

Neural Networks

1. Introduction Spring 2018

Neural Networks are taking over!

 Neural networks have become one of the major thrust areas recently in various pattern recognition, prediction, and analysis problems

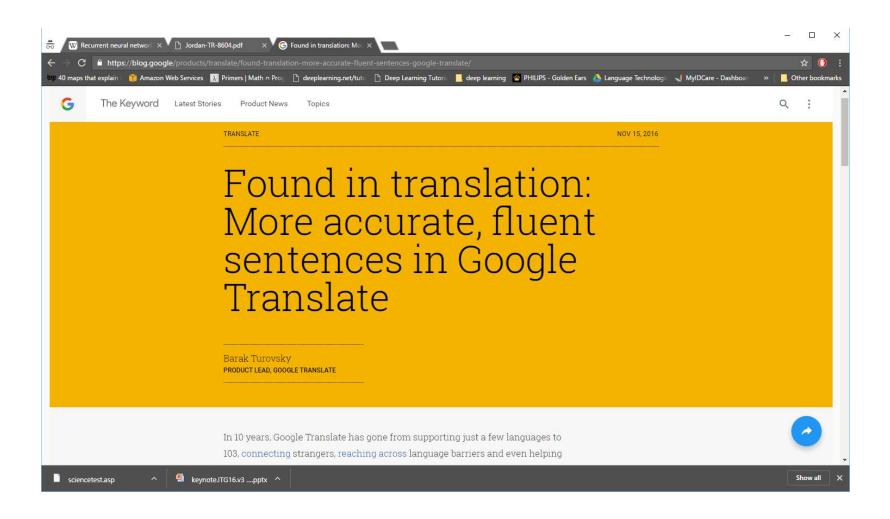
- In many problems they have established the state of the art
 - Often exceeding previous benchmarks by large margins

Recent success with neural networks

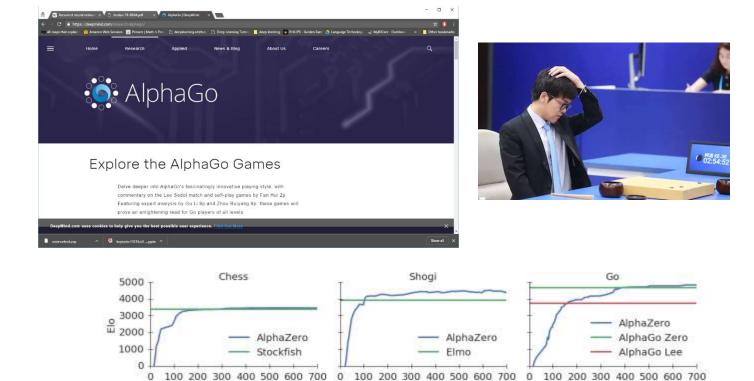


A bit of hyperbole, but still...

Recent success with neural networks



Recent success with neural networks



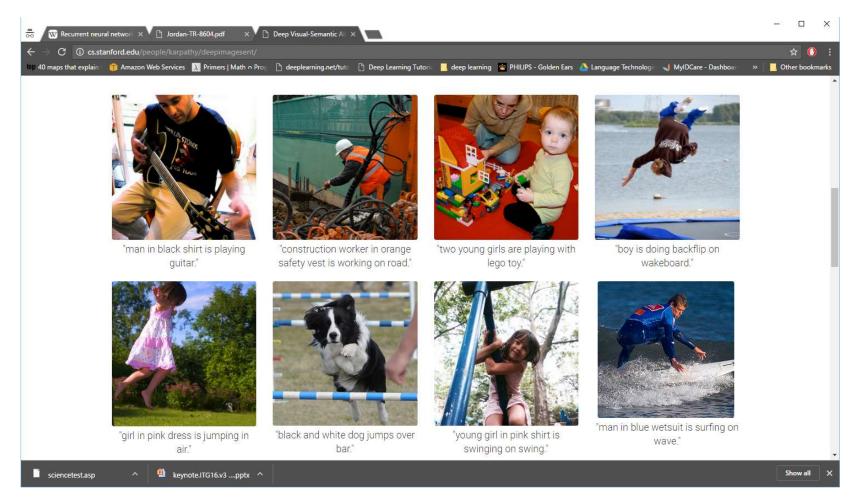
Thousands of Steps

Figure 1: Training AlphaZero for 700,000 steps. Elo ratings were computed from evaluation games between different players when given one second per move. a Performance of AlphaZero in chess, compared to 2016 TCEC world-champion program Stockfish. b Performance of AlphaZero in shogi, compared to 2017 CSA world-champion program Elmo. c Performance of AlphaZero in Go, compared to AlphaGo Lee and AlphaGo Zero (20 block / 3 day) (29).

Thousands of Steps

Thousands of Steps

Success with neural networks



Captions generated entirely by a neural network

Successes with neural networks

- And a variety of other problems:
 - Image recognition
 - Language understanding
 - Signal enhancement
 - Even generating art and predicting stock markets!

Neural nets can do anything!



Neural nets and the employment market



This guy didn't know about neural networks (a.k.a deep learning)



This guy learned about neural networks (a.k.a deep learning)

Objectives of this course

- Understanding neural networks
- Comprehending the models that do the previously mentioned tasks
 - And maybe build them
- Familiarity with some of the terminology
 - What are these:
 - http://www.datasciencecentral.com/profiles/blogs/concise-visualsummary-of-deep-learning-architectures
- Fearlessly design, build and train networks for various tasks
- You will not become an expert in one course

Course learning objectives: Broad level

Concepts

- Some historical perspective
- Forms of neural networks and underlying ideas
- Learning in neural networks
 - Training, concepts, practical issues
- Architectures and applications
- Will try to maintain balance between squiggles and concepts (concept >> squiggle)
- Practical
 - Familiarity with training
 - Implement various neural network architectures
 - Implement state-of-art solutions for some problems
- Overall: Set you up for further research/work in your research area

Course learning objectives: Topics

- Basic network formalisms:
 - MLPs
 - Convolutional networks
 - Recurrent networks
 - Boltzmann machines
- Some advanced formalisms
 - Generative models: VAEs
 - Adversarial models: GANs
- Topics we will touch upon:
 - Computer vision: recognizing images
 - Text processing: modelling and generating language
 - Machine translation: Sequence to sequence modelling
 - Modelling distributions and generating data
 - Reinforcement learning and games
 - Speech recognition

Reading

- List of books on course webpage
- Additional reading material also on course pages

Instructors and TAs

- Instructor: Me
 - bhiksha@cs.cmu.edu
 - x8-9826
- TAs:
 - Aggrey Muhebwa (amuhebwa Kigali)
 - Benjamin Striner (bstriner)
 - Jerry Ding (dalud)
 - Mounira Tlili (mst -- Doha)
 - Rajat Kulshreshtha (rkulshre)
 - Ryan Brigden (rbridgen)
 - Thoman Manzini (tmanzini)
- Office hours: On webpage
- http://deeplearning.cs.cmu.edu/



Logistics:Lectures...

- Have in-class and online sections
 - Including online sections in Kigali and Doha
- Lectures are being streamed
- Recordings will also be put up and links posted

- Important that you view the lectures
 - If nothing, the quizzes depend on it

Lecture Schedule

On website

- The schedule for the latter half of the semester may vary a bit
 - Guest lecturer schedules are fuzzy...

Guest lectures:

- 7 Feb: Scott Fahlman

- 19 Mar: Rich Stern

9 Apr: Graham Neubig

- 29 April: Byron Yu

- TBD: TBD

Recitations

- We will have 13 recitations
- Will cover implementation details and basic exercises
 - Very important if you wish to get the maximum out of the course
- Topic list on the course schedule
- First recitation is this Friday (19th Jan) and covers the details of AWS
- Strongly recommend attending all recitations
 - Even if you think you know everything

Recitations Schedule

- 19 Jan: AWS
- 26 Jan: Implementing a neural network: algebra, toolkits and basic setups
- 2 Feb: Making the network learn: Initialization, Optimization, Regularization, Tuning, etc.
- 9 Feb: All about convnets
- 16 Feb: All about recurrent networks
- 23 Feb: More on recurrence, sequence-to-sequence modelling, etc.
- 30 Feb: Visualizing what is learned
- 37 Feb: ...
- 44 Feb: ...
- 51 Feb: ...
- ...

