

# Lamport clocks

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# Synchronization

- Project 4 due today
- Homework 2 due Friday
- Book report due Friday
- FCE reminder
  - I will read (and take seriously) every word of what you write

# Outline

- Lamport clocks
  - Covered in 17.1, 17.2 (different focus from today)
  - Time, Clocks, and the Ordering of Events in a Distributed System
    - CACM 21:7 (1978)
- Leslie Lamport also famous for ...?

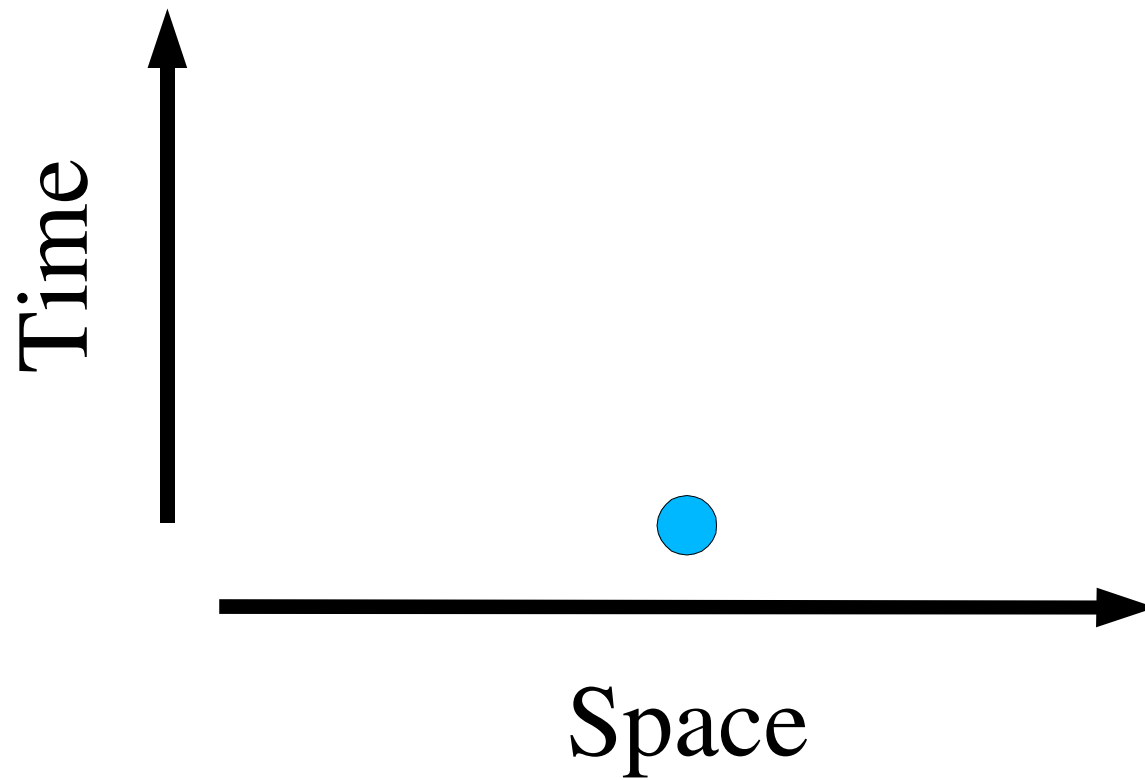
# Overview

- Light cones
- Meeting for beer
- “Happened before” partial order
- Logical clocks
- Advanced techniques

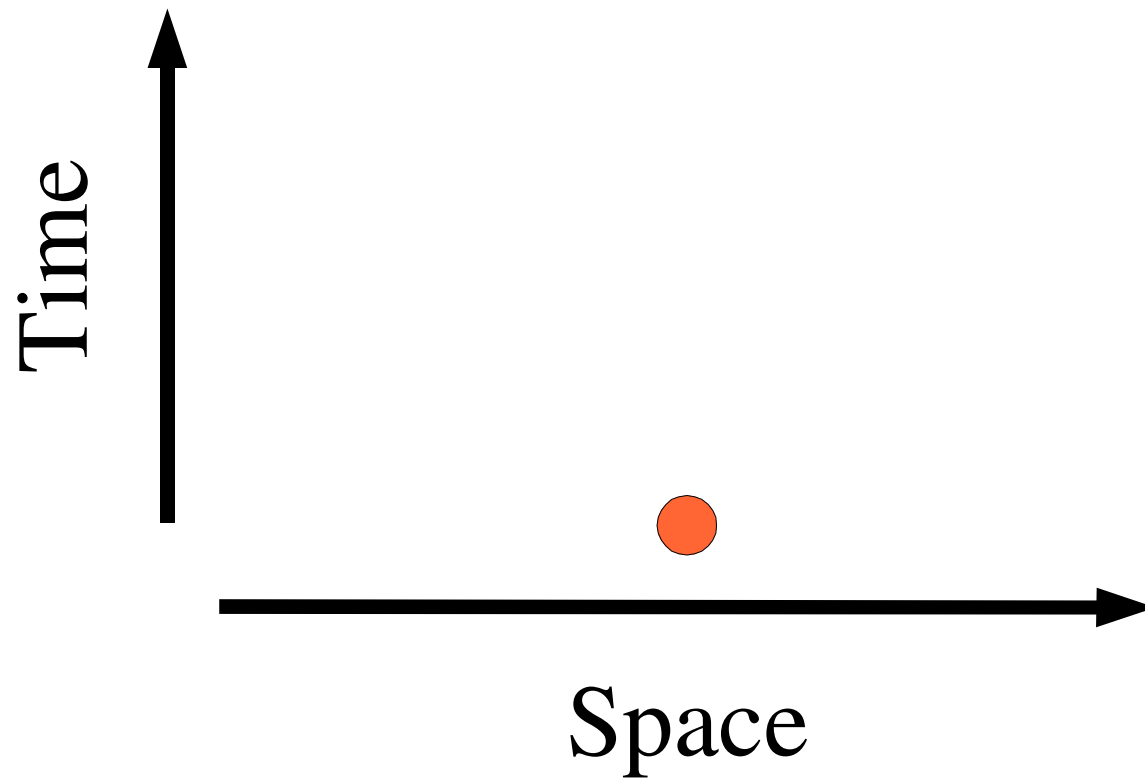
# Light cones

- Concept
  - Effects propagate at or below speed of light
    - Objects, light/radio/X-rays, gravity
  - *Knowledge* of events limited the same way
  - Event propagation modeled by expanding sphere
    - Four-dimensional “cone”

