

CMU S

15-826: Multimedia Databases and Data Mining

Lecture #12: Fractals - case studies Part III (regions, quadtrees, knn queries)

C. Faloutsos



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Must-read Material

 Alberto Belussi and Christos Faloutsos, <u>Estimating the Selectivity of Spatial Queries</u> <u>Using the `Correlation' Fractal Dimension</u> Proc. of VLDB, p. 299-310, 1995

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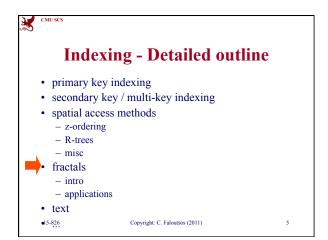
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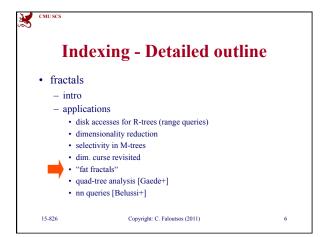
Optional Material

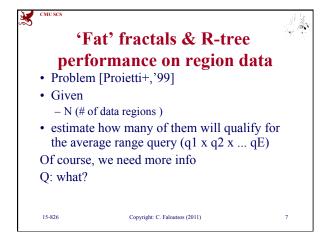
Optional, but very useful: Manfred Schroeder *Fractals, Chaos, Power Laws: Minutes from an Infinite Paradise* W.H. Freeman and Company, 1991

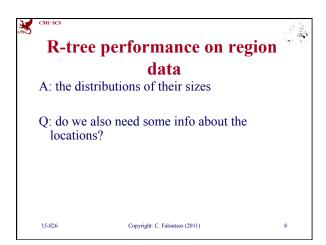
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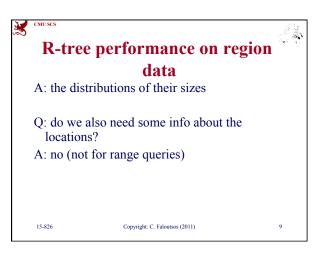


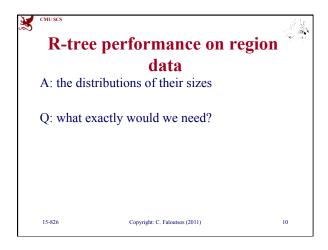


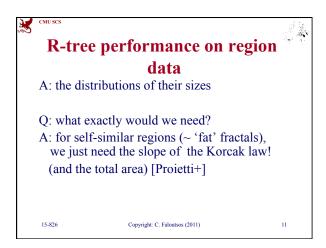


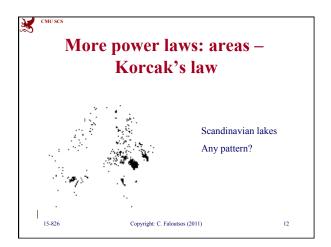


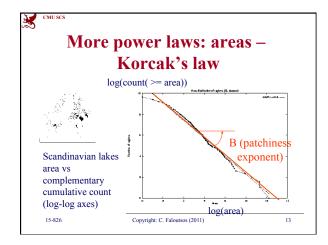












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R-tree performance on regions

- Once we know 'B' (and the total area)
- we can second-guess the individual sizes
- and then apply the [Pagel+93] formula
- Bottom line:

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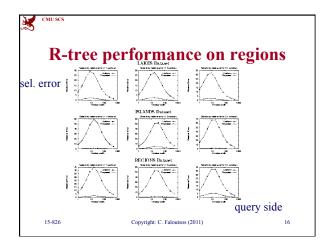
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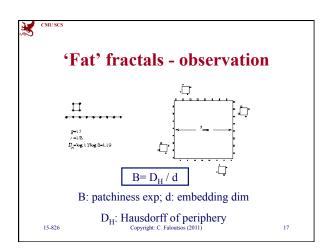


