

Probability Densities in Data Mining

- Why we should care
- Notation and Fundamentals of continuous PDFs
- Multivariate continuous PDFs
- Combining continuous and discrete random variables

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Probability Densities: Slide 2

Probability Densities: Slide

Why we should care

- Real Numbers occur in at least 50% of database records
- Can't always quantize them
- So need to understand how to describe where they come from
- A great way of saying what's a reasonable range of values
- A great way of saying how multiple attributes should reasonably co-occur

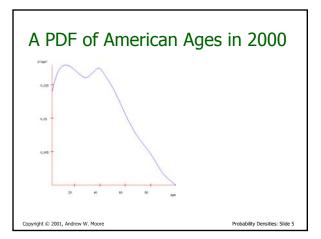
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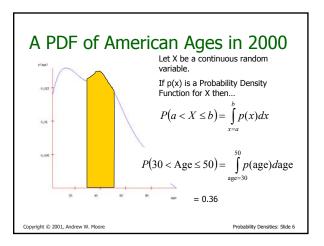
Probability Densities: Slide 3

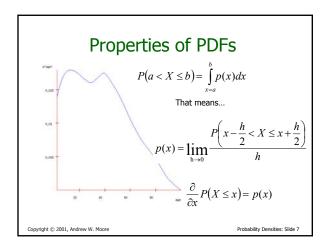


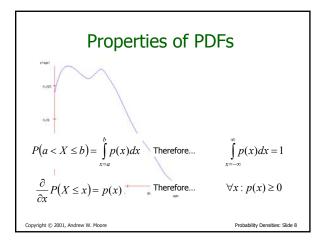
- Can immediately get us Bayes Classifiers that are sensible with real-valued data
- You'll need to intimately understand PDFs in order to do kernel methods, clustering with Mixture Models, analysis of variance, time series and many other things
- Will introduce us to linear and non-linear regression

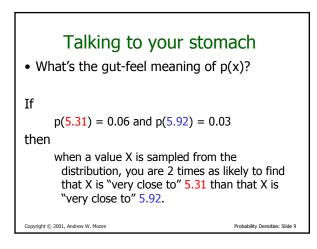
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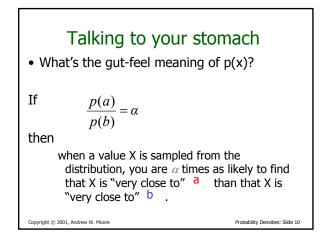