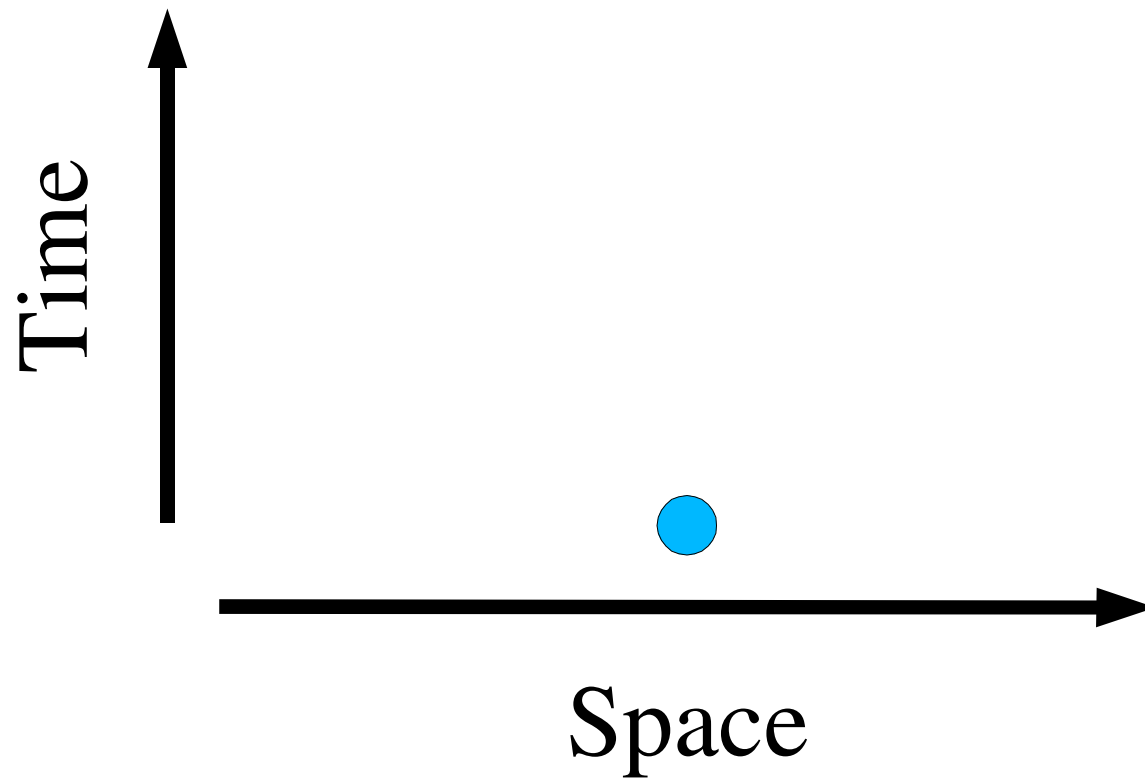
# Light cones



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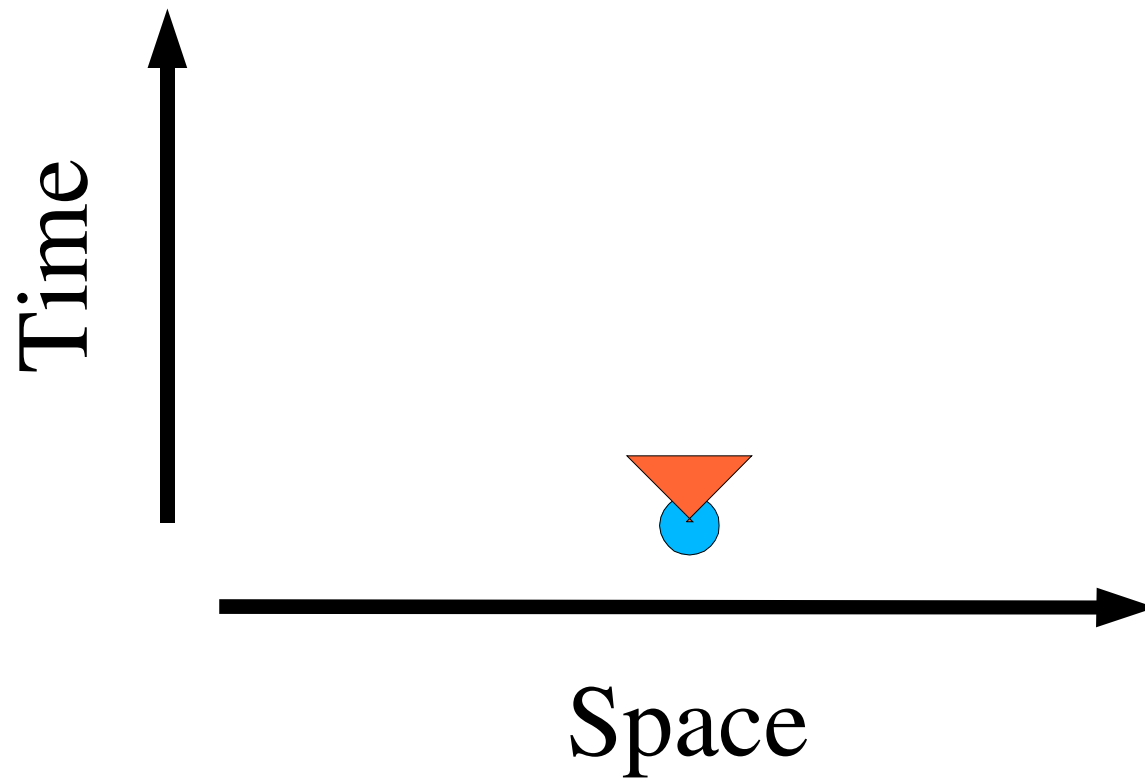


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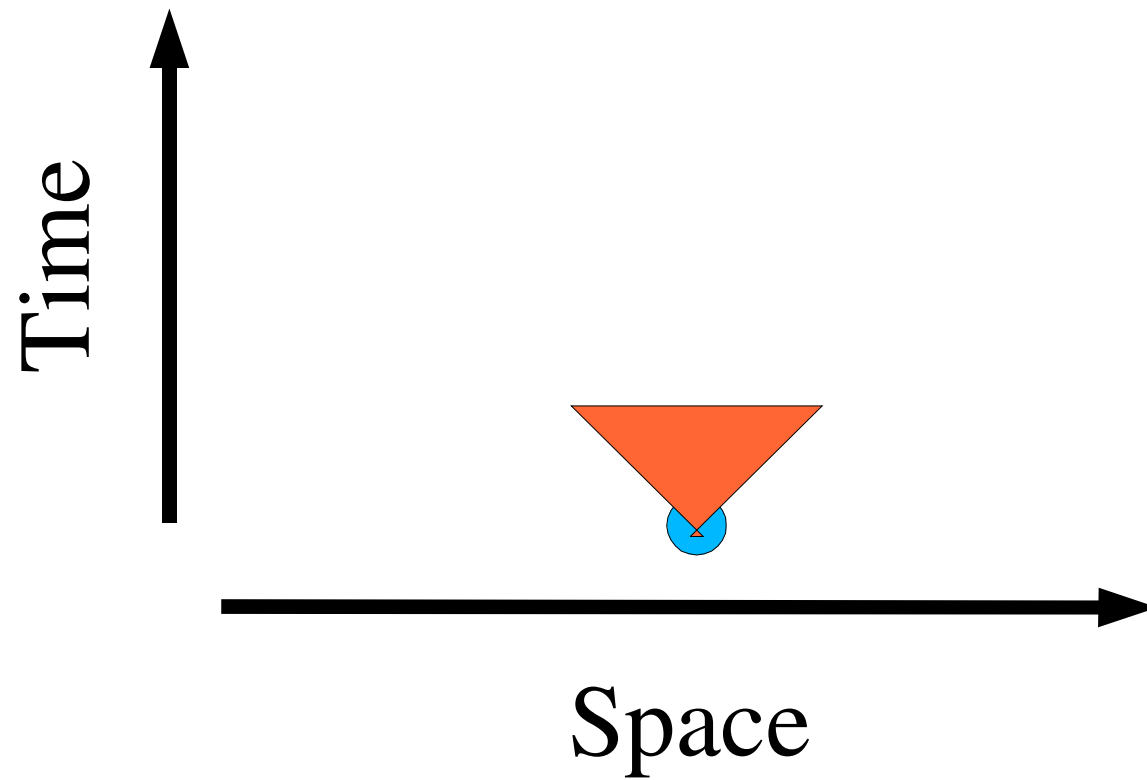