Grading

- Weekly multiple-choice Quizzes (25%)
- 5 homeworks (50%)
 - Basic MLPs
 - CNNs
 - RNNs
 - Sequence to sequence modelling: Speech recognition
 - GANs
- One project (25%)

Weekly Quizzes

- Weekly quizzes
 - 10 multiple-choice questions
 - Relate to topics covered that week
 - Released Friday, closed Saturday night
- There will be 13 total quizzes
 - We will consider the best 10
 - This is expected to account for any circumstancebased inability to work on quizzes
 - You could skip up to 3

Lectures and Quizzes

 Slides often contain a lot more information than is presented in class

 Quizzes will contain questions from topics that are on the slides, but not presented in class

Homeworks

- Homeworks come in two flavors
 - Autograded homeworks with deterministic solutions
 - You must upload them to autolab
 - Kaggle problems
 - You compete with your classmates on a leaderboard
 - We provide a baseline solution anyone who matches it automatically gets at least a B
- Homeworks: Late policy
 - But everyone gets up to 5 total grace days for the autolab HWs
 - You can distribute them as you want across your HWs
 - Once you use up your grace days, you lose 25% of your points for 1 day of delay, 50% for two, and get no points if you're 3 days or more late
 - Kaggle: Kaggle leaderboards shut on the deadline
 - May include a slack of up to 1 day if there are issues

Additional Logistics

- Discussions:
 - On Piazza

- Compute infrastructure:
 - Everyone gets Amazon tokens
 - Initially a token for \$50
 - Can get additional tokens of \$50 up to a total of \$150

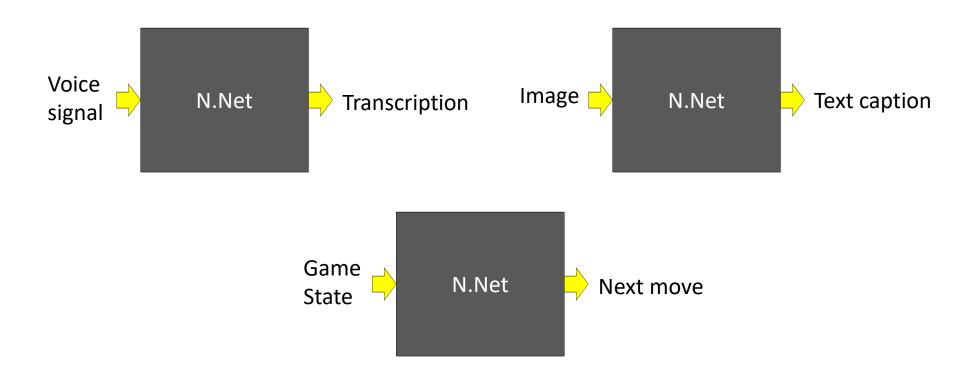
Perception: From Rosenblatt, 1962...

- "Perception, then, emerges as that relatively primitive, partly autonomous, institutionalized, ratiomorphic subsystem of cognition which achieves prompt and richly detailed orientation habitually concerning the vitally relevant, mostly distal aspects of the environment on the basis of mutually vicarious, relatively restricted and stereotyped, insufficient evidence in uncertainty-geared interaction and compromise, seemingly following the highest probability for smallness of error at the expense of the highest frequency of precision."
 - From "Perception and the Representative Design of Psychological Experiments," by Egon Brunswik, 1956 (posthumous).
- "That's a simplification. Perception is standing on the sidewalk, watching all the girls go by."
 - From "The New Yorker", December 19, 1959

Onward..



So what are neural networks??



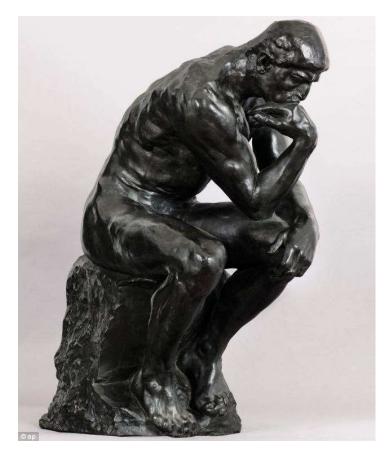
What are these boxes?

So what are neural networks??



• It begins with this...

So what are neural networks??



"The Thinker!" by Augustin Rodin

• Or even earlier.. with this...

The magical capacity of humans

- Humans can
 - Learn
 - Solve problems
 - Recognize patterns
 - Create
 - Cogitate
 - **–** ...



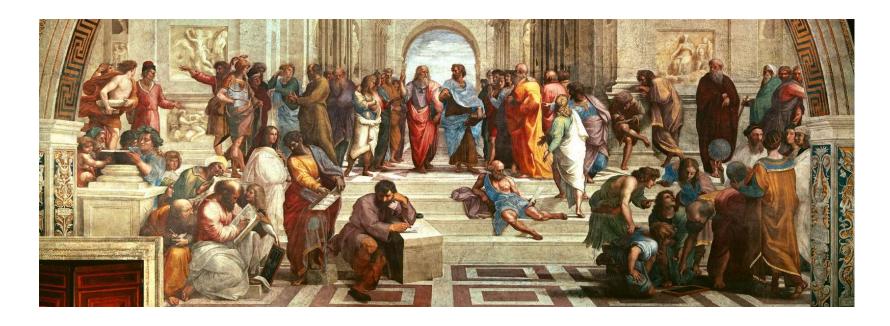
Dante!

- Worthy of emulation
- But how do humans "work"?

Cognition and the brain...

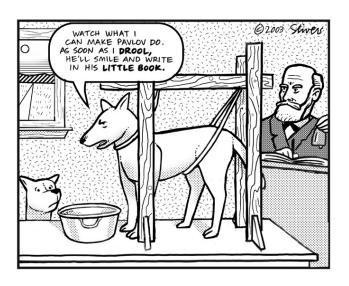
- "If the brain was simple enough to be understood - we would be too simple to understand it!"
 - Marvin Minsky

Early Models of Human Cognition



- Associationism
 - Humans learn through association
- 400BC-1900AD: Plato, David Hume, Ivan Pavlov...

What are "Associations"



- Lightning is generally followed by thunder
 - Ergo "hey here's a bolt of lightning, we're going to hear thunder"
 - Ergo "We just heard thunder; did someone get hit by lightning"?
- Association!

A little history: Associationism

- Collection of ideas stating a basic philosophy:
 - "Pairs of thoughts become associated based on the organism's past experience"
 - Learning is a mental process that forms associations between temporally related phenomena
- 360 BC: Aristotle
 - "Hence, too, it is that we hunt through the mental train, excogitating from the present or some other, and from similar or contrary or coadjacent. Through this process reminiscence takes place. For the movements are, in these cases, sometimes at the same time, sometimes parts of the same whole, so that the subsequent movement is already more than half accomplished."
 - In English: we memorize and rationalize through association



Aristotle and Associationism



- Aristotle's four laws of association:
 - The law of contiguity. Things or events that occur close together in space or time get linked together
 - The law of frequency. The more often two things or events are linked, the more powerful that association.
 - The law of similarity. If two things are similar, the thought of one will trigger the thought of the other
 - The law of contrast. Seeing or recalling something may trigger the recollection of something opposite.

A little history : **Associationism**

- More recent associationists (upto 1800s): John Locke, David Hume, David Hartley, James Mill, John Stuart Mill, Alexander Bain, Ivan Pavlov
 - Associationist theory of mental processes: there is only one mental process: the ability to associate ideas
 - Associationist theory of learning: cause and effect, contiguity, resemblance
 - Behaviorism (early 20th century): Behavior is learned from repeated associations of actions with feedback
 - Etc.

• But where are the associations stored??

• And how?

But how do we *store* them? Dawn of Connectionism

David Hartley's Observations on man (1749)

- We receive input through vibrations and those are transferred to the brain
- Memories could also be small vibrations (called vibratiuncles) in the same regions
- Our brain represents compound or connected ideas by connecting our memories with our current senses
- Current science did not know about neurons

Observation: The Brain



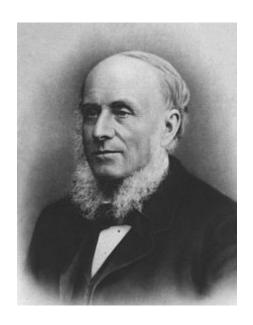
• Mid 1800s: The brain is a mass of interconnected neurons

Brain: Interconnected Neurons



- Many neurons connect in to each neuron
- Each neuron connects out to many neurons

Enter **Connectionism**



- Alexander Bain, philosopher, mathematician, logician, linguist, professor
- 1873: The information is in the *connections*
 - The mind and body (1873)

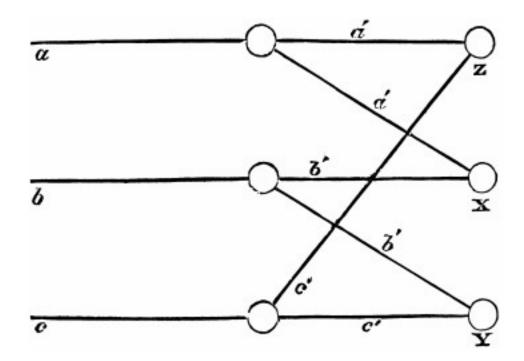
Enter: Connectionism

Alexander Bain (The senses and the intellect (1855), The emotions and the will (1859), The mind and body (1873))

- In complicated words:
 - Idea 1: The "nerve currents" from a memory of an event are the same but reduce from the "original shock"
 - Idea 2: "for every act of memory, ... there is a specific grouping, or co-ordination of sensations ... by virtue of specific growths in cell junctions"

Bain's Idea 1: Neural Groupings

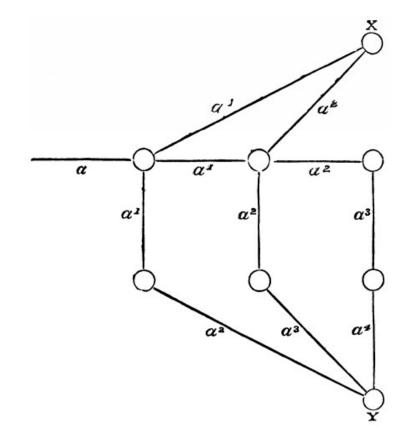
- Neurons excite and stimulate each other
- Different combinations of inputs can result in different outputs



Bain's Idea 1: Neural Groupings

 Different intensities of activation of A lead to the differences in when X and Y are activated

Even proposed a learning mechanism..



