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15-826: Multimedia Databases and Data Mining

Lecture #26: Graph mining - patterns

Christos Faloutsos

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Must-read Material

- Michalis Faloutsos, Petros Faloutsos and Christos Faloutsos, On Power-Law Relationships of the Internet Topology, SIGCOMM 1999.
- R. Albert, H. Jeong, and A.-L. Barabasi, Diameter of the World Wide Web Nature, 401, 130-131 (1999).
- Reka Albert and Albert-Laszlo Barabasi Statistical mechanics of complex networks, Reviews of Modern Physics, 74, 47 (2002).
- Jure Leskovec, Jon Kleinberg, Christos Faloutsos Graphs over Time: Densification Laws, Shrinking Diameters and Possible Explanations, KDD 2005, Chicago, IL, USA

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Must-read Material (cont'd)

- D. Chakrabarti and C. Faloutsos, Graph Mining: Laws, Generators and Algorithms, in ACM Computing Surveys, 38 (1), 2006
- J. Leskovec, D. Chakrabarti, J. Kleinberg, and C. Faloutsos, Realistic, Mathematically Tractable Graph Generation and Evolution, Using Kronecker Multiplication, in PKDD 2005, Porto, Portugal

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Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
- Problem#3: Scalability
- Conclusions

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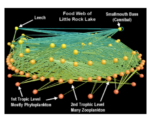
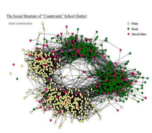
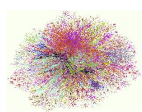
Graphs - why should we care?



Food Web [Martinez '91]



Friendship Network [Moody '01]



Internet Map [lumeta.com]

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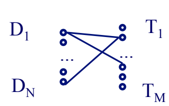
Graphs - why should we care?

- IR: bi-partite graphs (doc-terms)



- web: hyper-text graph
- ... and more:

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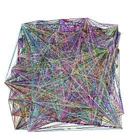
Graphs - why should we care?

- ‘viral’ marketing
- web-log (‘blog’) news propagation
- computer network security: email/IP traffic and anomaly detection
- ....

Outline

- Introduction – Motivation
- ➡ Problem#1: Patterns in graphs
  - Static graphs
  - Weighted graphs
  - Time evolving graphs
- Problem#2: Tools
- Problem#3: Scalability
- Conclusions

Problem #1 - network and graph mining



- What does the Internet look like?
- What does FaceBook look like?
- What is ‘normal’/‘abnormal’?
- which patterns/laws hold?

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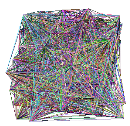
Problem #1 - network and graph mining



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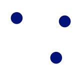
  - To spot **anomalies** (rarities), we have to discover **patterns**



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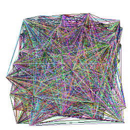
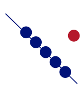
Problem #1 - network and graph mining



- What does the Internet look like?
- What does FaceBook look like?
- What is 'normal'/'abnormal'?
- which patterns/laws hold?
  - To spot **anomalies** (rarities), we have to discover **patterns**
  - **Large** datasets reveal patterns/anomalies that may be invisible otherwise…



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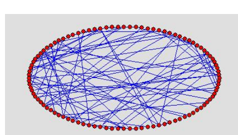
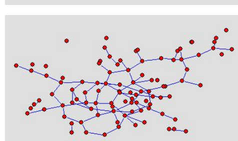
Are real graphs random?

- random (Erdos-Renyi) graph – 100 nodes, avg degree = 2
- before layout
- after layout
- No obvious patterns

(generated with: pajek http://vlado.fmf.uni-lj.si/pub/networks/pajek/)





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Graph mining

- Are real graphs random?

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Laws and patterns

- Are real graphs random?
- A: NO!!
  - Diameter
  - in- and out- degree distributions
  - other (surprising) patterns
- So, let's look at the data

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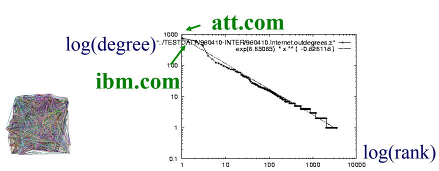
Solution# S.1

- Power law in the degree distribution [SIGCOMM99]

internet domains



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Solution# S.1

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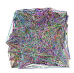

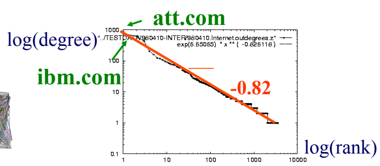

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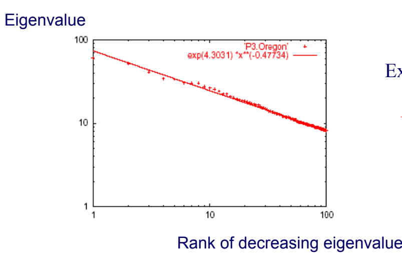
Solution# S.2: Eigen Exponent *E*



Exponent = slope

E = -0.48

May 2001

- A2: power law in the eigenvalues of the adjacency matrix

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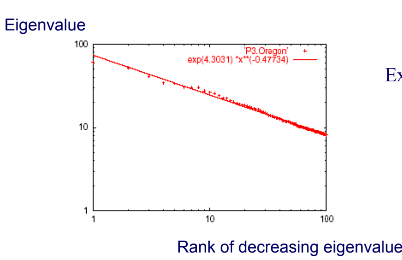
Solution# S.2: Eigen Exponent *E*



Exponent = slope

E = -0.48

May 2001

- [Mihail, Papadimitriou '02]: slope is ½ of rank exponent

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But:

How about graphs from other domains?

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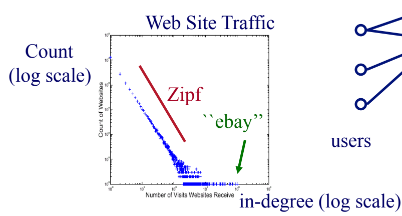
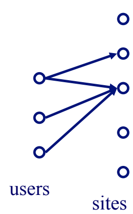
More power laws:

- web hit counts [w/ A. Montgomery]





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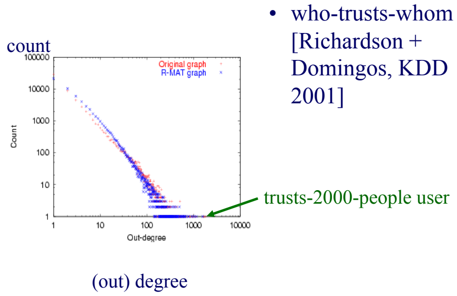
epinions.com

- who-trusts-whom [Richardson + Domingos, KDD 2001]



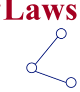
And numerous more

- # of sexual contacts
- Income [Pareto] –'80-20 distribution'
- Duration of downloads [Bestavros+]
- Duration of UNIX jobs ('mice and elephants')
- Size of files of a user
- …
- 'Black swans'

Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
  - Static graphs
    - degree, diameter, eigen,
    - ➡ triangles
    - cliques
  - Weighted graphs
  - Time evolving graphs
- Problem#2: Tools

Solution# S.3: Triangle 'Laws'



- Real social networks have a lot of triangles

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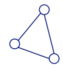
Solution# S.3: Triangle 'Laws'



- Real social networks have a lot of triangles
  - Friends of friends are friends
- Any patterns?