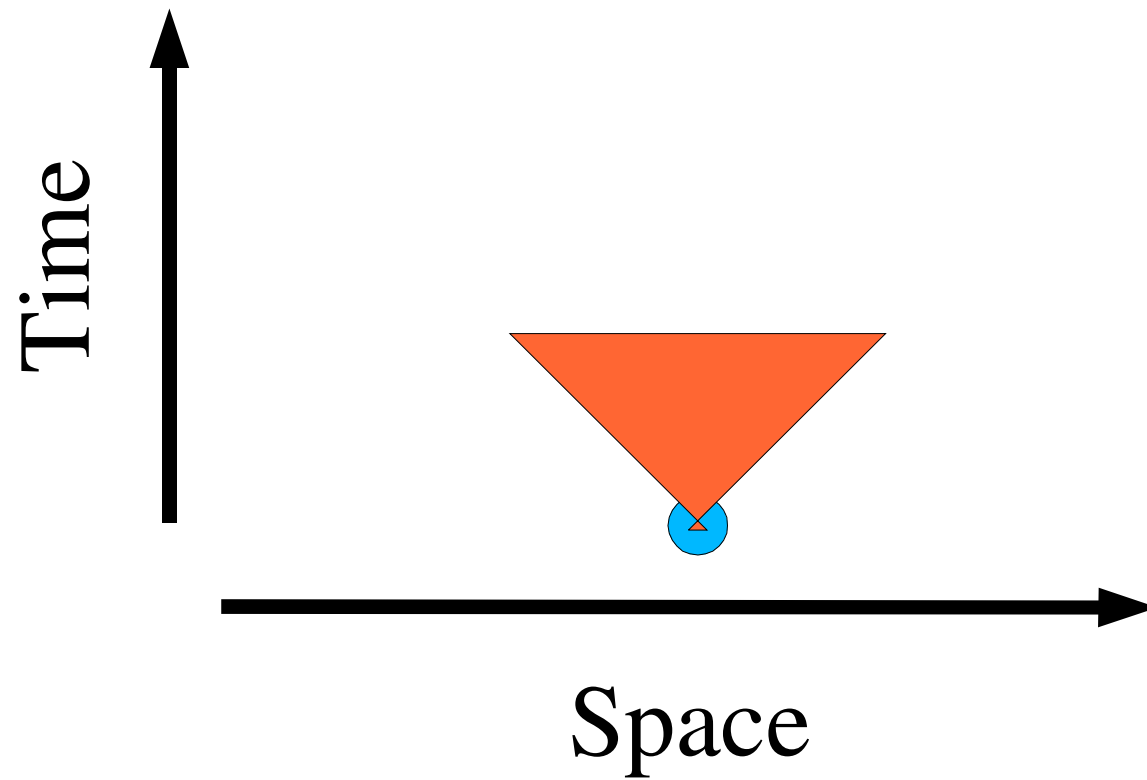
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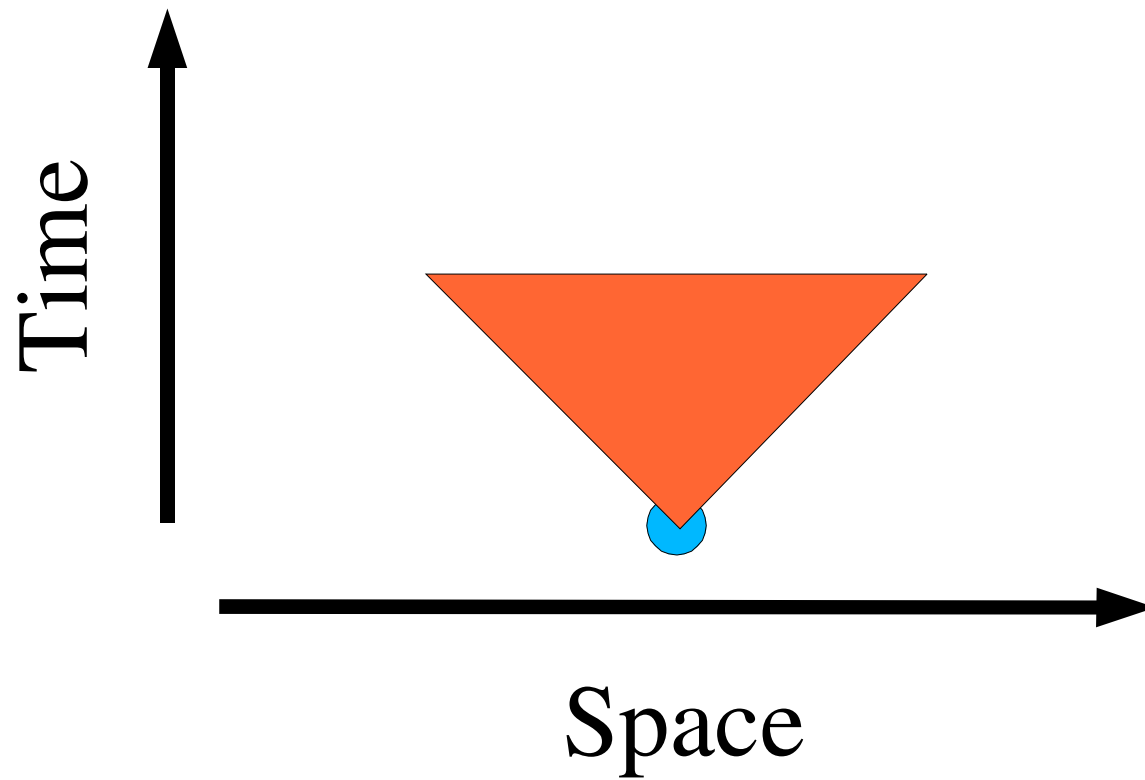
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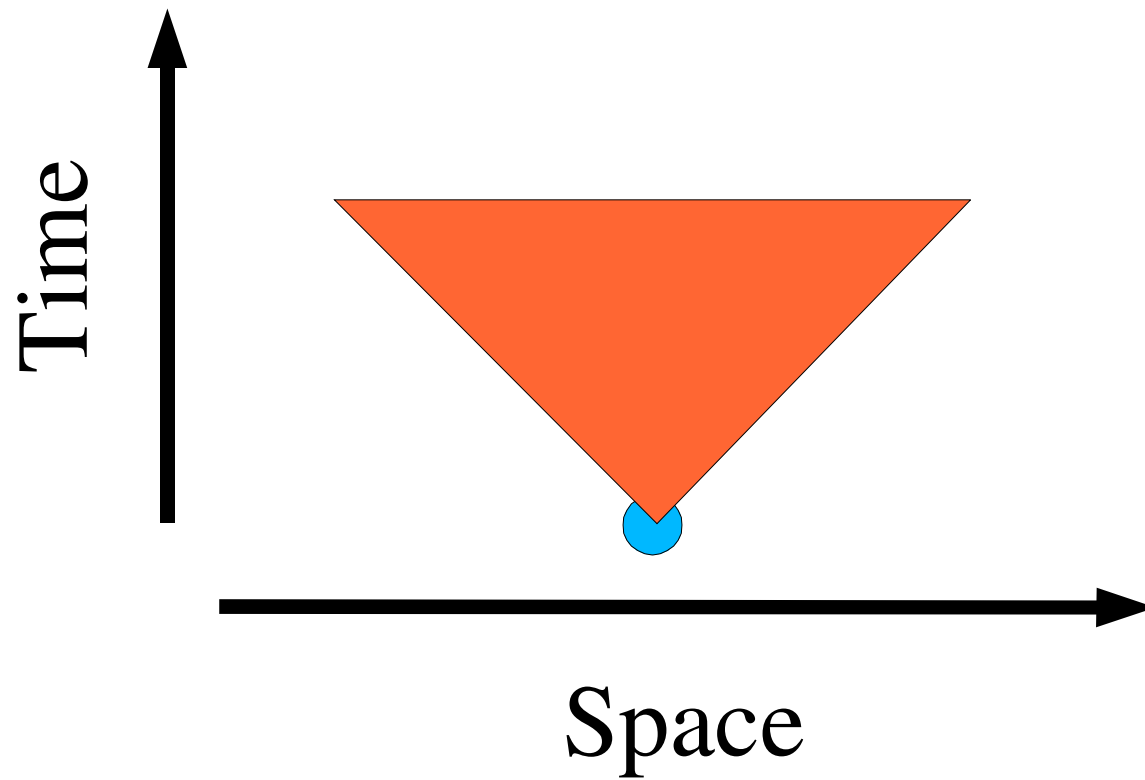
# Light cones



