

Anomaly detection in large graphs

Christos Faloutsos

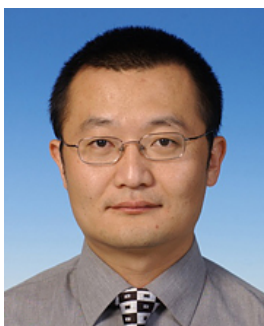
CMU

www.cs.cmu.edu/~christos/TALKS/17-05-26-HKUST/

Thank you!



- Prof. Qiang Yang



- Prof. Lei CHEN

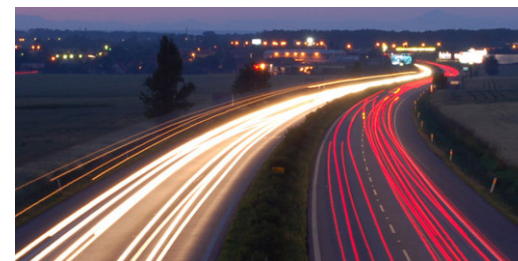
- Irene Lau

‘Hi’ to friends



Roadmap

- ➔ • Introduction – Motivation
 - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- Conclusions



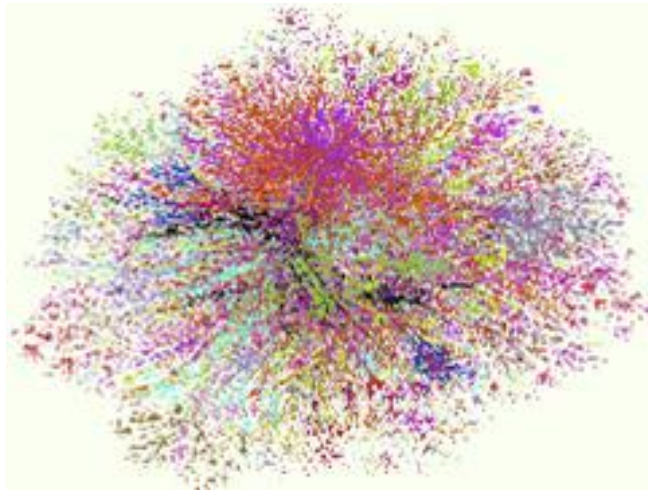
Graphs - why should we care?



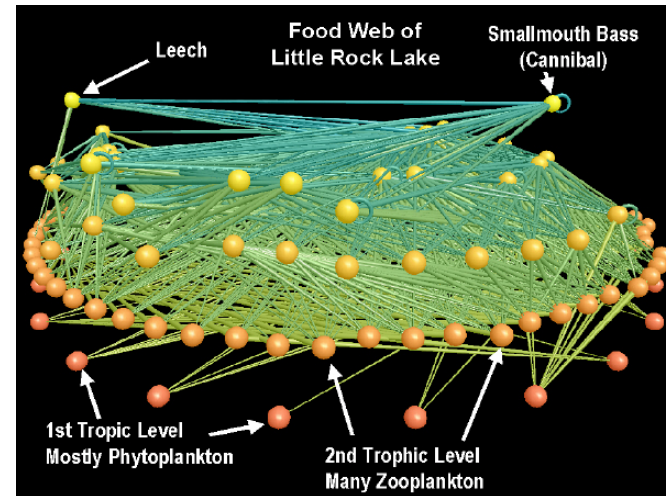
>\$10B; ~1B users



Graphs - why should we care?



Internet Map
[lumeta.com]



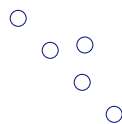
Food Web
[Martinez '91]

Graphs - why should we care?

- web-log ('blog') news propagation 
- computer network security: email/IP traffic and anomaly detection
- Recommendation systems 
-
- Many-to-many db relationship -> graph

Motivating problems

- P1: patterns? Fraud detection?



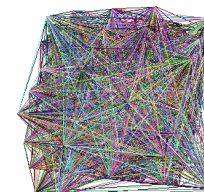
- P2: patterns in time-evolving graphs / tensors

destination



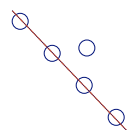
source

time



Motivating problems

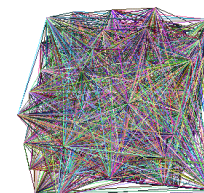
- P1: patterns? Fraud detection?



Patterns



anomalies



- P2: patterns in time-evolving graphs / tensors

destination

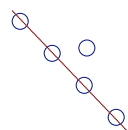


source

time

Motivating problems

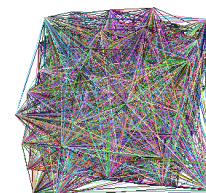
- P1: patterns? Fraud detection?



Patterns



anomalies*



- P2: patterns in time-evolving graphs / tensors

destination

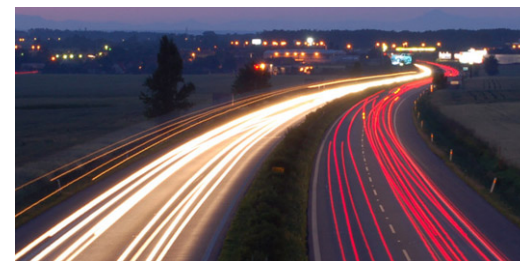


source

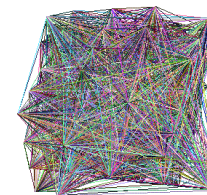
time

*** Robust Random Cut Forest Based Anomaly Detection on Streams** Sudipto Guha, Nina Mishra , Gourav Roy, Okke Schrijvers, ICML'16

Roadmap



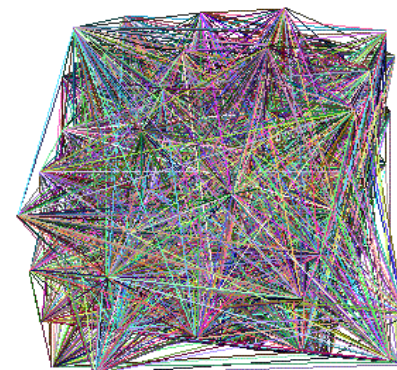
- Introduction – Motivation
 - Why study (big) graphs?
- ➔ • Part#1: Patterns & fraud detection
- Part#2: time-evolving graphs; tensors
- Conclusions



Part 1: Patterns, & fraud detection

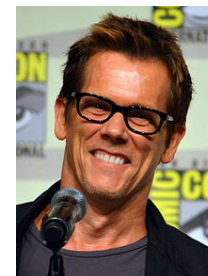
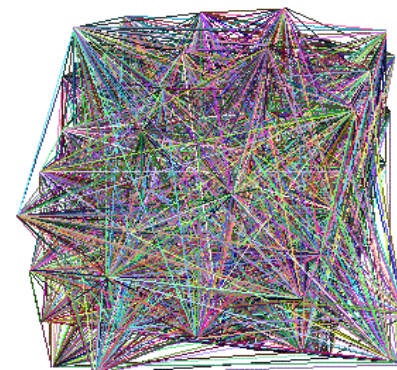
Laws and patterns

- Q1: Are real graphs random?



Laws and patterns

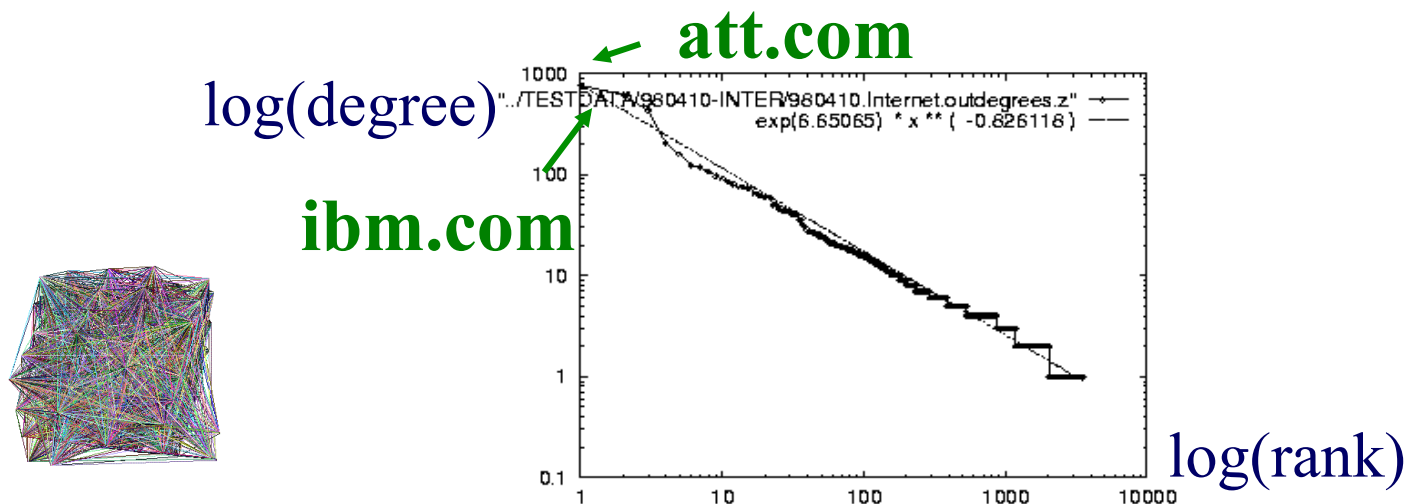
- Q1: Are real graphs random?
- A1: NO!!
 - Diameter ('6 degrees'; 'Kevin Bacon')
 - in- and out- degree distributions
 - other (surprising) patterns
- So, let's look at the data



Solution# S.1

- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

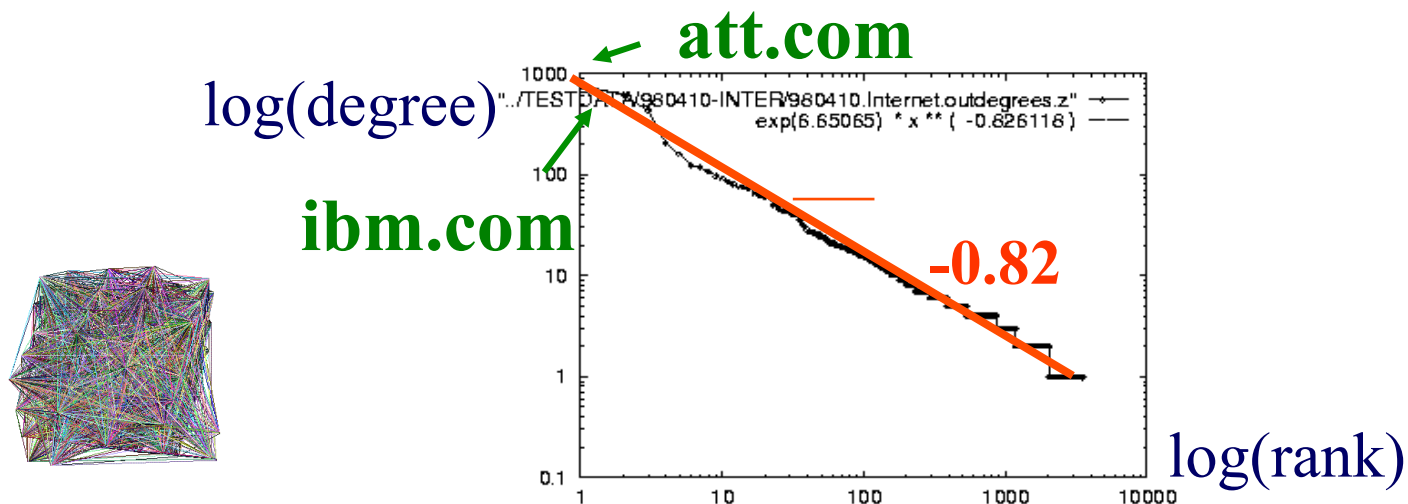
internet domains



Solution# S.1

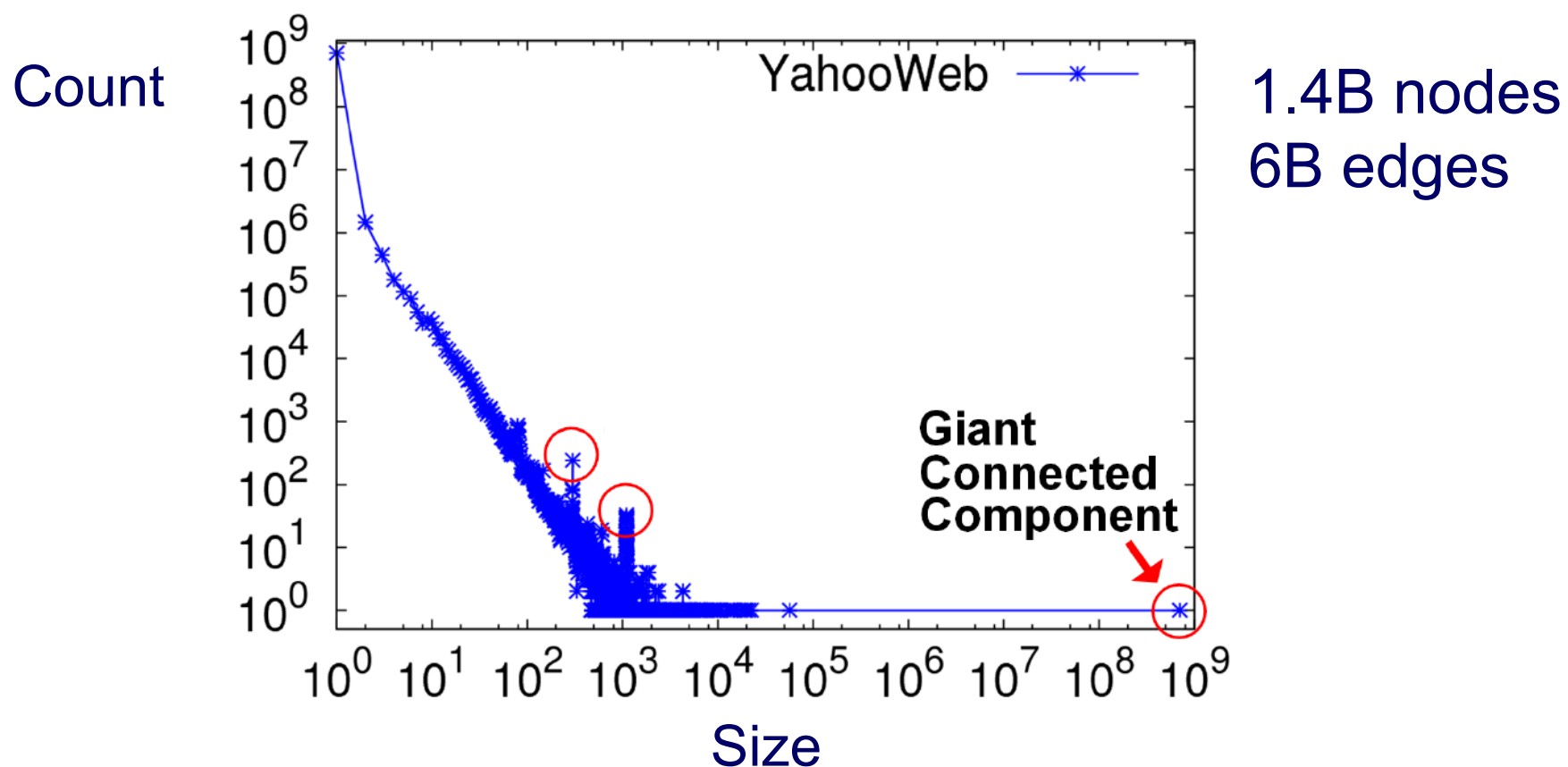
- Power law in the degree distribution [Faloutsos x 3 SIGCOMM99]