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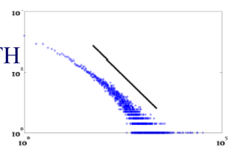
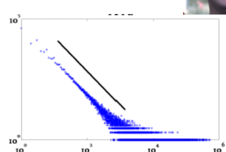
Triangle Law: #S.3
[Tsourakakis ICDM 2008]

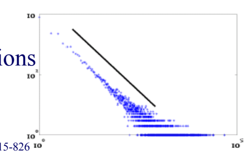
HEP-TH

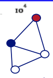


ASN



Epinions





X-axis: # of participating triangles
Y: count (~ pdf)

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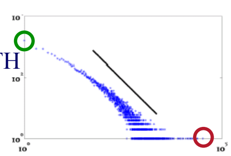
Triangle Law: #S.3
[Tsourakakis ICDM 2008]

HEP-TH



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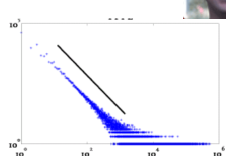

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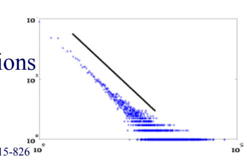

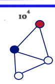

X-axis: # of participating triangles
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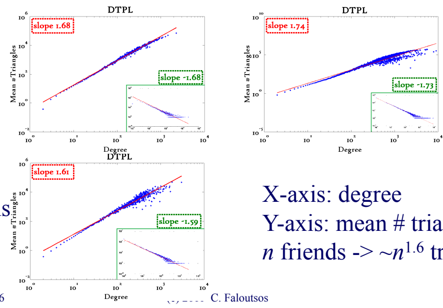
Triangle Law: #S.4
[Tsourakakis ICDM 2008]

Reuters

SN

Epinions



X-axis: degree
Y-axis: mean # triangles
n friends -> ~$n^{1.6}$ triangles

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Triangle Law: Computations
[Tsourakakis ICDM 2008]

But: triangles are expensive to compute
(3-way join; several approx. algos)
Q: Can we do that quickly?

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details

Triangle Law: Computations
[Tsourakakis ICDM 2008]

But: triangles are expensive to compute
(3-way join; several approx. algos)
Q: Can we do that quickly?
A: Yes!
#triangles = 1/6 Sum (λ_i^3)
(and, because of skewness (S2) ,
we only need the top few eigenvalues!

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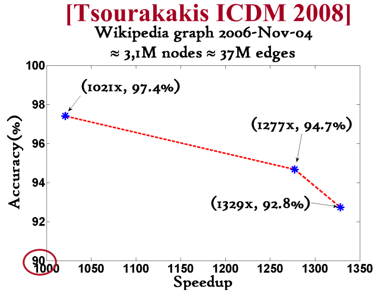
details

Triangle Law: Computations

[Tsourakakis ICDM 2008]



1000x+ speed-up, >90% accuracy

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Triangle counting for large graphs?

Anomalous nodes in Twitter(~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]

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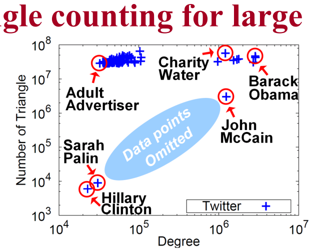
Triangle counting for large graphs?



Anomalous nodes in Twitter(~ 3 billion edges)

[U Kang, Brendan Meeder, +, PAKDD'11]

Any other 'laws'?

Yes!

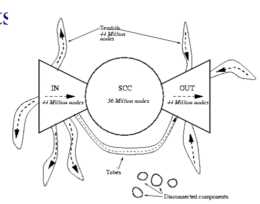
Any other 'laws'?

Yes!

- Small diameter (~ constant!) –
  - six degrees of separation / 'Kevin Bacon'
  - small worlds [Watts and Strogatz]

Any other 'laws'?

- Bow-tie, for the web [Kumar+ '99]
- IN, SCC, OUT, 'tendrils'
- disconnected components



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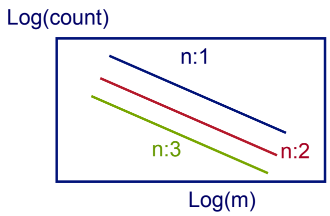
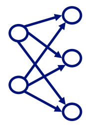
Any other 'laws'?

- power-laws in communities (bi-partite cores) [Kumar+, '99]





2:3 core
(m:n core)

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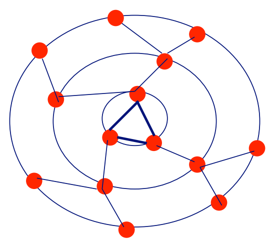
Any other 'laws'?

- "Jellyfish" for Internet [Tauro+ '01]
- core: ~clique
- ~5 concentric layers
- many 1-degree nodes



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EigenSpokes

B. Aditya Prakash, Mukund Seshadri, Ashwin Sridharan, Sridhar Machiraju and Christos Faloutsos: *EigenSpokes: Surprising Patterns and Scalable Community Chipping in Large Graphs,* PAKDD 2010, Hyderabad, India, 21-24 June 2010.