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# Light cones



# Light cones

- Future light cone
  - The part of spacetime potentially influenced by an event
- Past light cone
  - The part of spacetime that could have influenced an event

# Meeting for Beer

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- P1 transmits to P2
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  - I have transmitted the bar's name to the blackboard.
  - See you there!



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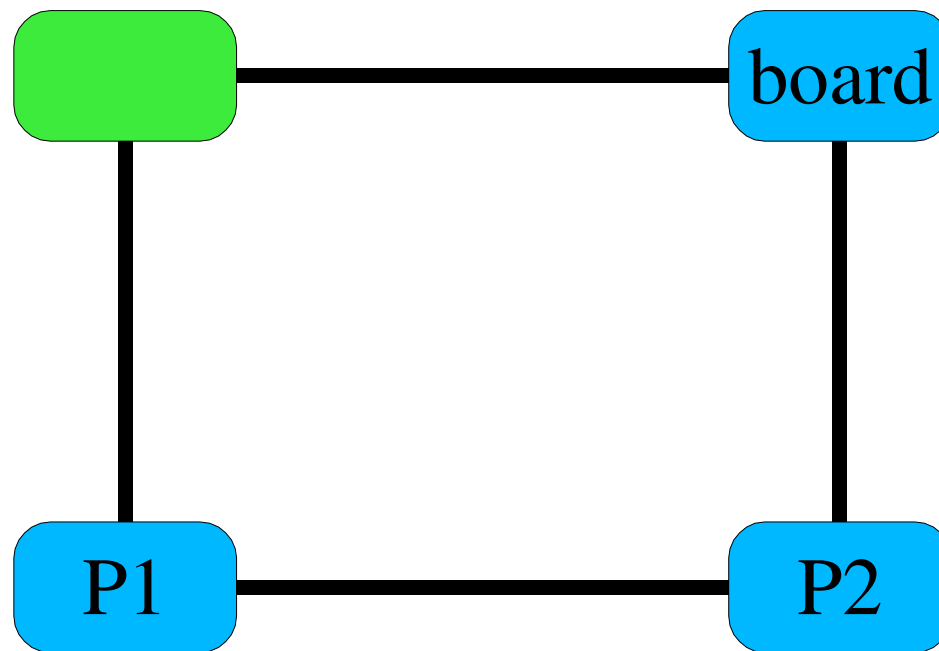
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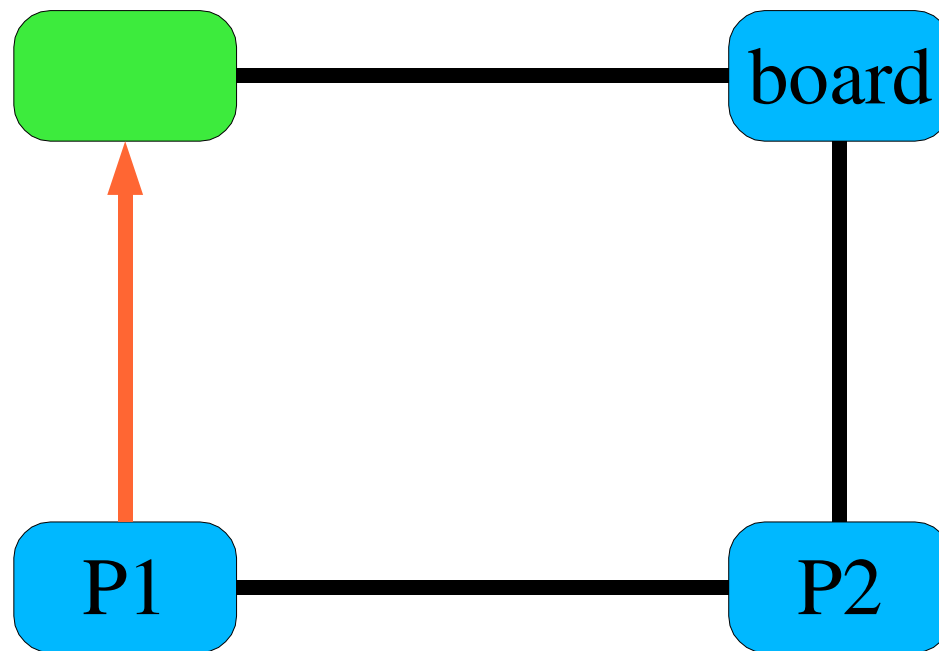
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- It says “Squirrel Cage” - *how???*