Bain's Idea 2: Making Memories

 "when two impressions concur, or closely succeed one another, the nerve currents find some bridge or place of continuity, better or worse, according to the abundance of nerve matter available for the transition."

 Predicts "Hebbian" learning (three quarters of a century before Hebb!)

Bain's Doubts

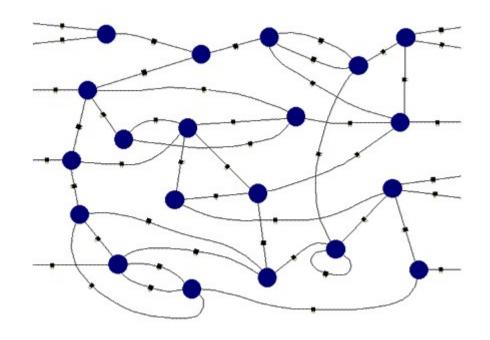
- "The fundamental cause of the trouble is that in the modern world the stupid are cocksure while the intelligent are full of doubt."
 - Bertrand Russell
- In 1873, Bain postulated that there must be one million neurons and 5 billion connections relating to 200,000 "acquisitions"
- In 1883, Bain was concerned that he hadn't taken into account the number of "partially formed associations" and the number of neurons responsible for recall/learning
- By the end of his life (1903), recanted all his ideas!
 - Too complex; the brain would need too many neurons and connections



Connectionism lives on..

- The human brain is a connectionist machine
 - Bain, A. (1873). Mind and body. The theories of their relation. London: Henry King.
 - Ferrier, D. (1876). The Functions of the Brain. London:
 Smith, Elder and Co
- Neurons connect to other neurons.
 The processing/capacity of the brain is a function of these connections
- Connectionist machines emulate this structure

Connectionist Machines

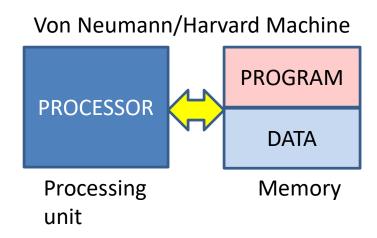


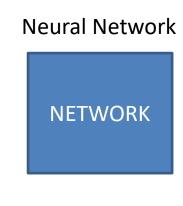
- Network of processing elements
- All world knowledge is stored in the connections between the elements



Connectionist Machines

- Neural networks are connectionist machines
 - As opposed to Von Neumann Machines



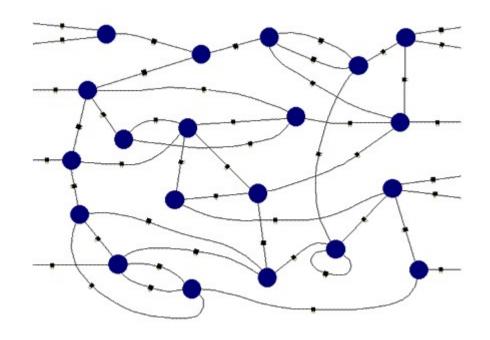


- The machine has many non-linear processing units
 - The program is the connections between these units
 - Connections may also define memory

Recap

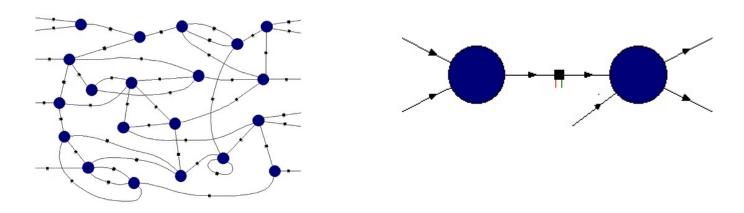
- Neural network based AI has taken over most AI tasks
- Neural networks originally began as computational models of the brain
 - Or more generally, models of cognition
- The earliest model of cognition was associationism
- The more recent model of the brain is connectionist
 - Neurons connect to neurons
 - The workings of the brain are encoded in these connections
- Current neural network models are connectionist machines

Connectionist Machines



- Network of processing elements
- All world knowledge is stored in the connections between the elements
- *Multiple* connectionist paradigms proposed..

Turing's Connectionist Machines



- Basic model: A-type machines
 - Networks of NAND gates
- Connectionist model: B-type machines (1948)
 - Connection between two units has a "modifier"
 - If the green line is on, the signal sails through
 - If the red is on, the output is fixed to 1
 - "Learning" figuring out how to manipulate the coloured wires
 - Done by an A-type machine

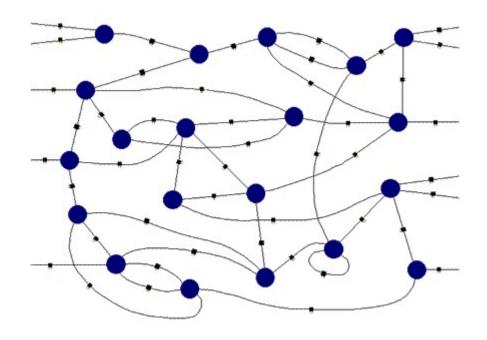
Connectionist paradigms: PDP Parallel Distributed Processing

- Requirements for a PDP system
 (Rumelhart, Hinton, McClelland, '86; quoted from Medler, '98)
 - A set of processing units
 - A state of activation
 - An output function for each unit
 - A pattern of connectivity among units
 - A propagation rule for propagating patterns of activities through the network of connectivities
 - An activation rule for combining the inputs impinging on a unit with the current state of that unit to produce a new level of activation for the unit
 - A learning rule whereby patterns of connectivity are modified by experience
 - An environment within which the system must operate

Connectionist Systems

- Requirements for a connectionist system (Bechtel and Abrahamson, 91)
 - The connectivity of units
 - The activation function of units
 - The nature of the learning procedure that modifies the connections between units, and
 - How the network is interpreted semantically

Connectionist Machines

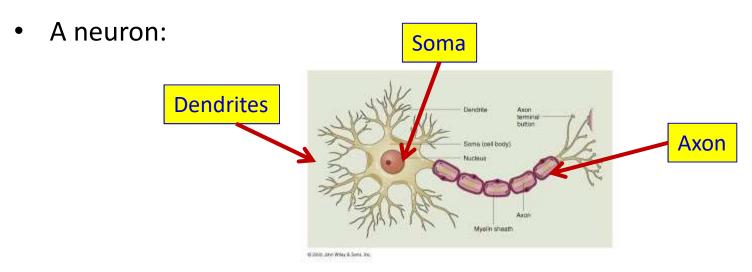


- Network of processing elements
 - All world knowledge is stored in the connections between the elements
- But what are the individual elements?



Modelling the brain

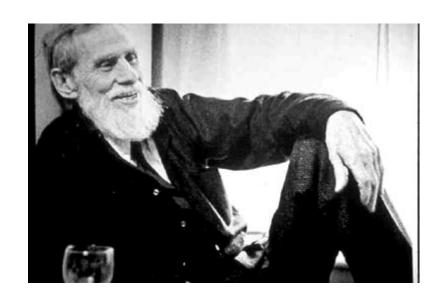
What are the units?



- Signals come in through the dendrites into the Soma
- A signal goes out via the axon to other neurons
 - Only one axon per neuron
- Factoid that may only interest me: Adult neurons do not undergo cell division

McCullough and Pitts

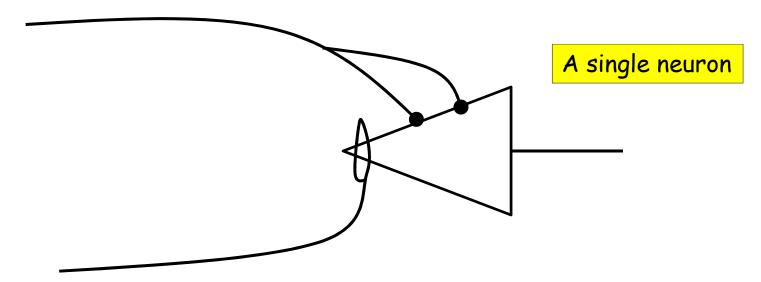




- The Doctor and the Hobo..
 - Warren McCulloch: Neurophysician
 - Walter Pitts: Homeless wannabe logician who arrived at his door

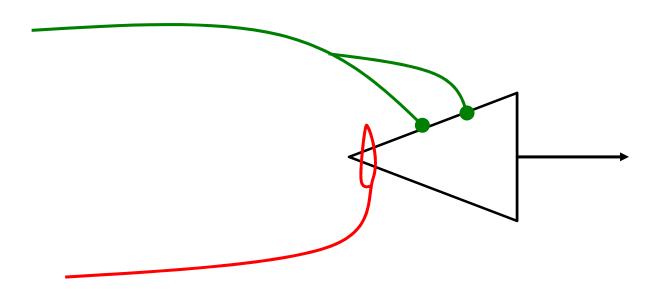


The McCulloch and Pitts model



- A mathematical model of a neuron
 - McCulloch, W.S. & Pitts, W.H. (1943). A Logical
 Calculus of the Ideas Immanent in Nervous Activity,
 Bulletin of Mathematical Biophysics, 5:115-137, 1943
 - Pitts was only 20 years old at this time

Synaptic Model



- Excitatory synapse: Transmits weighted input to the neuron
- Inhibitory synapse: Any signal from an inhibitory synapse forces output to zero
 - The activity of any inhibitory synapse absolutely prevents excitation of the neuron at that time.
 - Regardless of other inputs