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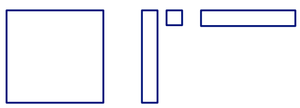
EigenSpokes

- Eigenvectors of adjacency matrix
  - equivalent to singular vectors (symmetric, undirected graph)

$$A = U \Sigma U^T$$



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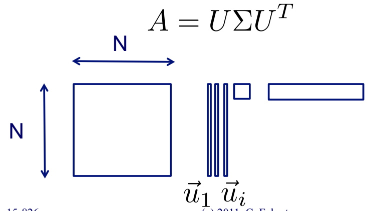

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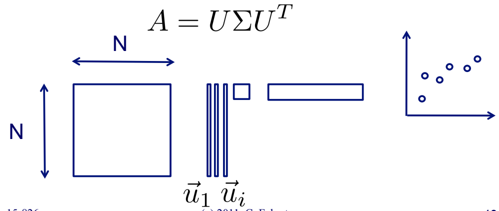

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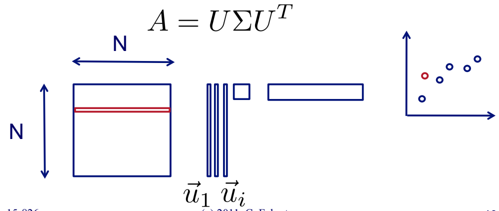

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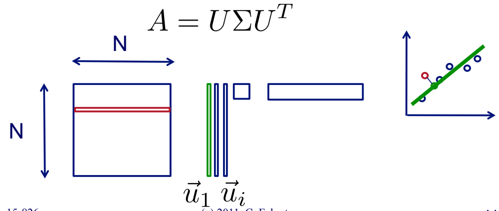

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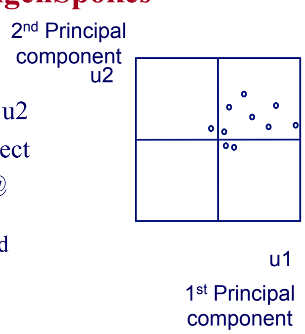
EigenSpokes

- EE plot:
- Scatter plot of scores of u1 vs u2
- One would expect
  - Many points @ origin
  - A few scattered ~randomly



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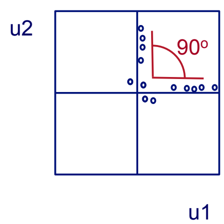

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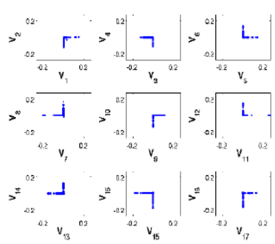
EigenSpokes - pervasiveness

- Present in mobile social graph
  - across time and space
- Patent citation graph



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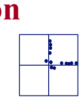
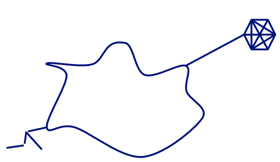
EigenSpokes - explanation

Near-cliques, or near-bipartite-cores, loosely connected





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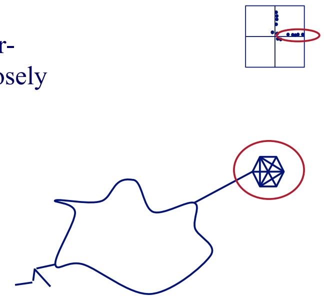

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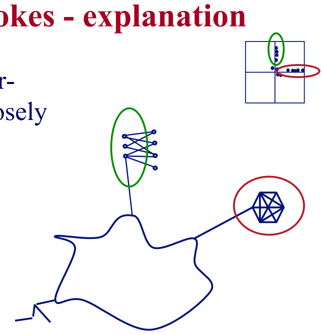

EigenSpokes - explanation

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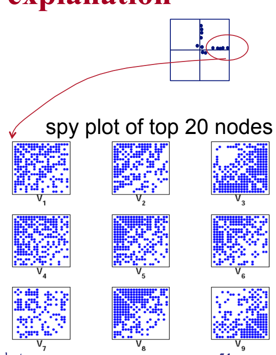

So what?

- Extract nodes with high *scores*
- high connectivity
- Good "communities"

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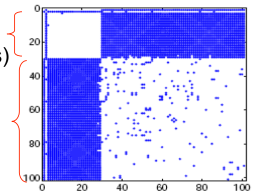
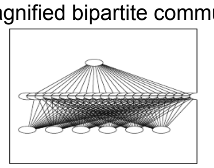
Bipartite Communities!

patents from same inventor(s)

`cut-and-paste' bibliography!



magnified bipartite community



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Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
  - Static graphs
    - degree, diameter, eigen,
    - triangles
    - cliques
  - ➡ Weighted graphs
  - Time evolving graphs
- Problem#2: Tools

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Observations on weighted graphs?

- A: yes - even more 'laws'!

M. McGlohon, L. Akoglu, and C. Faloutsos *Weighted Graphs and Disconnected Components: Patterns and a Generator.* *SIG-KDD* 2008

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Observation W.1: Fortification

Q: How do the weights of nodes relate to degree?

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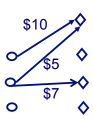
Observation W.1: Fortification

More donors, more $?



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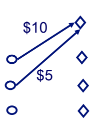
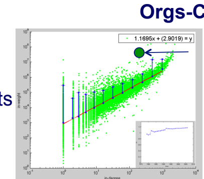
Observation W.1: fortification: Snapshot Power Law

- Weight: super-linear on in-degree
- exponent 'iw': 1.01 < iw < 1.26

More donors, <u>even</u> more $





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Outline

- Introduction – Motivation
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  - Static graphs
  - Weighted graphs
  - Time evolving graphs
- Problem#2: Tools
- …

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Problem: Time evolution

- with Jure Leskovec (CMU -> Stanford)

- and Jon Kleinberg (Cornell – sabb. @ CMU)

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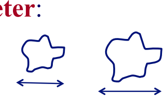
T.1 Evolution of the Diameter

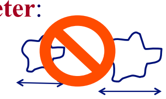
- Prior work on Power Law graphs hints at **slowly growing diameter**:
  - diameter ~ O(log N)
  - diameter ~ O(log log N)



- What is happening in real data?

T.1 Evolution of the Diameter

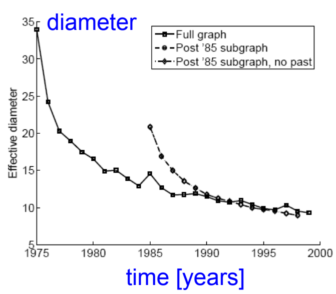
- Prior work on Power Law graphs hints at **slowly growing diameter**:
  - diameter ~ O(log N)
  - diameter ~ O(log log N)



- What is happening in real data?
- Diameter **shrinks** over time

T.1 Diameter – "Patents"

- Patent citation network
- 25 years of data
- @1999
  - 2.9 M nodes
  - 16.5 M edges



T.2 Temporal Evolution of the Graphs

- N(t) … nodes at time t
- E(t) … edges at time t
- Suppose that
  - N(t+1) = 2 * N(t)
- Q: what is your guess for
  - E(t+1) =? 2 * E(t)

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T.2 Temporal Evolution of the Graphs