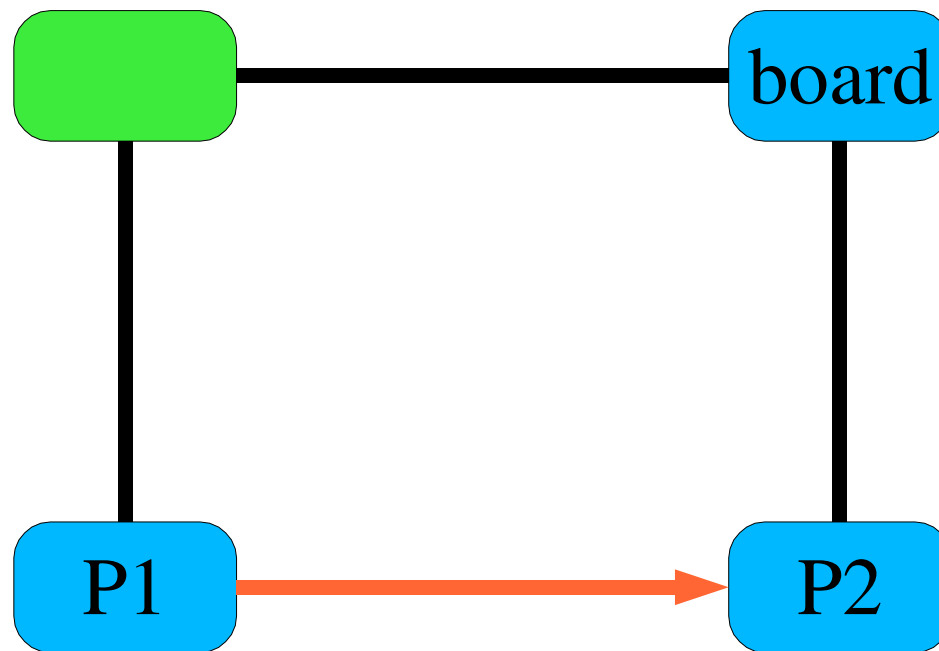
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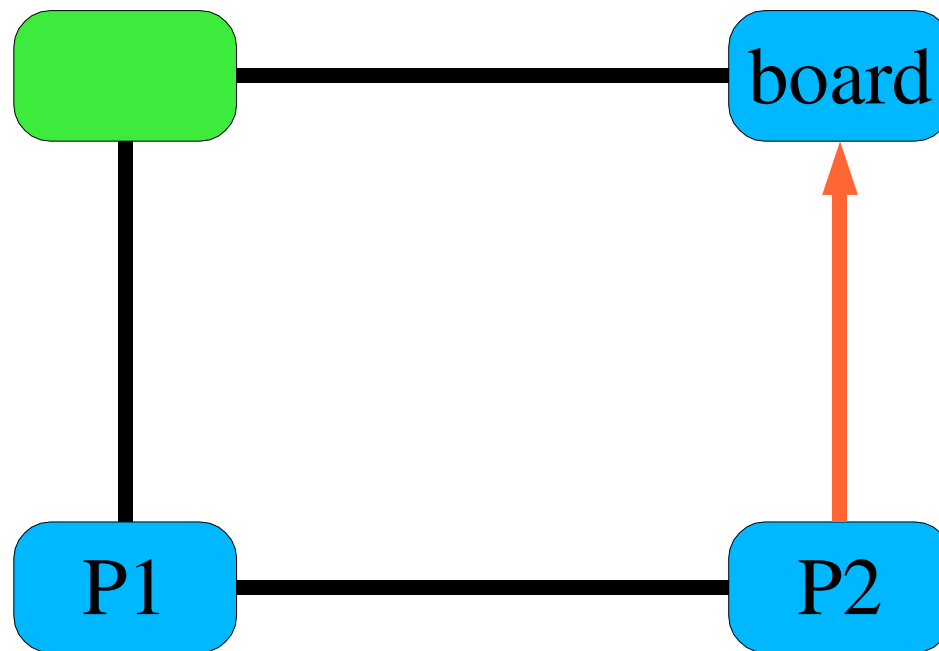
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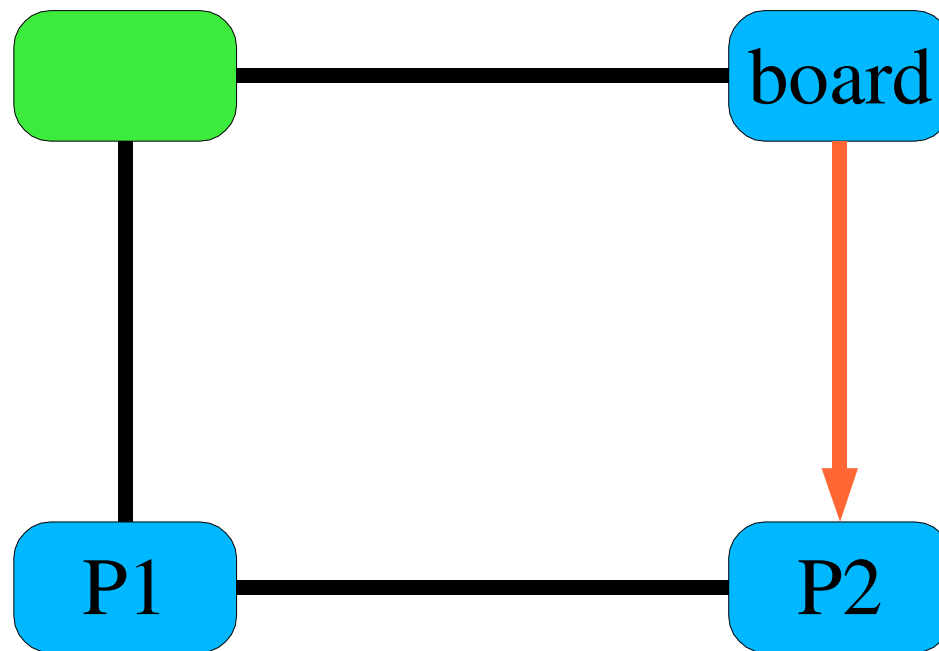
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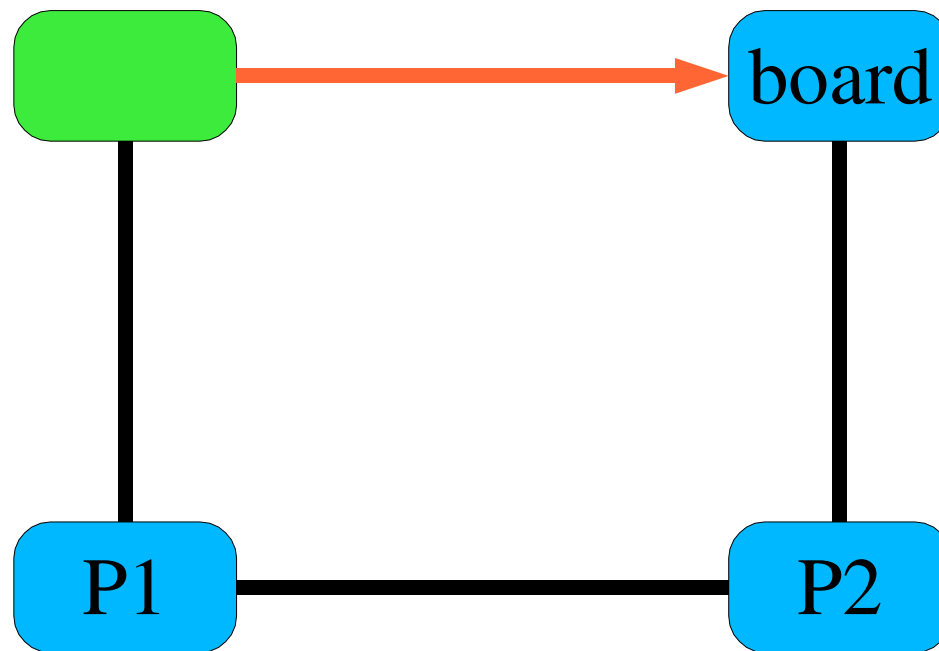