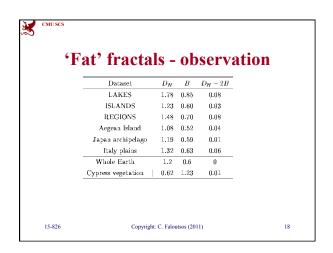
R-tree performance on regions

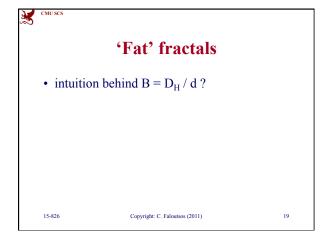
Dataset	N	A	В
LAKES	816	75,910	0.85
ISLANDS	470	136,893	0.60
REGIONS	757	190,526	0.70

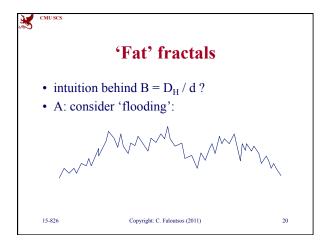
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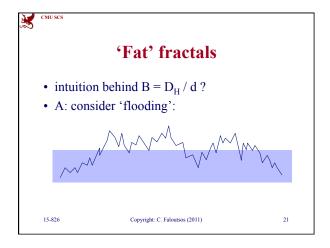