McCullouch and Pitts model

- Made the following assumptions
 - The activity of the neuron is an "all-or-none" process
 - A certain fixed number of synapses must be excited within the period of latent addition in order to excite a neuron at any time, and this number is independent of previous activity and position of the neuron
 - The only significant delay within the nervous system is synaptic delay
 - The activity of any inhibitory synapse absolutely prevents excitation of the neuron at that time
 - The structure of the net does not change with time

Simple "networks" of neurons can perform Boolean operations

Boolean Gates

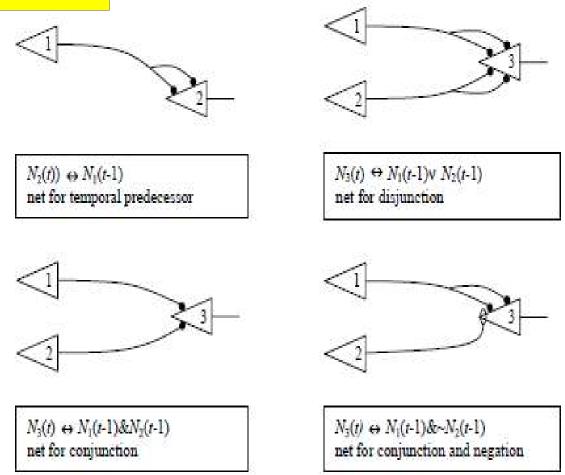


Figure 1. Diagrams of McCulloch and Pitts nets. In order to send an output pulse, each neuron must receive two excitory inputs and no inhibitory inputs. Lines ending in a dot represent excitatory connections; lines ending in a hoop represent inhibitory connections.

Complex Percepts & Inhibition in action

They can even create illusions of "perception"

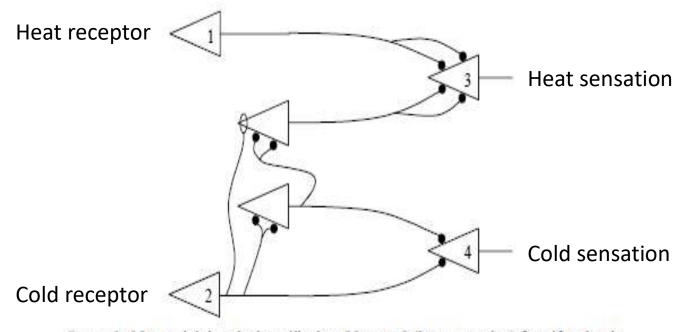
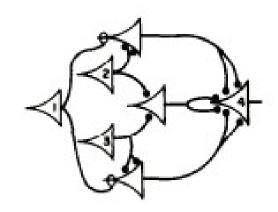


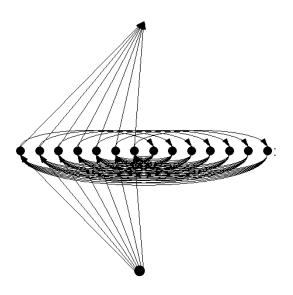
Figure 2. Net explaining the heat illusion. Neuron 3 (heat sensation) fires if and only if it receives two inputs, represented by the lines terminating on its body. This happens when either neuron 1 (heat reception) fires or neuron 2 (cold reception) fires once and then immediately stops firing. When neuron 2 fires twice in a row, the intermediate (unnumbered) neurons excite neuron 4 rather than neuron 3, generating a sensation of cold.

McCulloch and Pitts Model

- Could compute arbitrary Boolean propositions
 - Since any Boolean function can be emulated, any Boolean function can be composed



- Models for memory
 - Networks with loops can "remember"
 - We'll see more of this later
 - Lawrence Kubie (1930): Closed loops in the central nervous system explain memory



Criticisms

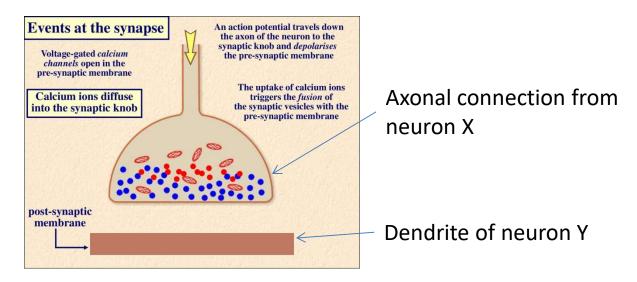
- They claimed that their nets
 - should be able to compute a small class of functions
 - also if tape is provided their nets can compute a richer class of functions.
 - additionally they will be equivalent to Turing machines
 - Dubious claim that they're Turing complete
 - They didn't prove any results themselves
- Didn't provide a learning mechanism..

Donald Hebb

- "Organization of behavior", 1949
- A learning mechanism:
 - "When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased."
 - As A repeatedly excites B, its ability to excite B improves
 - Neurons that fire together wire together



Hebbian Learning



- If neuron x_i repeatedly triggers neuron y, the synaptic knob connecting x_i to y gets larger
- In a mathematical model:

$$w_i = w_i + \eta x_i y$$

- Weight of i^{th} neuron's input to output neuron y
- This simple formula is actually the basis of many learning algorithms in ML

Hebbian Learning

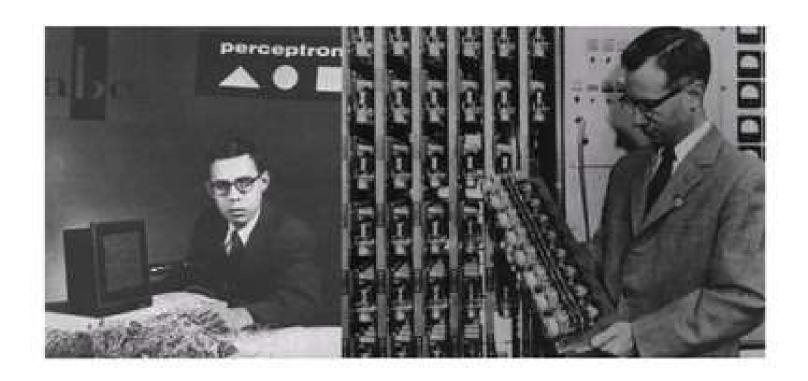
Fundamentally unstable

- Stronger connections will enforce themselves
- No notion of "competition"
- No reduction in weights
- Learning is unbounded
- Number of later modifications, allowing for weight normalization, forgetting etc.
 - E.g. Generalized Hebbian learning, aka Sanger's rule

$$w_{ij} = w_{ij} + \eta y_j \left(x_i - \sum_{k=1}^j w_{ik} y_k \right)$$

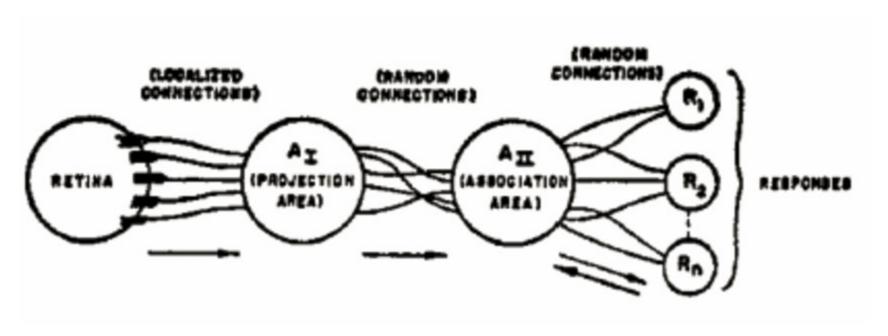
 The contribution of an input is incrementally distributed over multiple outputs..

A better model



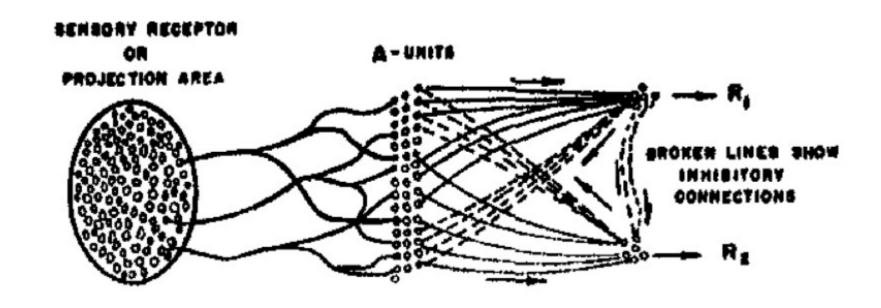
- Frank Rosenblatt
 - Psychologist, Logician
 - Inventor of the solution to everything, aka the Perceptron (1958)

Rosenblatt's perceptron



- Original perceptron model
 - Groups of sensors (S) on retina combine onto cells in association area A1
 - Groups of A1 cells combine into Association cells A2
 - Signals from A2 cells combine into response cells R
 - All connections may be excitatory or inhibitory

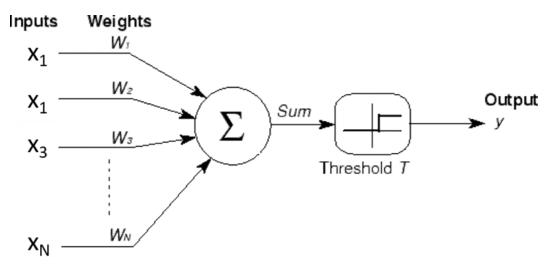
Rosenblatt's perceptron



- Even included feedback between A and R cells
 - Ensures mutually exclusive outputs