internet domains



S2: connected component sizes

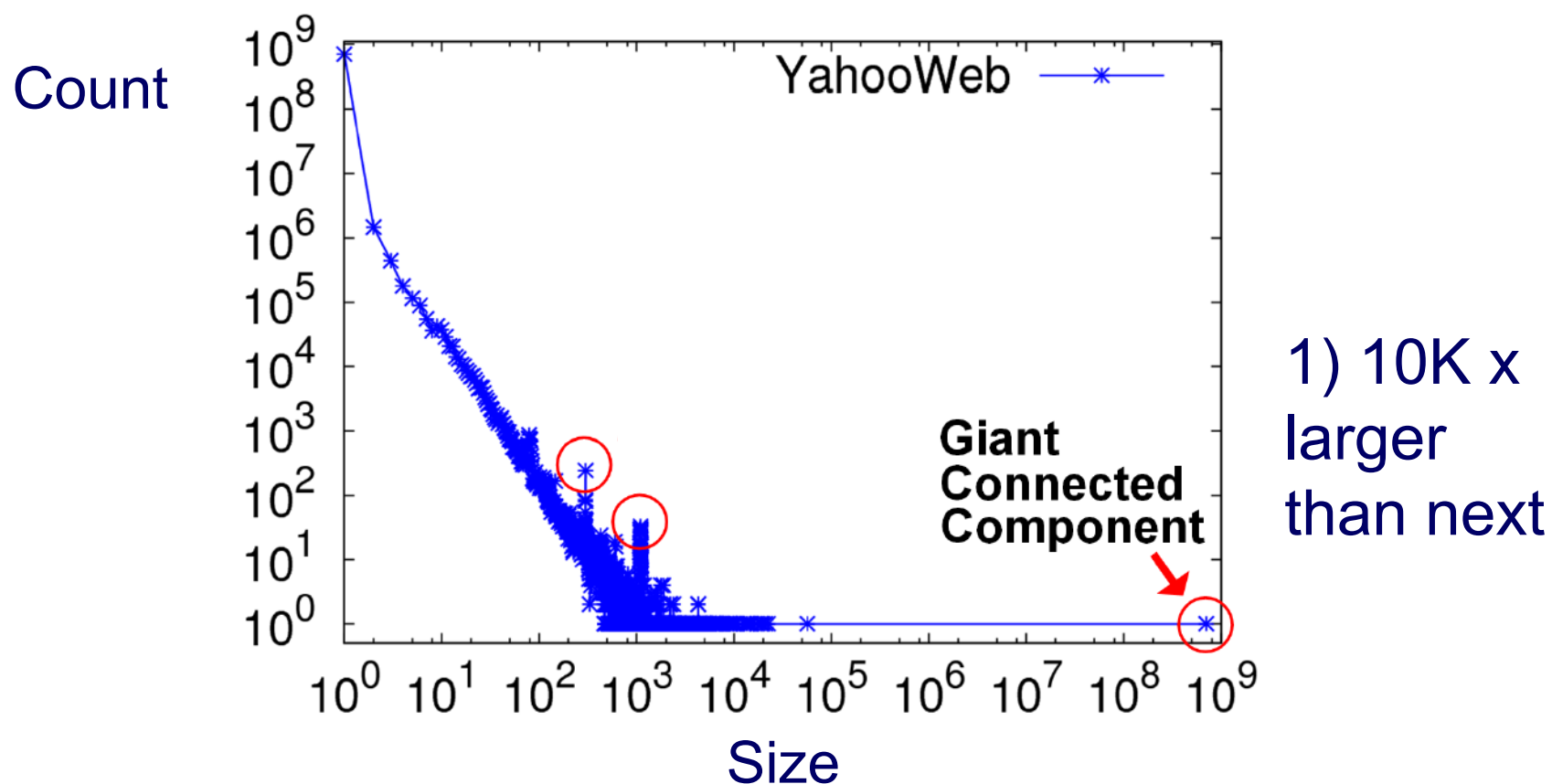
- Connected Components – 4 observations:



S2: connected component sizes



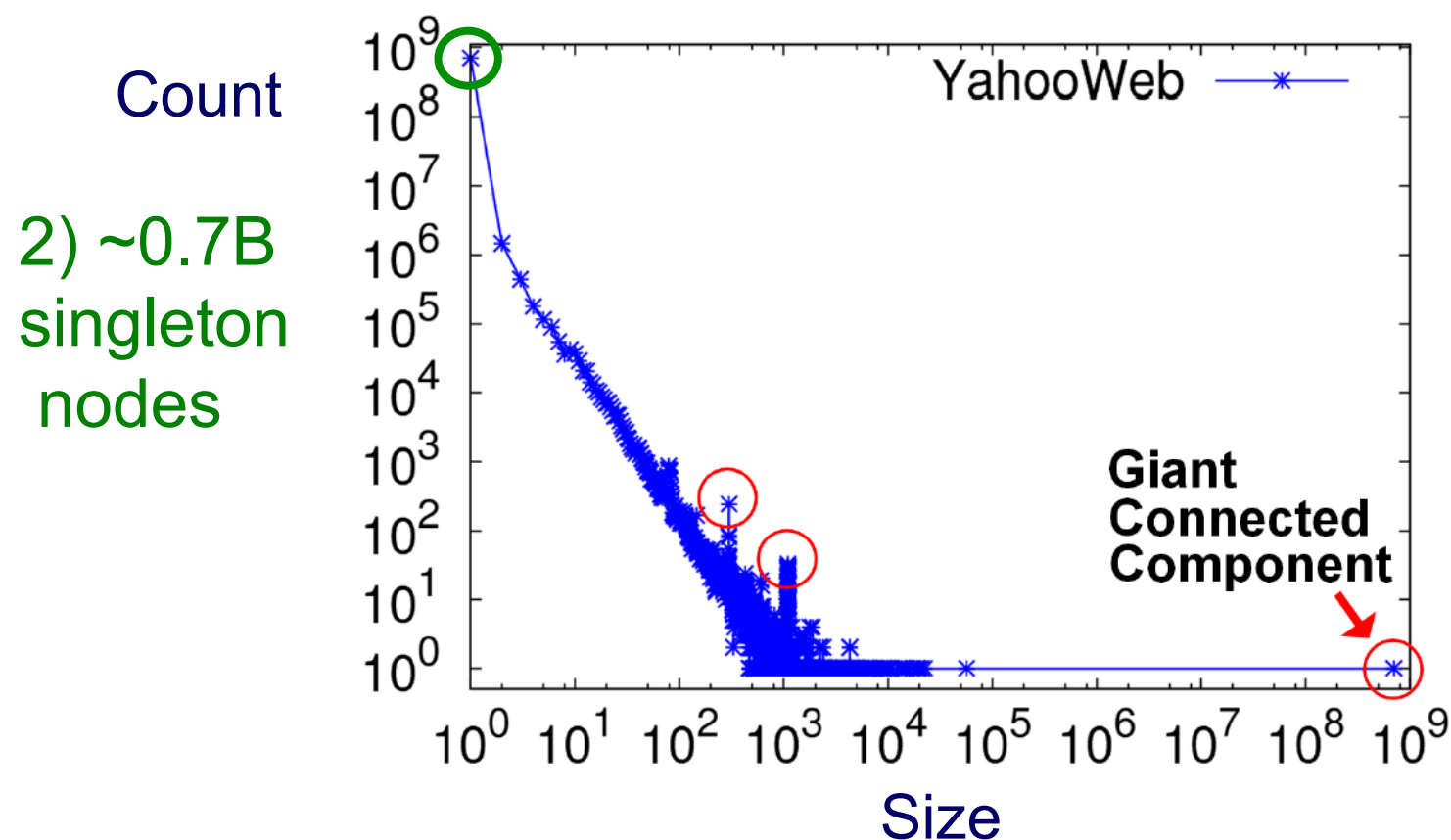
- Connected Components



S2: connected component sizes



- Connected Components

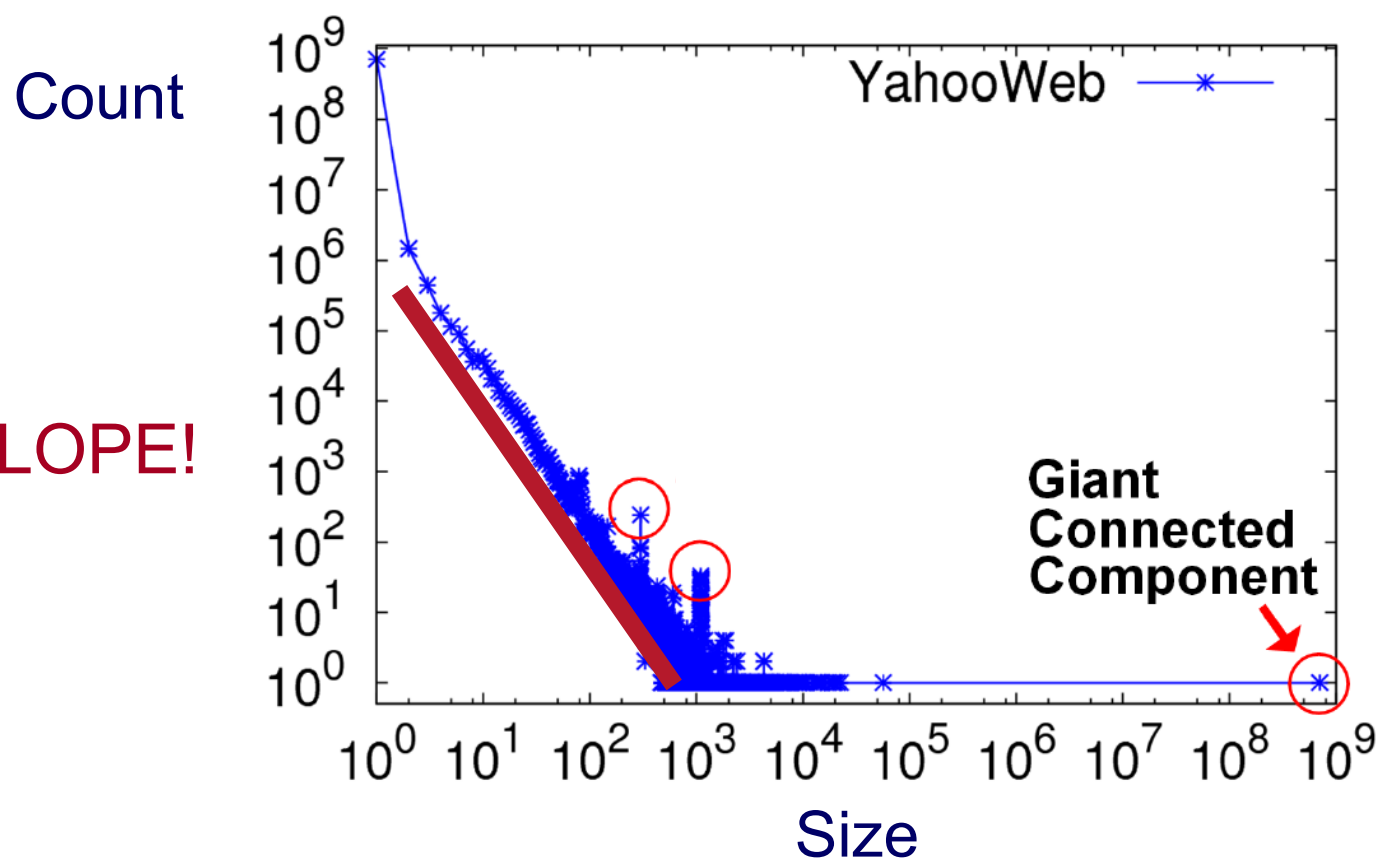


S2: connected component sizes



- Connected Components

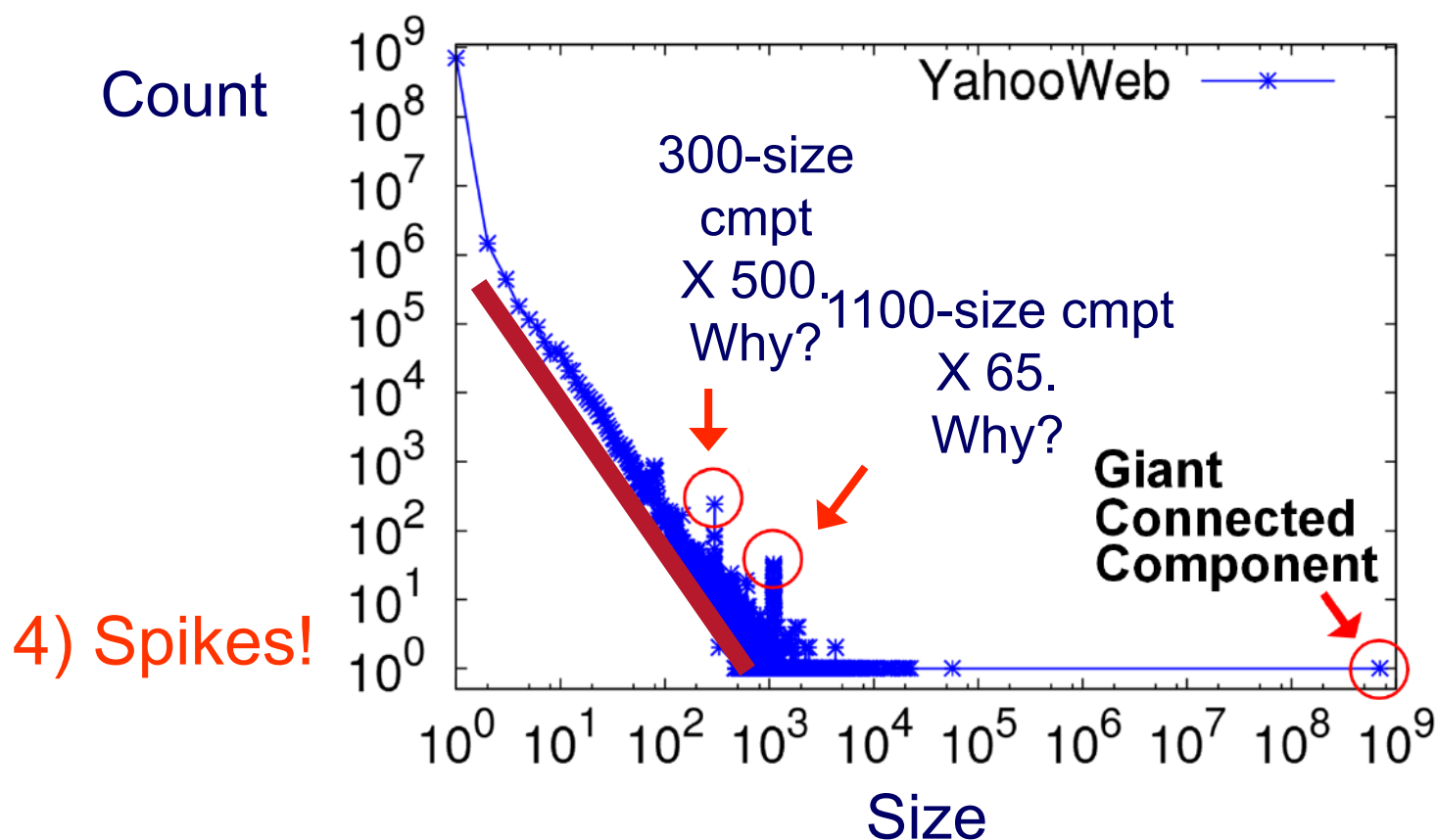
3) SLOPE!



