

Extending LCS for Biology

The LCS/Edit distance problem is not a "practical" model for comparing DNA or proteins.

Why?

Good example of the simple model failing.

Extending LCS for Biology

The LCS/Edit distance problem is not a "practical" model for comparing DNA or proteins.

- Some amino-acids are "closer" to each others than others (e.g. more likely to mutate among each other, or closer in structural form).
- Some amino-acids have more "information" than others and should contribute more.
- The cost of a deletion (insertion) of length n should not be counted as n times the cost of a deletion (insertion) of length 1.
- Biologist often care about finding "local" alignments instead of a global alignment.

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What we will talk about today

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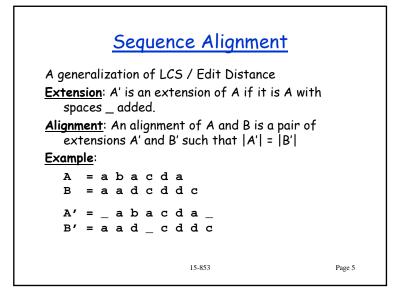
Extensions

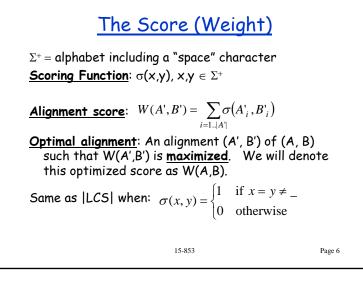
- Sequence Alignment: a generalization of LCS to account for the closeness of different elements
- <u>Gap Models</u>: More sophisticated models for accounting for the cost of adjacent insertions or deletions
- <u>Local Alignment</u>: Finding parts of one sequence in parts of another sequence.

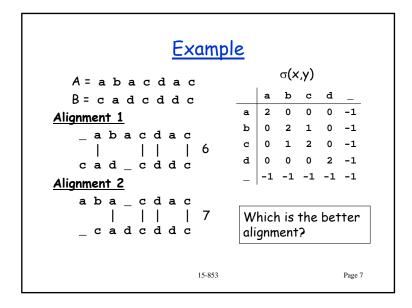
Applications

 <u>FASTA</u> and <u>BLAST</u>: The most common sequence matching tools used in Molecular Biology.

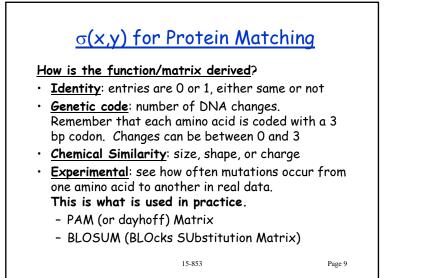
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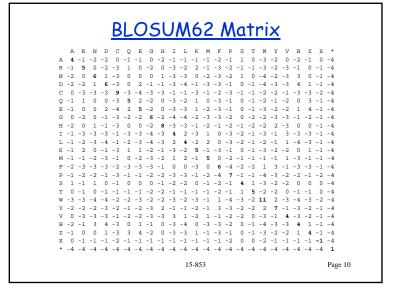