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# What went wrong?

- P1 thought
  - Blackboard update *happened before* invitation
- P2 thought
  - Invitation *happened before* blackboard update
- When does an event “happen”?
  - When its effects propagate “everywhere relevant”
- What does “happen before” mean?
- Could that green node really be so slow?

# Universe Model

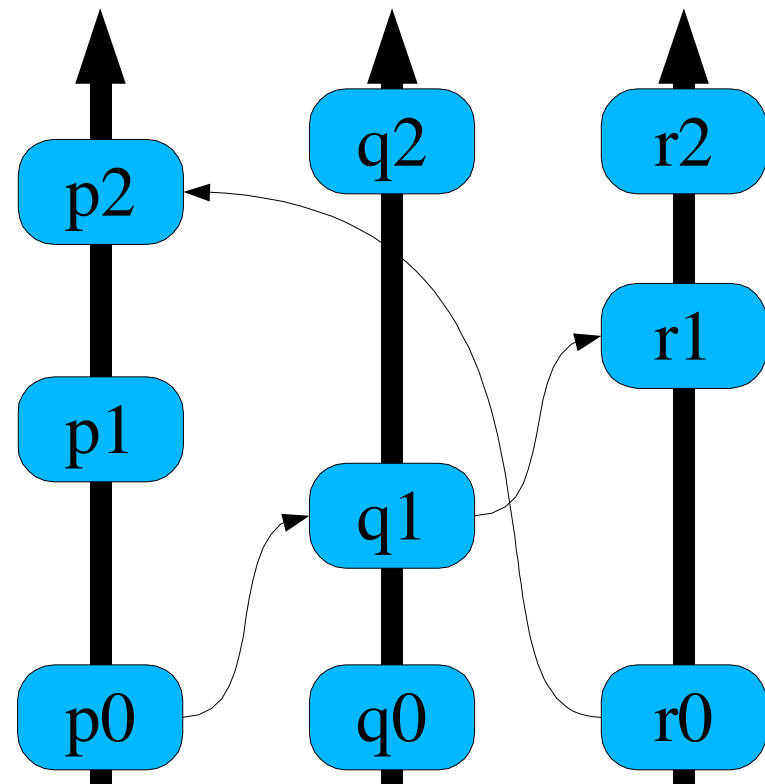
- System = set of processes
- Process = sequence of events
- Event
  - Internal: `++x`;
  - Message transmission
  - Message reception

# “Happened before” partial order

- A *happens before* B ( $A \rightarrow B$ )
  - If A and B happen inside a process, in (A, B) order
  - If A = transmission, B = reception, of same message
  - If  $A \rightarrow B$  and  $B \rightarrow C$ , then  $A \rightarrow C$
- A and B are *concurrent* when
  - $A \nrightarrow B$  and  $B \nrightarrow A$
- Observe:  $A \nrightarrow A$

# Space-time Diagram

- $\rightarrow$ 
  - inside a process, or
  - follow a message
- $p0 \rightarrow r2$
- concurrent
  - $p0, q0, r0$
  - $p1, q1$
  - $q1, r0$
  - $p1, r0$



→ means “possibly causes”

- $p_0$  possibly causes  $p_1$ 
  - ...by storing something in P's memory
- $p_0$  possibly causes  $q_1$ 
  - Message could trigger  $q_1$
- Concurrent events
  - ...cannot cause each other

# Logical clocks

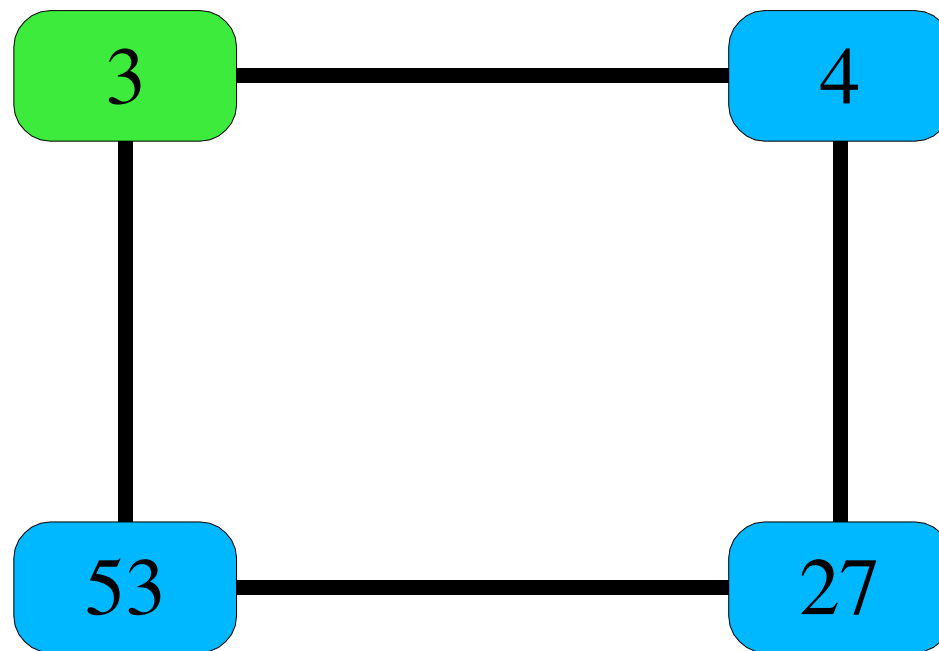
- Can we assign timestamps to events?
- Want
  - If  $A \rightarrow B$  then  $C(A) < C(B)$
- Events inside  $P_i$ 
  - $a \rightarrow b \Rightarrow C_i(a) < C_i(b)$
- Message from  $P_i$  to  $P_j$ 
  - $a=P_i$ 's send,  $b=P_j$ 's receive  $\Rightarrow C_i(a) < C_j(b)$