Simplified mathematical model



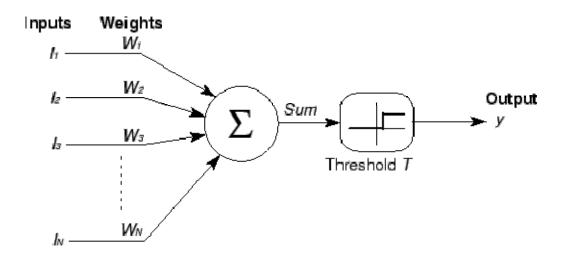
- Number of inputs combine linearly
 - Threshold logic: Fire if combined input exceeds threshold

$$Y = \begin{cases} 1 & if \sum_{i} w_i x_i - T > 0 \\ 0 & else \end{cases}$$



His "Simple" Perceptron

- Originally assumed could represent any Boolean circuit and perform any logic
 - "the embryo of an electronic computer that [the Navy] expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence," New York Times (8 July) 1958
 - "Frankenstein Monster Designed by Navy That Thinks," Tulsa,
 Oklahoma Times 1958



Also provided a learning algorithm

$$\mathbf{w} = \mathbf{w} + \eta (d(\mathbf{x}) - y(\mathbf{x}))\mathbf{x}$$

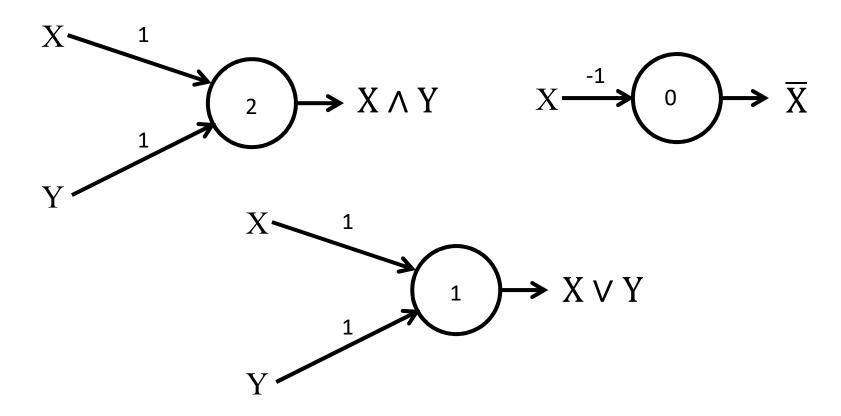
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Sequential Learning: d(x) is the desired output in response to input x
```

y(x) is the actual output in response to x

- Boolean tasks
- Update the weights whenever the perceptron output is wrong
- Proved convergence



Perceptron

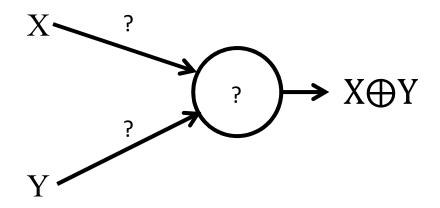


- Easily shown to mimic any Boolean gate
- But...



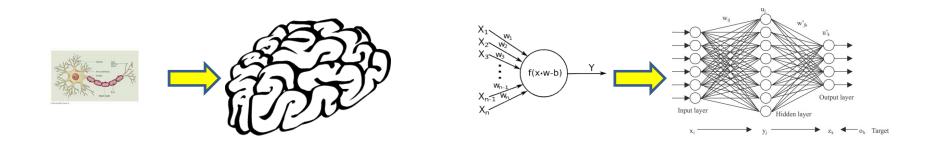
Perceptron

No solution for XOR! Not universal!



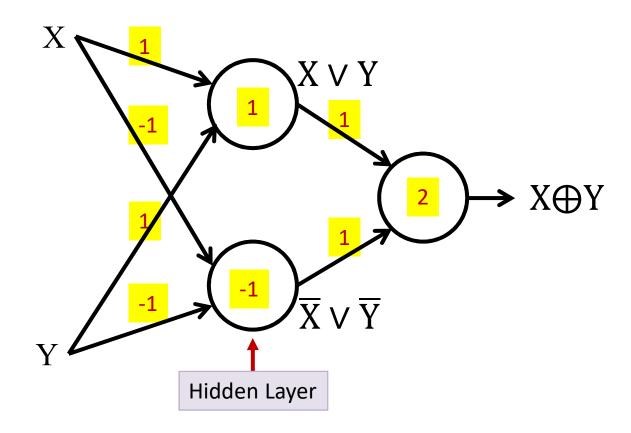
Minsky and Papert, 1968

A single neuron is not enough



- Individual elements are weak computational elements
 - Marvin Minsky and Seymour Papert, 1969, Perceptrons:
 An Introduction to Computational Geometry
- Networked elements are required

Multi-layer Perceptron!

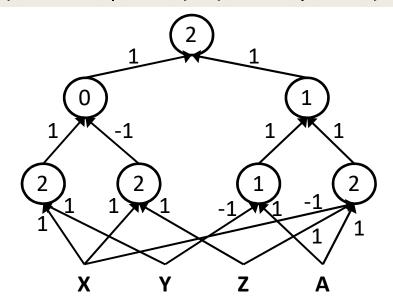


XOR

- The first layer is a "hidden" layer
- Also originally suggested by Minsky and Paper 1968

A more generic model

 $((A\&\bar{X}\&Z)|(A\&\bar{Y}))\&((X\&Y)|\overline{(X\&Z)})$

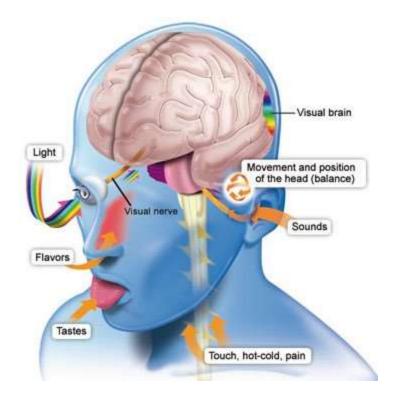


- A "multi-layer" perceptron
- Can compose arbitrarily complicated Boolean functions!
 - In cognitive terms: Can compute arbitrary Boolean functions over sensory input
 - More on this in the next class

Story so far

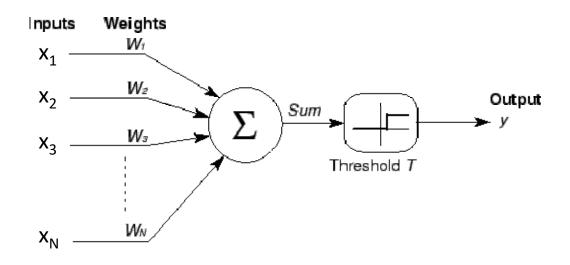
- Neural networks began as computational models of the brain
- Neural network models are connectionist machines
 - The comprise networks of neural units
- McCullough and Pitt model: Neurons as Boolean threshold units
 - Models the brain as performing propositional logic
 - But no learning rule
- Hebb's learning rule: Neurons that fire together wire together
 - Unstable
- Rosenblatt's perceptron: A variant of the McCulloch and Pitt neuron with a provably convergent learning rule
 - But individual perceptrons are limited in their capacity (Minsky and Papert)
