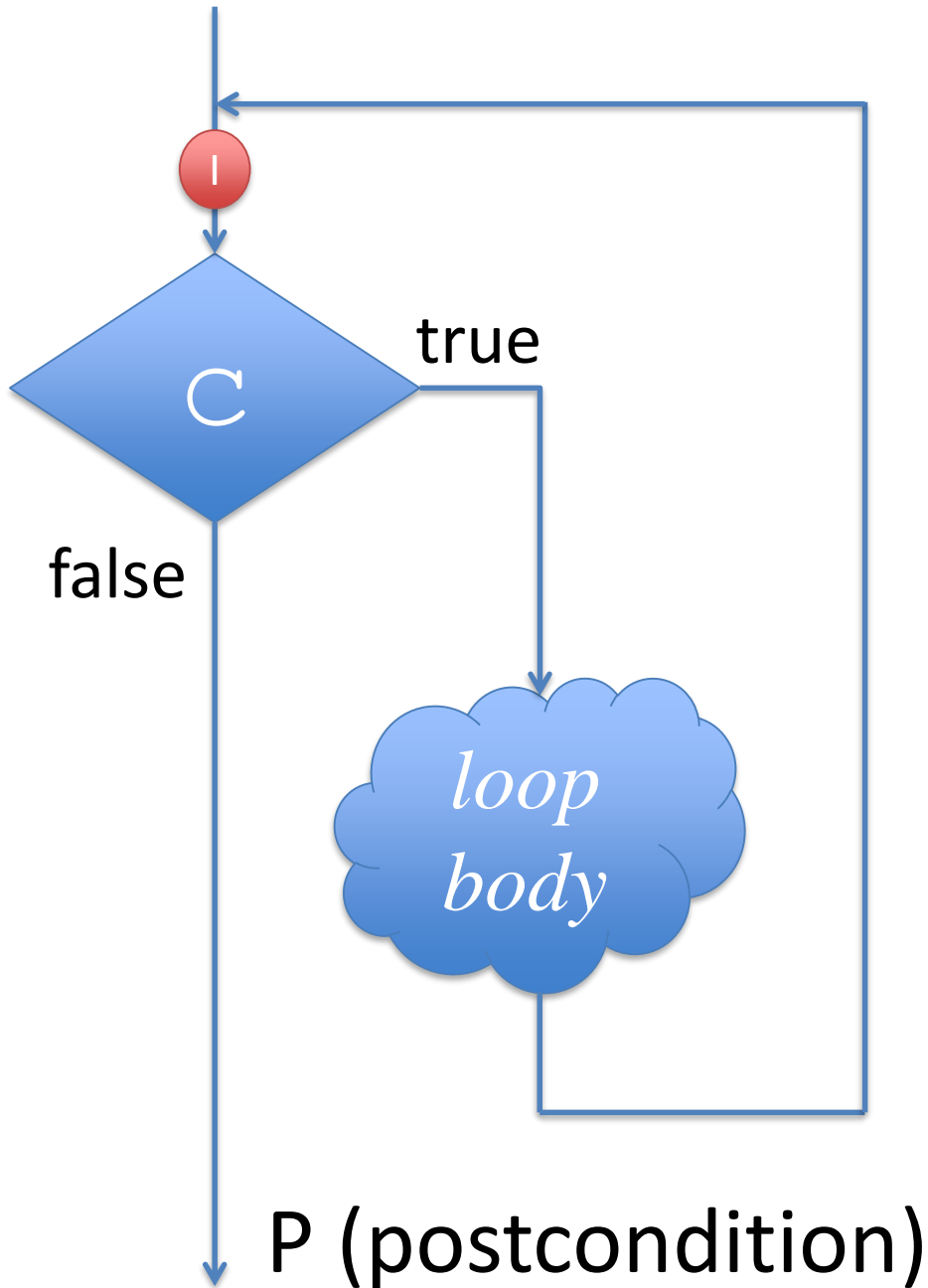


```
while (c) {  
    loop body  
}
```