S2: connected component sizes



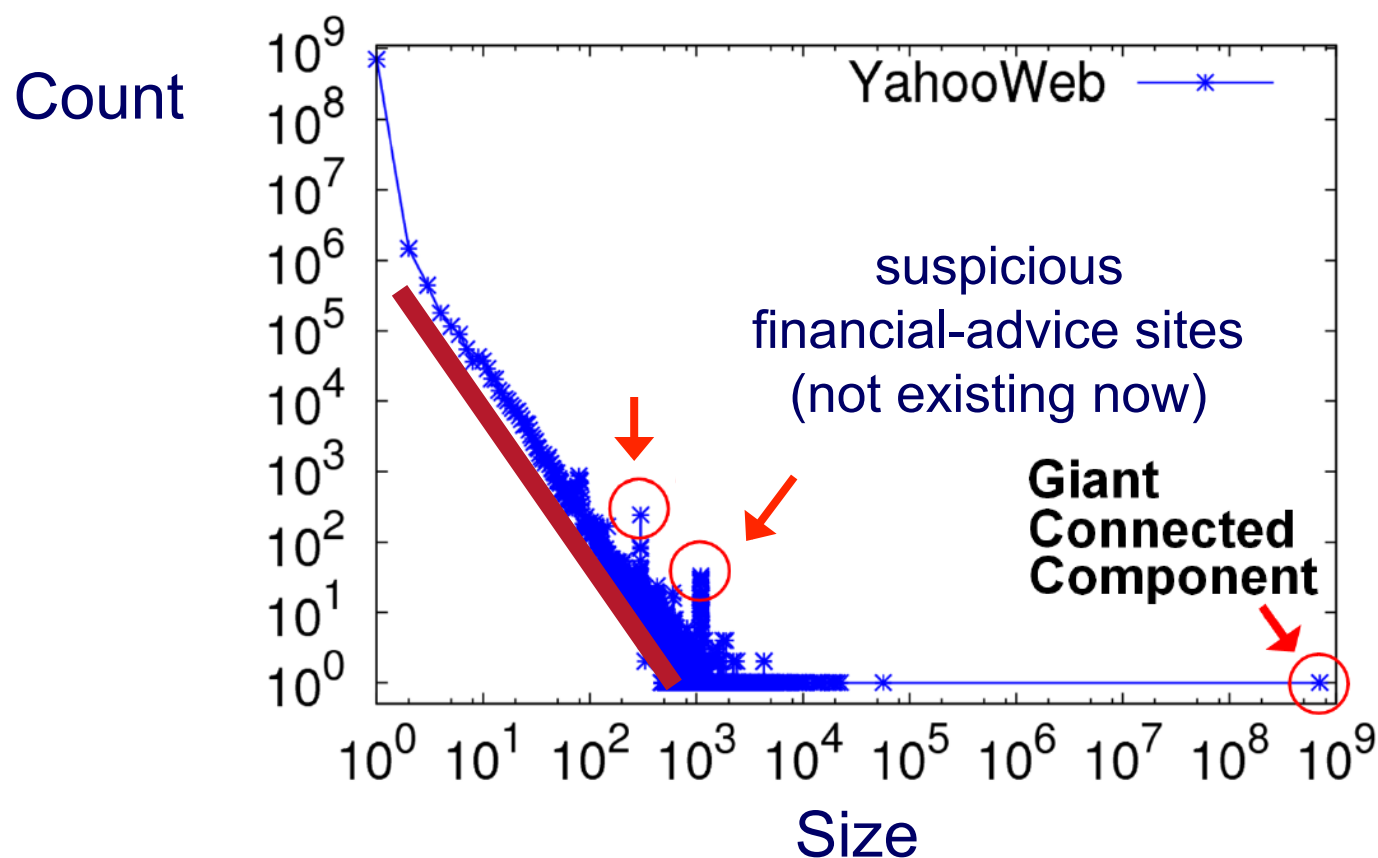
- Connected Components



S2: connected component sizes

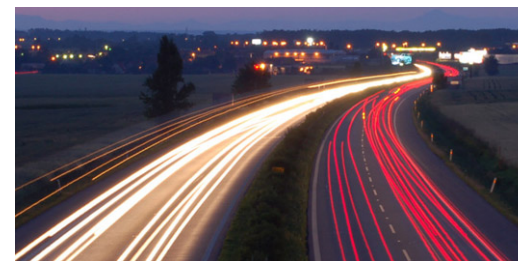


- Connected Components

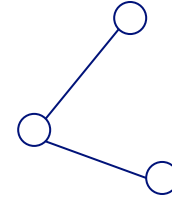


Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs
 - ➔ – P1.1: Patterns: Degree; Triangles
 - P1.2: Anomaly/fraud detection
- Part#2: time-evolving graphs; tensors
- Conclusions

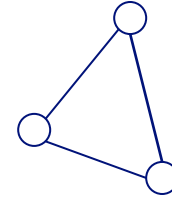


Solution# S.3: Triangle ‘Laws’

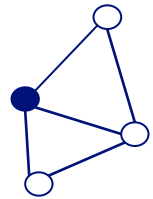


- Real social networks have a lot of triangles

Solution# S.3: Triangle ‘Laws’



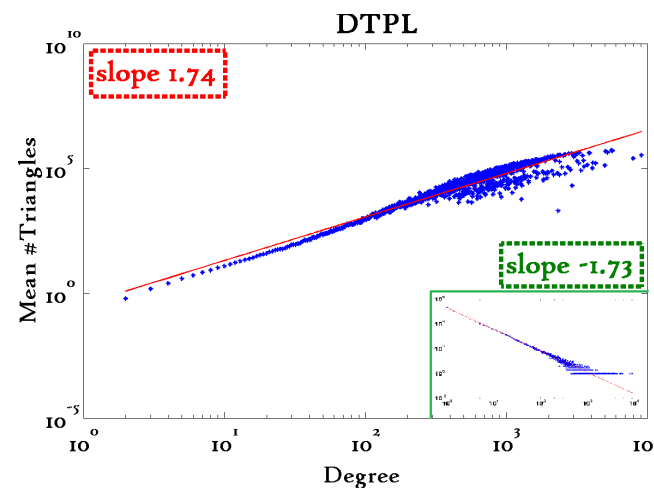
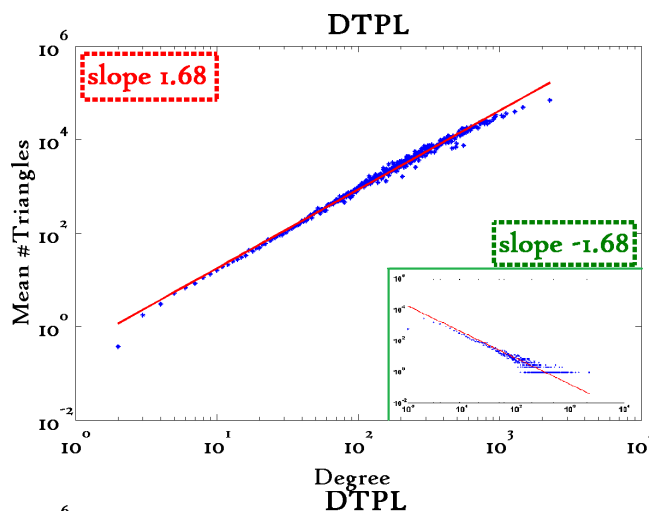
- Real social networks have a lot of triangles
 - Friends of friends are friends
- Any patterns?
 - 2x the friends, 2x the triangles ?



Triangle Law: #S.3

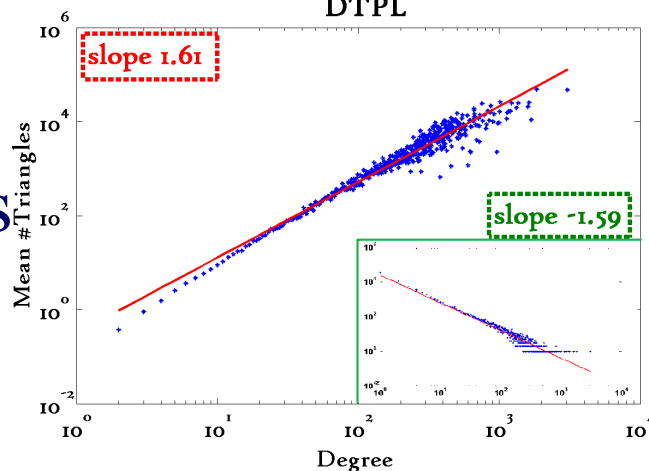
[Tsourakakis ICDM 2008]

Reuters



SN

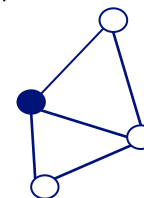
Epinions



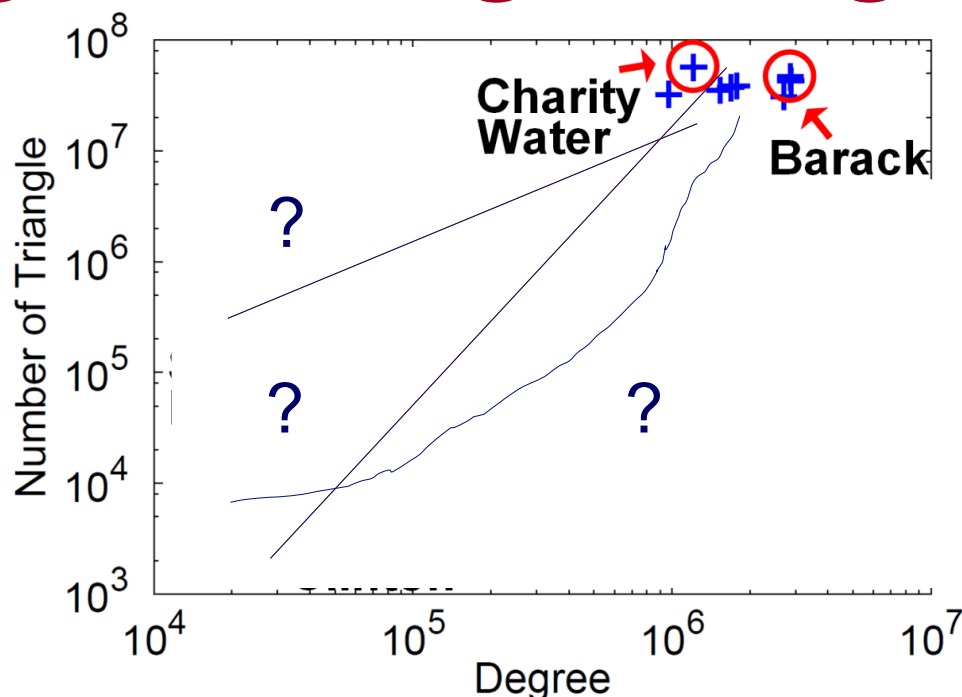
X-axis: degree

Y-axis: mean # triangles

n friends $\rightarrow \sim n^{1.6}$ triangles



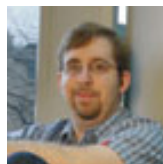
Triangle counting for large graphs?



Anomalous nodes in Twitter (~ 3 billion edges)

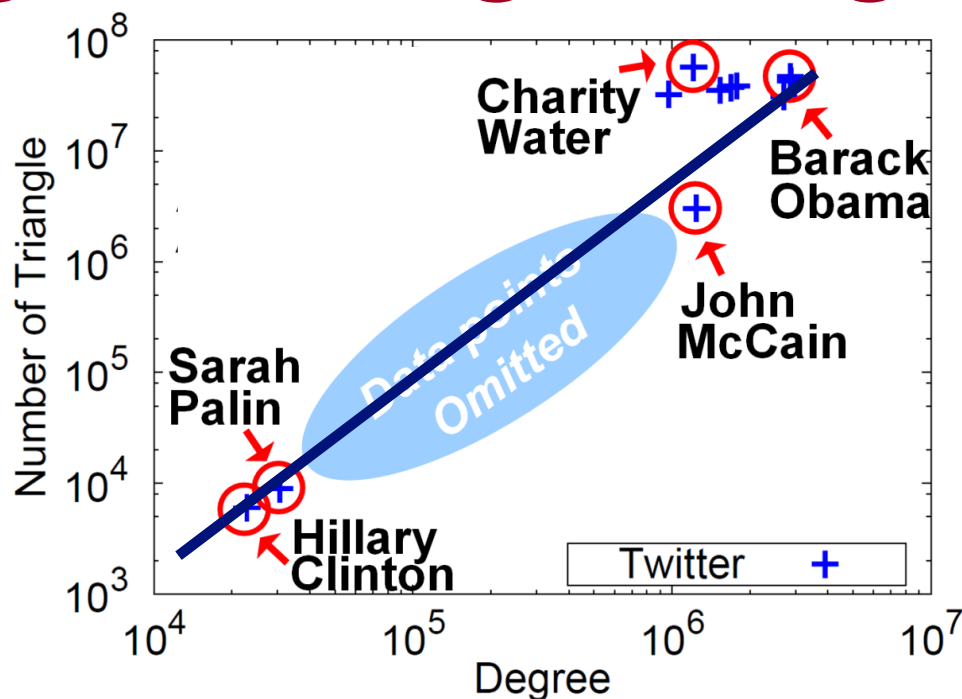
[U Kang, Brendan Meeder, +, PAKDD'11]

HKUST, May



(c) C. Faloutsos, 2017

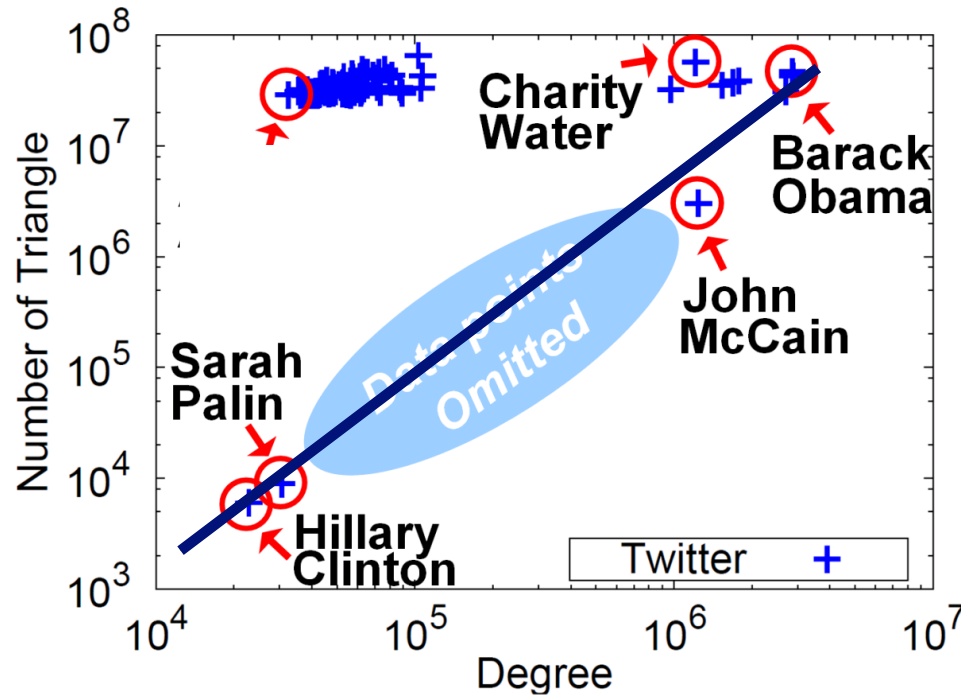
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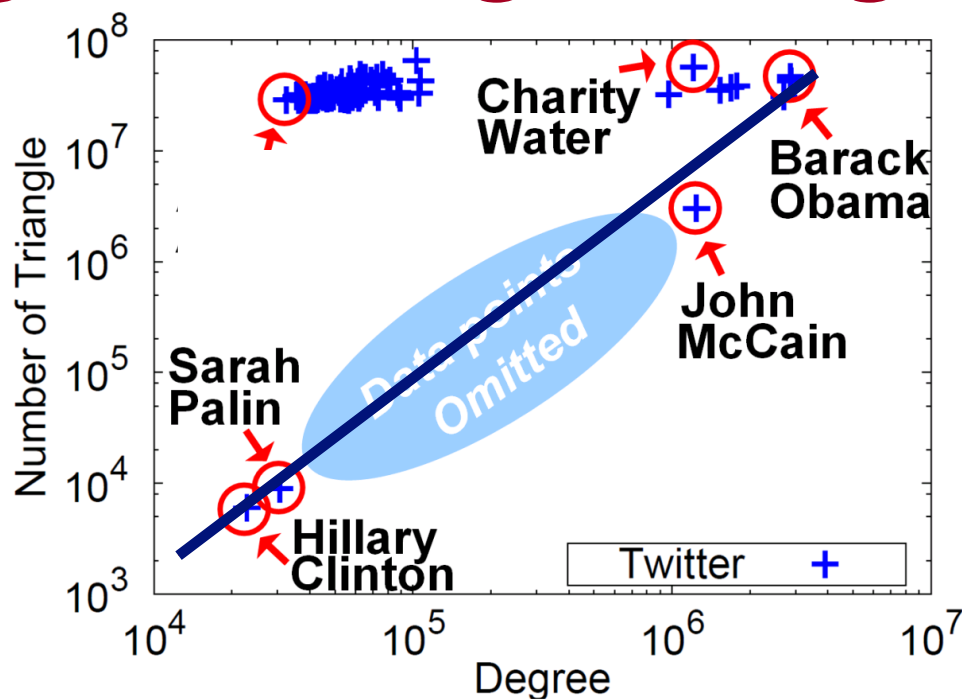
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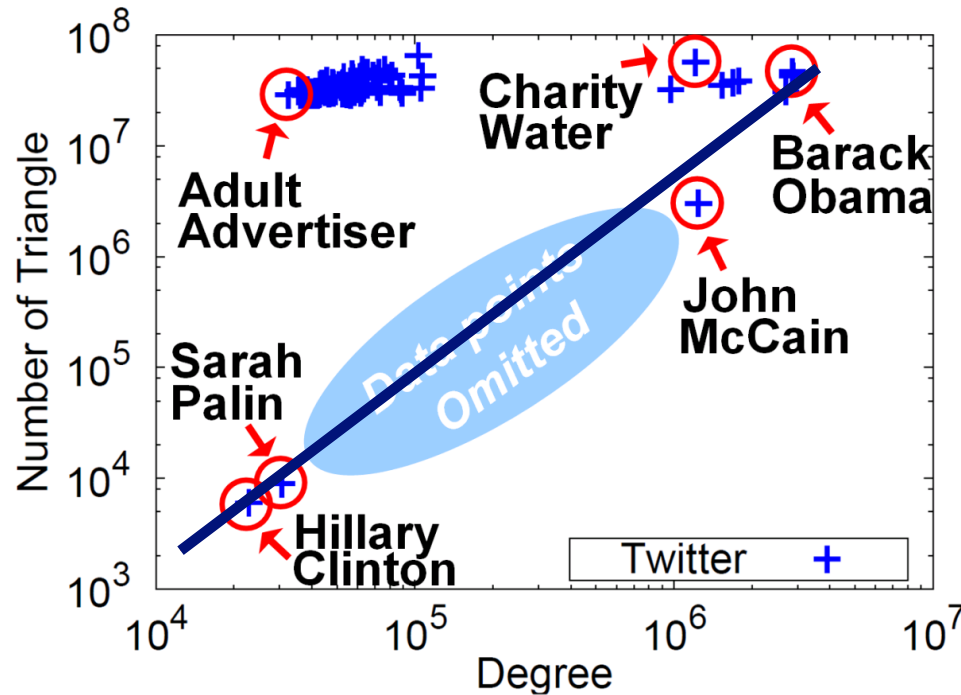
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MORE Graph Patterns