- Multi-layer perceptrons can model arbitrarily complex Boolean functions

But our brain is not Boolean



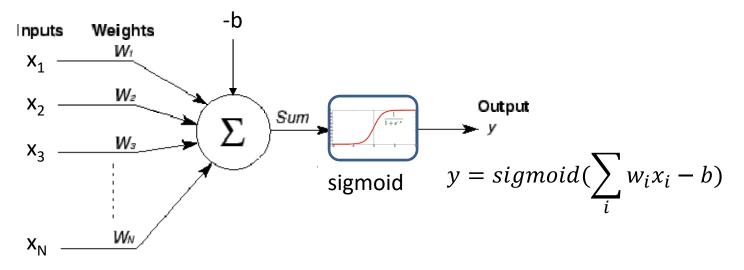
- We have real inputs
- We make non-Boolean inferences/predictions

The perceptron with *real* inputs



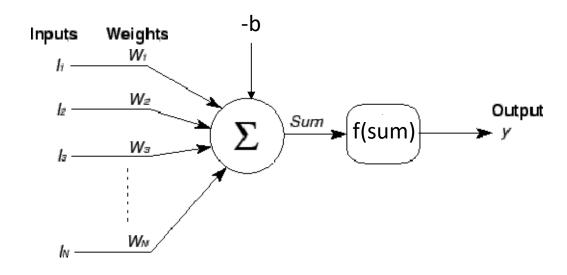
- $x_1...x_N$ are real valued
- $W_1 \dots W_N$ are real valued
- Unit "fires" if weighted input exceeds a threshold

The perceptron with *real* inputs and a real *output*



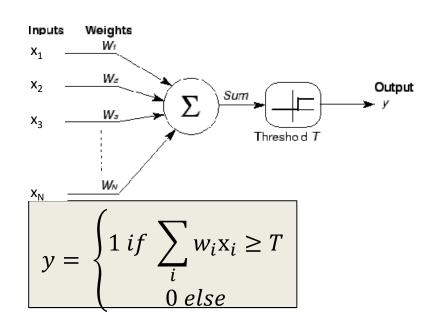
- $x_1...x_N$ are real valued
- $W_1...W_N$ are real valued
- The output y can also be real valued
 - Sometimes viewed as the "probability" of firing

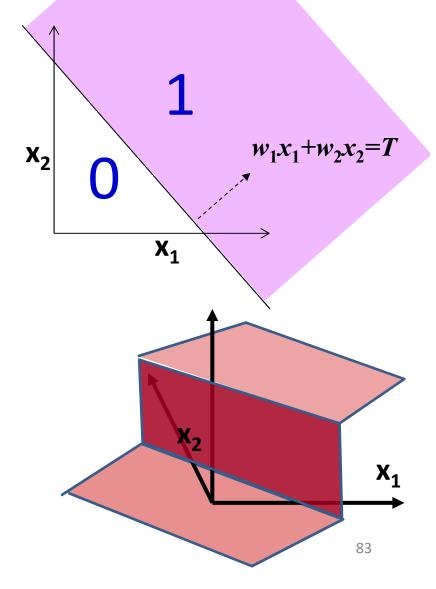
The "real" valued perceptron



- Any real-valued "activation" function may operate on the weightedsum input
 - We will see several later
 - Output will be real valued
- The perceptron maps real-valued inputs to real-valued outputs
- Is useful to continue assuming Boolean outputs though, for interpretation

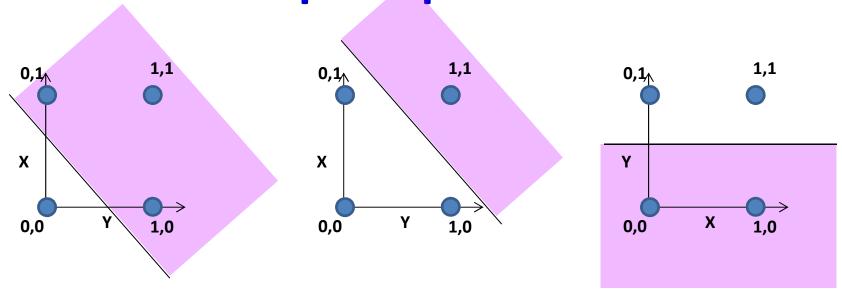
A Perceptron on Reals





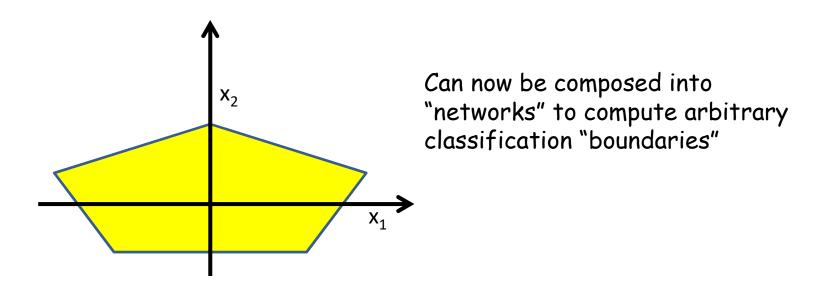
- A perceptron operates on real-valued vectors
 - This is a linear classifier

Boolean functions with a real perceptron

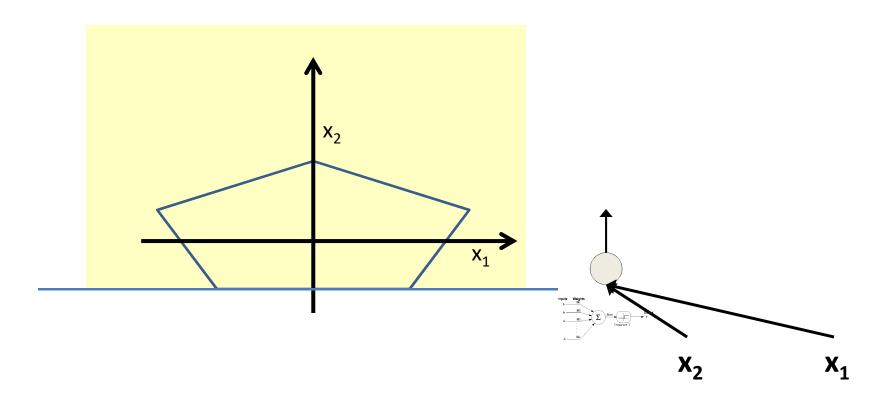


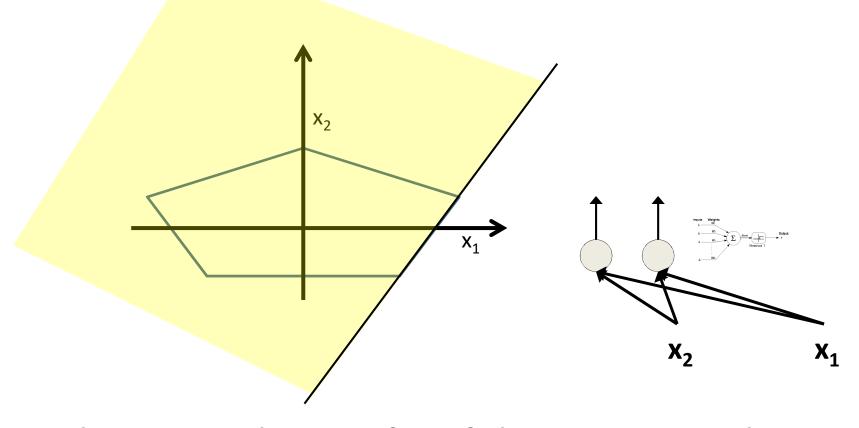
- Boolean perceptrons are also linear classifiers
 - Purple regions have output 1 in the figures
 - What are these functions
 - Why can we not compose an XOR?

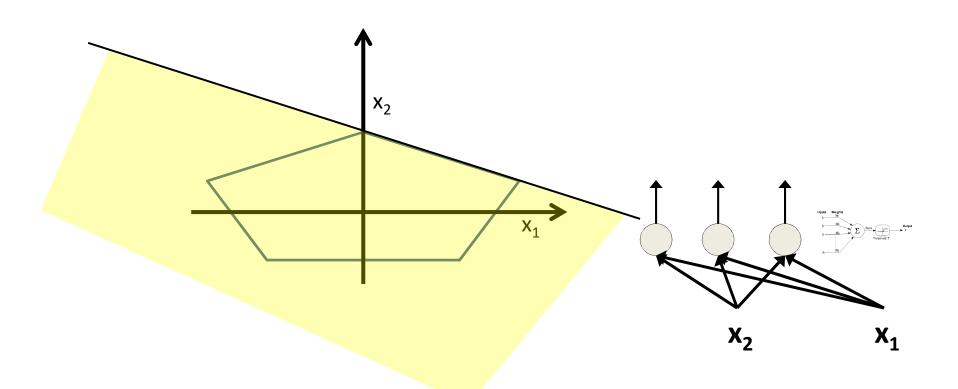
Composing complicated "decision" boundaries

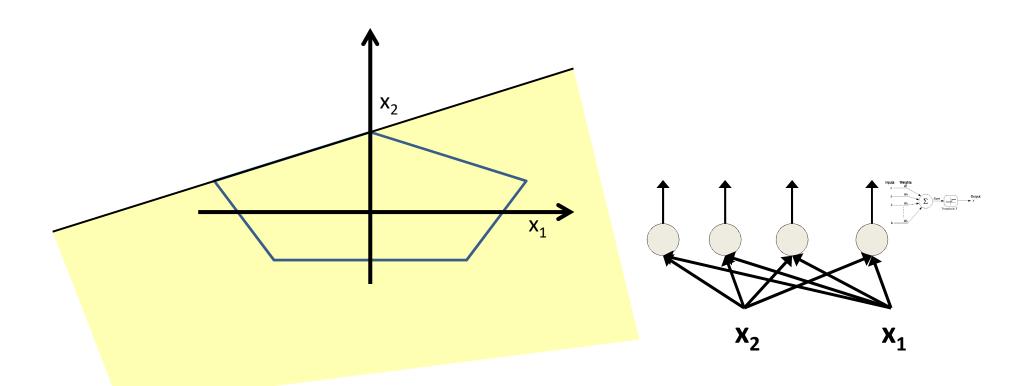


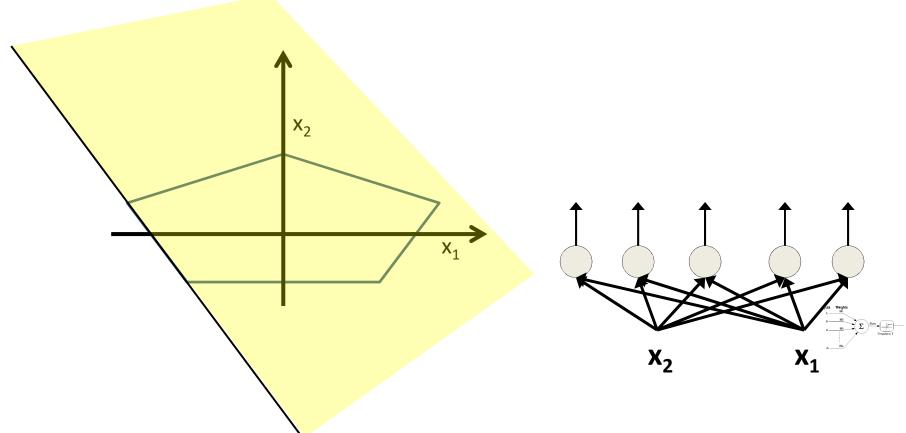
 Build a network of units with a single output that fires if the input is in the coloured area

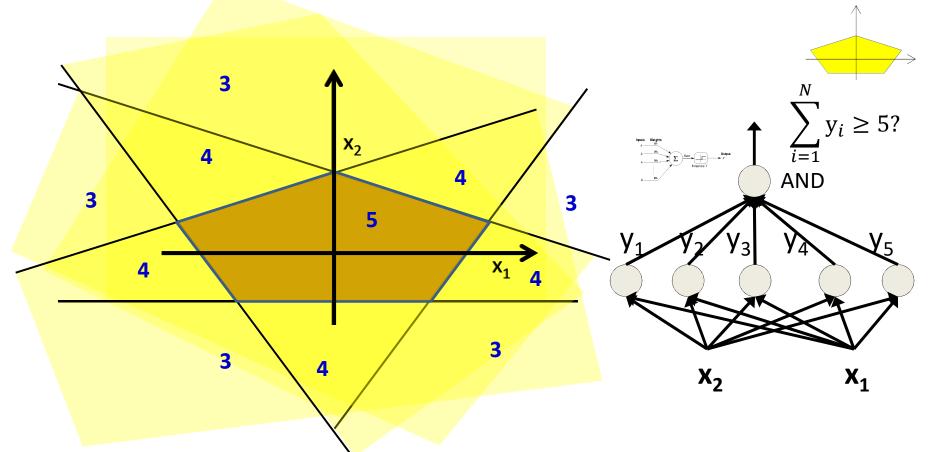




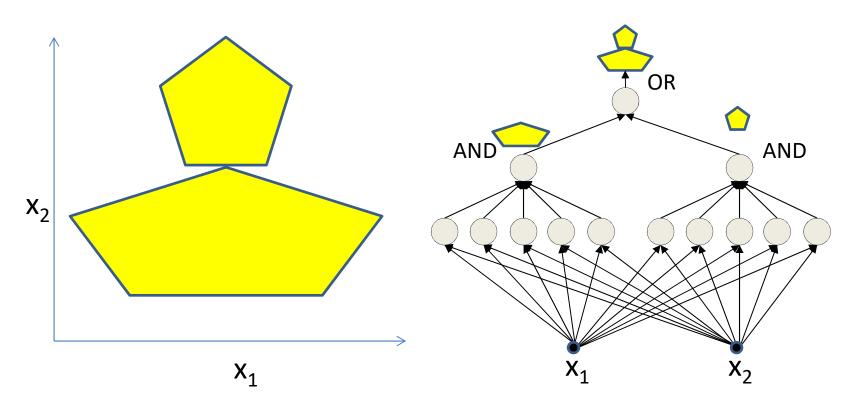






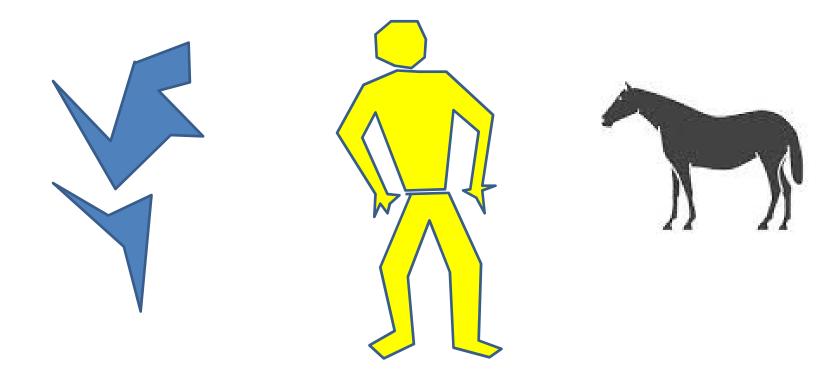


More complex decision boundaries



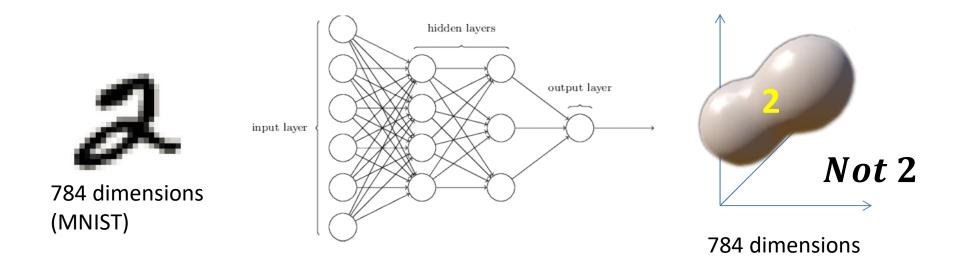
- Network to fire if the input is in the yellow area
 - "OR" two polygons
 - A third layer is required

Complex decision boundaries



- Can compose very complex decision boundaries
 - How complex exactly? More on this in the next class

Complex decision boundaries



- Classification problems: finding decision boundaries in high-dimensional space
 - Can be performed by an MLP
- MLPs can classify real-valued inputs

Story so far

MLPs are connectionist computational models

- Individual perceptrons are computational equivalent of neurons
- The MLP is a layered composition of many perceptrons