- N(t) … nodes at time t
- E(t) … edges at time t
- Suppose that

  N(t+1) = 2 * N(t)
- Q: what is your guess for

  E(t+1) =?2 * E(t)
- A: over-doubled!
  - But obeying the ``Densification Power Law''

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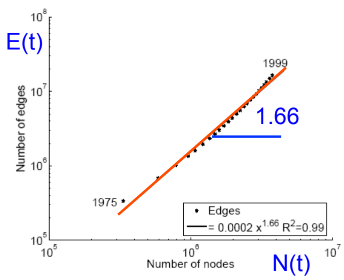
T.2 Densification – Patent Citations

- Citations among patents granted
- @1999
  - 2.9 M nodes
  - 16.5 M edges
- Each year is a datapoint



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Outline

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  - Static graphs
  - Weighted graphs
  - Time evolving graphs
- Problem#2: Tools
- …

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More on Time-evolving graphs

M. McGlohon, L. Akoglu, and C. Faloutsos
Weighted Graphs and Disconnected Components: Patterns and a Generator.
SIG-KDD 2008

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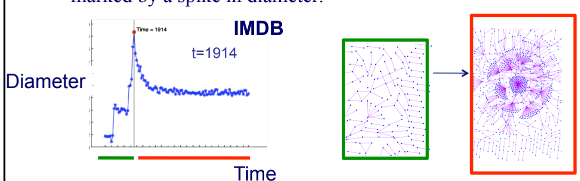
[Gelling Point]

- Most real graphs display a gelling point
- After gelling point, they exhibit typical behavior. This is marked by a spike in diameter.



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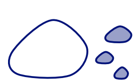
Observation T.3: NLCC behavior

Q: How do NLCC's emerge and join with the GCC?

(``NLCC'' = non-largest conn. components)
- Do they continue to grow in size?
- or do they shrink?
- or stabilize?



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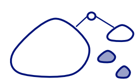

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Observation T.3: NLCC behavior

Q: How do NLCC's emerge and join with the GCC?

(``NLCC'' = non-largest conn. components)

YES – Do they continue to grow in size?
YES – or do they shrink?
YES – or stabilize?

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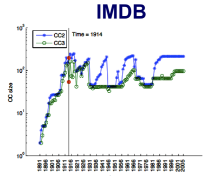
Observation T.3: NLCC behavior

- After the gelling point, the GCC takes off, but NLCC's remain ~constant (actually, **oscillate**).

IMDB

CC size



Time-stamp

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Timing for Blogs

- with Mary McGlohon (CMU->Google)
- Jure Leskovec (CMU->Stanford)
- Natalie Glance (now at Google)
- Mat Hurst (now at MSR)

[SDM'07]

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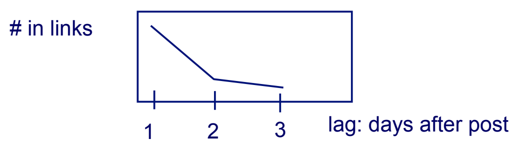
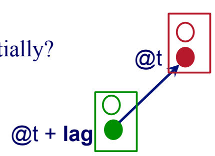
T.4 : popularity over time



Post popularity drops-off – exponentially?



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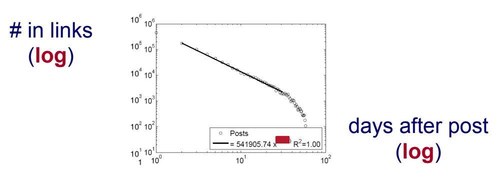
T.4 : popularity over time



Post popularity drops-off – exponentially?
POWER LAW!
Exponent?

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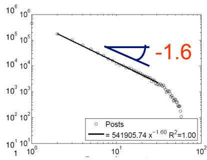
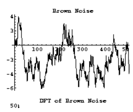
T.4 : popularity over time

in links (log)



days after post (log)

Post popularity drops-off – exponentially?
POWER LAW!
Exponent? -1.6
- close to -1.5: Barabasi's stack model
- and like the zero-crossings of a random walk



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-1.5 slope

J. G. Oliveira & A.-L. Barabási Human Dynamics: The Correspondence Patterns of Darwin and Einstein. *Nature* **437,** 1251 (2005) . [PDF]

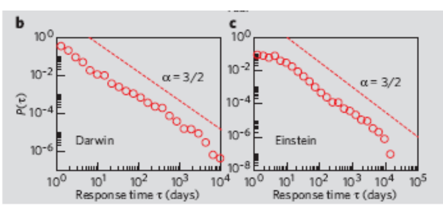

Figure 1 | The correspondence patterns of Darwin and Einstein.

1 77

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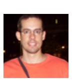
T.5: duration of phonecalls

Surprising Patterns for the Call Duration Distribution of Mobile Phone Users



Pedro O. S. Vaz de Melo, Leman Akoglu, Christos Faloutsos, Antonio A. F. Loureiro

PKDD 2010

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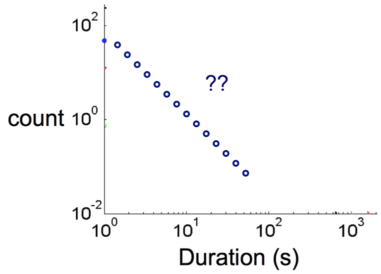
Probably, power law (?)



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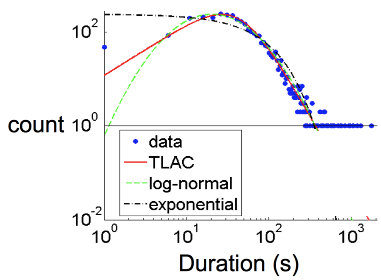
No Power Law!



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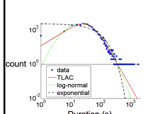
'TLaC: Lazy Contractor'

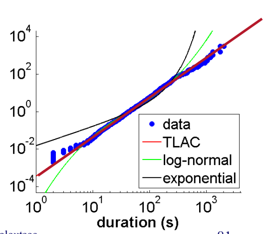
- The longer a task (phonecall) has taken,
- The even longer it will take



Odds ratio=

Casualties(<x): Survivors(>=x)

== power law



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Data Description

- Data from a private mobile operator of a large city
  - 4 months of data
  - 3.1 million users
  - more than 1 billion phone records
- Over 96% of 'talkative' users obeyed a TLAC distribution ('talkative': >30 calls)

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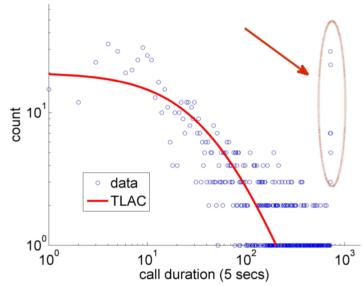
Outliers:



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Outline

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  - Belief Propagation
  - Immunization
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- Conclusions

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OddBall: Spotting Anomalies in Weighted Graphs


Leman Akoglu, Mary McGlohon, Christos Faloutsos
Carnegie Mellon University
School of Computer Science

PAKDD 2010, Hyderabad, India

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Main idea

For each node,

- extract 'ego-net' (=1-step-away neighbors)
- Extract features (#edges, total weight, etc etc)
- Compare with the rest of the population

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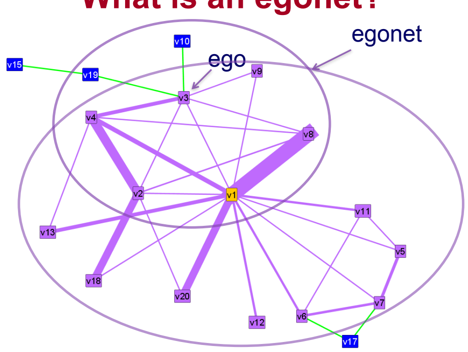
What is an egonet?



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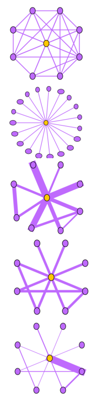
Selected Features

- N_i: number of neighbors (degree) of ego i
- E_i: number of edges in egonet i
- W_i: total weight of egonet i
- $\lambda_{w,i}$: principal eigenvalue of the weighted adjacency matrix of egonet I



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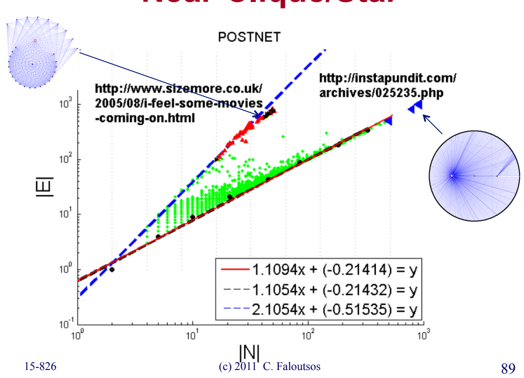
Near-Clique/Star



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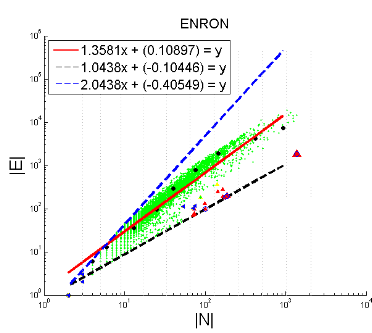
Near-Clique/Star



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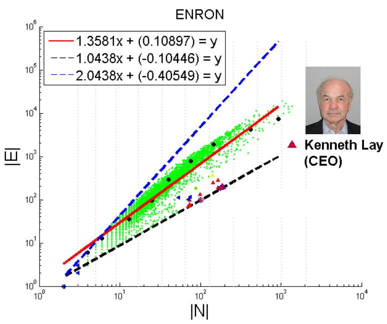
Near-Clique/Star



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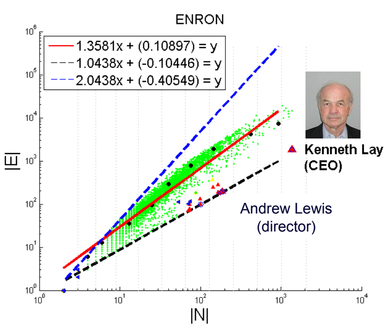
Near-Clique/Star



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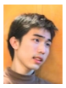
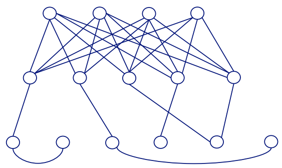
E-bay Fraud detection




w/ Polo Chau &
Shashank Pandit, CMU
[www'07]



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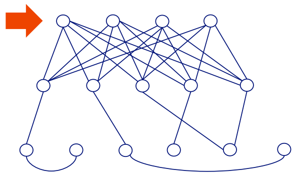
E-bay Fraud detection



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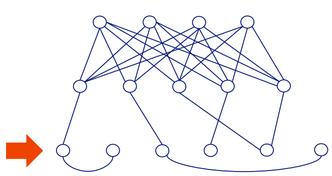
E-bay Fraud detection



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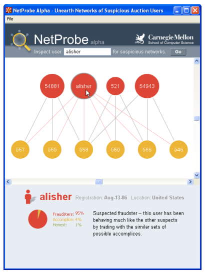
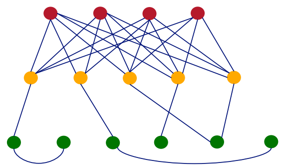
E-bay Fraud detection - NetProbe





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Popular press

USA TODAY
The Washington Post
Los Angeles Times

And less desirable attention:

- E-mail from 'Belgium police' ('copy of your code?')

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  - ➡ Belief Propagation – antivirus app
  - Immunization
- Problem#3: Scalability
- Conclusions

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Polonium: Tera-Scale Graph Mining and Inference for Malware Detection

SDM 2011, Mesa, Arizona

Polo Chau
Machine Learning Dept

Carey Nachenberg
Vice President & Fellow

Jeffrey Wilhelm
Principal Software Engineer

Adam Wright
Software Engineer

Prof. Christos Faloutsos
Computer Science Dept

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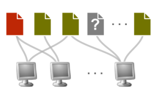
Polonium: The Data

60+ terabytes of data *anonymously* contributed by participants of worldwide *Norton Community Watch* program

- 50+ million machines
- 900+ million executable files



Constructed a machine-file bipartite graph (0.2 TB+)

- 1 billion nodes (machines and files)
- 37 billion edges

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Polonium: Key Ideas

- Use Belief Propagation to propagate domain knowledge in machine-file graph to detect malware
- Use "guilt-by-association" (i.e., homophily)
  - E.g., files that appear on machines with many bad files are more likely to be bad
- Scalability: handles 37 billion-edge graph

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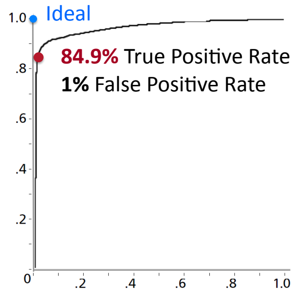
Polonium: One-Interaction Results



True Positive Rate
% of malware correctly identified

False Positive Rate
% of non-malware wrongly labeled as malware

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Immunization and epidemic thresholds

- Q1: which nodes to immunize?
- Q2: will a virus vanish, or will it create an epidemic?