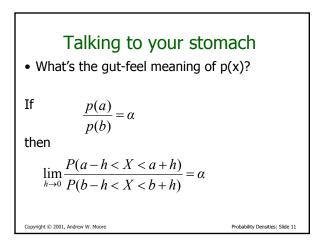


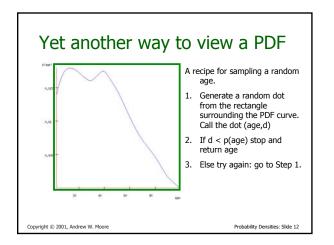


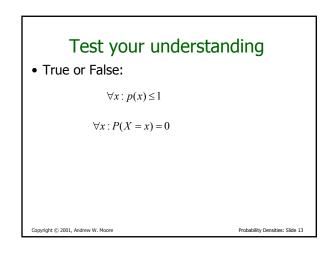


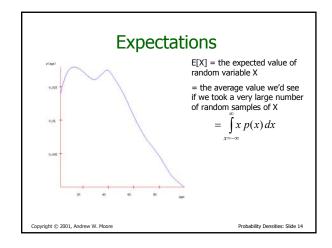


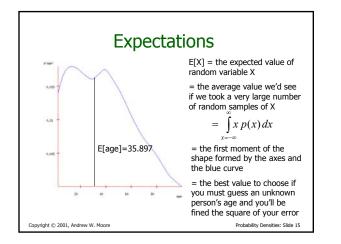


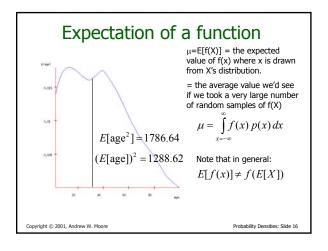


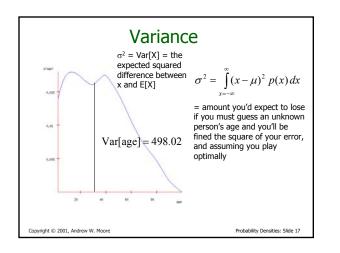


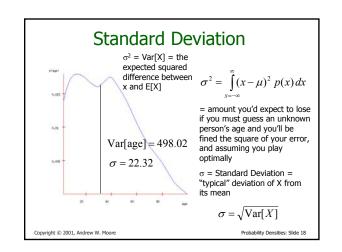


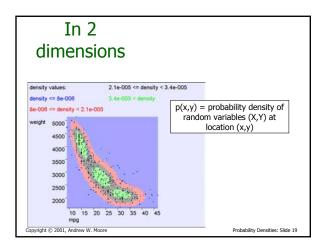


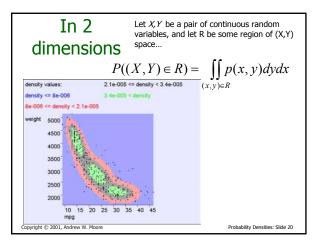


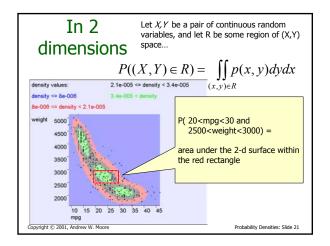


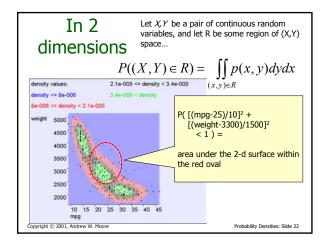




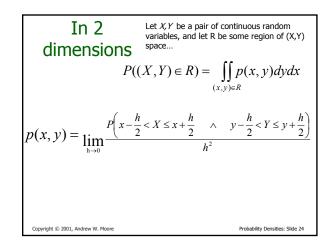


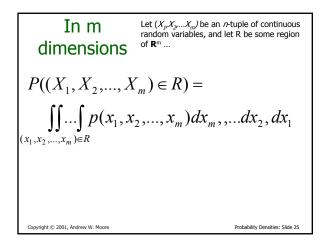


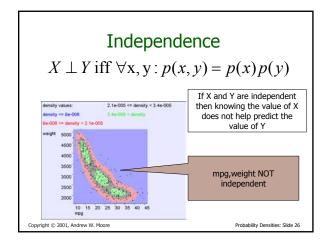


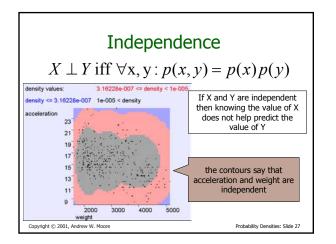


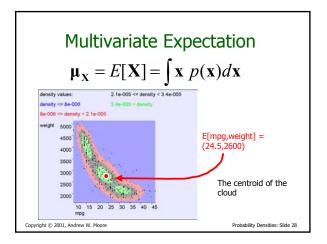
Let X, Y be a pair of continuous random variables, and let R be some region of (X,Y) space... $P((X,Y) \in R) = \iint_{(x,y) \in R} p(x,y) dy dx$ Take the special case of region R = "everywhere". Remember that with probability 1, (X,Y) will be drawn from "somewhere". So. $\int_{x=-\infty}^{\infty} \int_{y=-\infty}^{\infty} p(x,y) dy dx = 1$

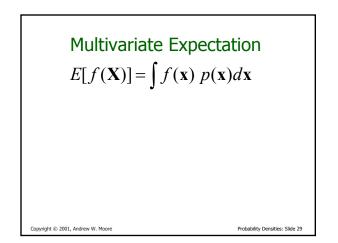


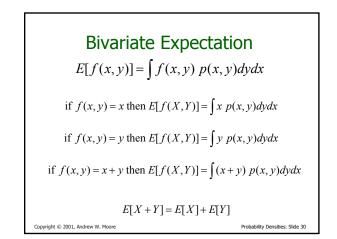


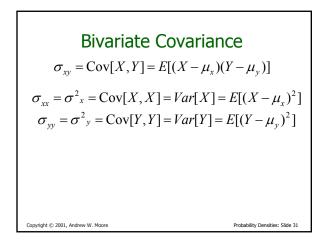


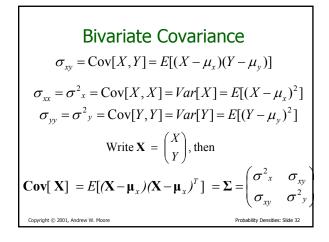


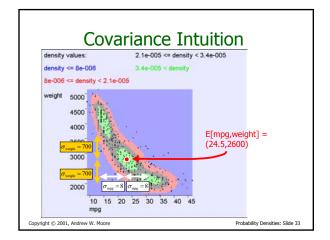


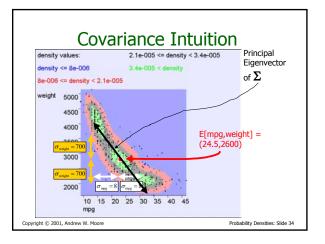


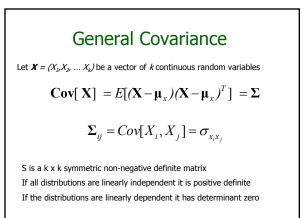






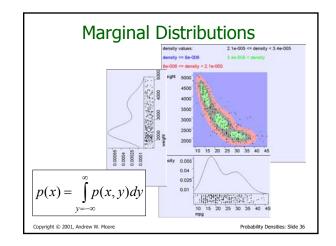


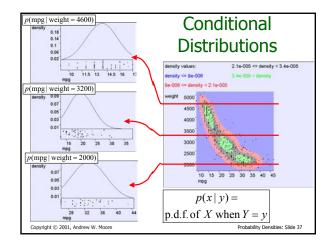


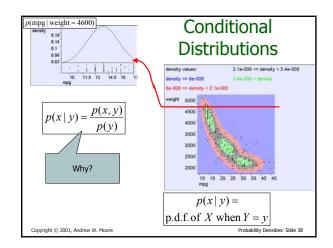


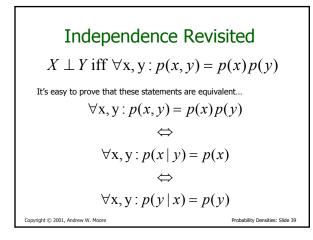


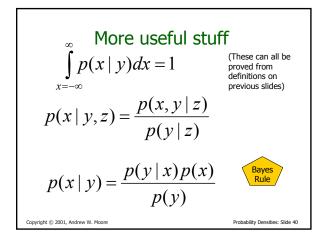
Probability Densities: Slide 35











What you should know You should be able to play with discrete, continuous and mixed joint distributions • You should be happy with the difference between p(x) and P(A)• You should be intimate with expectations of continuous and discrete random variables You should smile when you meet a covariance matrix Independence and its consequences should be second nature

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Probability Densities: Slide 41