

We want a_{ij}^{new} = new estimate of $P(q_{t+1} = s_j | q_t = s_i, \lambda^{\text{old}})$

Also estimate estimate

$$b_j(o=k) = \text{new est of } P(o_t = k | q_t = s_j)$$

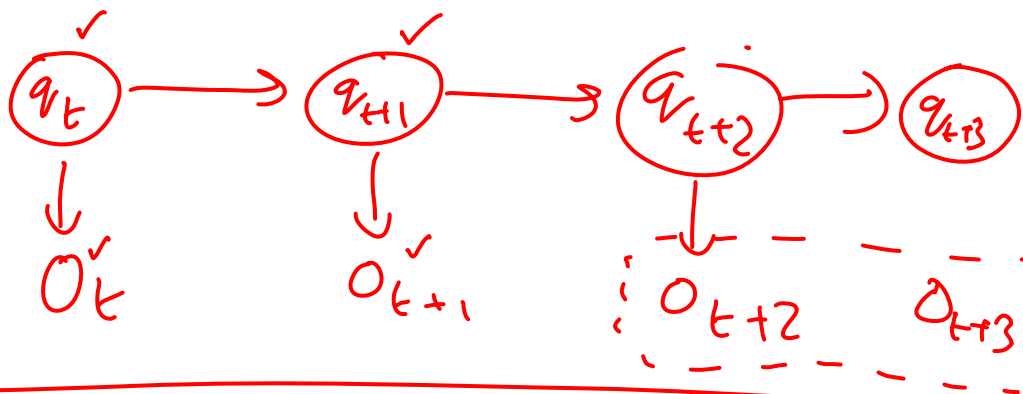
params of
old HMM

$$P(q_t = i \wedge q_{t+1} = j \wedge o_1 \dots o_T | \lambda^{old})$$

$$P(o_{t+2} \dots o_T | q_t = i \wedge q_{t+1} = j \wedge o_1 \dots o_{t+1}) P(q_t = i \wedge q_{t+1} = j \wedge o_1 \dots o_{t+1})$$

$$P(o_{t+2} \dots o_T | q_{t+1} = j)$$

$$\beta_{t+1}(j)$$



$$P(A \wedge B) = P(A|B)P(B)$$

$$\alpha_t(i) = P(q_t = s_i \wedge o_1 \dots o_t)$$

$$\beta_t(j) = P(o_{t+1} \dots o_T | q_t = s_j)$$

$$\begin{aligned}
 & P(q_t = i \wedge q_{t+1} = j \wedge o_1 \dots o_T \mid \lambda) \\
 = & \underbrace{P(o_{t+2} \dots o_T \mid q_t = i \wedge q_{t+1} = j \wedge o_1 \dots o_{t+1})}_{\beta_{t+1}(j)} \underbrace{P(q_t = i \wedge q_{t+1} = j \wedge o_1 \dots o_{t+1})}_{\alpha_t(i)} \\
 & \beta_{t+1}(j)
 \end{aligned}$$

$$\alpha_t(i) = P(q_t = s_i \wedge o_1 \dots o_t)$$

$$\beta_t(j) = P(o_{t+1} \dots o_T \mid q_t = s_j)$$