# Logical clocks

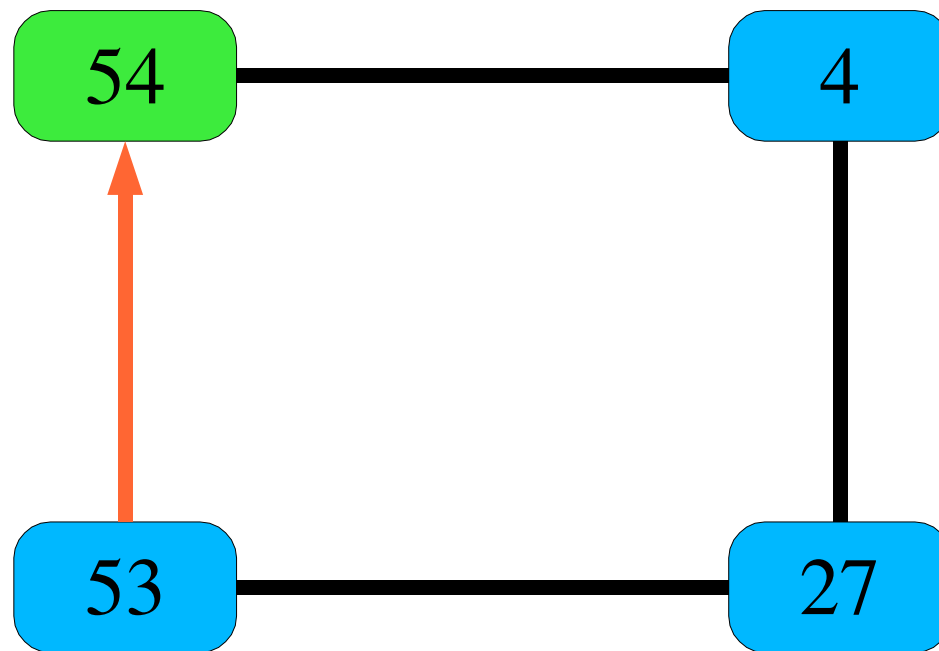
- Events inside  $P_i$ 
  - Increment  $C_i()$  between successive events
- Message from  $P_i$  to  $P_j$ 
  - Sender: place *timestamp*  $T$  in message:  $C_i(\text{send})$
  - Receiver: ensure  $C_j(\text{receive}) > T$