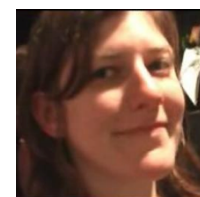
	Unweighted	Weighted
Static	✓ L01. Power-law degree distribution [Faloutsos et al. '99, Kleinberg et al. '99, Chakrabarti et al. '04, Newman '04] ✓ L02. Triangle Power Law (TPL) [Tsourakakis '08] L03. Eigenvalue Power Law (EPL) [Siganos et al. '03] L04. Community structure [Flake et al. '02, Girvan and Newman '02]	L10. Snapshot Power Law (SPL) [McGlohon et al. '08]
Dynamic	L05. Densification Power Law (DPL) [Leskovec et al. '05] L06. Small and shrinking diameter [Albert and Barabási '99, Leskovec et al. '05] ✓ L07. Constant size 2nd and 3rd connected components [McGlohon et al. '08] L08. Principal Eigenvalue Power Law (λ_1PL) [Akoglu et al. '08] L09. Bursty/self-similar edge/weight additions [Gomez and Santonja '98, Gribble et al. '98, Crovella and	L11. Weight Power Law (WPL) [McGlohon et al. '08]

RTG: A Recursive Realistic Graph Generator using Random Typing Leman Akoglu and Christos Faloutsos. *PKDD'09*.

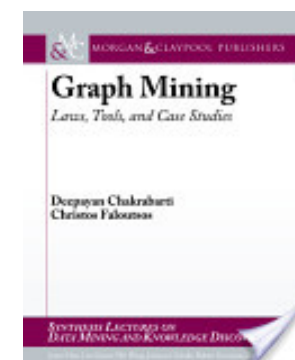
MORE Graph Patterns

	Unweighted	Weighted
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- Mary McGlohon, Leman Akoglu, Christos Faloutsos. *Statistical Properties of Social Networks*. in "Social Network Data Analytics" (Ed.: Charu Aggarwal)

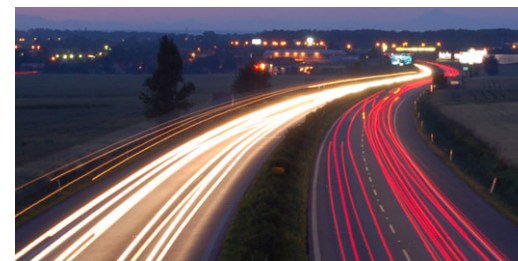


- Deepayan Chakrabarti and Christos Faloutsos, [*Graph Mining: Laws, Tools, and Case Studies*](#) Oct. 2012, Morgan Claypool.



Roadmap

- Introduction – Motivation
- Part#1: Patterns in graphs



- P1.1: Patterns



- P1.2: Anomaly / fraud detection

- No labels – spectral

Patterns



anomalies

- With labels: Belief Propagation

- Part#2: time-evolving graphs; tensors
- Conclusions

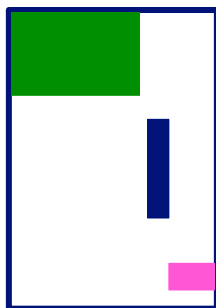
How to find ‘suspicious’ groups?

- ‘blocks’ are normal, right?



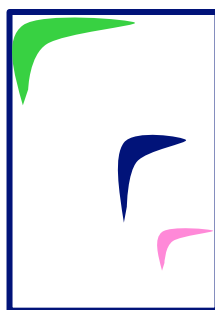
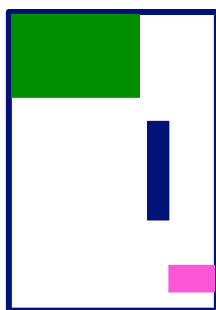
idols

fans



Except that:

- ‘blocks’ are normal, ~~right?~~
- ‘hyperbolic’ communities are more realistic [Araujo+, PKDD’14]

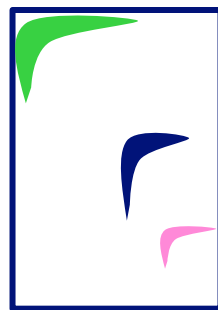
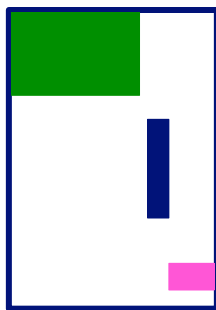


Except that:

- ‘blocks’ are usually **suspicious**
- ‘hyperbolic’ communities are more realistic [Araujo+, PKDD’14]



Q: Can we spot blocks, easily?



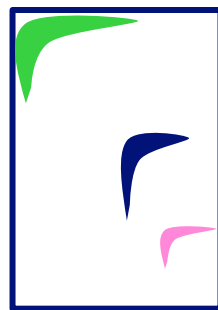
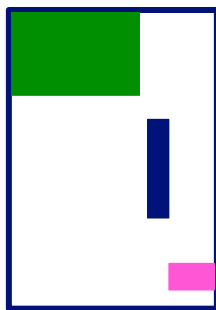
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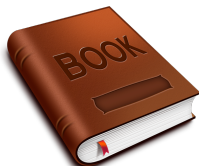
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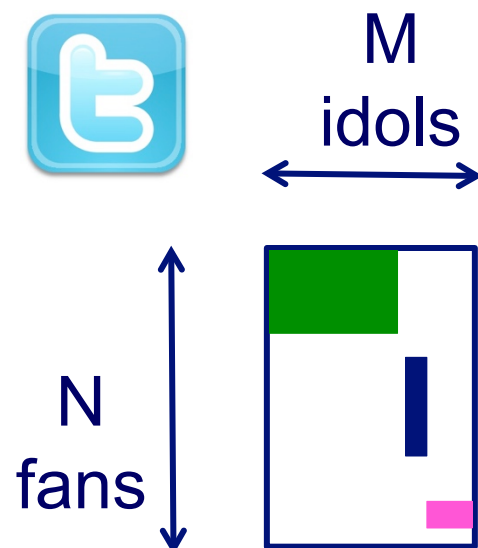
A: Silver bullet: SVD!



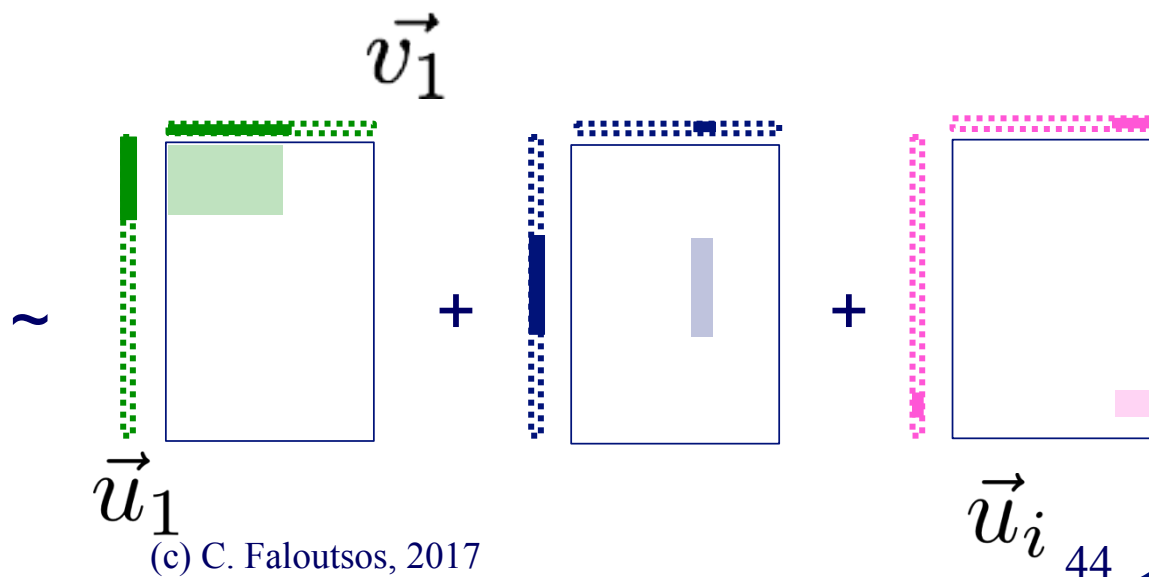


Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks

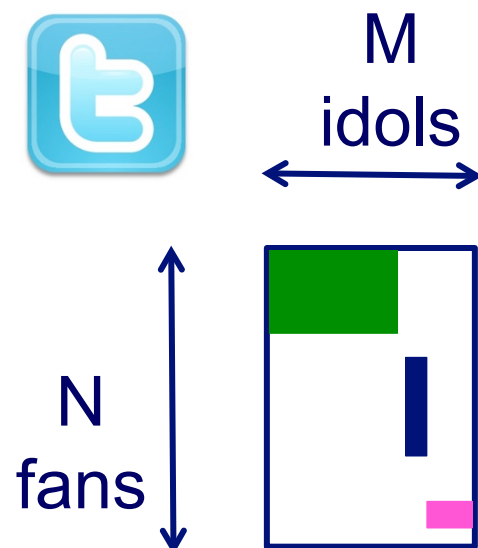


'music lovers' 'singers' $\vec{v}_1$
 'sports lovers' 'athletes'
 'citizens' 'politicians'



Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks



$$\begin{array}{c}
 \text{'music lovers' 'singers'} \quad \text{'sports lovers' 'athletes'} \quad \text{'citizens' 'politicians'} \\
 \vec{v}_1 \quad \quad \quad \vec{v}_1 \quad \quad \quad \vec{v}_1 \\
 \sim \quad \quad \quad + \quad \quad \quad + \quad \quad \quad \\
 \vec{u}_1 \quad \quad \quad \vec{u}_i \quad \quad \quad \vec{u}_{45}
 \end{array}$$

(c) C. Faloutsos, 2017

Inferring Strange Behavior from Connectivity Pattern in Social Networks

PAKDD'14



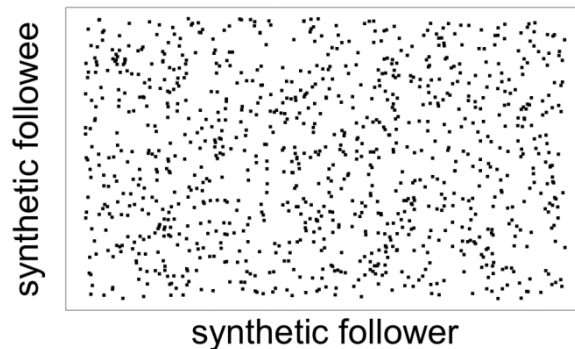
Meng Jiang, Peng Cui, Shiqiang Yang (Tsinghua)
Alex Beutel, Christos Faloutsos (CMU)



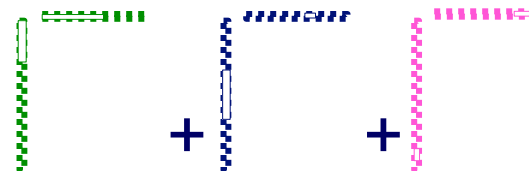
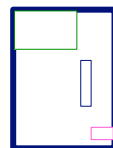
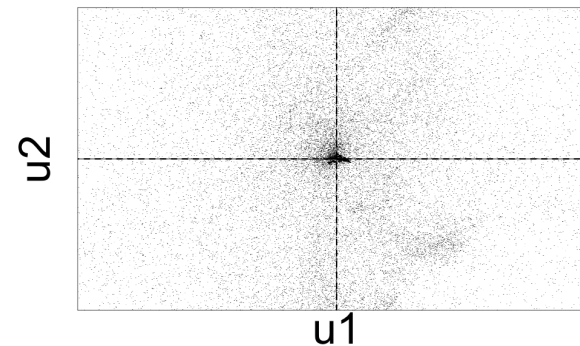
Lockstep and Spectral Subspace Plot

- Case #0: No lockstep behavior in random power law graph of 1M nodes, 3M edges
- Random $\longleftrightarrow$ “Scatter”

Adjacency Matrix



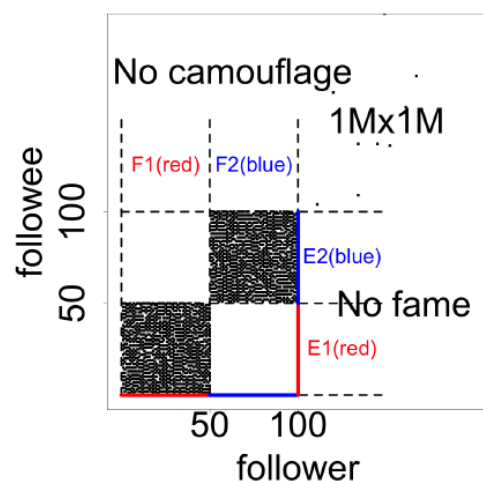
(dimensionality reduction)
Spectral Subspace Plot



