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- Ramakrinshan+Gehrke, Chapter 28.4
- J. Orenstein, $\qquad$ Dis S Pr ACM SIGMOD, May Database System, Proc. ACM SIGMOD, May, 1986, pp. 326-336, Washington D.C.
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| $3^{3}{ }^{\text {cutscs }}$ |  |
| :---: | :---: |
| Outline |  |
| Goal: ‘Find similar / interesting things’ <br> - Intro to DB |  |
| - Indexing - similarity search <br> - Data Mining |  |
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| $3^{\text {max }}$ |  |  |
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| Indexing - Detailed outline |  |  |
| - primary key indexing <br> - secondary key / multi-key indexing |  |  |
|  |  |  |
| - spatial access methods |  |  |
| - problem dfn |  |  |
| - z -ordering |  |  |
| - R-trees |  |  |
| - ... |  |  |
| - text |  |  |
|  |  |  |

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- primary key indexing
- secondary key / multi-key indexing $\qquad$
- spatial access methods
- problem dfn $\qquad$
- z-ordering
- R-trees $\qquad$
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- $\ldots$ $\qquad$


## $\mathrm{m}^{\mathrm{cmuscs}}$ <br> Spatial Access Methods problem

- Given a collection of geometric objects (points, lines, polygons, ...)
- organize them on disk, to answer spatial queries (like??) $\qquad$

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## Spatial Access Methods problem

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- Given a collection of geometric objects (points, lines, polygons, ...)
- organize them on disk, to answer

> - point queries

- range queries
- k -nn queries
- spatial joins ('all pairs' queries)



## Spatial Access Methods problem

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- Given a collection of geometric objects (points, lines, polygons, ...) $\qquad$
- organize them on disk, to answer
- point queries $\qquad$
- range queries
- k-nn queries
- spatial joins ('all pairs' queries)

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## $3^{\text {cmuscs }}$ <br> Spatial Access Methods problem

- Given a collection of geometric objects (points, lines, polygons, ...)
- organize them on disk, to answer
- point queries
- range queries
- k -nn queries
- spatial joins ('all pairs' queries)


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## Spatial Access Methods problem

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$\qquad$ (points, lines, polygons, ...)

- organize them on disk, to answer

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## Spatial Access Methods problem

- Given a collection of geometric objects (points, lines, polygons, ...)
- organize them on disk, to answer
- point queries
- range queries
- k-nn queries
- spatial joins ('all pairs' within $\varepsilon$ )

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## $\int^{3 / 3} \quad$ Indexing - Detailed outline

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- primary key indexing
- secondary key / multi-key indexing
- spatial access methods
- problem dfn
- z -ordering
- R-trees $\qquad$
- text $\qquad$
- 1.226 $\qquad$

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Q: solution? (w/ good clustering, and easy to compute, for $2-\mathrm{d}$ and $n$-d?)


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bit-shuffling

| x | y |
| :---: | :---: |
| 00 | 11 |

y

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## $\int^{\text {z-ordering }}$

Drill: $z$-value of magenta cell, with the three methods? $\qquad$
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## z-ordering - Detailed outline

- spatial access methods
- z -ordering
- main idea - 3 methods
- use w/ B-trees; algorithms (range, knn queries ...)
- analysis; variations
- R-trees
- ...
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z-ordering - usage \& algo's
Q2': range queries - how to reduce \# of qualifying of ranges?

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z-ordering - usage $\boldsymbol{\&}$ algo's
Q2'": range queries - how to break a query into ranges?

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## $\int^{\text {z-ordering - usage \& algo's }}$

Q2'’: range queries - how to break a query into ranges?
A: recursively, quadtree-style; decompose only non-full quadrants $\qquad$


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Q: How to search (range etc queries) - eg 'red' range query


| $z$ | obj-id |  |
| :--- | :--- | :--- |
| 0010 | etc |  |
| 0101 | A |  |
| 1000 | C |  |
| $11^{* *}$ | B |  |

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## zordering - regions

Almost identical to range queries for point data, except for the "don't cares" - i.e., z1 = 1100 ?? $11^{* *}=z 2$
Specifically: does z1 contain/avoid/intersect $\qquad$ z2?
Q: what is the criterion to decide?
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| $3^{\text {cmuscs }}$ |  |  |
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| z-ordering - regions |  |  |
| $\mathrm{z} 1=1100$ ?? $11^{* *}=\mathrm{z} 2$ |  |  |
| Specifically: does zl contain/avoid/intersect z2? |  |  |
| Q : what is the criterion to decide? |  |  |
| A: Prefix property: let r1, r2 be the corresponding regions, and let r 1 be the smallest ( $=>$ z1 has fewest '*'s). Then: |  |  |
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Drill (True/False). Given:

- $\mathrm{zl}=011001^{* *}$
- z2 $=01^{* * * * * *}$
- $\mathrm{z} 3=0100^{* * * *}$

T/F r2 contains r1
T/F r3 contains r1
T/F r3 contains r2 $\qquad$

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## z-ordering - regions

Spatial joins: find (quickly) all
counties intersecting lakes

| Z | obj-id | etc | Z | obj-id | etc |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0010 | ALG |  | 0011 | Erie |  |
| $\ldots$ | $\ldots$ |  | 0101 | Erie |  |
| 1000 | WAS |  | $\cdots$ |  |  |
| 11** | ALG |  | 10** | Ont. |  |

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## 

Spatial joins: find (quickly) all
counties intersecting lakes

Solution: merge the lists of (sorted) z-values, looking for the prefix property
footnote\#1: ‘*’ needs careful treatment footnote\#2: need dup. elimination

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'Looks' better (never long jumps). How to derive it?


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(How long is the coastline, say, of England?
Paradox: The answer changes with the yardstick -> fractals ...)


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Z-ordering - analysis
Q: So, is Hilbert really better?
A: 27\% fewer runs, for 2-d (similar for 3-d)

| Q: are there formulas for \#runs, \#of quadtree |
| :--- |
| blocks etc? |
| A: Yes ([Jagadish; Moon+ etc] see textbook) |
| ${ }_{15}$ (5.826 |

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Q: So, is Hilbert really better?
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