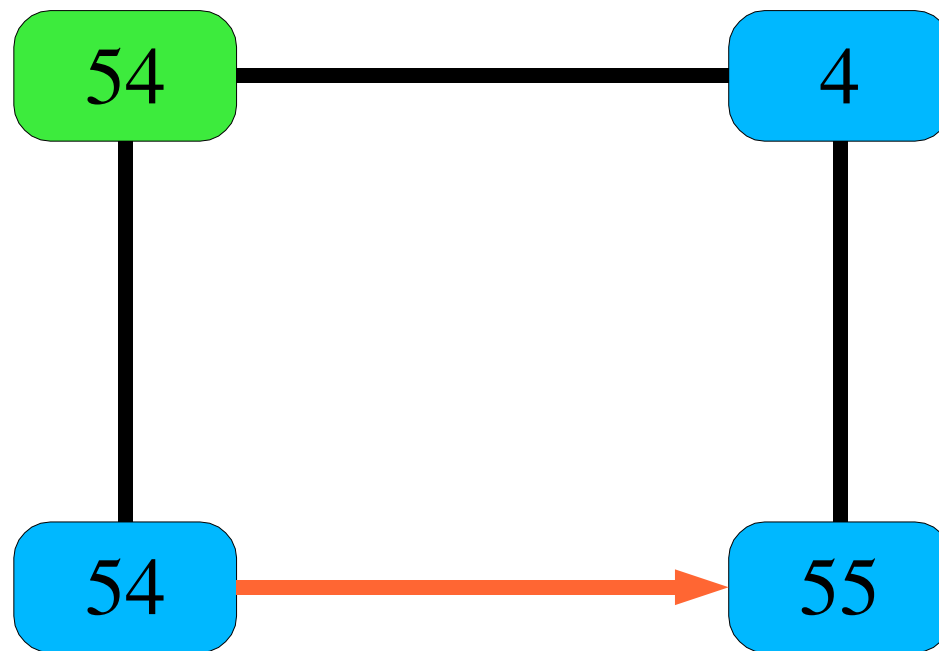
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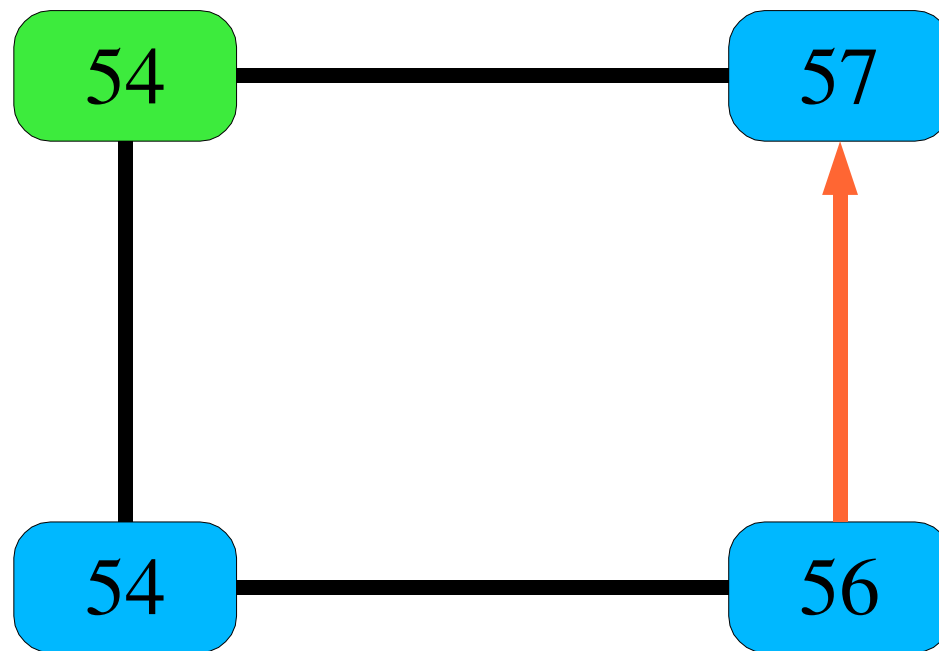
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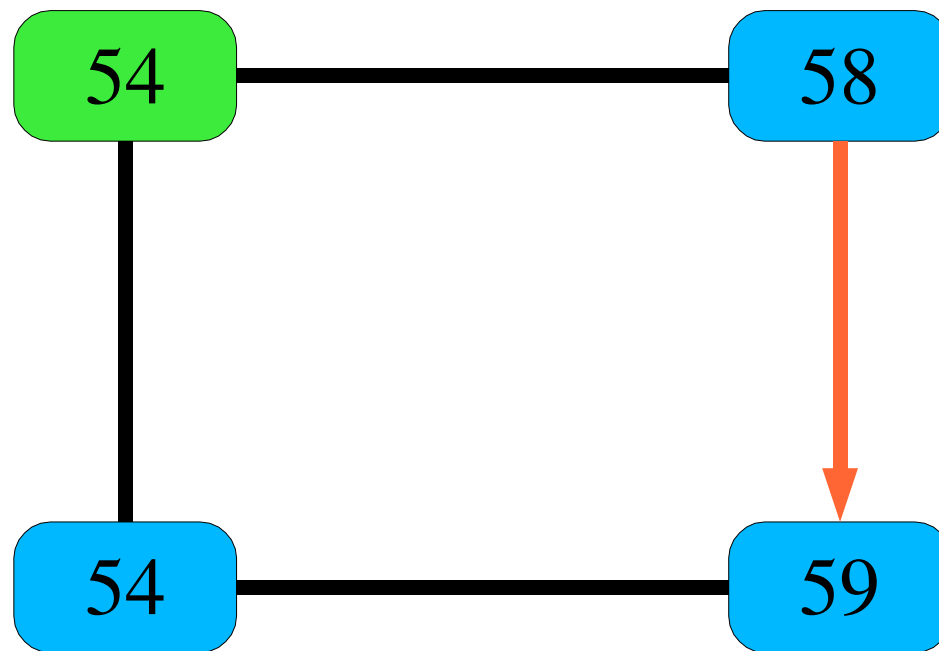
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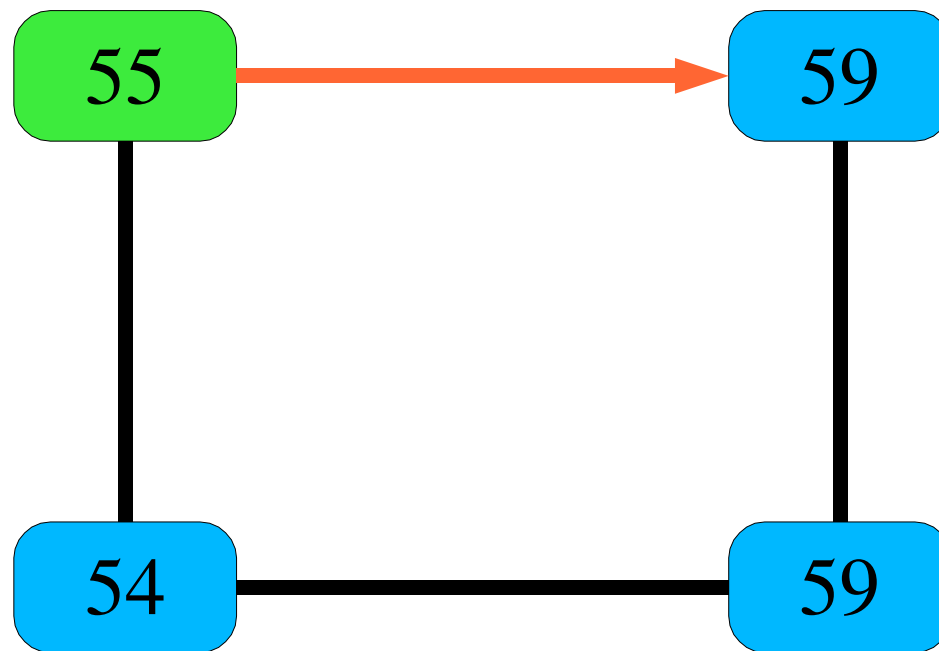
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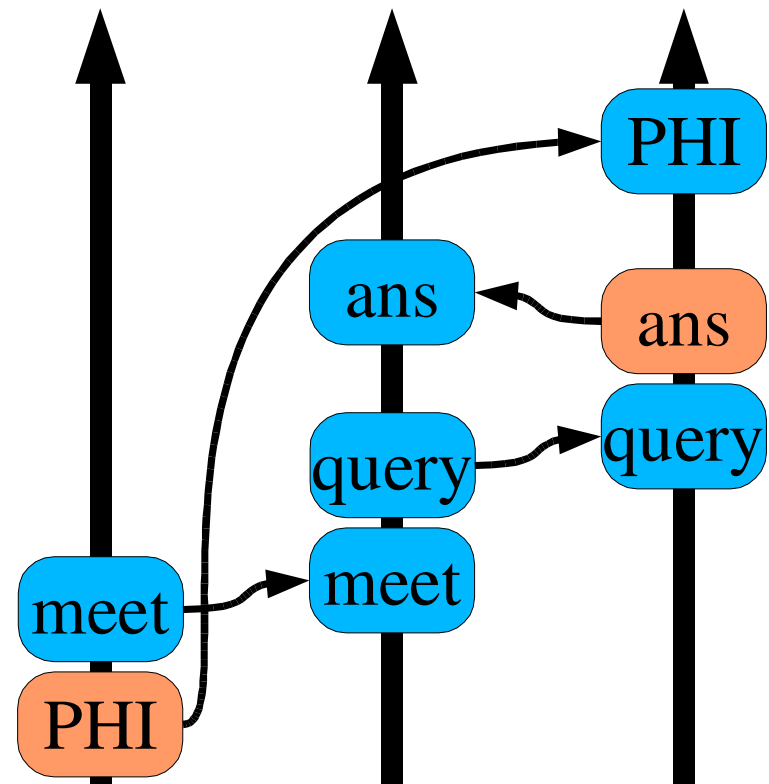


# What this means

- P1 wants
  - <“PHI” written> *happened before* <read by P2>
- Equivalent to “59 < 57” (oops)
- The events were *concurrent*
- “PHI” *could not cause* P2's bar trip

# Space-time Diagram

- P1 wants
  - <“PHI” declared>  
*happened before* <P2 decided>
- Equivalent to “59 < 57” (oops)
- The events were *concurrent*
- “PHI” *could not cause* P2's bar trip





# Fixing the problem

- P1 should wait for board to acknowledge
- “PHI” causes ACK
- ACK causes “Meet me at...”
- “Meet me at...” causes bar trip
- Then: “PHI” causes bar trip

# Extensions

- Define *total ordering* of system events
  - Typical (timestamp, process #) tuple comparison
    - Process # used to break timestamp ties
- Distributed agreement algorithms
  - Such as “*fair* distributed mutual exclusion”
    - Requests must be granted “in order”
    - See text: 17.2
- Adding physical (real-time) clocks

# Summary

- Light cones
- “Happened before” partial order
- Potential causality
- Another definition of concurrency
  - You've dealt with single-clock race conditions
    - (one memory bus provides one global clock)
  - In distributed systems there is no global clock
- Timestamps track message causality