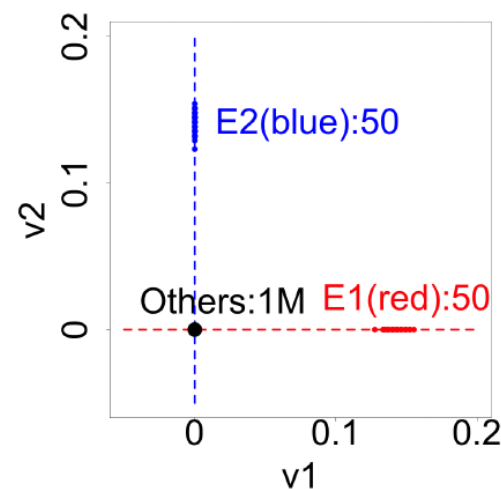
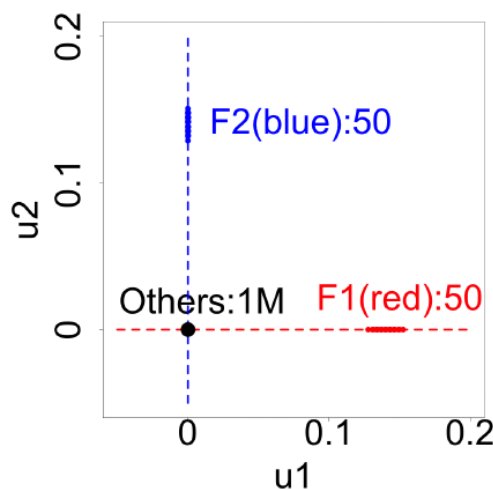
Lockstep and Spectral Subspace Plot

- Case #1: non-overlapping lockstep
- “Blocks” $\longleftrightarrow$ “Rays”

Adjacency Matrix



Spectral Subspace Plot

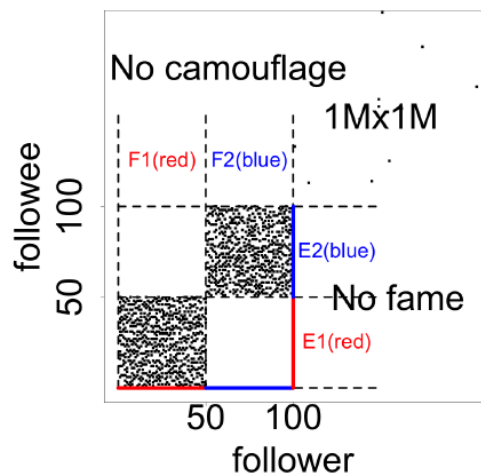


Rule 1 (short “rays”): two blocks, high density (90%), no “camouflage”, no “fame”

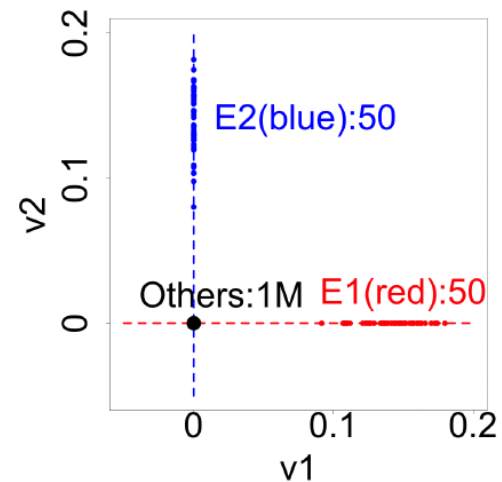
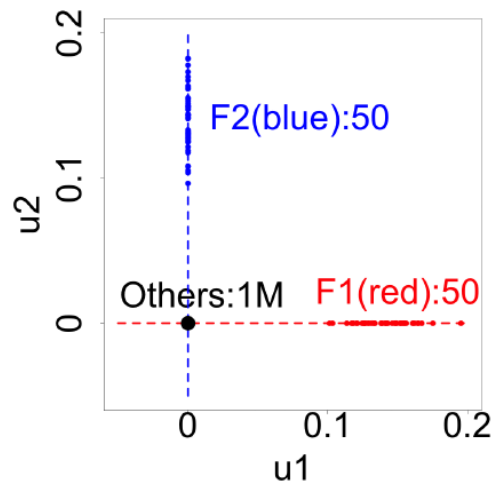
Lockstep and Spectral Subspace Plot

- Case #2: non-overlapping lockstep
- “Blocks; low density” $\longleftrightarrow$ Elongation

Adjacency Matrix



Spectral Subspace Plot



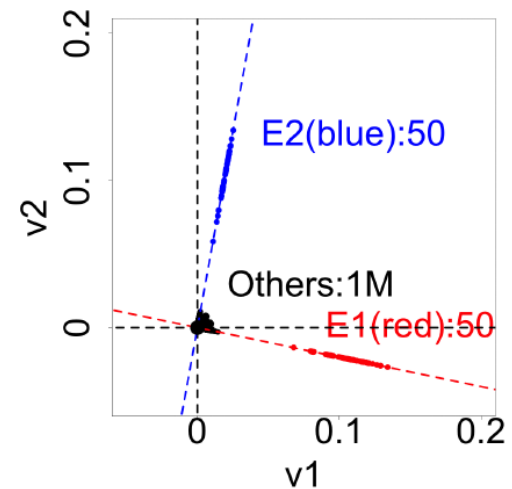
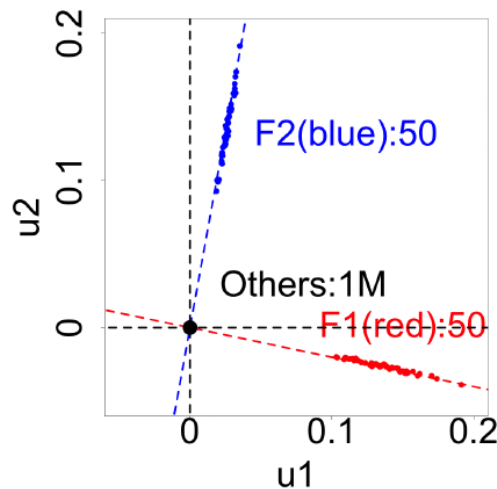
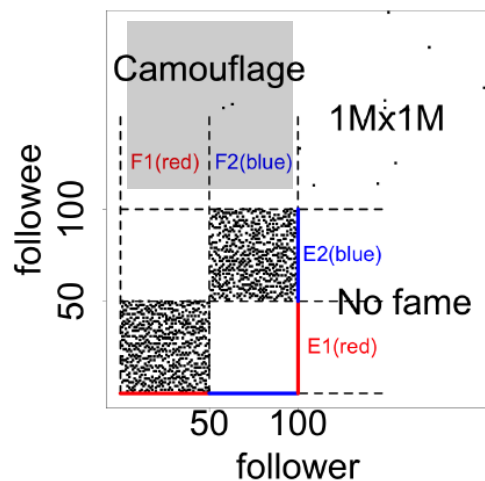
Rule 2 (long “rays”): two blocks, low density (50%), no “camouflage”, no “fame”

Lockstep and Spectral Subspace Plot

- Case #3: non-overlapping lockstep
- “Camouflage” (or “Fame”) $\longleftrightarrow$ Tilting “Rays”

Adjacency Matrix

Spectral Subspace Plot

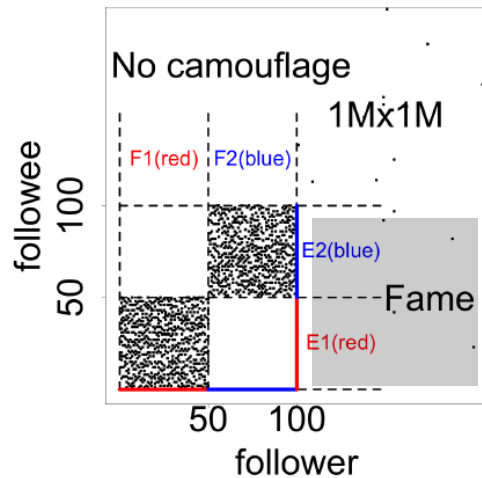


Rule 3 (tilting “rays”): two blocks, with “camouflage”, no “fame”

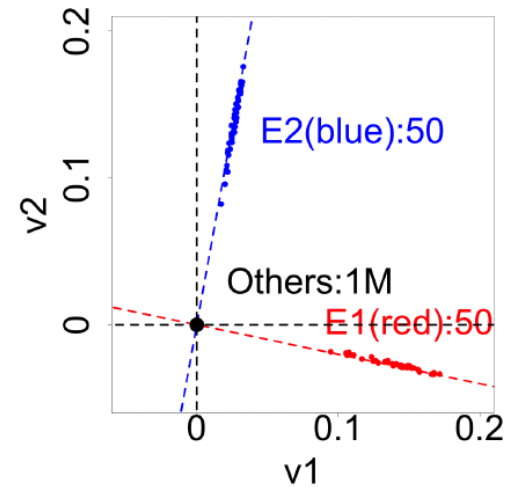
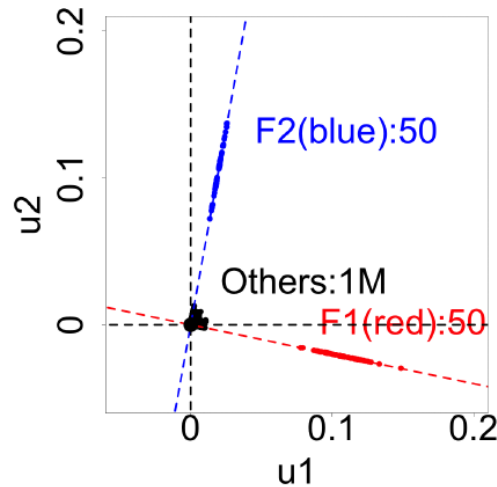
Lockstep and Spectral Subspace Plot

- Case #3: non-overlapping lockstep
- “Camouflage” (or “**Fame**”) $\longleftrightarrow$ Tilting
“Rays”

Adjacency Matrix



Spectral Subspace Plot



Rule 3 (tilting “rays”): two blocks, no “camouflage”, with “fame”

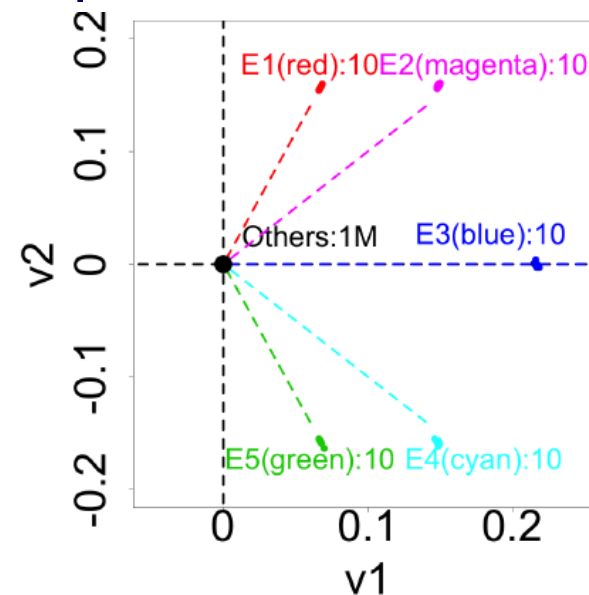
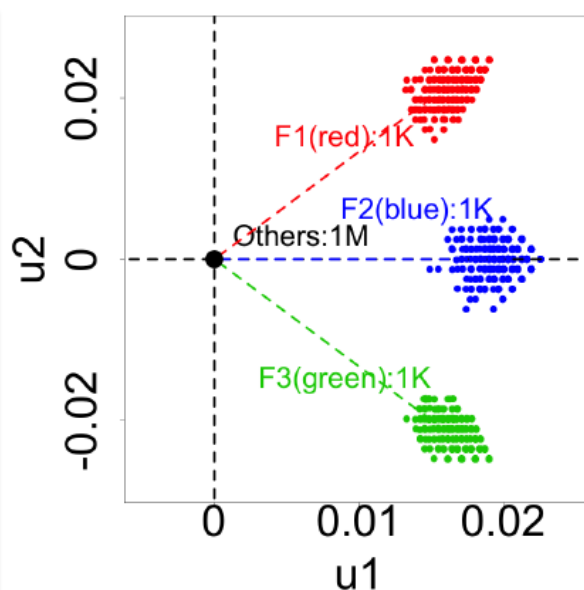
Lockstep and Spectral Subspace Plot

- Case #4: ? lockstep
- “?” $\longleftrightarrow$ “Pearls”

Adjacency Matrix

Spectral Subspace Plot

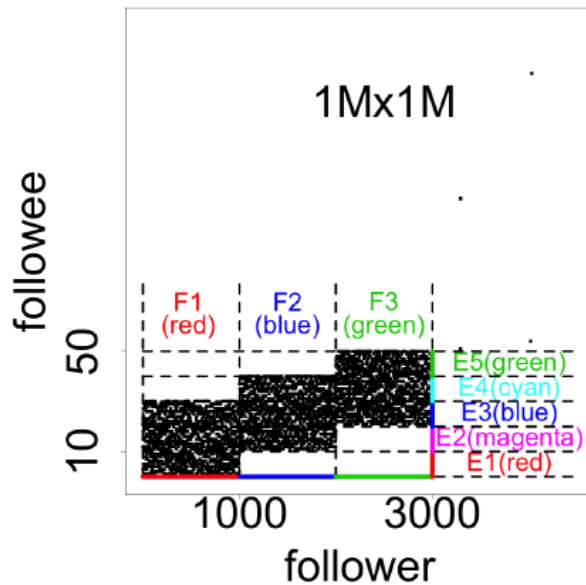
?



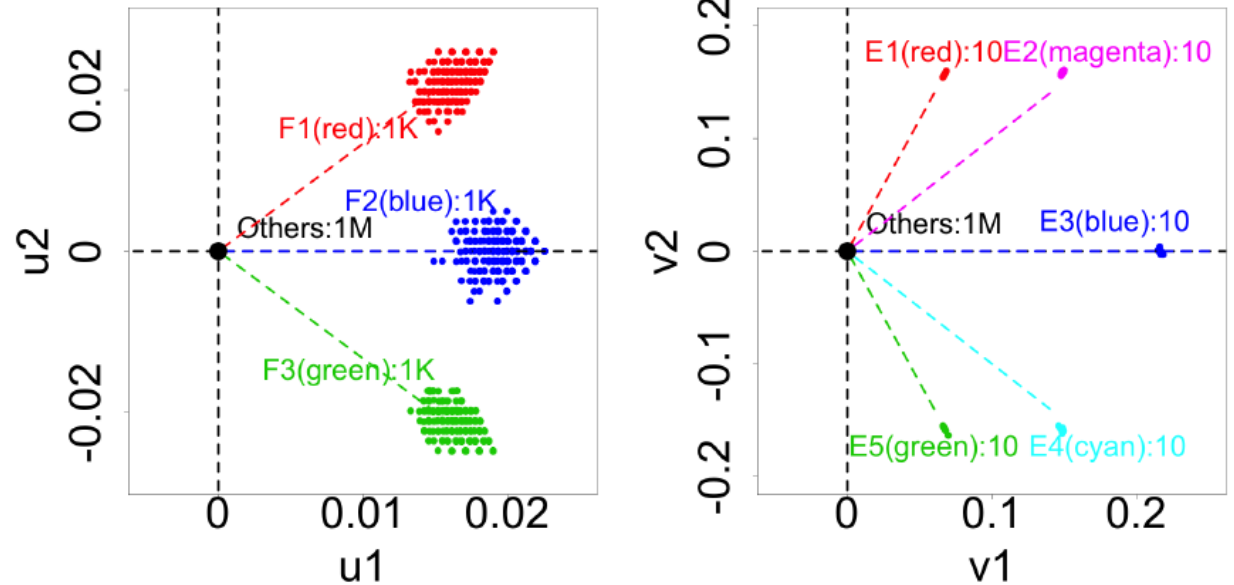
Lockstep and Spectral Subspace Plot

- Case #4: **overlapping** lockstep
- “Staircase” $\longleftrightarrow$ “Pearls”

Adjacency Matrix



Spectral Subspace Plot

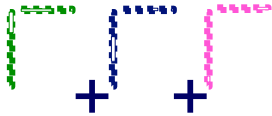


Rule 4 (“pearls”): a “staircase” of three partially overlapping blocks.