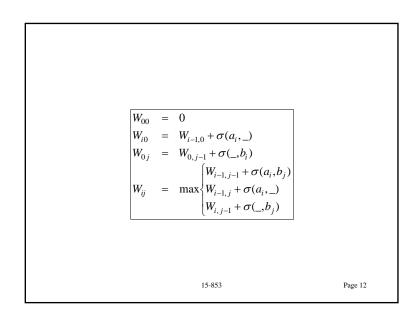


<u>Scores vs. Distances</u>
<u>Maximizing vs. Minimizing.</u>
<u>Scores</u> :
 Can be positive, zero, or negative. We try to maximize scores.
<u>Distances</u> :
 Must be non-negative, and typically we assume they obey the triangle inequality (i.e. they are a metric). We try to minimize distances.
Scores are more flexible, but distances have better mathematical properties. The local alignment method we will use requires scores.
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<u>Optimal Alic</u>	gnn	nent Recursive So	lution
Edit Distance,	froi	<u>m last lecture:</u>	
D(Α, ε)	=	A	
D(ε, Β)	=	B	
D(A:x, B:x)	=	D(A, B)	
D(A:a, B:b)	=	min(1 + D(A:a, B), 1 + D(A, B:b))
<u>The optimal ali</u>	gnm	<u>ent problem:</u>	
W(ε, ε)	=	0	
W(ε, B:b)	=	σ(_, b) + W(ε, B)	
W(A:a, ε)	=	σ (a, _) + W(A , ε)	
W(A:a, B:b)	=	$max(\sigma(a, b) + W(A, B))$	
		σ(_, b) + W(A:a, B),	
		σ(a, _)+ W(A, B:b))	
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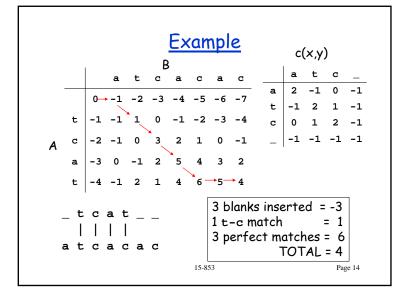


Dynamic programming

for i = 1 to n
$M[i,1] = \sigma(A[i], _)$
for j = 1 to m
$M[1,j] = \sigma(, B[i]);$
for i = 1 to n
for $j = 1$ to m
$M[i,j] = max3(\sigma(A[i],B[j]) + M[i-1,j-1]),$
$\sigma(A[i], _) + M[i-1,j],$
$\sigma(, B[j]) + M[i , j-1]);$

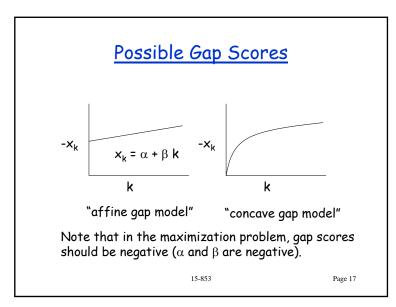
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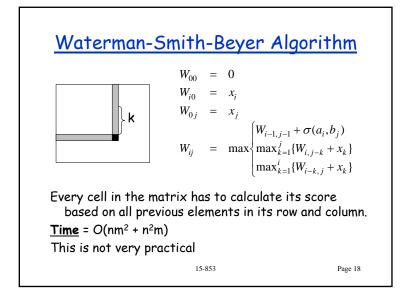


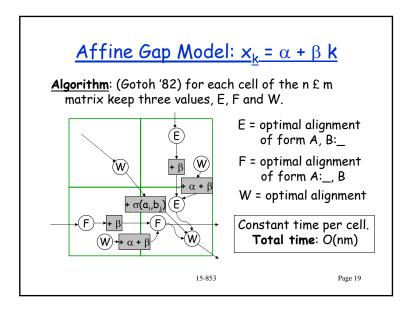


Gap Penalties **Optimizations** Space efficiency: Problem with technique so far: Longer indels (insertions or deletions) should not be weighted as The divide-and-conquer technique still works. the sum of single indels. The Ukkonen/Myers algorithm: Gap: indel of k characters is a gap of length k A variant works, but O(dn) time is no longer **Gap score**: let x_k be the score of a gap of length k guaranteed since the distance from the diagonal cannot in general be directly bounded by the score. Bounds, however, can be given in terms of relative What is a good gap scoring function? weights of matrix elements and the technique Can the dynamic programming approach be works reasonably well in practice. extended? **<u>Real Problem</u>**: solves global-alignment problem when biologists care about the local-alignment problem. 15-853 Page 15 15-853

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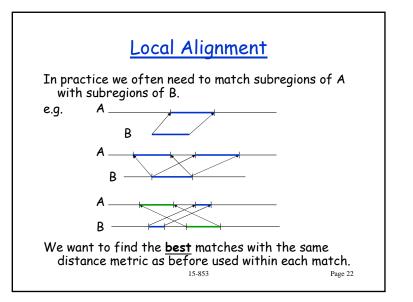