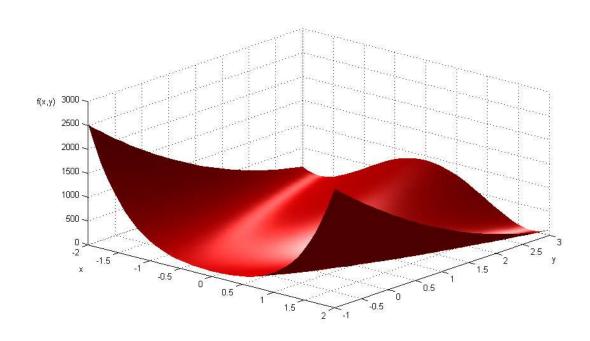
MLPs can model Boolean functions

- Individual perceptrons can act as Boolean gates
- Networks of perceptrons are Boolean functions

MLPs are Boolean machines

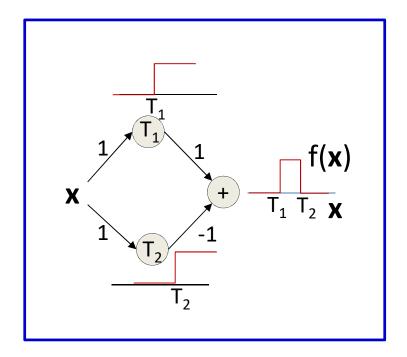
- They represent Boolean functions over linear boundaries
- They can represent arbitrary decision boundaries
- They can be used to classify data

But what about continuous valued outputs?



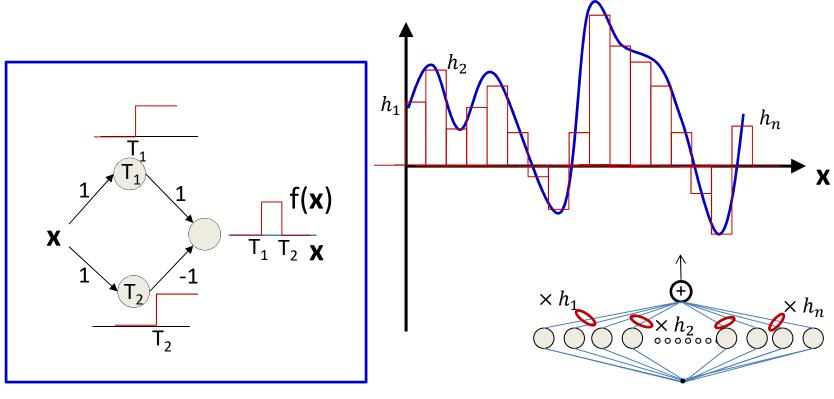
- Inputs may be real valued
- Can outputs be continuous-valued too

MLP as a continuous-valued regression



- A simple 3-unit MLP with a "summing" output unit can generate a "square pulse" over an input
 - Output is 1 only if the input lies between T₁ and T₂
 - T₁ and T₂ can be arbitrarily specified

MLP as a continuous-valued regression



- A simple 3-unit MLP can generate a "square pulse" over an input
- An MLP with many units can model an arbitrary function over an input
 - To arbitrary precision
 - Simply make the individual pulses narrower
- This generalizes to functions of any number of inputs (next class)

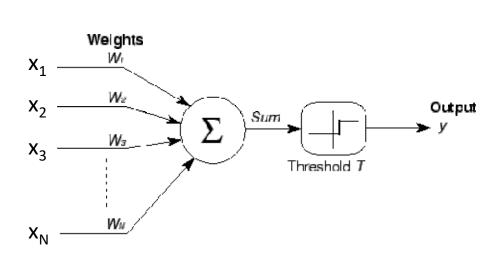
Story so far

- Multi-layer perceptrons are connectionist computational models
- MLPs are classification engines
 - They can identify classes in the data
 - Individual perceptrons are feature detectors
 - The network will fire if the combination of the detected basic features matches an "acceptable" pattern for a desired class of signal
- MLP can also model continuous valued functions

So what does the perceptron really model?

- Is there a "semantic" interpretation?
 - Cognitive version: Is there an interpretation beyond the simple characterization as Boolean functions over sensory inputs?

Lets look at the weights

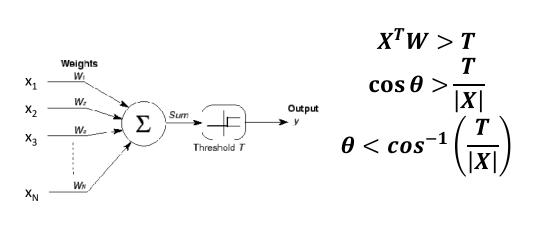


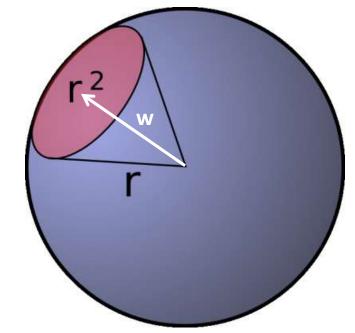
$$y = \begin{cases} 1 & \text{if } \sum_{i} w_i x_i \ge T \\ 0 & \text{else} \end{cases}$$

$$y = \begin{cases} 1 & if \ \mathbf{x}^T \mathbf{w} \ge T \\ 0 & else \end{cases}$$

- What do the weights tell us?
 - The neuron fires if the inner product between the weights and the inputs exceeds a threshold

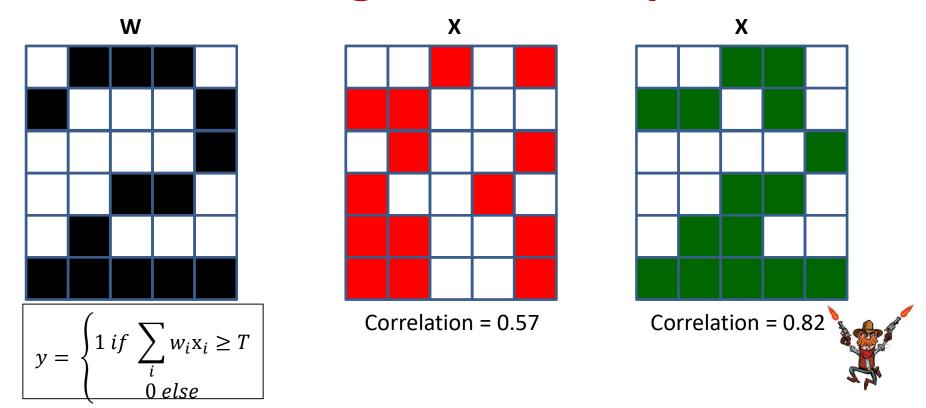
The weight as a "template"





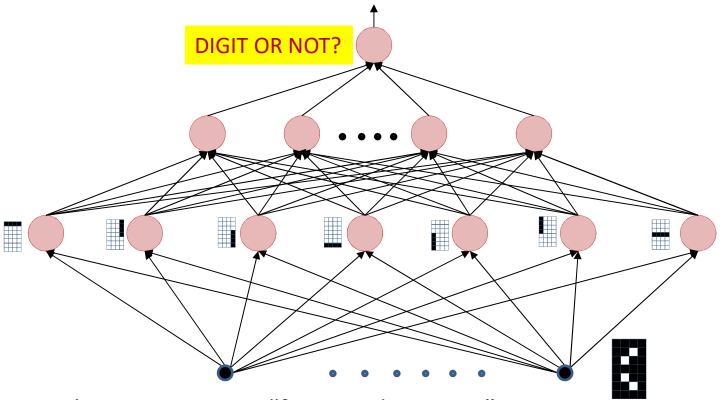
- The perceptron fires if the input is within a specified angle of the weight
- Neuron fires if the input vector is close enough to the weight vector.
 - If the input pattern matches the weight pattern closely enough

The weight as a template



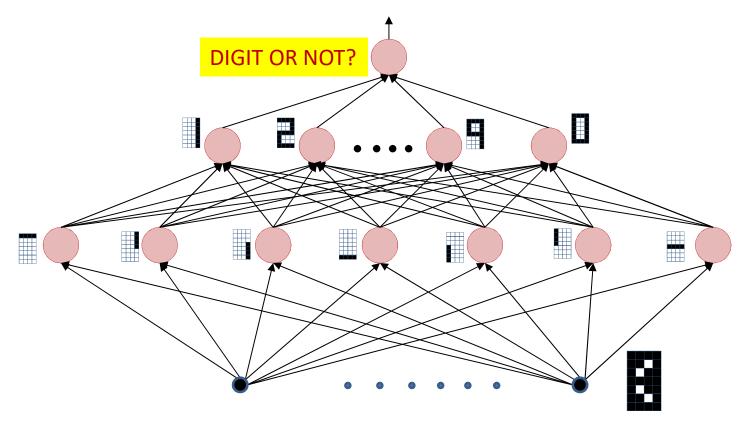