Dataset

- Tencent Weibo 
- 117 million nodes (with profile and UGC data)
- 3.33 billion directed edges



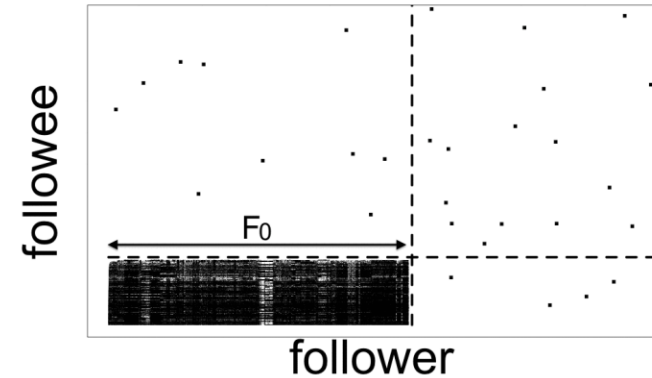
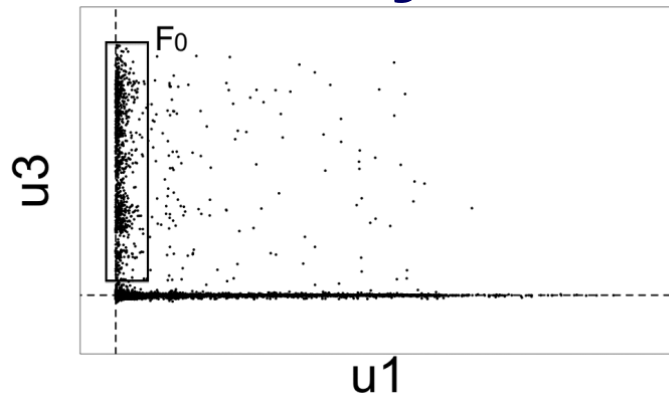


“Rays”

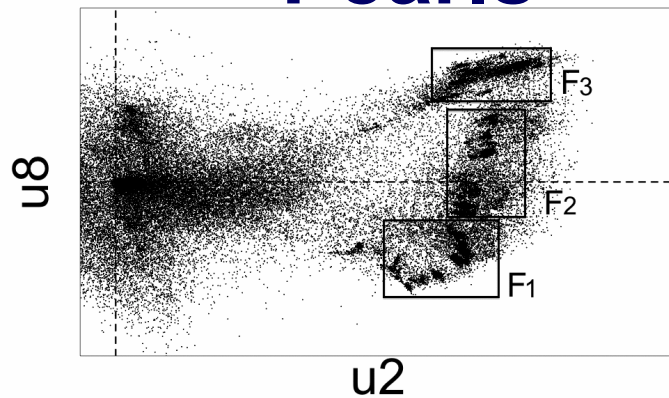
Real Data



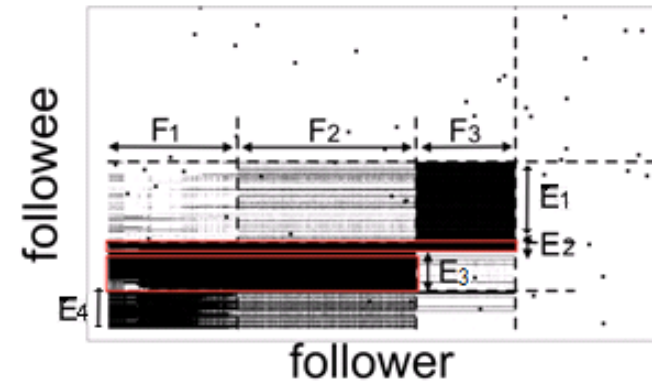
“Block”



“Pearls”



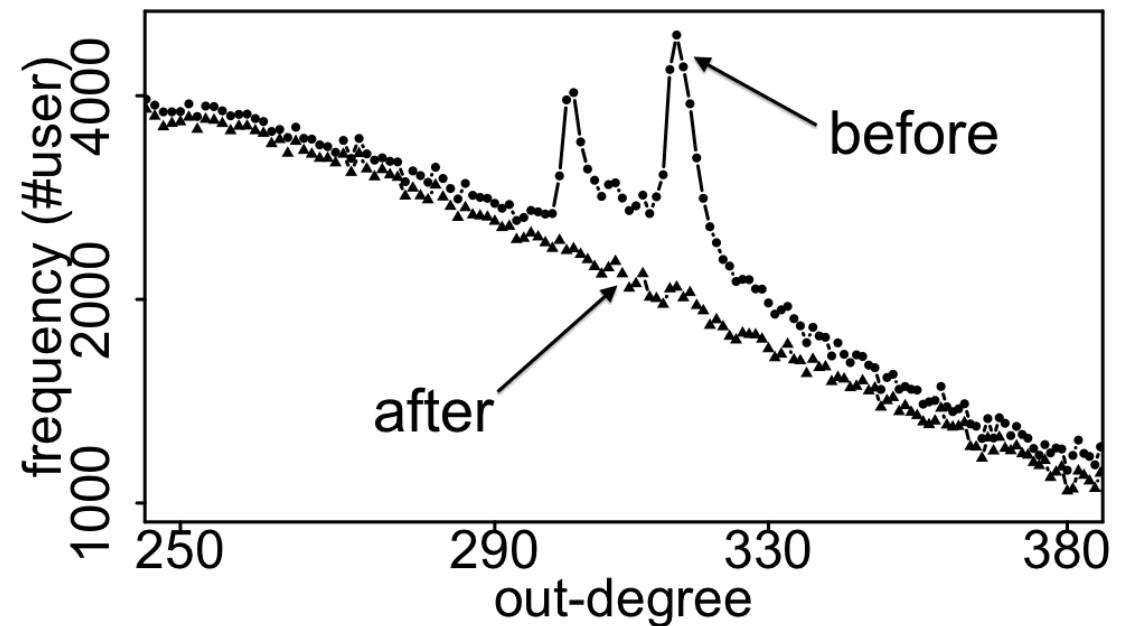
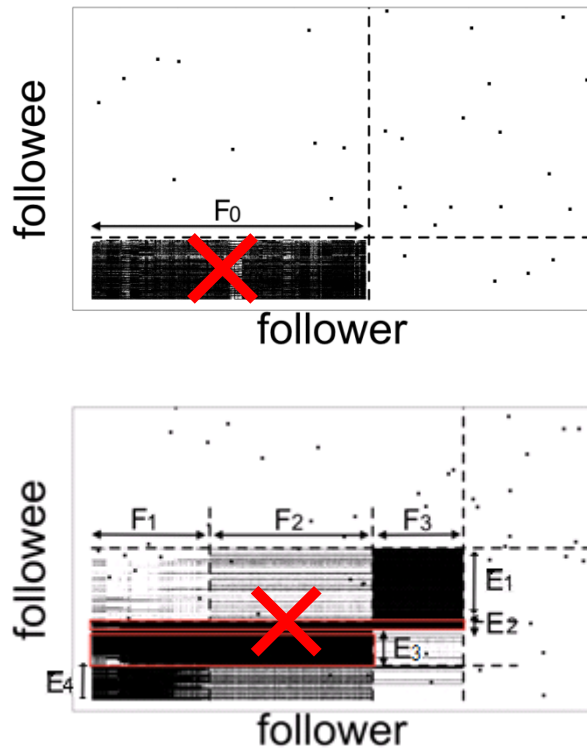
“Staircase”



Real Data

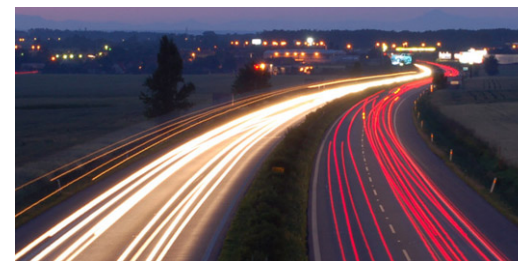


- Spikes on the out-degree distribution

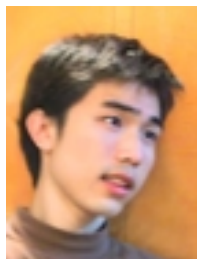


Roadmap

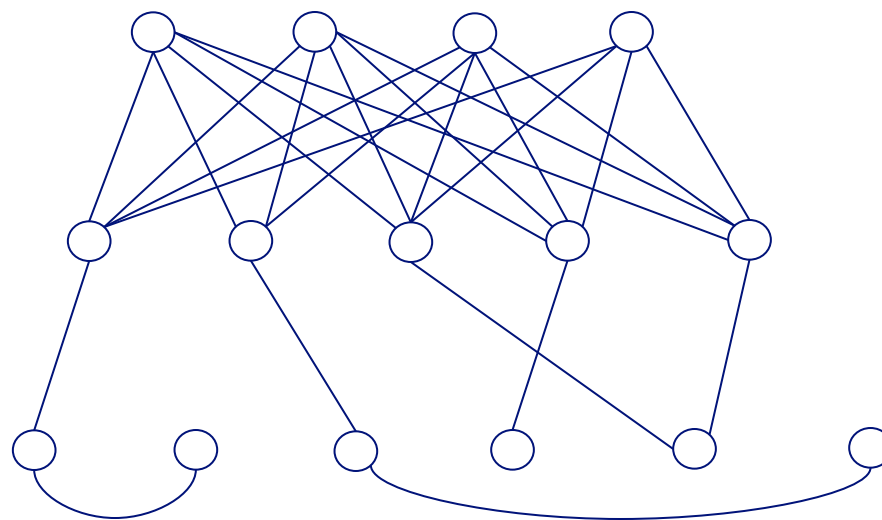
- Introduction – Motivation
- Part#1: Patterns in graphs
 - P1.1: Patterns
 - P1.2: Anomaly / fraud detection
 - No labels – spectral methods
 - With labels: Belief Propagation
- ➔ • Part#2: time-evolving graphs; tensors
- Conclusions



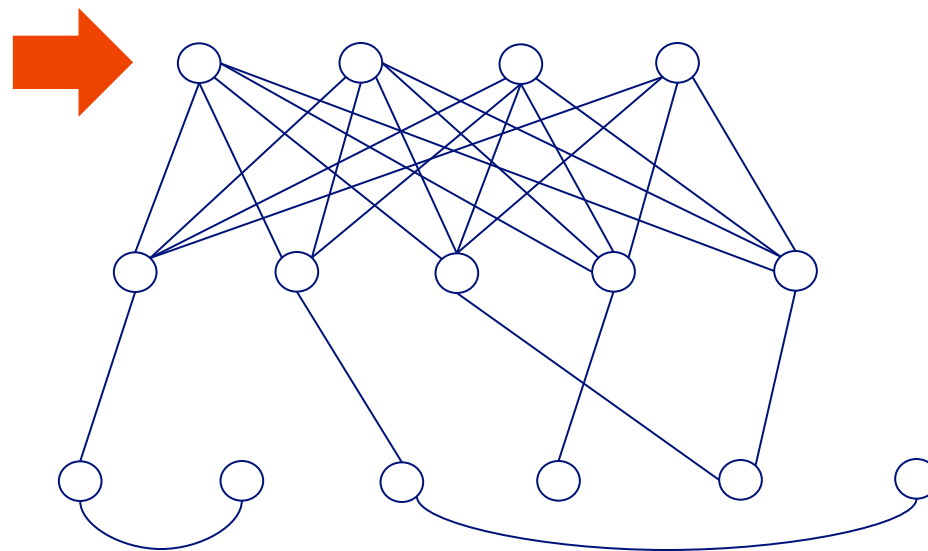
E-bay Fraud detection



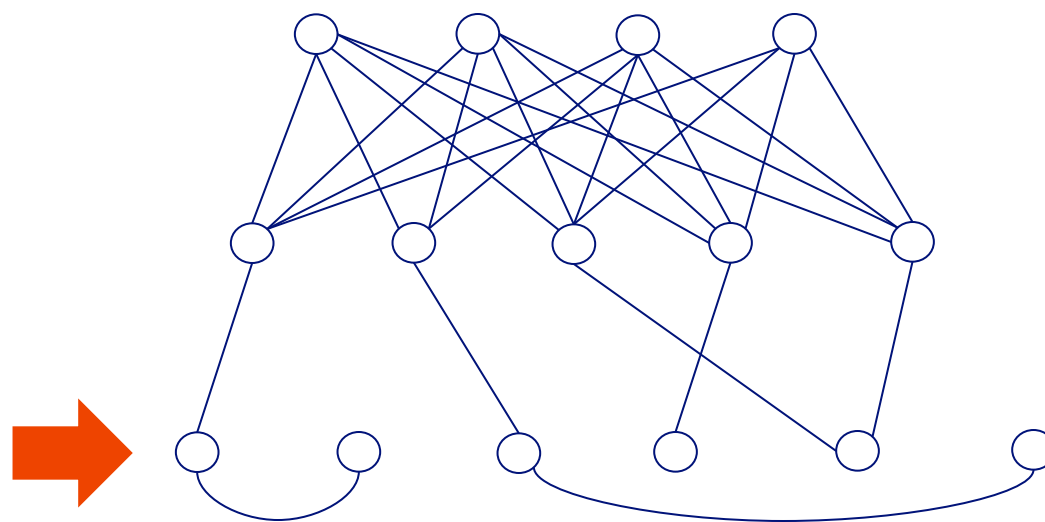
w/ Polo Chau &
Shashank Pandit, CMU
[www'07]



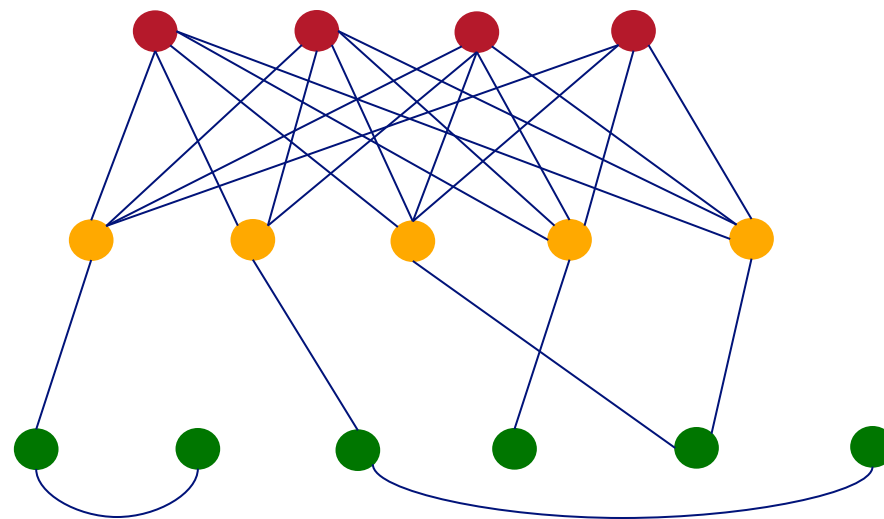
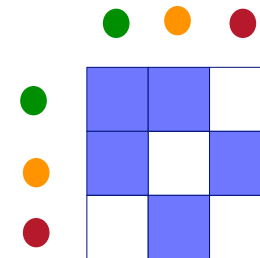
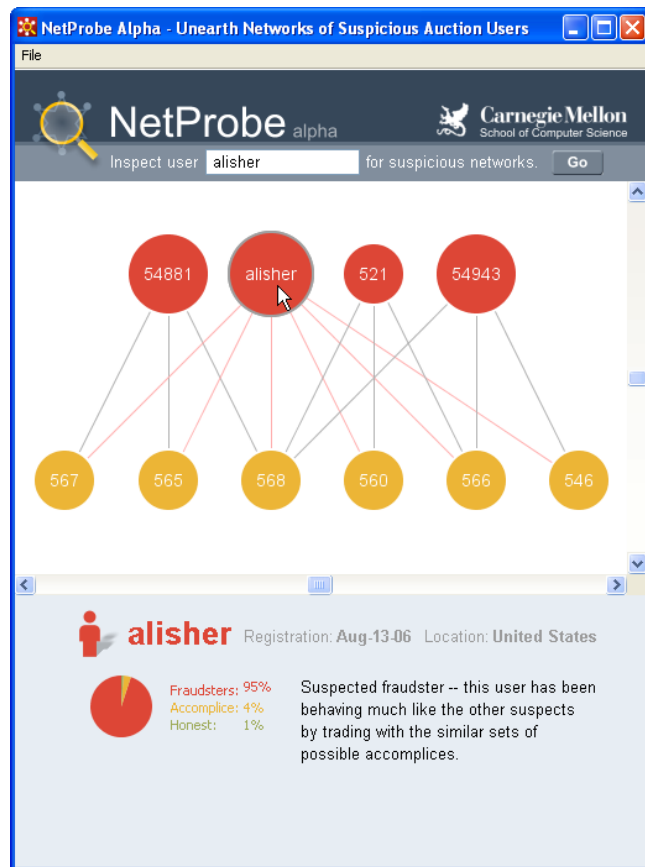
E-bay Fraud detection



E-bay Fraud detection



E-bay Fraud detection - NetProbe



Popular press



The Washington Post

Los Angeles Times

And less desirable attention:

- E-mail from ‘Belgium police’ (‘copy of your code?’)