Loop Invariant

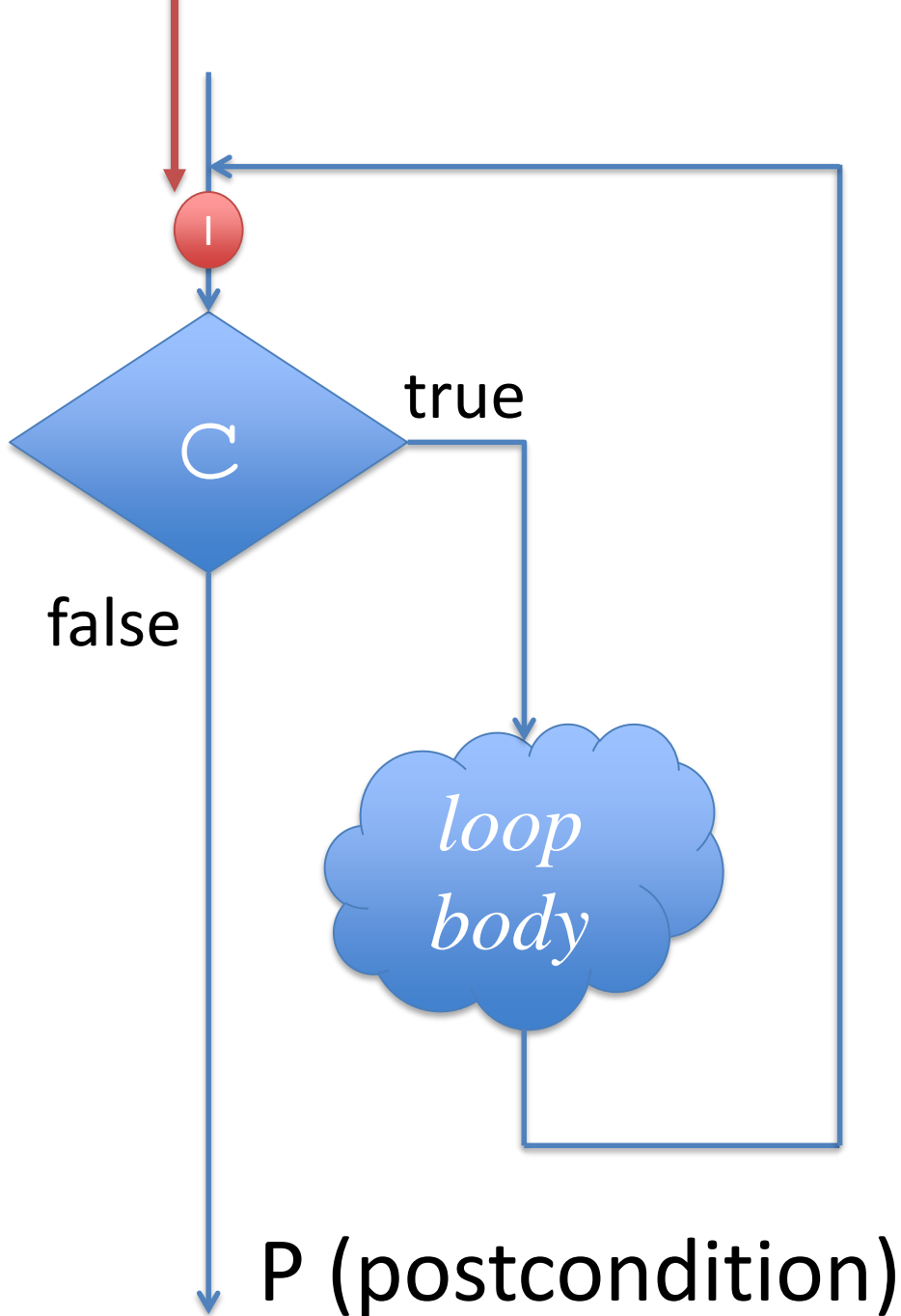
- Def'n: A boolean condition that is checked *immediately before every evaluation of the loop guard*.



```
while (c)
//@loop_invariant I;
{
    loop body
}
//@assert P;
```

