Data Representation

15-110 – Monday 01/24

Announcements

- Eberly Center Study
- Week 2: online as well
- Check1 was due at noon today. If you forgot to turn it in, you can still submit up until the revision deadline!
 - We'll get feedback released on Tuesday

Learning Objectives

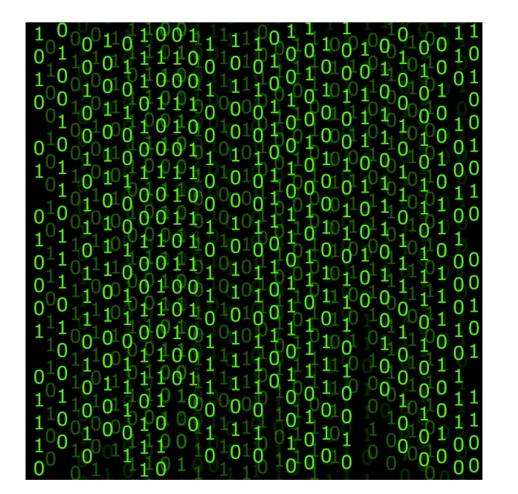
- Understand how different number systems can represent the same information
- Translate **binary numbers** to decimal, and vice versa
- Interpret binary numbers as abstracted types, including colors and text

Number Systems

Computers Run on Os and 1s

Computers represent everything by using 0s and 1s. You've likely seen references to this before.

How can we represent text, or images, or sound with 0s and 1s? This brings us back to **abstraction**.



Abstraction is About Representation

Recall our definition of abstraction from the first lecture:

Abstraction is a technique used to make complex systems manageable by changing the amount of detail used to **represent** or interact with the system.

We'll use abstraction to translate 0s and 1s to decimal numbers, then translate those numbers to other types.

Number Systems – Coins

A **number system** is a way of representing numbers using symbols.

One example of a number system is currency. In the US currency system, how much is each of the following symbols worth?



Number Systems – Dollars

Alternatively, we can represent money using **dollars and cents**, in decimal form.

For example, a medium coffee at Tazza is **\$2.65**.



Converting Coins to Dollars

We can **convert between number systems** by translating a value from one system to the other.

For example, the coins on the left represent the same value as \$0.87

Using pictures is clunky. Let's make a new representation system for coins.



Coin Number Representation

To represent coins, we'll make a number with four digits.

The first represents quarters, the second dimes, the third nickels, and the fourth pennies.

c.3.1.0.2 =

3*\$0.25 + 1*\$0.10 + 0*\$0.05 + 2*\$0.01 =



LIBERT

Converting Dollars to Coins

In recitation, you created an algorithm to convert money from dollars to coins, minimizing the number of coins used.

How did your algorithm work?

Conversion Example

What is \$0.59 in coin representation?

0.59 = 2*0.25 + 0*0.10 + 1*0.05 + 4*0.01 = c.2.0.1.4

Activity: Coin Conversion

You do: Now try the following calculations:

What is c.1.1.1.2 in dollars?

What is \$0.61 in coin representation?

Number Systems - Decimal

When we work with ordinary numbers outside of any specific context, we usually use the **decimal** number system.

Moving from the right, the first digit is the number of 1s, the second is 10s, the third is 100s, etc. Each digit represents a **power of 10**. For example, 1980 in decimal is 1 * 1000 + 9 * 100 + 8 * 10 + 0 * 1

But this isn't the only abstract number system we can use!

^{10³} 1000	10²100	¹⁰¹ 10	^{10°} 1
1	9	8	0

Number Systems – Binary

We can represent numbers using only 0s and 1s with the **binary number system**.

Instead of counting the number of 1s, 5s, 10s, and 25s in coins, or 1s, 10s, 100s, and 1000s in abstract amounts, count the number of 1s, 2s, 4s, and 8s. For example, 1101 in binary is 1 * 8 + 1 * 4 + 0 * 2 + 1 * 1.

Why these numbers? They're **powers of 2**. This is a number in **base 2**, which only needs the digits 0 and 1.

^{2³} 8	^{2²} 4	²¹ 2	²⁰ 1
1	1	0	1

Bits and Bytes

When working with binary and computers, we often refer to a set of binary values used together to represent a number.

A single binary value is called a **bit**.

A set of 8 bits is called a **byte**.

We commonly use some number of **bytes** to represent data values.