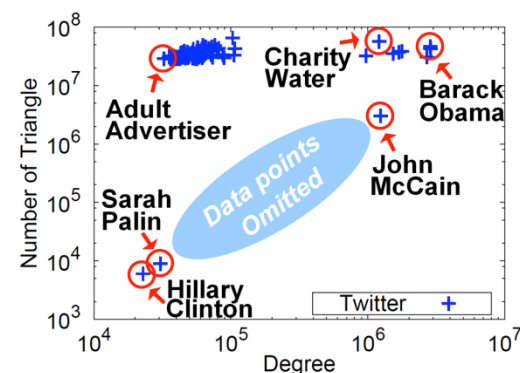
Summary of Part#1

- *many* patterns in real graphs
 - Power-laws everywhere
 - Long (and growing) list of tools for anomaly/fraud detection

Patterns

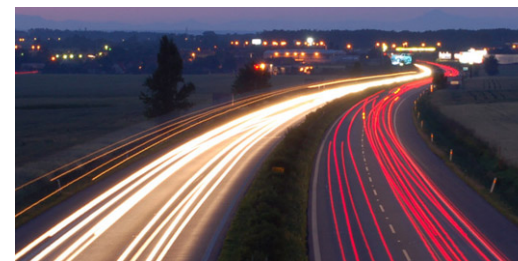


anomalies



Roadmap

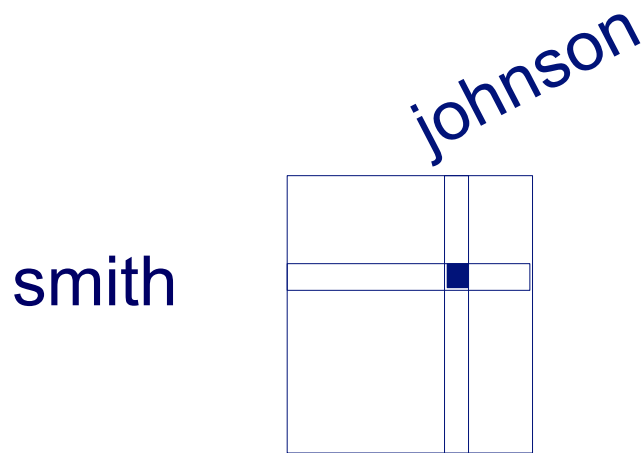
- Introduction – Motivation
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs
 - ➔ – P2.1: tools/tensors
 - P2.2: other patterns
- Conclusions



Part 2: Time evolving graphs; tensors

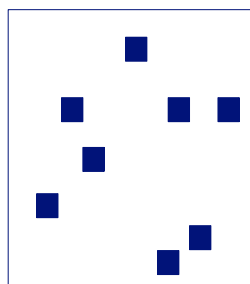
Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



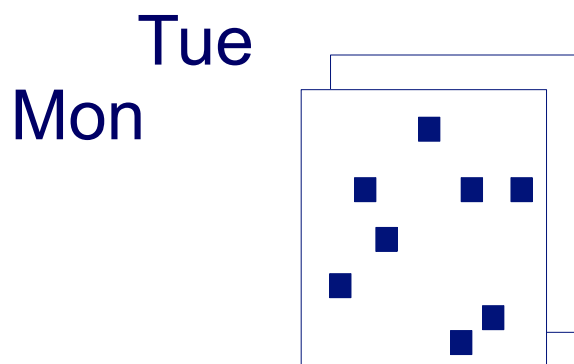
Graphs over time $\rightarrow$ tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



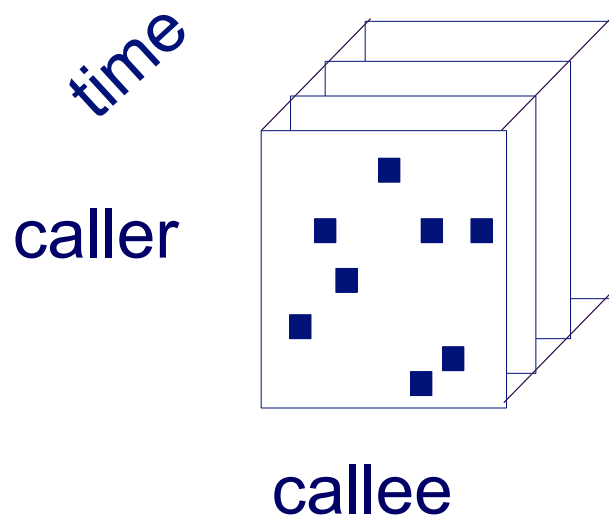
Graphs over time -> tensors!

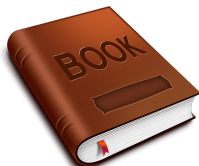
- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies



Graphs over time -> tensors!

- Problem #2.1:
 - Given who calls whom, and when
 - Find patterns / anomalies





Crush intro to SVD

- Recall: (SVD) matrix factorization: finds blocks

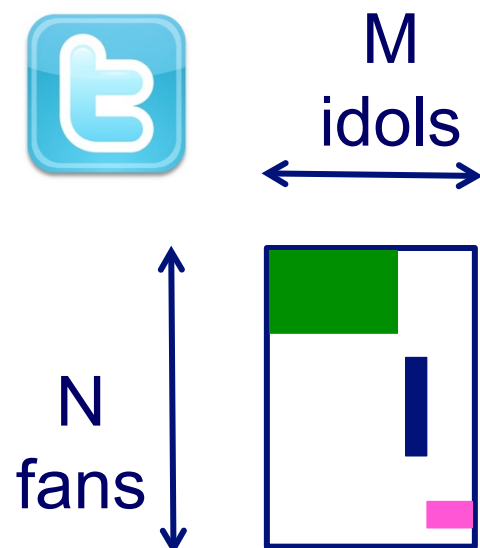


Diagram illustrating the SVD matrix factorization process:

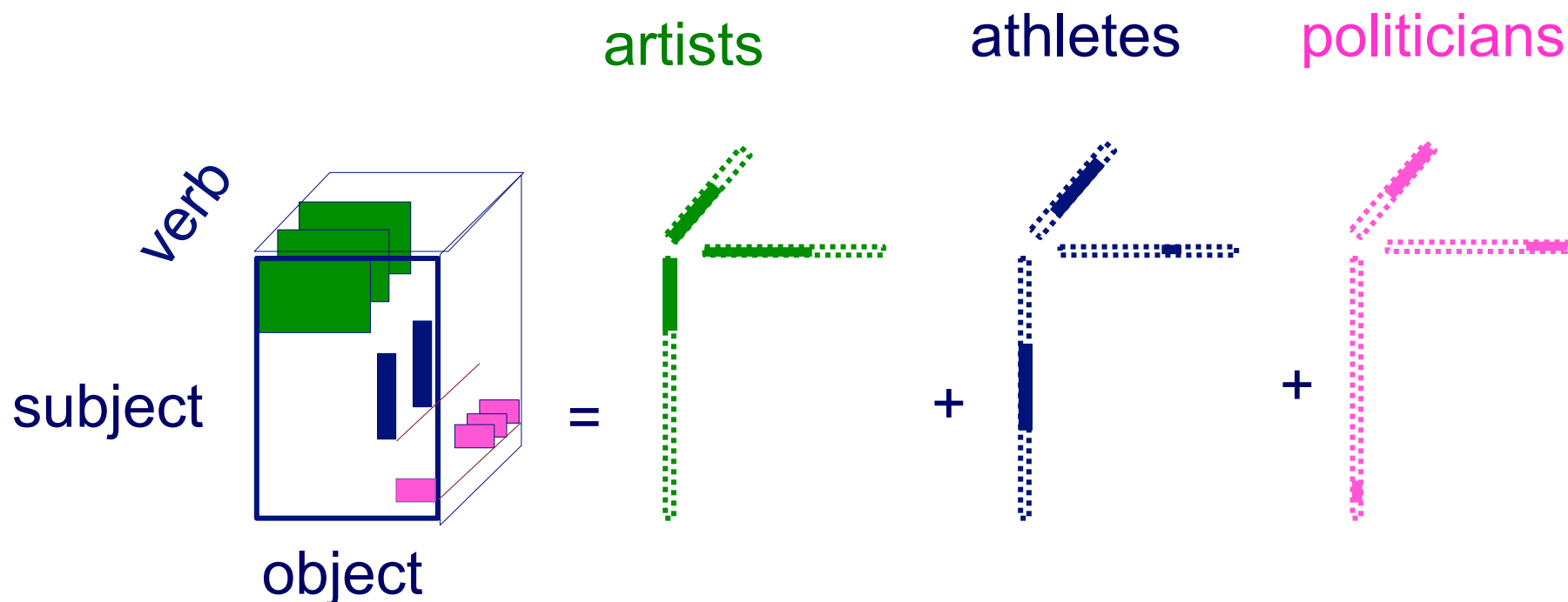
The matrix M is approximated by the sum of three rank-1 matrices:

$$M \approx \vec{u}_1 \vec{v}_1^T + \dots + \vec{u}_i \vec{v}_i^T + \dots + \vec{u}_{93} \vec{v}_{93}^T$$

The vectors $\vec{u}_1$, $\vec{v}_1$, $\vec{u}_i$, and $\vec{v}_{93}$ are shown as vertical and horizontal bars with colored blocks, representing different user preferences (e.g., 'music lovers', 'sports lovers', 'citizens', 'singers', 'athletes', 'politicians').

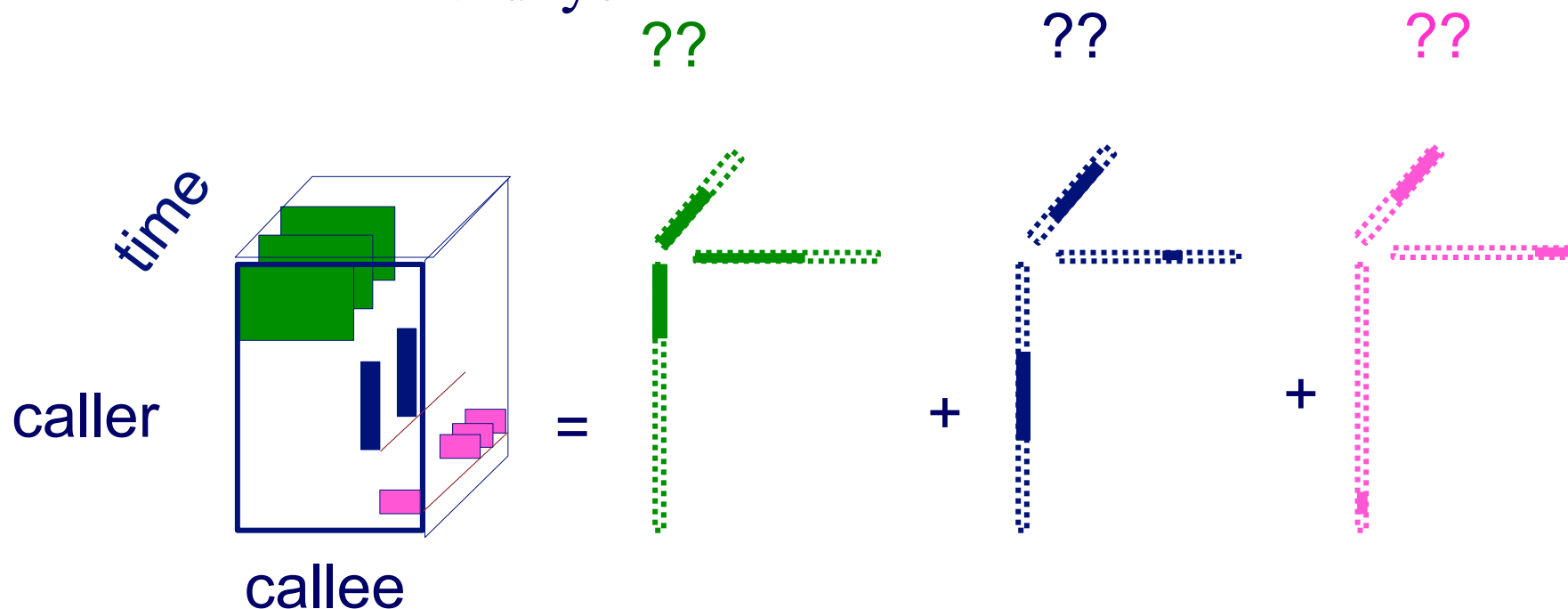
Answer: tensor factorization

- PARAFAC decomposition

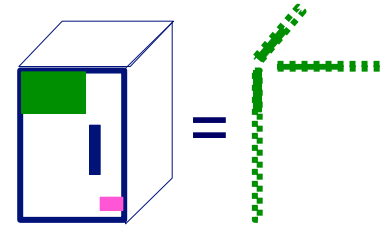


Answer: tensor factorization

- PARAFAC decomposition
- Results for who-calls-whom-when
 - 4M x 15 days

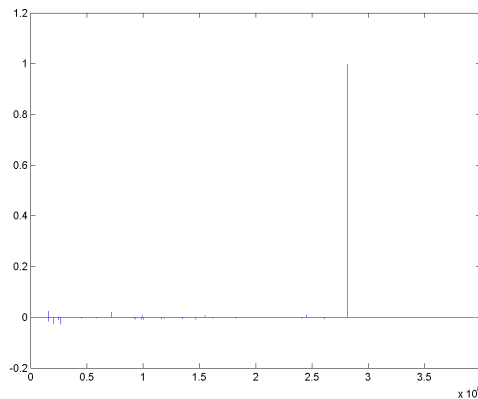


Anomaly detection in time-evolving graphs

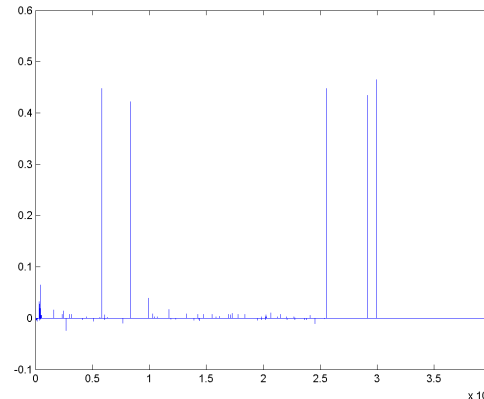


- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks

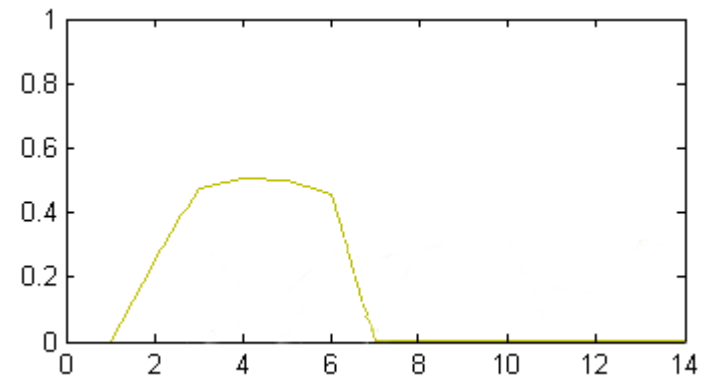
1 caller



5 receivers

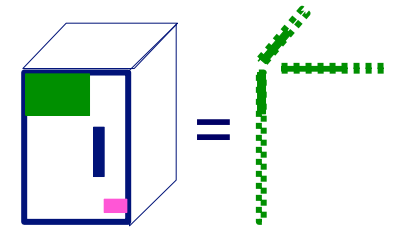


4 days of activity



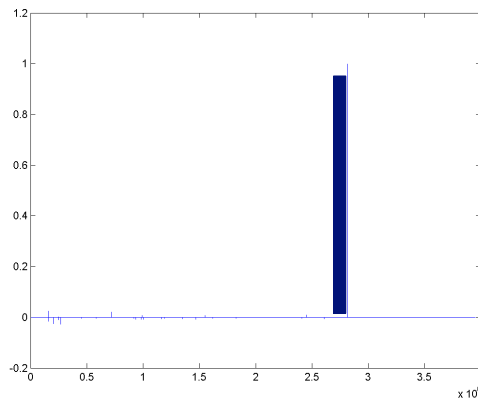
~200 calls to EACH receiver on EACH day!