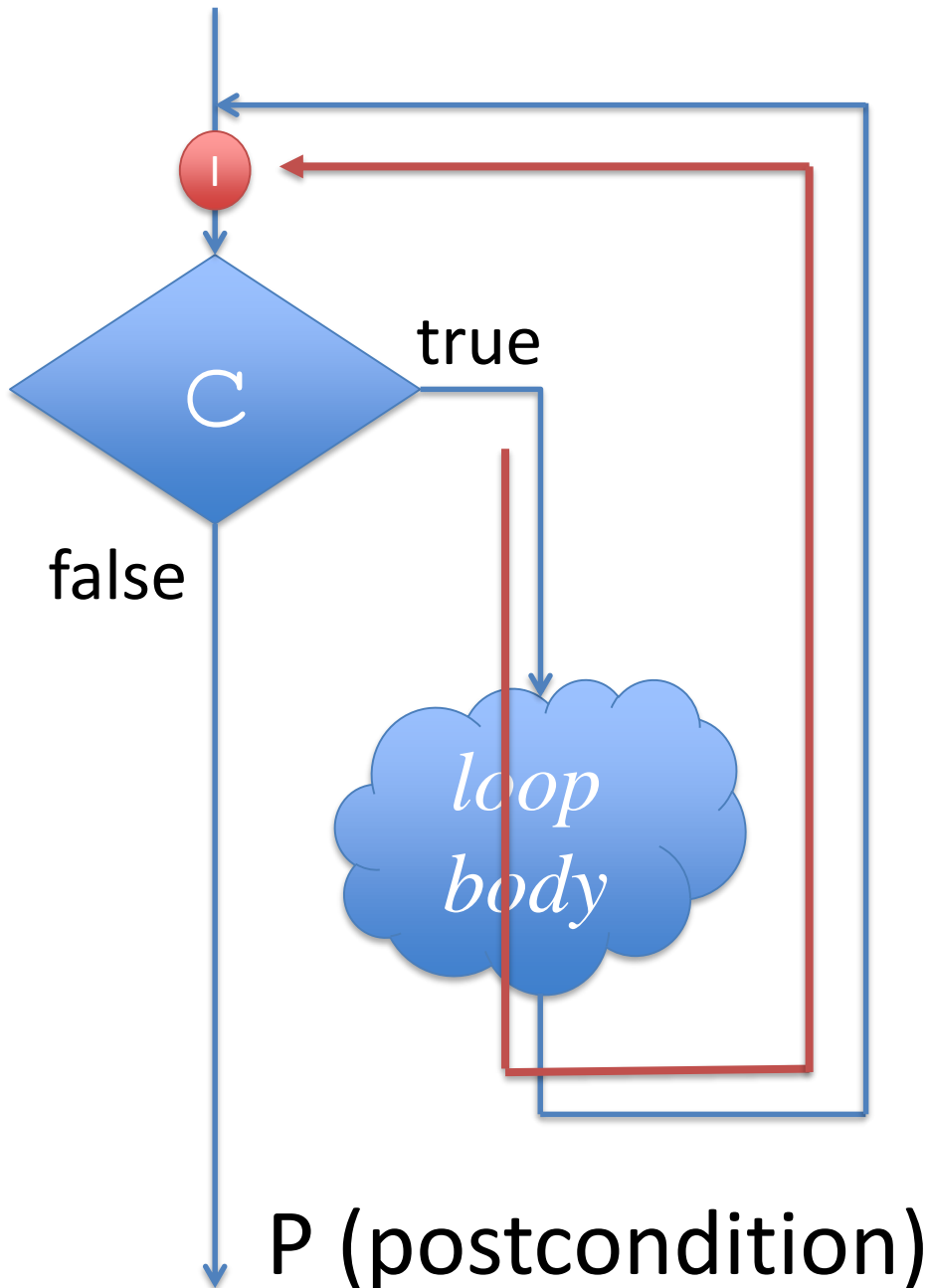
Loop Invariant

- Def'n: A boolean condition that is checked *immediately before every evaluation of the loop guard*.
- It is true even if the loop runs 0 times (i.e. is skipped).
- It is true immediately before each evaluation of the loop guard, including the last evaluation if the loop terminates.
- It is true immediately after the loop terminates, if the loop terminates.



