Reminder: Assignments are individual assignments, not done in pairs. The work must be all your own.

You may hand in a handwritten solution or a printout of a typeset solution at the beginning of lecture on Tuesday, October 29. Please read the late policy for written assignments on the course web page. If you decide not to typeset your answers, make sure the text and pictures are legible and clear.
Problem 1: Memory Layout (25 points)

Consider the following C0 source code on the left and the assembly code produced by your compiler on the right. Note that it uses tail-call optimization to avoid a recursive call.

(a) Explain why the compiler assigned variable \( q \) to the register \%rbx.

(b) calloc takes arguments of type size_t, which expands to an unsigned long int and is therefore 64 bits wide, according to the x86-64 ABI. Why is it correct to use movl instructions instead of movq to set the argument registers?

(c) The assembly code does not conform to the x86-64 ABI. Explain why not and provide a correction.

(d) The assembly code contains a further bug. Identify it and provide a correction. Do not be concerned about whether the source program might have a bug; we are only concerned with whether the assembly code correctly matches the source.

(e) We are compiling in production mode, ignoring contracts. The given assembly code relies on OS memory protection in order to signal an error in case the argument to _c0_inc is the null pointer 0. Insert an appropriate check in one place that avoids relying on OS memory protection. You may assume a jump target raise_mem that will raise the appropriate memory exception. Briefly explain the rationale for your choice.
Problem 2: Polymorphism (35 points)

The C0 language provides only a very weak form of polymorphism, essentially using `struct s*` in a library header, where `struct s` has not yet been defined. C provides a more expressive, but inherently unsafe mechanism by allowing pointers of type `void*`. A pointer of this type can reference data of any type. We then use implicit or explicit casts to convert to and from this type. Some discussion and examples can be found in the notes on Lecture 19 in the course on Principles of Imperative Computation. In this problem we explore a safe version of `void*` which may eventually make its way into C1.

Tagging and Untagging Data

The key to making the type `void*` safe is to tag pointers of this type with their actual type. When we cast values of this type to actual types we can then compare tags to make sure the operation is type-safe. We have new tagging and untagging constructs

\[ e ::= \ldots \mid \text{tag}(\tau*, e) \mid \text{untag}(\tau*, e) \]

with the following typing rules

\[ \Gamma \vdash e : \tau* \quad \Gamma \vdash \text{tag}(\tau*, e) : \text{void}* \quad \Gamma \vdash \text{untag}(\tau*, e) : \tau* \]

Tagging is always safe: we can forget that \( e \) references a value of type \( \tau \) and just weaken the type to `void`. Untagging will signal a runtime error if the tag of \( e \) is different from \( \tau* \). For example, if \( p : \text{int}* \) then the expression

\[ \text{untag}(\text{bool}* , \text{tag}(\text{int}* , p)) \]

will type-check, but should yield a runtime error while untagging since `bool* ≠ int*`.

A Safe Implementation

In the safe implementation, a value of type `void*` will always be either null (0), or a pointer to 16 bytes of memory on the heap. The first 8 bytes represent the actual type \( \tau* \), the second 8 represent the actual value of type \( \tau* \), which must be an address. We assume we can calculate \( \text{tprep}(\tau*) = w \), where \( w \) is a 8-byte tag value uniquely representing the type \( \tau* \). The default value for type `void*` is null (0).

(a) Provide the evaluation rules for \( \text{tag}(\tau*, e) \). You should define new rules for the judgments \( H ; \eta \vdash e \downarrow v ; H' \) and \( H ; \eta \vdash e \uparrow \text{exn} \). Your rules do not need to check whether memory is exhausted. You should also describe the evaluation of \( \text{tag}(\tau*, e) \) informally, which will help us assign partial credit in case your rules are not completely correct.

(b) Provide the evaluation rules for \( \text{untag}(\tau*, e) \). This should fail if the tag of \( e \) does not match \( \tau* \), in which case you should raise a tag exception. You should define new rules for the same two judgments as in part (a), and accompany them with an informal description.
(c) Describe code generation for the tag and untag expression forms in the style we used for arrays on page L14.7 of the lecture notes. You may use function calls

\[ t^{64} \leftarrow \text{malloc}(s^{64}) \]

to obtain the address \( t \) of \( s \) bytes of uninitialized memory, and use the jump target \( \text{raise\_tag} \) to signal a tag exception.

**An Unsafe Implementation**

The unsafe implementation should forego tag checking. As a result, we do not need to tag or untag at all, since we trust the programmer that tags would have been correct. In other words, \( \text{tag}(\tau*, e) \) would be like \((\text{void*})e\) in C, and \( \text{untag}(\tau*, e) \) like \((\text{tau*})e\), relevant only at the type-checking phase.

(d) Explain why compiling \( e_1 == e_2 \) for pointers \( e_1 \) and \( e_2 \) to a naive pointer comparison is not always correct in safe mode.

(e) Explain how to compile \( e_1 == e_2 \) in both safe and unsafe modes so that program behavior is the same for both modes (assuming, of course, that the program is indeed safe and will not raise an exception).