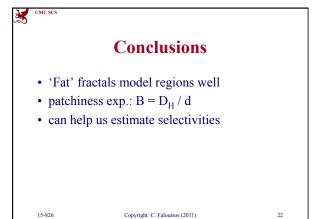


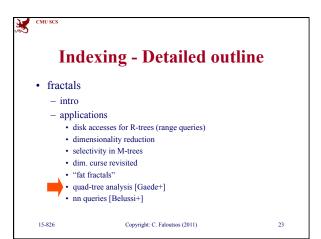


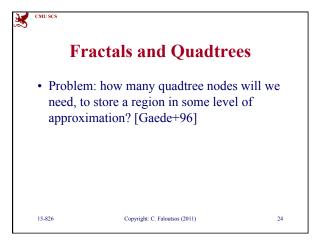


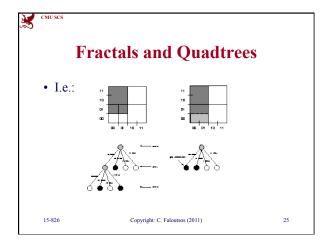


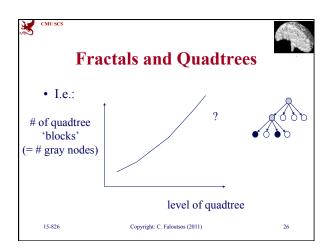


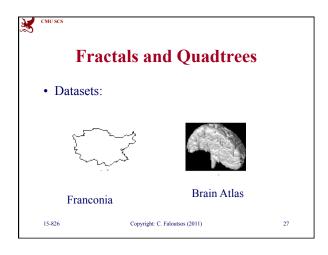


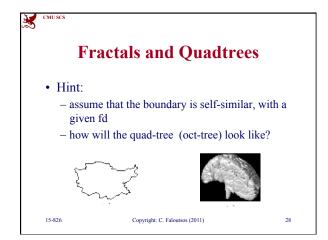


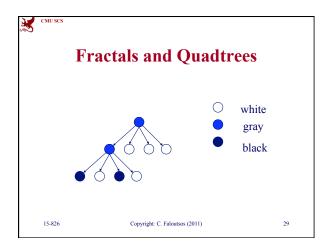


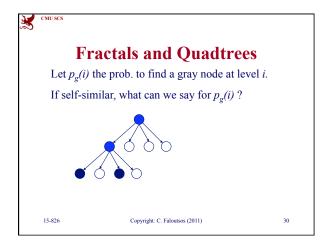


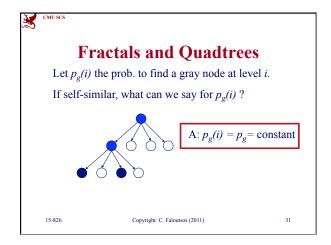


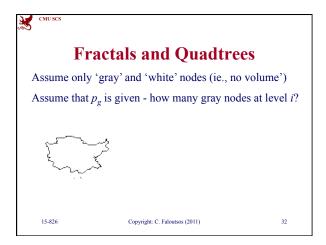


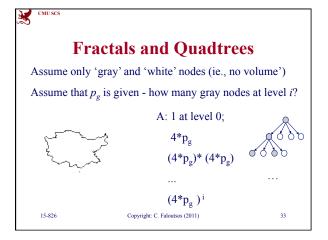


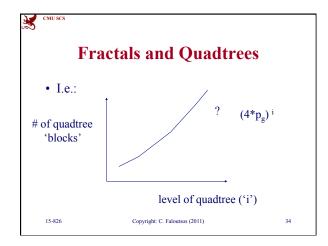


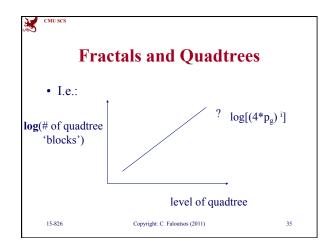


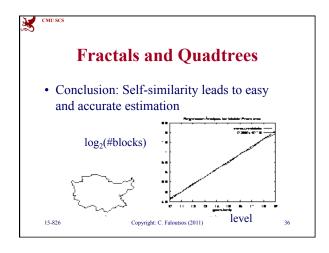




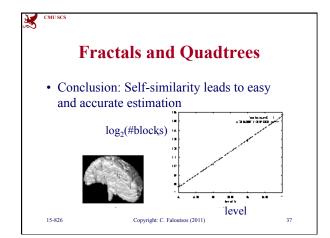


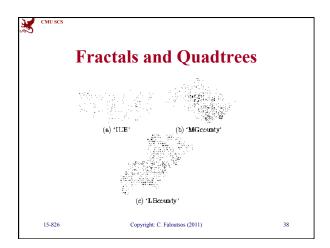


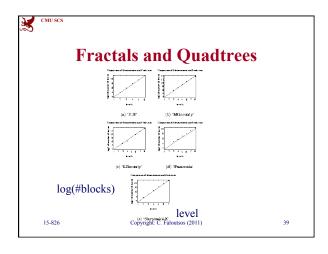




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Fractals and Quadtrees

• Final observation: relationship between p_{g} and fractal dimension?

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Fractals and Quadtrees

- Final observation: relationship between p_{φ} and fractal dimension?
- A: very close: $(4*p_{o})^{i} = \#$ of gray nodes at level i =# of Hausdorff grid-cells of side $(1/2)^i = r$ Eventually: $D_H = 2 + \log_2(p_g)$

and, for E-d spaces: $D_H = E + \log_2(p_g)$

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Fractals and Quadtrees

for E-d spaces: $D_H = E + log_2(p_g)$ Sanity check:

- point in 2-d: $D_H = 0$
- line in 2-d: $D_H = 1$ $p_{g} = ??$
- plane in 2-d: D_H =2 $p_{g} = ??$
- point in 3-d: $D_H = 0$ $p_g = ??$

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Fractals and Quadtrees for E-d spaces: $D_H = E + \log_2(p_g)$ Sanity check: - point in 2-d: $D_H = 0$ $p_{g} = 1/4$ - line in 2-d: $D_H = 1$ $p_{g} = 1/2$ - plane in 2-d: $D_H=2$ $p_g = 1$ - point in 3-d: $D_H = 0$ $p_g = 1/8$

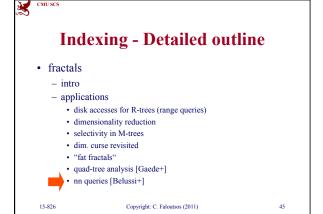
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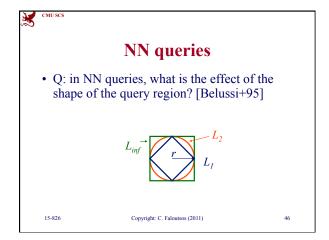
Fractals and Quadtrees