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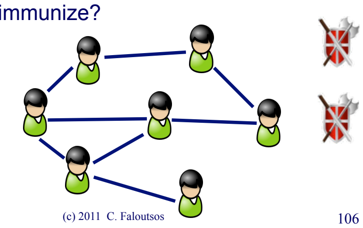
Q1: Immunization:

- Given
  - a network,
  - k vaccines, and
  - the virus details
- Which nodes to immunize?



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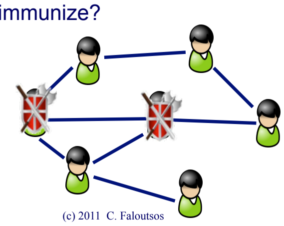

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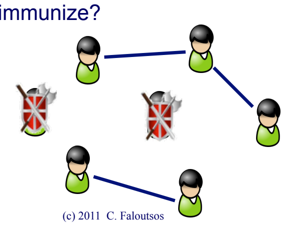

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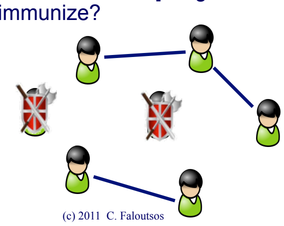
Q1: Immunization:

- Given
  - a network,
  - k vaccines, and
  - the virus details
- Which nodes to immunize?

A: immunize the ones that maximally raise the `epidemic threshold' [Tong+, ICDM'10]



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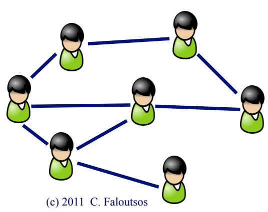
details

Q2: will a virus take over?

- Flu-like virus (no immunity, 'SIS')
- Mumps (life-time immunity, 'SIR')
- Pertussis (finite-length immunity, 'SIRS')

β: attack prob
δ: heal prob



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details

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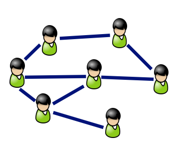
- Flu-like virus (no immunity, 'SIS')
- Mumps (life-time immunity, 'SIR')
- Pertussis (finite-length immunity, 'SIRS')

β: attack prob
δ: heal prob

A: depends on connectivity
(avg degree? Max degree?
variance? Something else?



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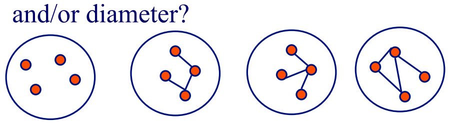
Epidemic threshold τ

What should τ depend on?

- avg. degree? and/or highest degree?
- and/or variance of degree?
- and/or third moment of degree?
- and/or diameter?



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Epidemic threshold

- [Theorem] We have no epidemic, if

$$\boxed{\beta/\delta < \tau = 1/\lambda_{1,A}}$$

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Epidemic threshold

- [Theorem] We have no epidemic, if

recovery prob. epidemic threshold

$$\boxed{\beta/\delta < \tau = 1/\lambda_{1,A}}$$

attack prob. largest eigenvalue of adj. matrix ***A***

Proof: [Wang+03] (for SIS=flu only)

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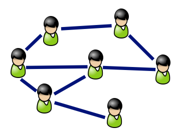
A2: will a virus take over?

- For **all** typical virus propagation models (flu, mumps, pertussis, HIV, etc)
- The **only** connectivity measure that matters, is

  $1/\lambda_1$

  the first eigenvalue of the adj. matrix
  [Prakash+, '10, arxiv]



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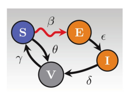
Thresholds for some models

- *s = effective strength*
- *s < 1 : below threshold*



Models	Effective Strength (s)	Threshold (tipping point)
SIS, SIR, SIRS, SEIR	$s = \lambda \, . \left(\frac{\beta}{\delta}\right)$	$s = 1$
SIV, SEIV	$s = \lambda \, . \left(\frac{\beta\gamma}{\delta(\gamma+\theta)}\right)$	
$SI_1I_2V_1V_2$ (**H.I.V.**)	$s = \lambda \, . \left(\frac{\beta_1 v_2 + \beta_2 \varepsilon}{v_2(\varepsilon + v_1)}\right)$	

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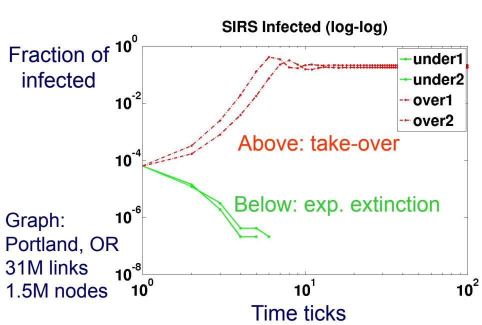
A2: will a virus take over?



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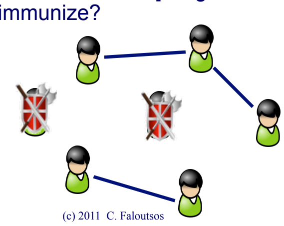
Q1: Immunization:

•Given
  •a network,
  •k vaccines, and
  •the virus details
•Which nodes to immunize?

A: immunize the ones that maximally raise the `epidemic threshold' [Tong+, ICDM'10]



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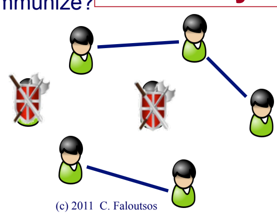
Q1: Immunization:

•Given
  •a network,
  •k vaccines, and
  •the virus details
•Which nodes to immunize?

A: immunize the ones that

Max eigen-drop $\Delta\lambda$ for any virus!