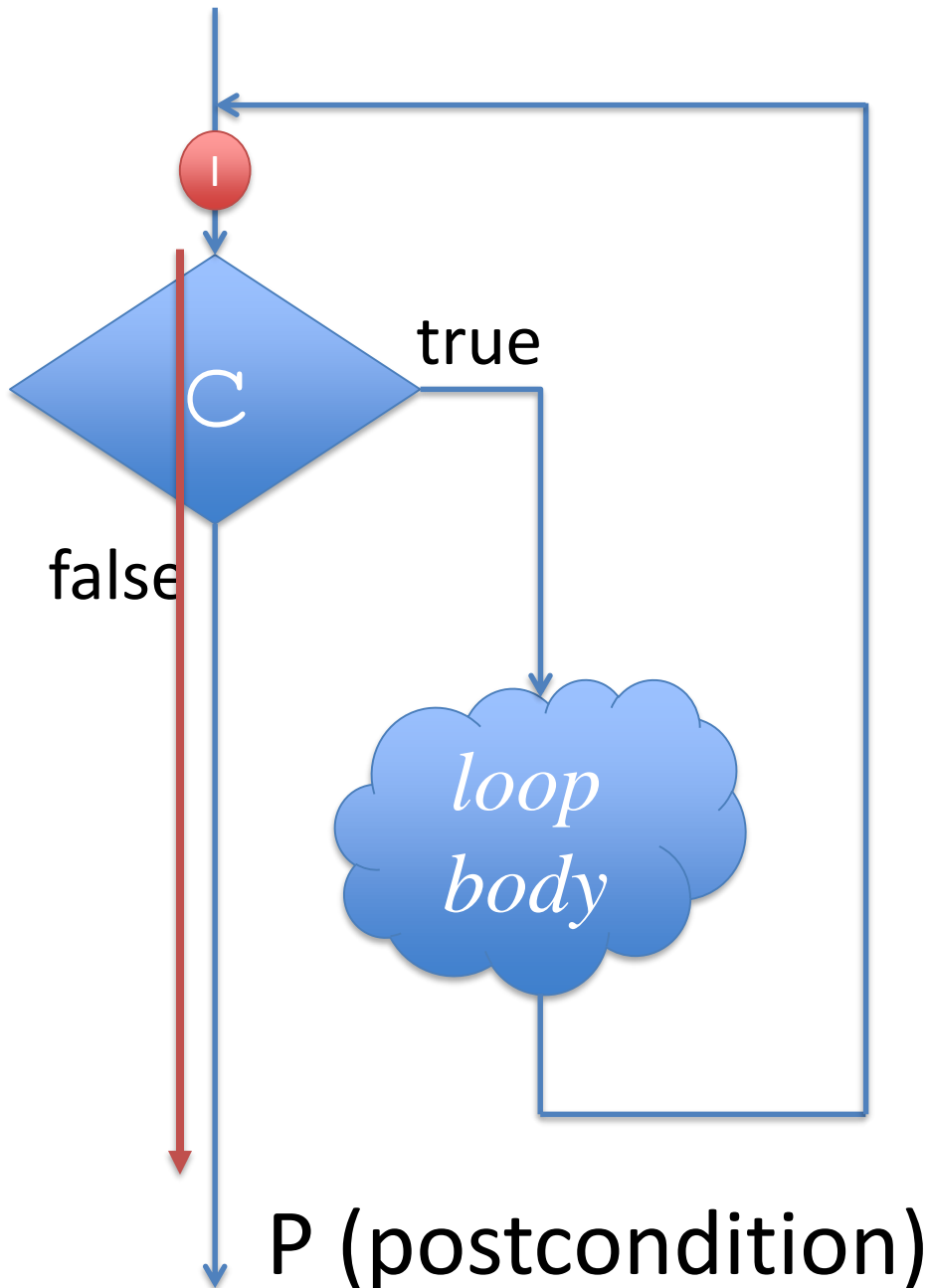
1. INIT

Show that the loop invariant **I** is true immediately before the first evaluation of the loop guard **C**.