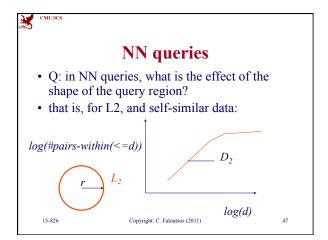
Final conclusions:

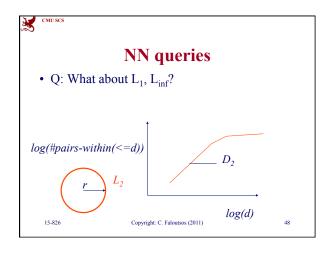
- self-similarity leads to estimates for # of zvalues = # of quadtree/oct-tree blocks
- close dependence on the Hausdorff fractal dimension of the boundary

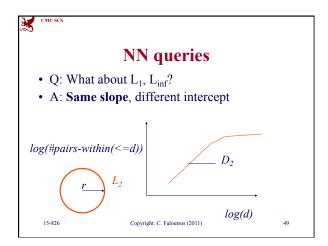
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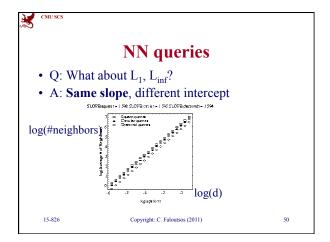


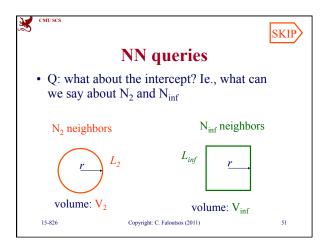


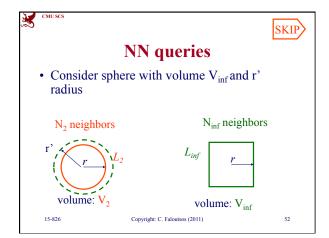










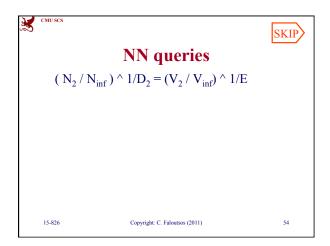


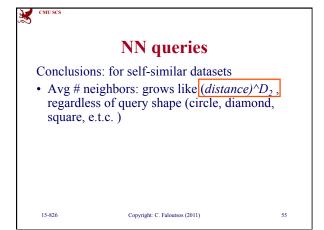
NN queries

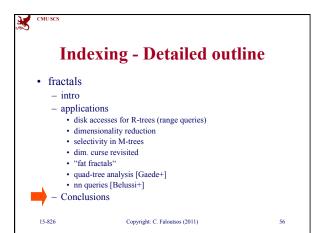
• Consider sphere with volume V_{inf} and r' radius

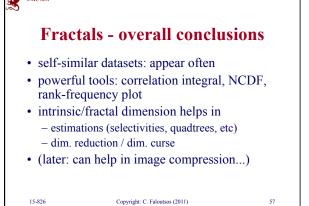
• $(r/r') ^E = V_2 / V_{inf}$ • $(r/r') ^D_2 = N_2 / N_2'$ • $N_2' = N_{inf}$ (since shape does not matter)

• and finally:









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References

 Belussi, A. and C. Faloutsos (Sept. 1995). Estimating the Selectivity of Spatial Queries Using the 'Correlation' Fractal Dimension. Proc. of VLDB, Zurich, Switzerland.

- Faloutsos, C. and V. Gaede (Sept. 1996). Analysis of the zordering Method Using the Hausdorff Fractal Dimension. VLDB. Bombay. India.
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 3. Proietti, G. and C. Faloutsos (March 23-26, 1999). I/O complexity for range queries on region data stored using an Rtree. International Conference on Data Engineering (ICDE), Sydney, Australia.

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