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Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
  - OddBall (anomaly detection)
  - Belief propagation
  - Immunization
- ➡ Problem#3: Scalability -PEGASUS
- Conclusions

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Scalability

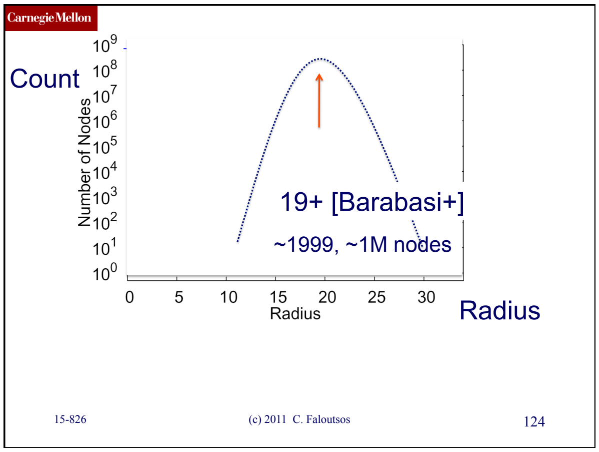
- Google: > 450,000 processors in clusters of ~2000 processors each [Barroso, Dean, Hölzle, *"Web Search for a Planet: The Google Cluster Architecture"* IEEE Micro 2003]
- Yahoo: 5Pb of data [Fayyad, KDD'07]
- Problem: machine failures, on a daily basis
- How to parallelize data mining tasks, then?
- A: map/reduce – hadoop (open-source clone) http://hadoop.apache.org/

Outline – Algorithms & results

	Centralized	Hadoop/ PEGASUS
Degree Distr.	old	old
Pagerank	old	old
➡ Diameter/ANF	old	**HERE**
Conn. Comp	old	**HERE**
Triangles	**done**	**HERE**
Visualization	**started**	

HADI for diameter estimation

- *Radius Plots for Mining Tera-byte Scale Graphs* **U Kang**, Charalampos Tsourakakis, Ana Paula Appel, Christos Faloutsos, Jure Leskovec, SDM'10
- Naively: diameter needs **O(N**2)** space and up to O(N**3) time – **prohibitive** (N~1B)
- Our HADI: linear on E (~10B)
  - Near-linear scalability wrt # machines
  - Several optimizations -> 5x faster


Carnegie Mellon
Count
Number of Nodes
10^9 10^8 10^7 10^6 10^5 10^4 10^3 10^2 10^1 10^0
19+ [Barabasi+]
~1999, ~1M nodes
0 5 10 15 20 25 30
Radius
Radius
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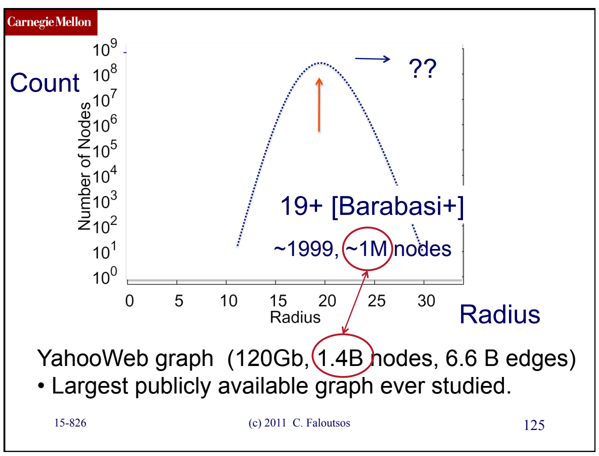
Carnegie Mellon
Count
Number of Nodes
10^9 10^8 10^7 10^6 10^5 10^4 10^3 10^2 10^1 10^0
??
19+ [Barabasi+]
~1999, ~1M nodes
0 5 10 15 20 25 30
Radius
Radius
YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)
• Largest publicly available graph ever studied.
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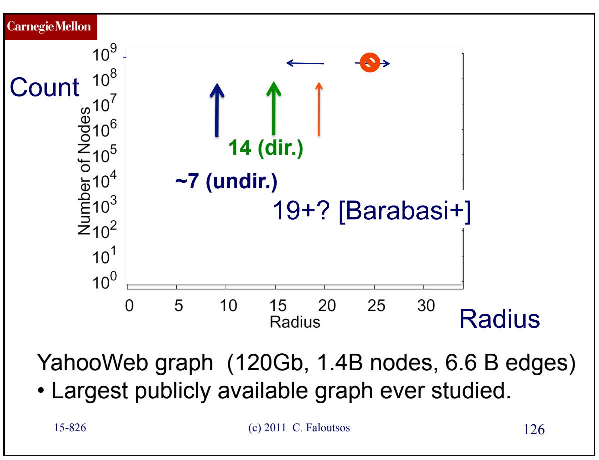
Carnegie Mellon
Count
Number of Nodes
10^9 10^8 10^7 10^6 10^5 10^4 10^3 10^2 10^1 10^0
14 (dir.)
~7 (undir.)
19+? [Barabasi+]
0 5 10 15 20 25 30
Radius
Radius
YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)
• Largest publicly available graph ever studied.
15-826
(c) 2011 C. Faloutsos
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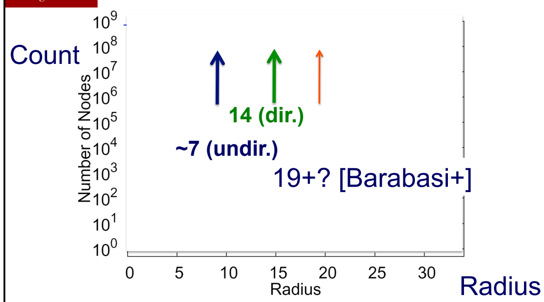

YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)
- 7 degrees of separation (!)
- Diameter: shrunk

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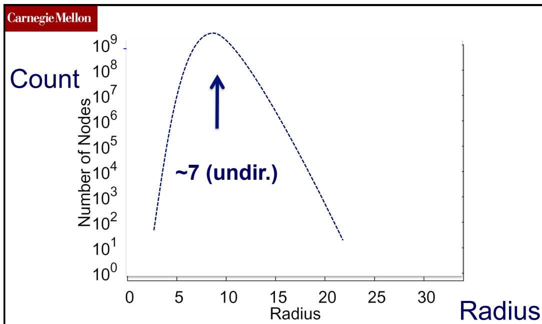

YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)
Q: Shape?

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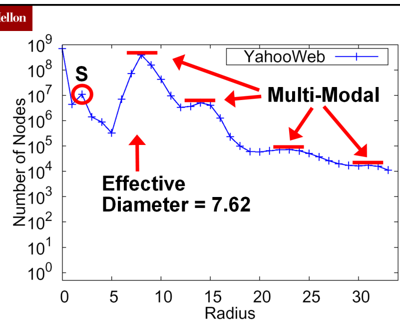

YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)
- effective diameter: surprisingly small.
- Multi-modality (?!)

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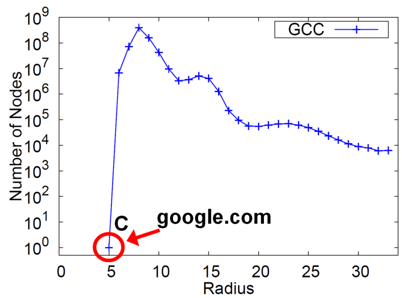

Radius Plot of **GCC** of YahooWeb.

