

Midterm Review

Topics

- Arrays – sorted, unsorted
- LL's – sorted, unsorted, singly, doubly, multi
- Algorithm complexity
- Stacks and queues and applications
- Recursion
- Binary Search Trees

Exam Format

- 80 minutes
- Written , in class exam
- One page of cheat sheet allowed
- No code examples
- Types of questions
 - Short answers ✓
 - Write/trace methods
 - Recursion on java with helper methods
 - Algorithm analysis

Arrays

Operations

big O

insert

delete

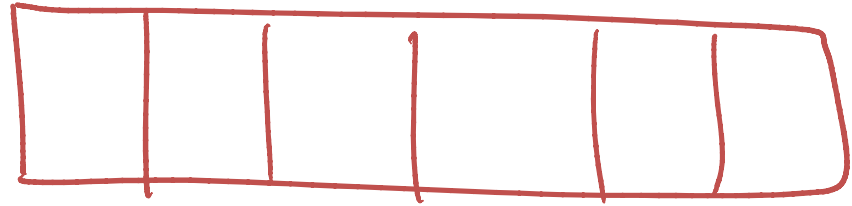
Search

Sort

Set an element

Reverse

Resize



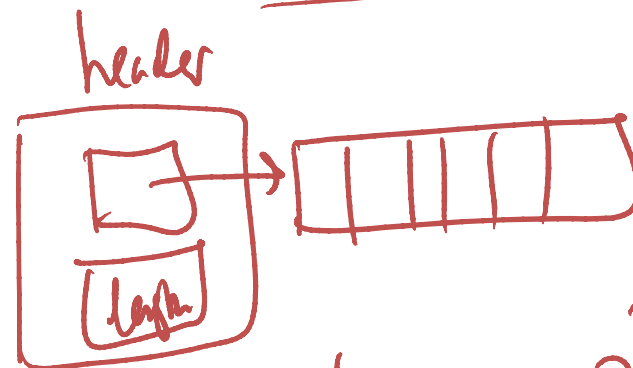
Contiguous

Random access

fixed size

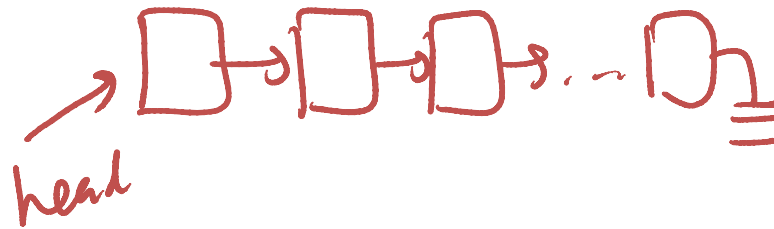
homogeneous

primitive types or
objects

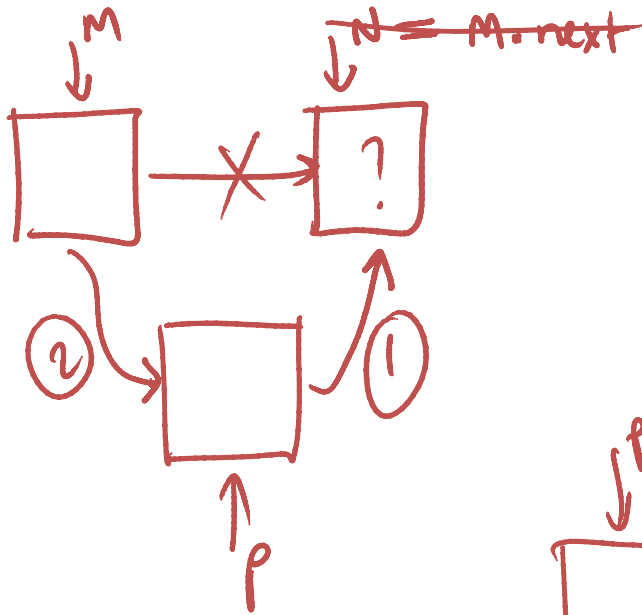
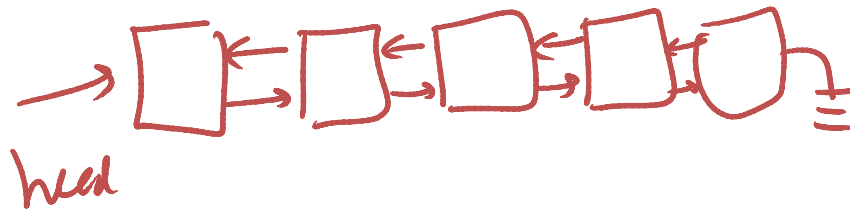