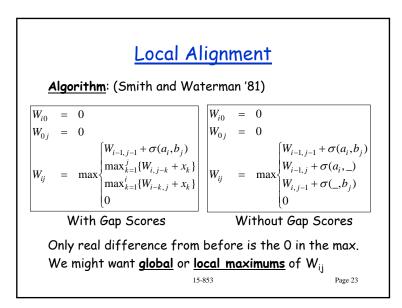


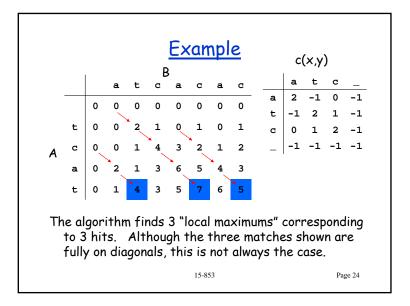
· · 00	=	0
W_{i0}	=	$\alpha + \beta i$
W_{0j}	=	$\alpha + \beta j$
		$W_{i-1,j-1} + \sigma(a_i,b)$
W_{ij}	=	$\max \left\{ E_{ij} \right\}$
		$ig (F_{ij}$
	W_{i0} W_{0j} W_{ij}	$W_{00} = W_{i0} = B$ $W_{0j} = W_{0j} = W_{ij} = B$

Function Form		
	$O(nm^2 + n^2m)$	
x _k = α + β k	O(nm)	
$x_k = \alpha + \beta \log(k)$	O(nm)?	
	O(nmlogn)	
l-segments	O(Inm)	
	$x_k = \alpha + \beta \log(k)$	

Other Gap Models







Database Search

Basic model:

- 1. User selects a database and submits a source sequence S, typically via the web (or email)
- 2. The remote computer compares S to each target T in its database. The runtime depends on the length of S and the size of the database.
- 3. The remote computer returns a ranked list of the "best" hits found in the database, usually based on local alignment.

Example of BLAST

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Algorithms in the "real world"

Dynamic programming is too expensive even with optimizations.

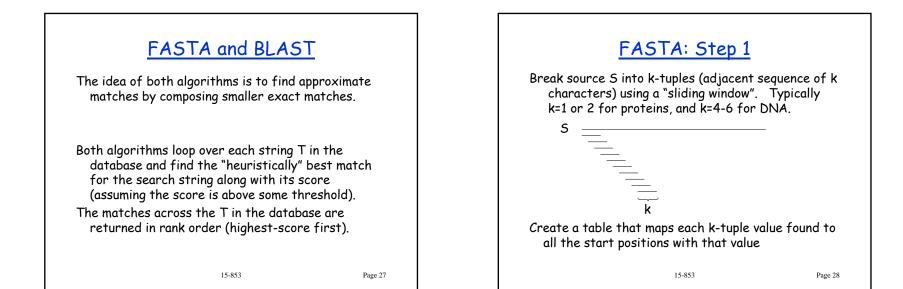
Heuristics are used that approximate the dynamic programming solution. Dynamic program is often used at end to give final score.

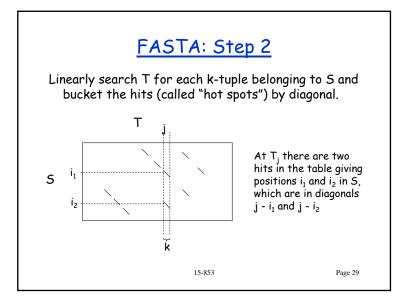
Main two programs in practice:

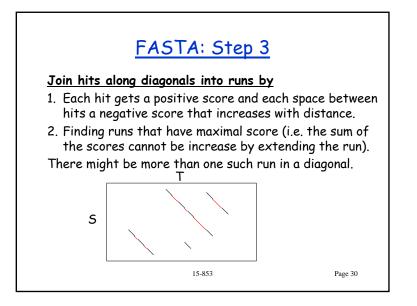
- FASTA (1985)
- <u>BLAST</u> (Basic Local Alignment Search Tool) (1990)