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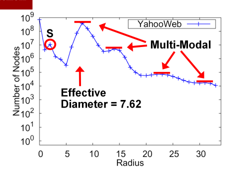

YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- effective diameter: surprisingly small.
- Multi-modality: probably mixture of cores .

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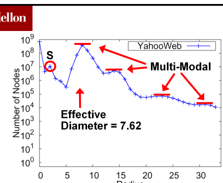
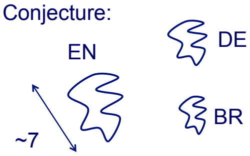


Conjecture:



YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- effective diameter: surprisingly small.
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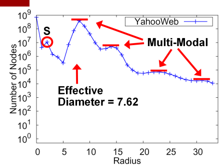
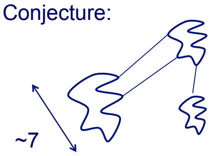


Conjecture:



YahooWeb graph (120Gb, 1.4B nodes, 6.6 B edges)

- effective diameter: surprisingly small.
- Multi-modality: probably mixture of cores .

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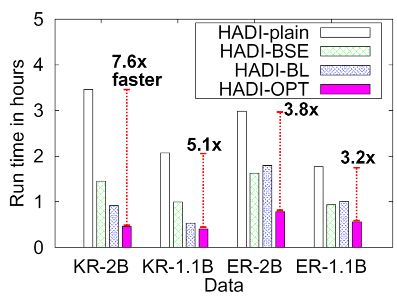
details



Running time - Kronecker and Erdos-Renyi Graphs with billions edges.

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Outline – Algorithms & results

	Centralized	Hadoop/ PEGASUS
Degree Distr.	old	old
Pagerank	old	old
Diameter/ANF	old	HERE
➡ Conn. Comp	old	HERE
Triangles		HERE
Visualization	started	

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Generalized Iterated Matrix Vector Multiplication (GIMV)

PEGASUS: A Peta-Scale Graph Mining System - Implementation and Observations. U Kang, Charalampos E. Tsourakakis, and Christos Faloutsos. (ICDM) 2009, Miami, Florida, USA. Best Application Paper (runner-up).

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details

Generalized Iterated Matrix Vector Multiplication (GIMV)

- PageRank
- proximity (RWR)
- Diameter
- Connected components
- (eigenvectors,
- Belief Prop.
- …)

Matrix – vector Multiplication (iterated)

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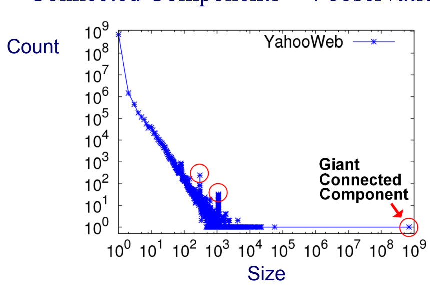
Example: GIM-V At Work

- Connected Components – 4 observations:



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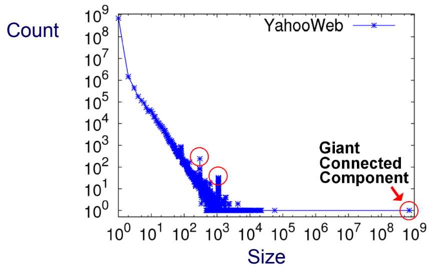
Example: GIM-V At Work

- Connected Components



1) 10K x larger than next

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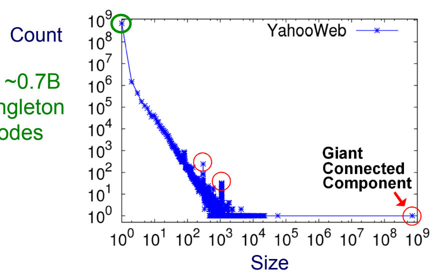
Example: GIM-V At Work

- Connected Components

2) ~0.7B singleton nodes



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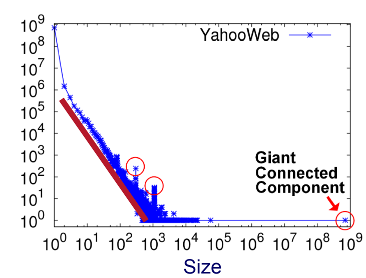
Example: GIM-V At Work

- Connected Components

3) SLOPE!



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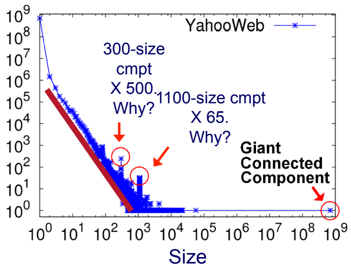
Example: GIM-V At Work

- Connected Components



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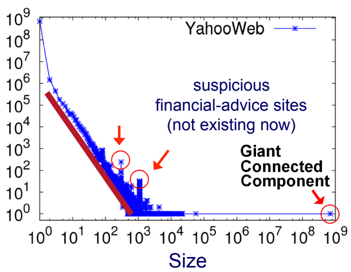
Example: GIM-V At Work

- Connected Components



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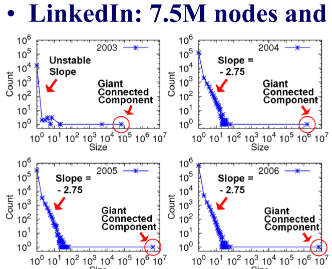
GIM-V At Work

- Connected Components over Time
- **LinkedIn: 7.5M nodes and 58M edges**



Stable tail slope after the gelling point

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Outline

- Introduction – Motivation
- Problem#1: Patterns in graphs
- Problem#2: Tools
- Problem#3: Scalability
- ➡ Conclusions

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OVERALL CONCLUSIONS – low level:

- Several new **patterns** (fortification, shrinking diameter, triangle-laws, conn. components, etc)
- New **tools**:
  - anomaly detection (OddBall), belief propagation, immunization
- **Scalability**: PEGASUS / hadoop

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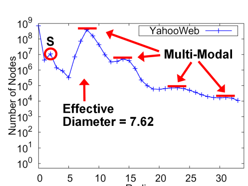
OVERALL CONCLUSIONS – high level

- **BIG DATA: Large** datasets reveal patterns/ outliers that are invisible otherwise



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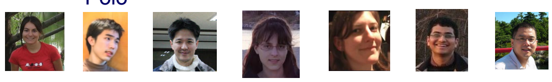
(Project info)

www.cs.cmu.edu/~pegasus

Chau, Polo

Koutra, Danae

Prakash, Aditya



Akoglu, Leman

Kang, U

McGlohon, Mary

Tong, Hanghang

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