$$\text{largest signed} = 2^{31} - 1$$

LL's

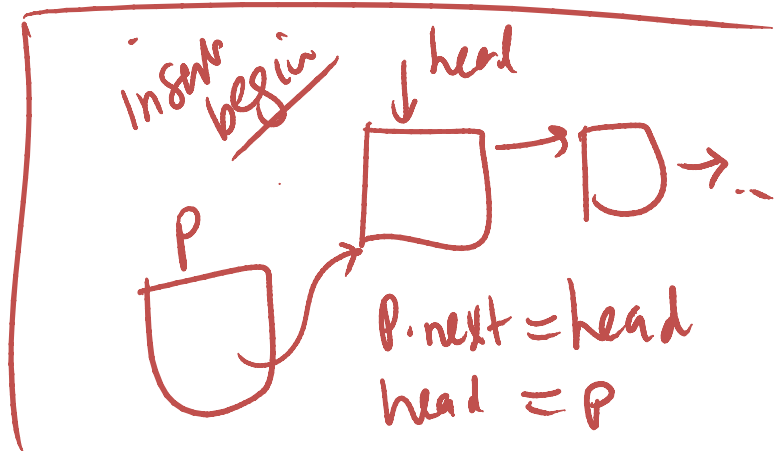
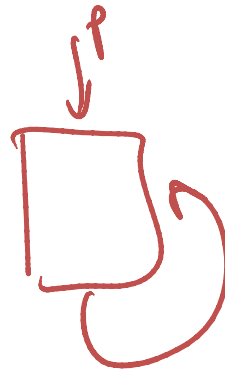


