## The Practice and Promise of Substructural Frameworks

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Logical frameworks are based on the premise that fundamental concepts and constructions in the definition of logics and programming languages should be directly supported in the framework. For LF, these include variable binding, substitution, as well as parametric and hypothetical judgments. Absent are intrinsic notions of state, consumable resource, or concurrency, which appear to be similarly fundamental. Integrating these into logical frameworks has led to the development of substructural frameworks such as LLF (linear) [1], RLF (relevant) [3], OLF (ordered) [7], CLF (concurrent) [13, 2] and HLF (hybrid) [9]. Recent implementations such as Lollimon [4], Celf [10], and HLF [9] have allowed us to gain some experience with using these languages [8, 14, 15, 11, 12].

A promising related specification technique for programming languages is substructural operational semantics (SSOS) [5, 6]. We illustrate this technique and the logical framework features that support it through several sample programming constructs. We also sketch our current approach to analyzing such specifications, which has been the most challenging part in the development of the next generation of logical frameworks.

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