Counting in Binary

0 =	128	64	32	16	8	4	2	1	1 –	128	64	32	16	8	4	2	1
0 –	0	0	0	0	0	0	0	0	т —	0	0	0	0	0	0	0	1
2 =	128	64	32	16	8	4	2	1	3 =	128	64	32	16	8	4	2	1
2 -	0	0	0	0	0	0	1	0	5 =	0	0	0	0	0	0	1	1
Λ_	128	64	32	16	8	4	2	1	F _	128	64	32	16	8	4	2	1
4 =	0	0	0	0	0	1	0	0	5 =	0	0	0	0	0	1	0	1
C	128	64	32	16	8	4	2	1	7	128	64	32	16	8	4	2	1
6 =	0	0	0	0	0	1	1	0	/ =	0	0	0	0	0	1	1	1

Converting Binary to Decimal

To convert a binary number to decimal, just add each power of 2 that is represented by a 1.

For example, 00011000 = 16 + 8 = 24

128	64	32	16	8	4	2	1
0	0	0	1	1	0	0	0

Another example:

10010001 = 128 + 16 + 1 = 145

128	64	32	16	8	4	2	1
1	0	0	1	0	0	0	1

Converting Decimal to Binary

Converting decimal to binary uses the **same process** as converting dollars to coins.

Look for the largest power of 2 that can fit in the number and subtract it from the number. Repeat with the next power of 2, etc., until you reach 0.

For example, 36 = 32 + 4 = 00100100

Another example:

103 = 64 + 32 + 4 + 2 + 1

128	64	32	16	8	4	2	1
0	0	1	0	0	1	0	0

128	64	32	16	8	4	2	1
0	1	1	0	0	1	1	1

Activity: Converting Binary

You do: Now try converting numbers on your own.

First: what is **01011011** in decimal?

Second: what is **75** in binary?

Abstracted Types

Binary and Abstraction

Now that we can represent numbers using binary, we can represent **everything** computers store using binary.

We just need to use **abstraction** to interpret bits or numbers in particular ways.

Let's consider dates, images, and text.

Discussion: Representing Dates

It can be helpful to think logically about how to represent a value before learning how it's done in practice. Let's do that now.

Discuss: We can convert binary directly into numbers, but how do we represent dates (i.e., 01/24/2022)?

Answer: Representing Dates

Simple Approach: reserve 4 bits to represent the month, 5 bits to represent the date and 12 bits to represent the year. Convert the month, day, year normally from decimal to binary.

Actual Approach: count seconds from a certain date (00:00:00 of 01/01/1970) and convert the number of seconds to binary. Any dates before this date would be negative numbers, and any dates after would be positive numbers!

We use 32 bits to represent each date; the first bit is used to indicate if the number was positive (0) or negative (1), and the remaining 31 bits are used to represent the number of seconds elapsed. Thus, we **restrict the number of bits** to represent the date to 31 bits.

More on dates: https://busyintelligence.blog/2019/05/22/how-does-a-computer-store-data-dates/

Represent Images as Grids of Colors

What if we want to represent an image? How can we convert that to numbers?

First, break the image down into a grid of colors, where each square of color has a distinct hue. A square of color in this context is called a **pixel**.

If we can represent a pixel in binary, we can interpret a series of pixels as an image.



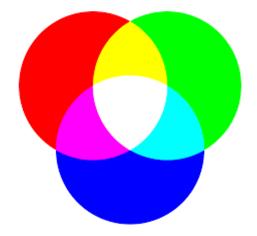
Representing Colors in Binary

We need to represent a single color (a pixel) as a number.

There are a few ways to do this, but we'll focus on **RGB**. Any color can be represented as a combination of Red, Green, and Blue.

Red, green, and blue intensity can be represented using one **byte** each, where 00000000 (0) is none and 11111111 (255) is very intense. Each pixel will therefore require 3 bytes to encode.

Try it out here: <u>w3schools.com/colors/colors_rgb.asp</u>



Example: Representing Beige

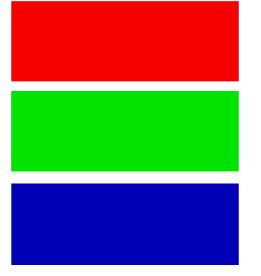
To make the campus-building beige, we'd need:

Red = 249 = 11111001

Green= 228 = 11100100

Blue = 183 = 10110111

Which makes beige!





Represent Text as Individual Characters

Next, how do we represent text?

First, we break it down into smaller parts, like with images. In this case, we can break text down into individual **characters**.

For example, the text "Hello World" becomes H, e, l, l, o, space, W, o, r, l, d

Use a Lookup Table to Convert Characters

Unlike colors, characters don't have a natural connection to numbers.