Insert



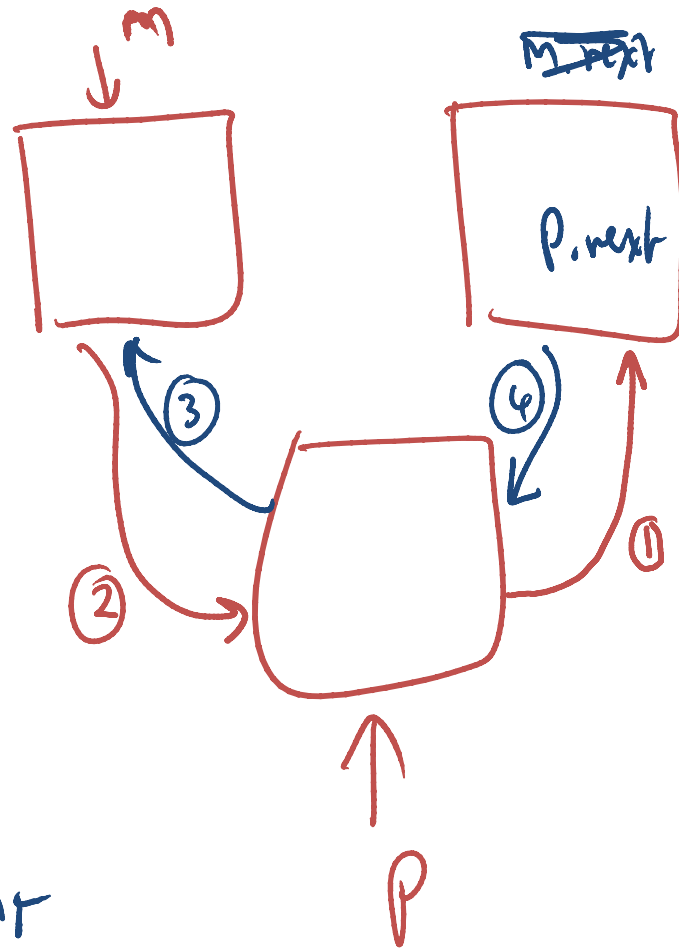
(2) $M.next = P$

(1) $P.next = M.next$



Operations

1. Insert Front
2. Insert
3. delete Front
4. delete
5. Find
6. Reverse →

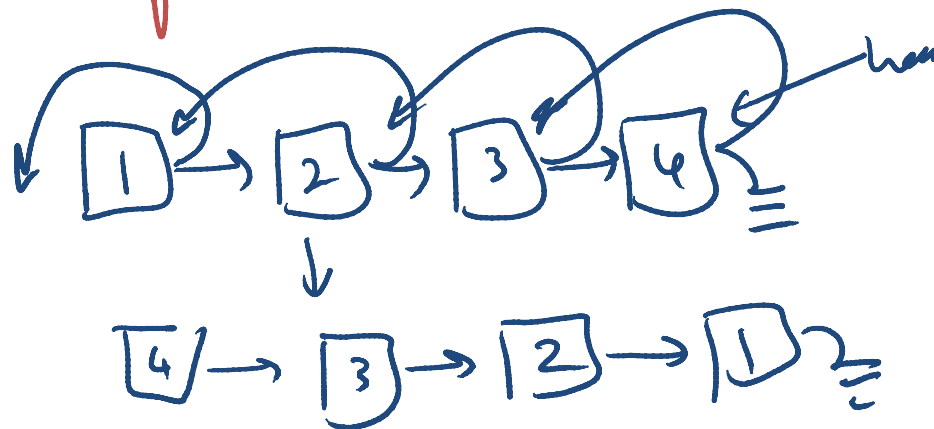


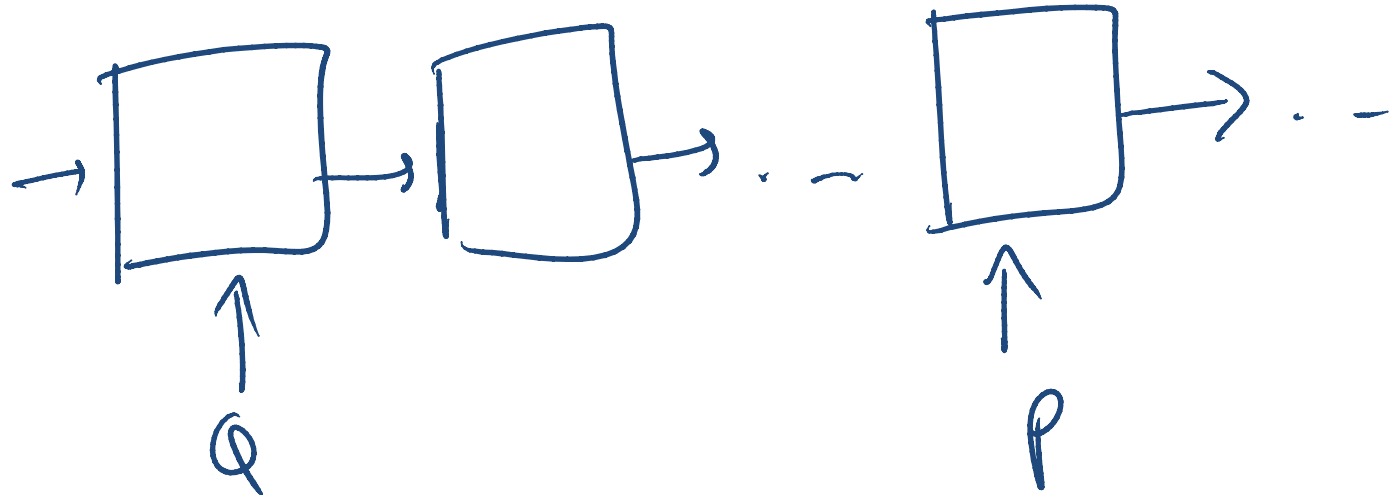
① : $P.next = M.next$

② : $M.next = P$

③ : $P.prev = M$

④ : $(P.next).prev = P$

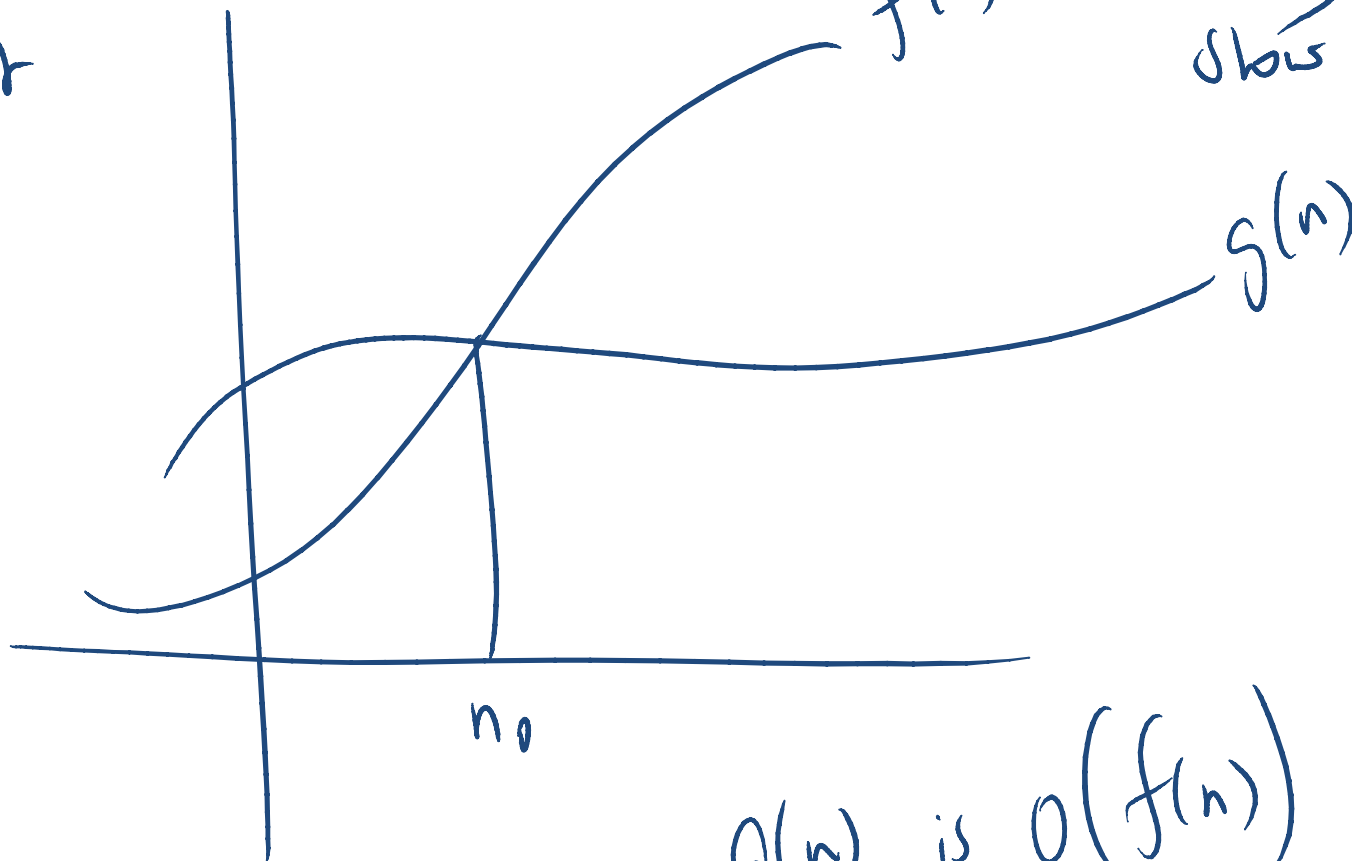




Swap(P, Q) → ??

$$O(1) < O(\lg n) < O(n) < O(n \lg n) < O(n^2) < O(n^p) < O(n!) < O(p^n)$$

$\leftarrow$ Fast slow $\rightarrow$



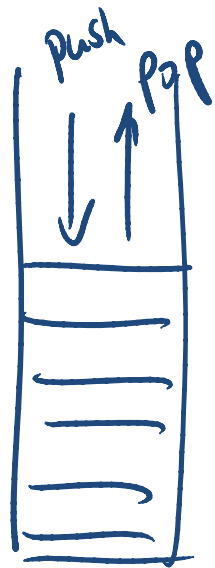
$g(n)$ is $O(f(n))$
 if $g(n) \leq f(n)$
 for all $n > n_0$

$$\begin{array}{l}
 \text{for } (i=1; i < n; i \overset{i+=2}{++}) \\
 \text{for } (j=i, j < n; j++)
 \end{array}
 \left. \vphantom{\begin{array}{l} \text{for } (i=1; i < n; i \overset{i+=2}{++}) \\ \text{for } (j=i, j < n; j++) \end{array}} \right\} O(n^2)$$