Anomaly detection in time-evolving graphs

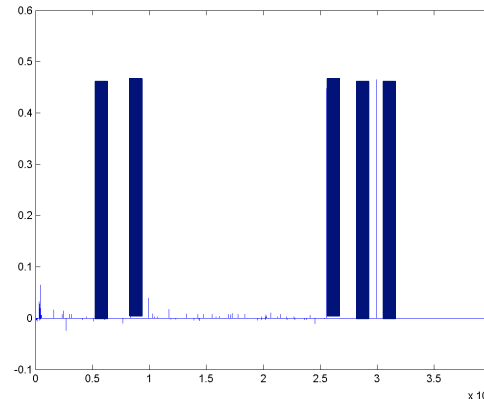


- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks

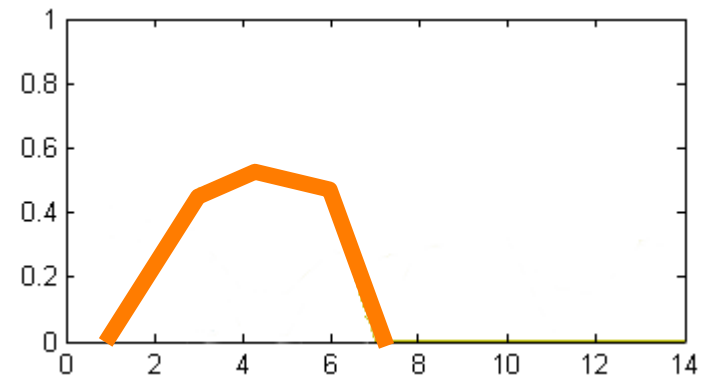
1 caller



5 receivers

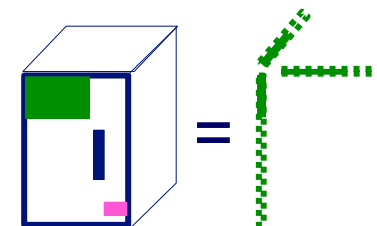


4 days of activity



~200 calls to EACH receiver on EACH day!

Anomaly detection in time-evolving graphs



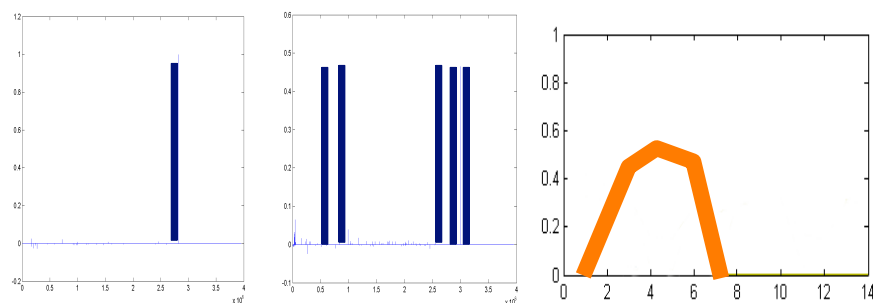
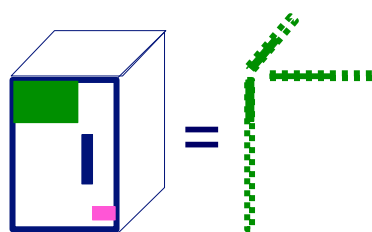
- Anomalous communities in phone call data:
 - European country, 4M clients, data over 2 weeks



Miguel Araujo, Spiros Papadimitriou, Stephan Günnemann,
Christos Faloutsos, Prithwish Basu, Ananthram Swami,
Evangelos Papalexakis, Danai Koutra. *Com2: Fast
Automatic Discovery of Temporal (Comet) Communities.*
PAKDD 2014, Tainan, Taiwan.

Part 2: Conclusions

- Time-evolving / heterogeneous graphs $\rightarrow$ tensors
- PARAFAC finds patterns
- Surprising temporal patterns (P.L. growth)



Roadmap



- Introduction – Motivation
 - Why study (big) graphs?
- Part#1: Patterns in graphs
- Part#2: time-evolving graphs; tensors
- ➔ • Acknowledgements and Conclusions

Thanks



Disclaimer: All opinions are mine; not necessarily reflecting the opinions of the funding agencies

Thanks to: NSF IIS-0705359, IIS-0534205, CTA-INARC; Yahoo (M45), LLNL, IBM, SPRINT, Google, INTEL, HP, iLab

Cast



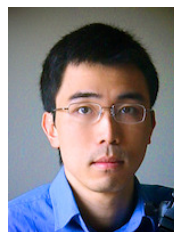
Akoglu,
Leman



Araujo,
Miguel



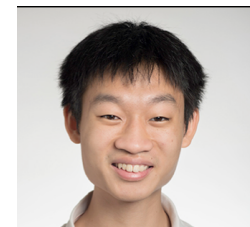
Beutel,
Alex



Chau,
Polo



Eswaran,
Dhivya



Hooi,
Bryan



Kang, U



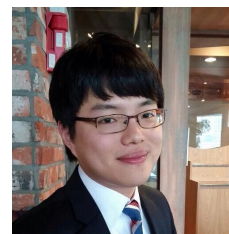
Koutra,
Danai



Papalexakis,
Vagelis



Shah,
Neil



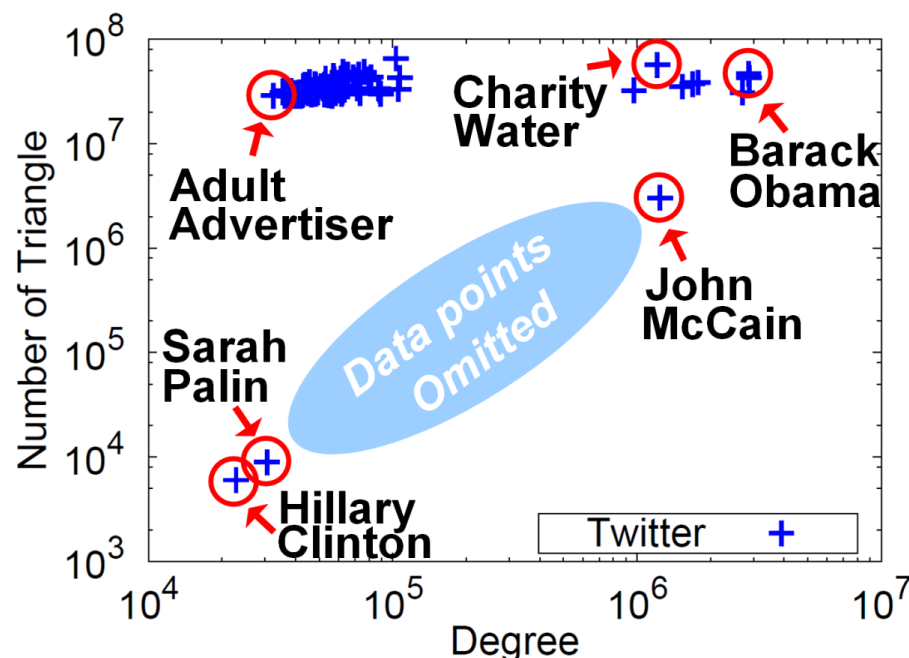
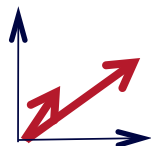
Shin,
Kijung



Song,
Hyun Ah

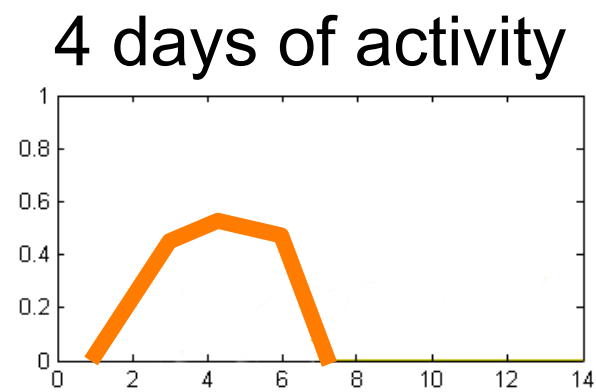
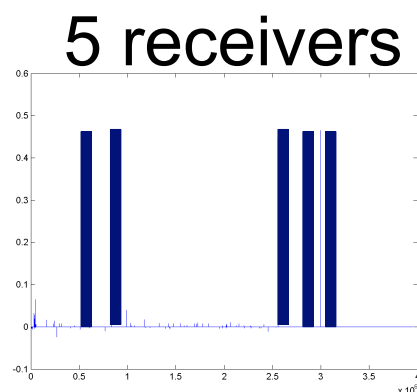
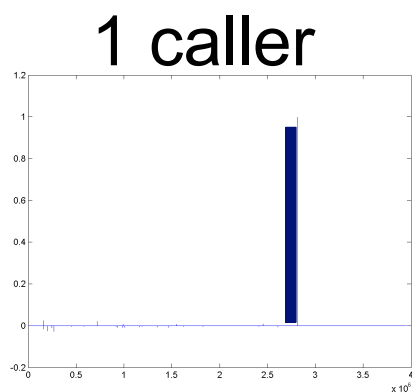
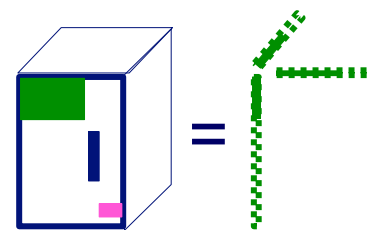
CONCLUSION#1 – Big data

- **Patterns**  **Anomalies**
- **Large datasets reveal patterns/outliers that are invisible otherwise**



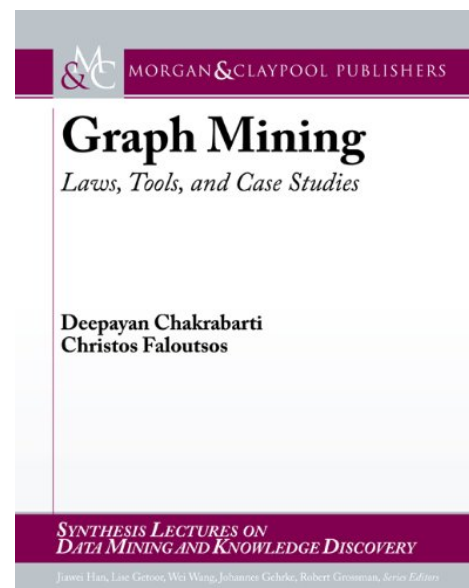
CONCLUSION#2 – tensors

- powerful tool



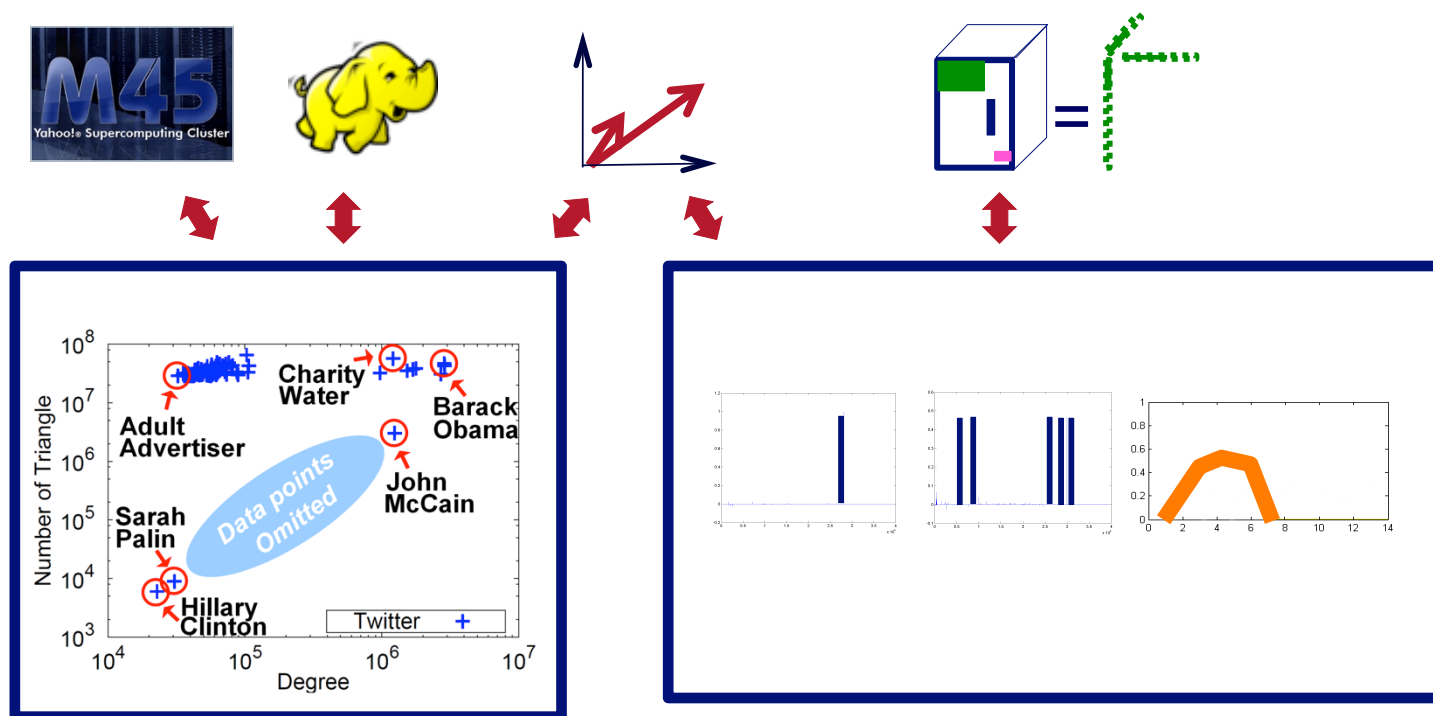
References

- D. Chakrabarti, C. Faloutsos: *Graph Mining – Laws, Tools and Case Studies*, Morgan Claypool 2012
- <http://www.morganclaypool.com/doi/abs/10.2200/S00449ED1V01Y201209DMK006>



TAKE HOME MESSAGE:

Cross-disciplinary



Thank you!

Cross-disciplinary