Instead, we can use a **lookup table** that maps each possible character to an integer.

As long as every computer uses the same lookup table, computers can always translate a set of numbers into the same set of characters.

ASCII is a Simple Lookup Table

For basic characters, we can use the encoding system called ASCII. This maps the numbers 0 to 255 to characters. Therefore, one character is represented by one byte.

Check it out here: <u>www.asciitable.com</u>

Dec Hex	Oct	Chr	Dec	Hex	Oct	HTML	Chr	Dec H	lex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr
0 0	000	NULL	32	20	040		Space	64 4	-0	100	@	@	96	60	140	`	`
11	001	Start of Header	33	21	041	!	1	65 4	-1	101	A	Α	97	61	141	a	а
2 2	002	Start of Text	34	22	042	"	п	66 4	-2	102	B	В	98	62	142	b	b
3 3	003	End of Text	35	23	043	#	#	67 4	-3	103	C	С	99	63	143	c	с
4 4	004	End of Transmission	36	24	044	\$	\$	68 4	4	104	D	D	100	64	144	d	d
5 5	005	Enquiry	37	25	045	%	%	69 4	-5	105	E	E	101	65	145	e	е
6 6	006	Acknowledgment	38	26	046	&	&	70 4	6	106	F	F	102	66	146	f	f
7 7		Bell	39	27	047	'	1	71 4	7	107	G	G	103		147	g	g
8 8	010	Backspace	40	28	050	((72 4	8	110	H	н	104	68	150	h	h
9 9	011	Horizontal Tab	41	29	051))	73 4	9	111	I	I	105		151	i	i
10 A	012	Line feed	42		052	*	*	74 4	A	112	J	J	106	6A		j	j
11 B		Vertical Tab	43	2B	053	+	+	75 4	В	113	K	K	107		153	k	k
12 C	014	Form feed	44	2C	054	,	7	76 4	C	114	L	L	108	6C	154	l	1
13 D	015	Carriage return		2D	055	-	-	77 4	Đ	115	M	Μ	109	6D	155	m	m
14 E	016	Shift Out	46	2E	056	.		78 4	-Е	116	N	Ν	110	6E	156	n	n
15 F		Shift In	47		057	/	/	79 4		117	O	0	111		157	o	ο
16 10	020	Data Link Escape	48	30		0	0	80 5	50	120	P	Р	112	70	160	p	р
17 11	021	Device Control 1	49			1	1	81 5			Q	Q	113			q	q
18 12	022	Device Control 2	50			2	2	82 5			R	R	114		162	r	r
19 13	023	Device Control 3	51			3	3	83 5			S	S	115		163	s	S
20 14		Device Control 4	52			4	4	84 5		124	T	Т	116		164	t	t
21 15		Negative Ack.	53	35	065	5	5	85 5	55	125	U	U	117	75	165	u	u
22 16	026	Synchronous idle	54	36	066	6	6	86 5	6	126	V	V	118		166	v	V
23 17		End of Trans. Block	55			7	7	87 5			W	W	119			w	W
24 18	030	Cancel	56		070	8	8	88 5		130	X	Х	120		170	x	х
25 19	031	End of Medium	57	39		9	9	89 5	59	131	Y	Y	121		171	y	у
26 1A	032	Substitute	58	3A		:	:	90 5	ĀΑ	132	Z	Z	122	7A	172	z	Z
27 1B	033	Escape	59			;	;	91 5		133	[[123		173	{	{
28 1C	034	File Separator		3C	074	<	<	92 5		134	\	\	124		174		
29 1D		Group Separator		3D		=	=	93 5]]	125			}	}
30 1E		Record Separator	62			>	>	94 5			^	^	126			~	~
31 1F	037	Unit Separator	63	3F	077	?	?	95 5	FΓ	137	_	_	127	7F	177		Del