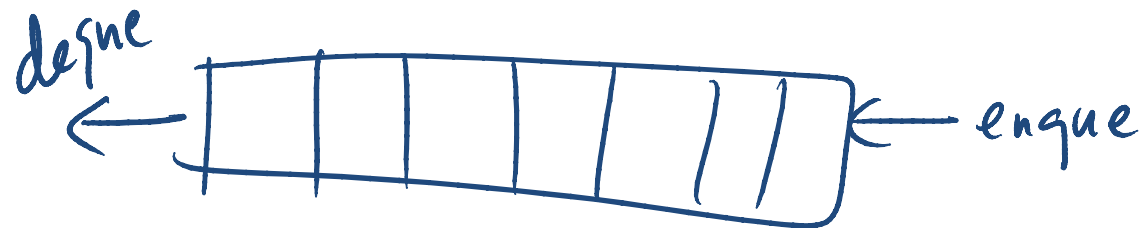
operation

$$\text{for } (i=1; i < n; i \neq 2) \rightarrow O(\log n)$$

Stacks | Queues



→ maze traversal (back tracking algorithm)
postfix eval



Recursion

$$f(n) = n + f(n-1) \quad f(0) = 0$$

$$f(n) = n \cdot f(n-1) \quad f(0) = 1$$

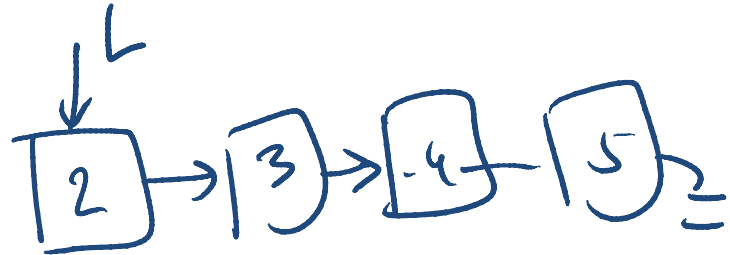
$$f(n) = 2 \cdot f(n-1) \quad f(0) = 1$$

$$f(n) = f(n-1) + f(n-2) \quad f(0) = f(1) = 1$$

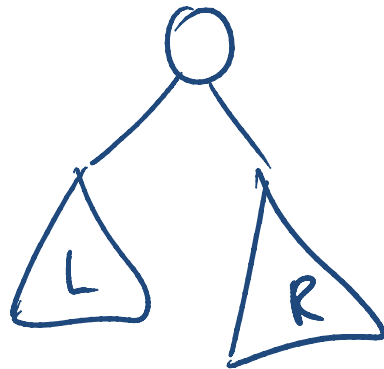
$n \geq 2$

Recursive Method

```
void foo(List L) {  
    if (L != null) {  
        System.out.println(L);  
        foo(L.next);  
    }  
}
```



BST

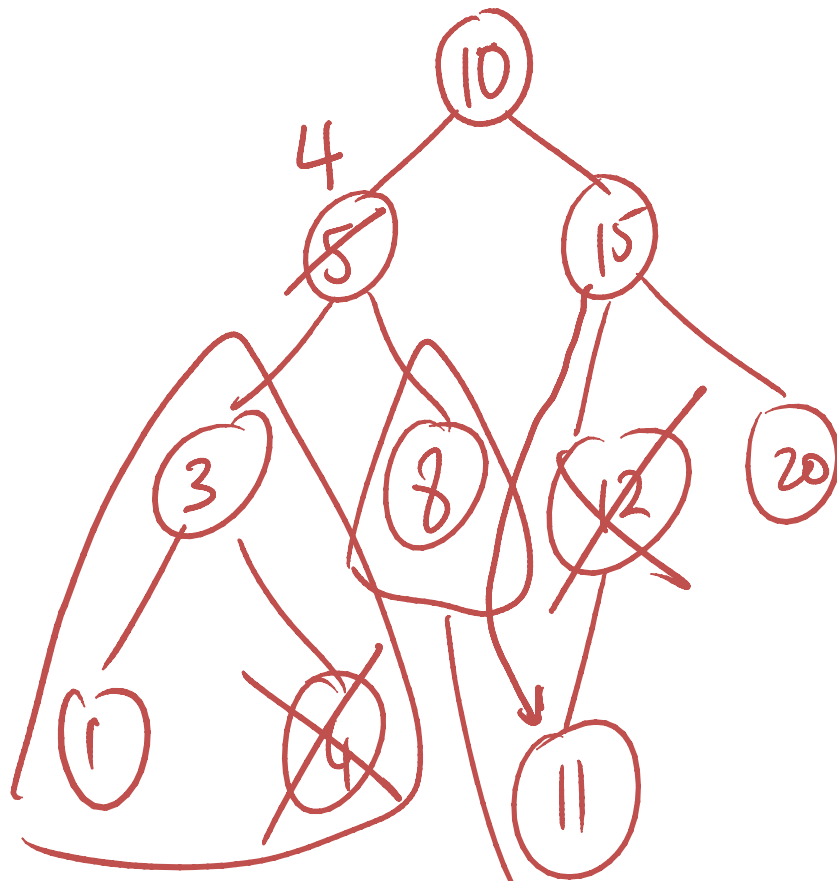


Full
Complete
Perfect

insert
delete

delete (11) $\rightarrow$ easy $\rightarrow$ (12). left = null

delete (12) $\rightarrow$ (15). left = (12). left



Final layout
left tree

Smallest
Right tree

