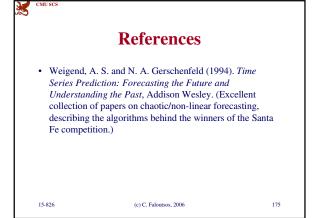


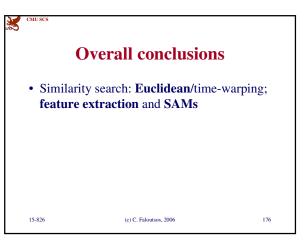
Conclusions

• Lag plots for non-linear forecasting (Takens' theorem)

• suitable for 'chaotic' signals



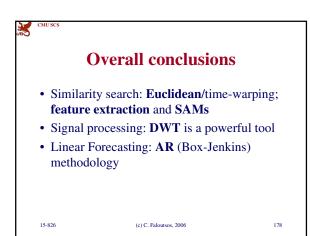




Overall conclusions

• Similarity search: Euclidean/time-warping; feature extraction and SAMs

• Signal processing: DWT is a powerful tool



Overall conclusions

• Similarity search: Euclidean/time-warping; feature extraction and SAMs

• Signal processing: DWT is a powerful tool

• Linear Forecasting: AR (Box-Jenkins) methodology; AWSOM

• Bursty traffic: multifractals (80-20 'law')