asciichars.com

Translating Text to Numbers

"Yay" = 01011001 -> 89 01100001 -> 97 01111001 -> 121

Dec Hex	Oct Chr	Dec Hex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr	Dec	Hex	Oct	HTML	Chr
0 0	000 NULL	32 20	040		Space	64	40	100	@	@	96	60	140	`	•
1 1	001 Start of Header	33 21	041	!	1	65	41	101	A	Α	97	61	141	a	a
2 2	002 Start of Text	34 22	042	"	п	66	42	102	B	В	98	62	142	b	b
3 3	003 End of Text	35 23	043	#	#	67	43	103	C	С	99	63	143	c	с
4 4	004 End of Transmission	36 24	044	\$	\$	68	44	104	D	D	100	64	144	d	d
5 5	005 Enquiry	37 25	045	%	%	69	45	105	E	E	101	65	145	e	е
6 6	006 Acknowledgment	38 26	046	&	&	70	46	106	F	F	102	66	146	f	f
7 7	007 Bell	39 27		'	1	71		107	G	G	103	67	147	g	g
8 8	010 Backspace	40 28	050	((72		110	H	Н	104		150	h	h
9 9	011 Horizontal Tab	41 29	051))	73	49		I	I	105		151	i	i
10 A	012 Line feed	42 2A	052	*	*	74			J	J	106		152	j	j
11 B	013 Vertical Tab	43 2B		+	+	75				К	107			k	k
12 C	014 Form feed	44 2C		,	,	76			L	L	108			l	
13 D	015 Carriage return	45 2D		-	-	77			M	Μ	109			m	m
14 E	016 Shift Out	46 2E		.		78			N	N	110		156	n	n
15 F	017 Shift In	47 2F		/	/	79			O	0	111			o	0
16 10	020 Data Link Escape	48 30		0	0	80			P	Р	112			p	р
17 11	021 Device Control 1	49 31		1	1	81		121	Q	Q	113			q	q
18 12	022 Device Control 2	50 32	062	2	2	82			R	R	114			r	r
19 13	023 Device Control 3	51 33		3	3	83			S	S	115			s	S
20 14	024 Device Control 4	52 34		4	4	84			T	Т	116			t	t
21 15	025 Negative Ack.	53 35		5	5	85			U	U	117			,	u
22 16	026 Synchronous idle	54 36		6	6	86			V	V	118			v	V
23 17	027 End of Trans. Block	55 37		7	7	87			W	W	119			w	W
24 18	030 Cancel	56 38		8	8	88			X	Х	120			x	х
25 19	031 End of Medium	57 39		9	9	89			Y	Υ	121			y	У
26 1A	032 Substitute	58 3A		:	:	90			Z	Z	122			z	Z
27 1B	033 Escape	59 3B		;	;	91			[[123			{	{
28 1C	034 File Separator	60 3C		<	<	92			\	1	124				
29 1D	035 Group Separator	61 3D		=	=	93]]	125			}	}
30 1E	036 Record Separator	62 3E		>	>	94			^	^	126			~	~
31 1F	037 Unit Separator	63 3F	077	?	?	95	5F	137	_	_	127	7F	177		Del

asciichars.com

For More Characters, Use Unicode

There are plenty of characters that aren't available in ASCII (characters from non-English languages, advanced symbols, emoji...) due to the limited size.

The Unicode system represents every character that can be typed into a computer. It uses up to 5 bytes, which can represent up to 1 trillion characters! Find all the Unicode characters here: <u>www.unicode-table.com</u>

The Unicode system is also **actively under development**. The Unicode Consortium regularly updates the standard to add new types of characters and emoji.

Discuss: what are the potential repercussions of using a single standard for all text on computers?

Learning Objectives

- Understand how different **number systems** can represent the same information
- Translate **binary numbers** to decimal, and vice versa
- Interpret binary numbers as abstracted types, including **colors** and **text**

Feedback form: <u>https://bit.ly/110-s22-feedback</u>

Bonus Slides

Computer Memory is Stored as Binary

Your computer keeps track of saved data and all the information it needs to run in its **memory**, which is represented as binary. You can think about your computer's memory as a really long list of bits, where each bit can be set to 0 or 1. But usually we think in terms of bytes, groups of 8 bits.

Every byte in your computer has an **address**, which the computer uses to look up its value.

	49	53	49	49	48	75	101	108	198	121	77	97	114	103	97	114	101	116	
• • •	<u></u>	1000	Addre	esses	1	1004			1	1008			1	1012			1	1016	•

Binary Values Depend on Interpretation

When you open a file on your computer, the application goes to the appropriate address, reads the associated binary, and **interprets** the binary values based on the file encoding it expects. That interpretation depends on the **application** you use when opening the file, and the **filetype**.

You can attempt to open **any file** using **any program**, if you convince your computer to let you try. Some programs may crash, and others will show nonsense because the binary isn't being interpreted correctly.

Example: try changing a .docx filetype to .txt, then open it in a plain text editor. .docx files have extra encoding, whereas .txt files use plain ASCII.

We Use Lots of Bytes!

In modern computing, we use a **lot** of bytes to represent information.

Smartphone Memory: 64 gigabytes = 64 **billion** bytes

Google databases: Over 100 million gigabytes = 100 quadrillion bytes!

CMU Wifi: 15 million bytes per second