2. PRESERVATION

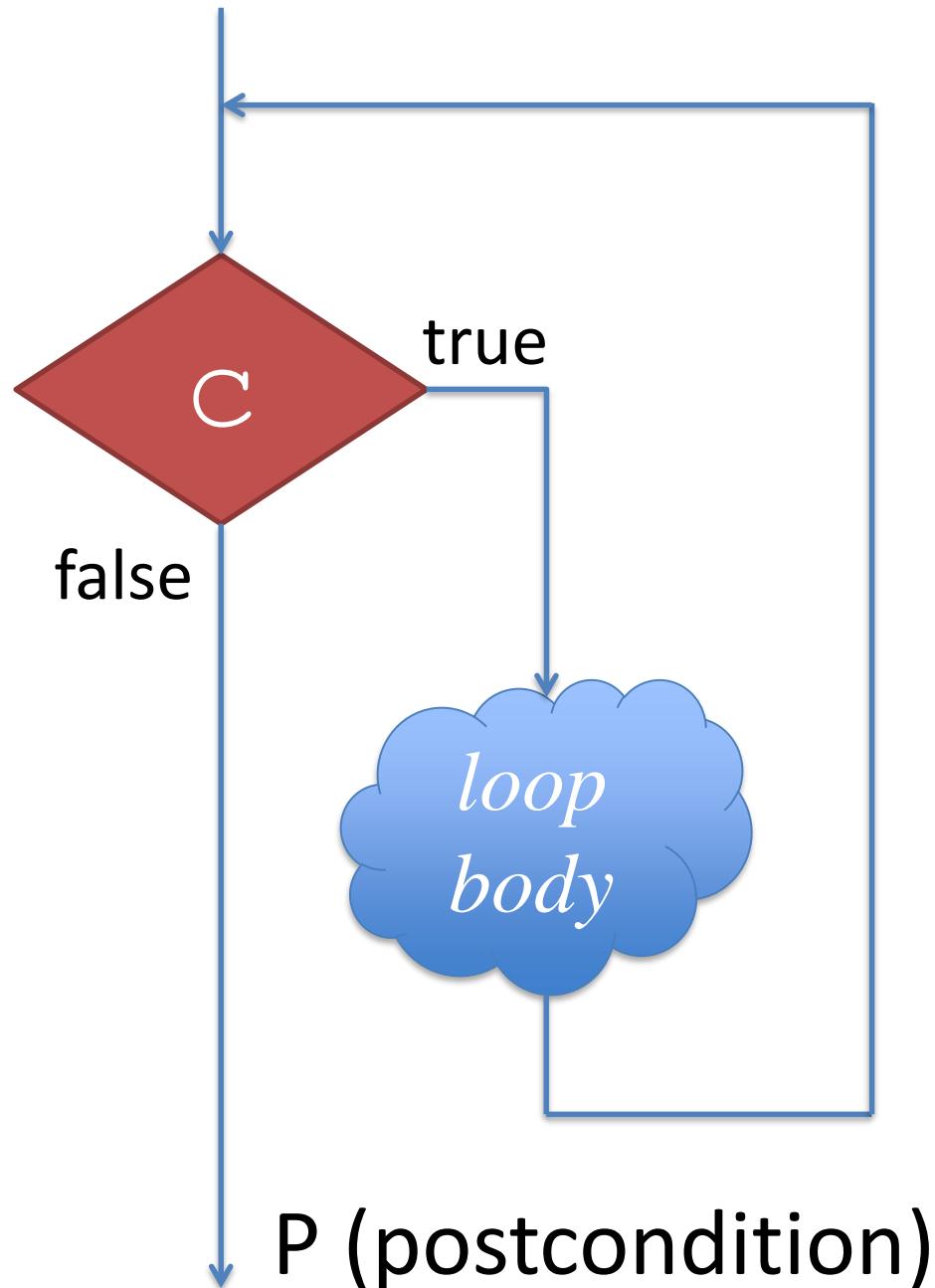
Show that if the loop invariant I is true immediately before the evaluation of the loop guard C , then I is true immediately before the next evaluation of the loop guard C .



3. EXIT

Once we have a valid loop invariant, we can show that the logical conjunction of the loop invariant **I** and the negation of the loop guard **C** implies the desired postcondition **P**:

$$I \wedge \sim C \rightarrow P$$



4. **TERMINATION**

Show that the loop will always terminate (i.e. that **C** must eventually be false).