- If the *correlation* between the weight pattern and the inputs exceeds a threshold, fire
- The perceptron is a correlation filter!

The MLP as a Boolean function over feature detectors



- The input layer comprises "feature detectors"
 - Detect if certain patterns have occurred in the input
- The network is a Boolean function over the feature detectors
- I.e. it is important for the first layer to capture relevant patterns

The MLP as a cascade of feature detectors



- The network is a cascade of feature detectors
 - Higher level neurons compose complex templates from features represented by lower-level neurons

Story so far

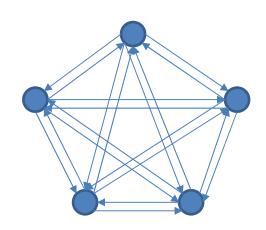
- Multi-layer perceptrons are connectionist computational models
- MLPs are Boolean machines
 - They can model Boolean functions
 - They can represent arbitrary decision boundaries over real inputs
- MLPs can approximate continuous valued functions
- Perceptrons are correlation filters
 - They detect patterns in the input

Other things MLPs can do

- Model memory
 - Loopy networks can "remember" patterns
 - Proposed by Lawrence Kubie in 1930, as a model for memory in the CNS



- Over integer, real and complex-valued domains
- MLPs can model both a posteriori and a priori distributions of data
 - A posteriori conditioned on other variables
- They can rub their stomachs and pat their heads at the same time..

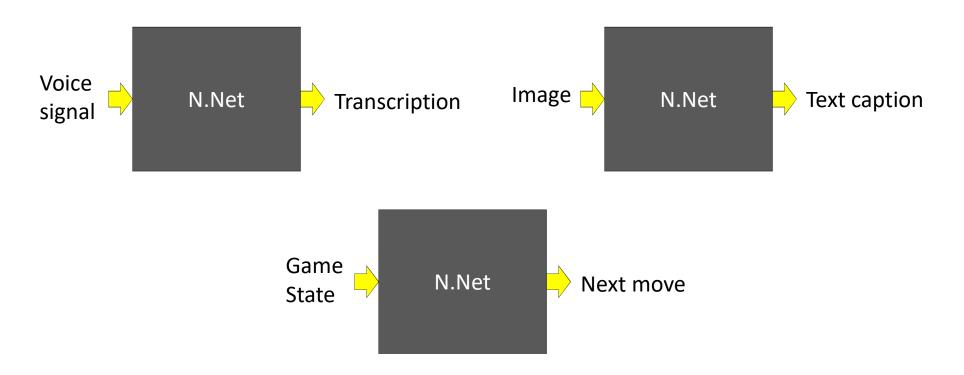




NNets in Al

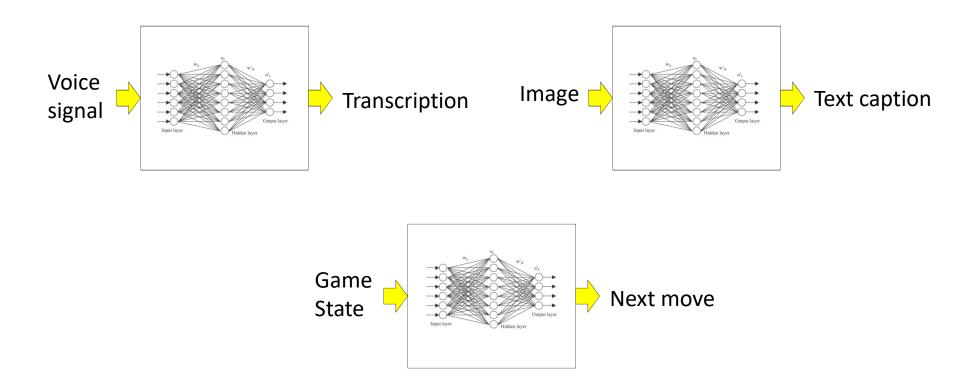
- The network is a function
 - Given an input, it computes the function layer wise to predict an output

These tasks are functions



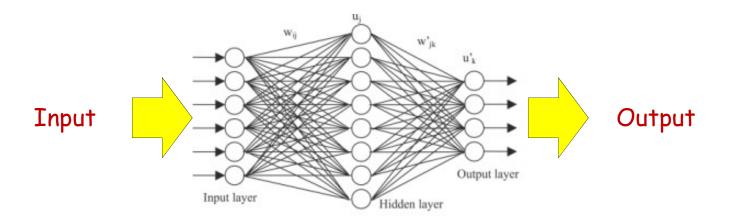
- Each of these boxes is actually a function
 - E.g f: Image \rightarrow Caption

These tasks are functions



- Each box is actually a function
 - E.g f: Image \rightarrow Caption
 - It can be approximated by a neural network

The network as a function



- Inputs are numeric vectors
 - Numeric representation of input, e.g. audio, image, game state, etc.
- Outputs are numeric scalars or vectors
 - Numeric "encoding" of output from which actual output can be derived
 - E.g. a score, which can be compared to a threshold to decide if the input is a face or not
 - Output may be multi-dimensional, if task requires it

Story so far

- Multi-layer perceptrons are connectionist computational models
- MLPs are classification engines
- MLP can also model continuous valued functions
- Interesting AI tasks are functions that can be modelled by the network

Next Up

- More on neural networks as universal approximators
 - And the issue of depth in networks