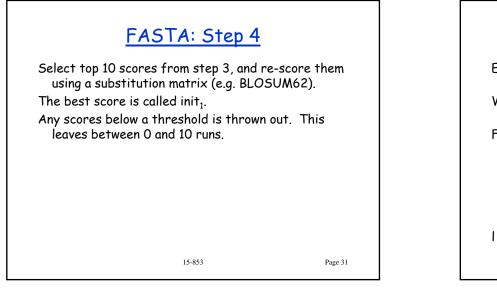
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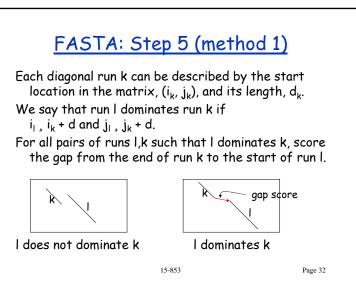
Lipman involed in both, Myers involved in BLAST. There are many variants of both.

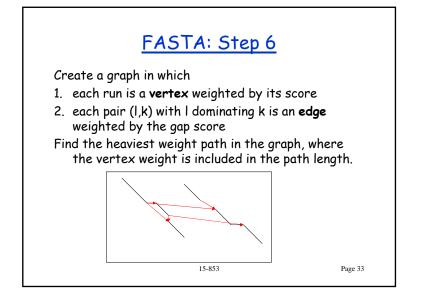


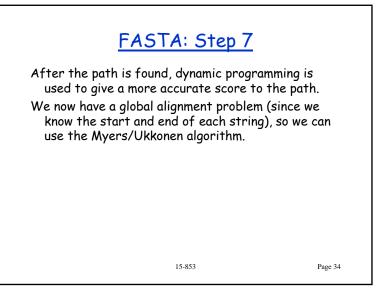


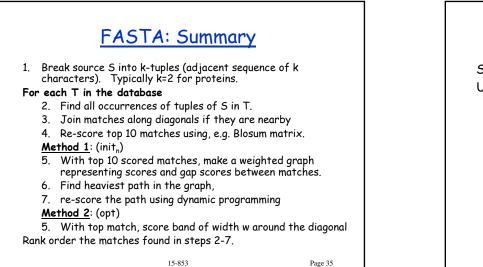






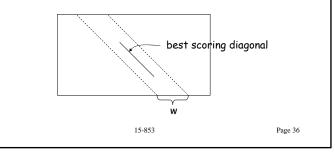






FASTA: Step 5 (method 2)

Select best score for a diagonal (this was $init_1$) Use dynamic programming to score a band of width w (typically 16 or 32 for proteins) around the best diagonal



BLAST

- 1. Break source 5 into k-tuples (adjacent sequence of k characters). Typically k=3 for proteins.
- For each k-tuple w (word), find all possible k-tuples that score better than <u>threshold t</u> when compared to w (using e.g. BLOSUM matrix). This gives an expanded set S_e of k-tuples.

For each T in the database

- 3. Find all occurrences (hits) of S_e in T.
- Extend each hit along the diagonal to find a locally maximum score, and keep if above a <u>threshold s</u>. This is called a high-scoring pair (<u>HSP</u>). This extension takes 90% of the time.

Optimization: only do this if two hits are found nearby on the diagonal.

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BLAST

The initial BLAST did not deal with indels (gaps), but a similar method as in FASTA (i.e. based on a graph) can be, and is now, used.

The BLAST thresholds are set based on statistical analysis to make sure that few false positives are found, while not having many false negatives.

- Note that the main difference from FASTA is the use of a substitution matrix in the first stage, thus allowing a larger k for the same accuracy.
- A finite-state-machine is used to find k-tuples in T, and runs in O(|T|) time independently of k.

The BLAST page

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