

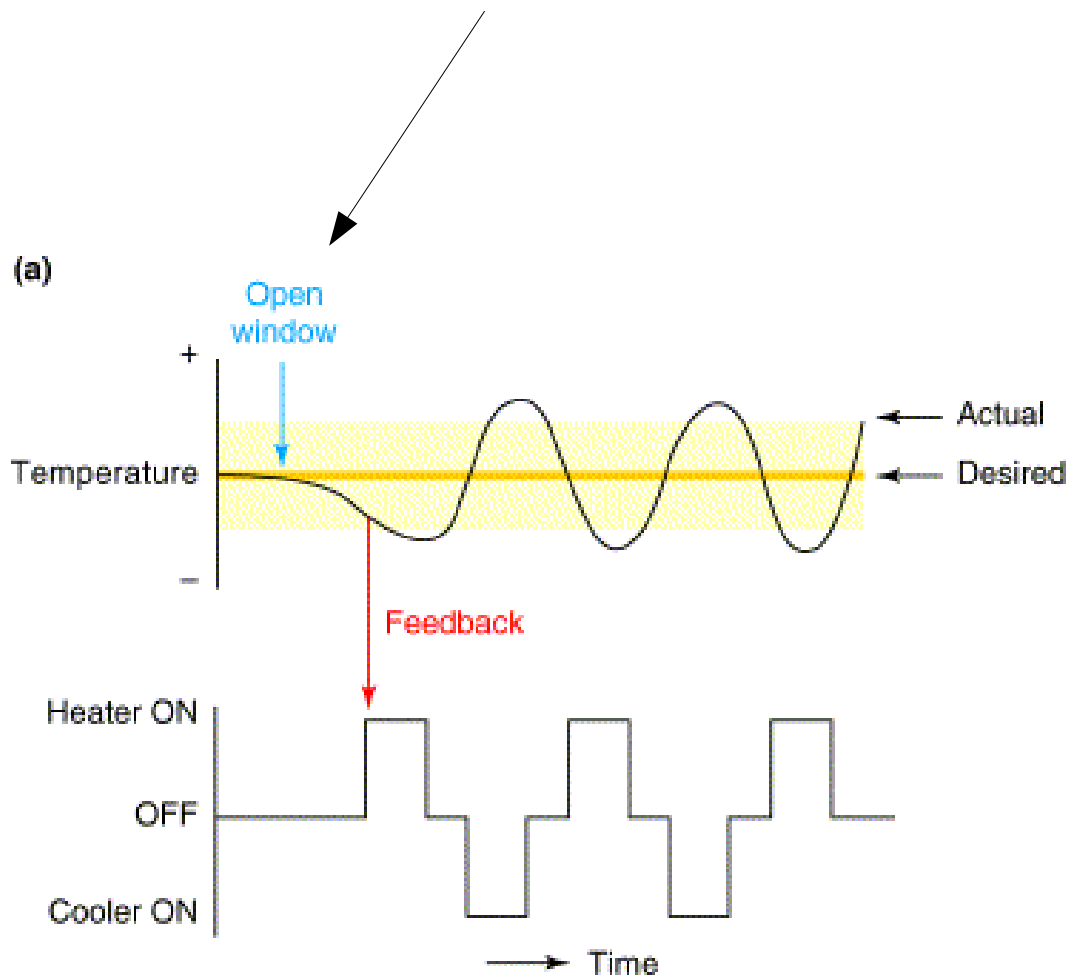
# Cerebellar Timing and Classical Conditioning

## Computational Models of Neural Systems

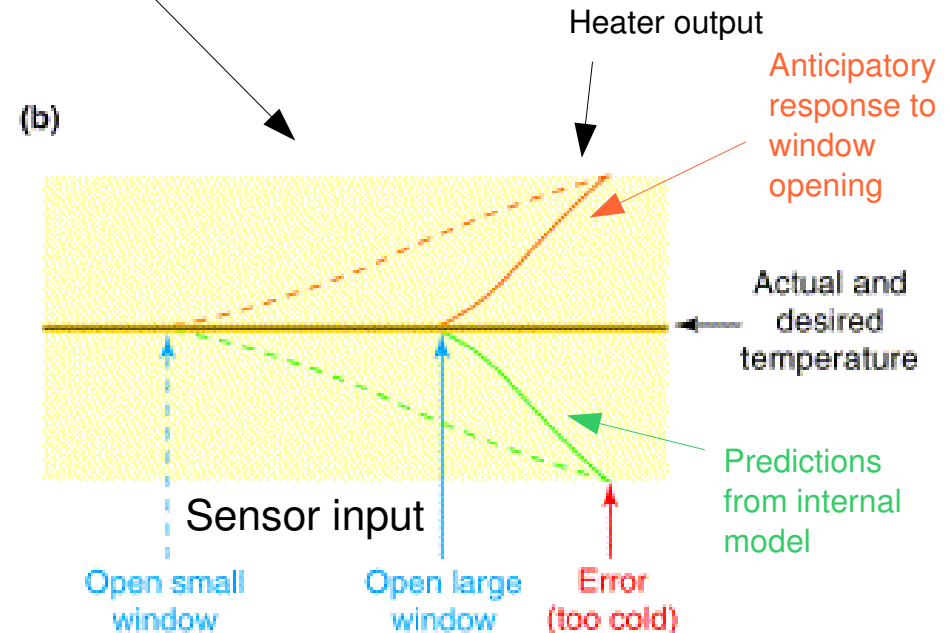
### Lecture 2.4

David S. Touretzky  
September, 2017

# Feedback vs. Feedforward Control



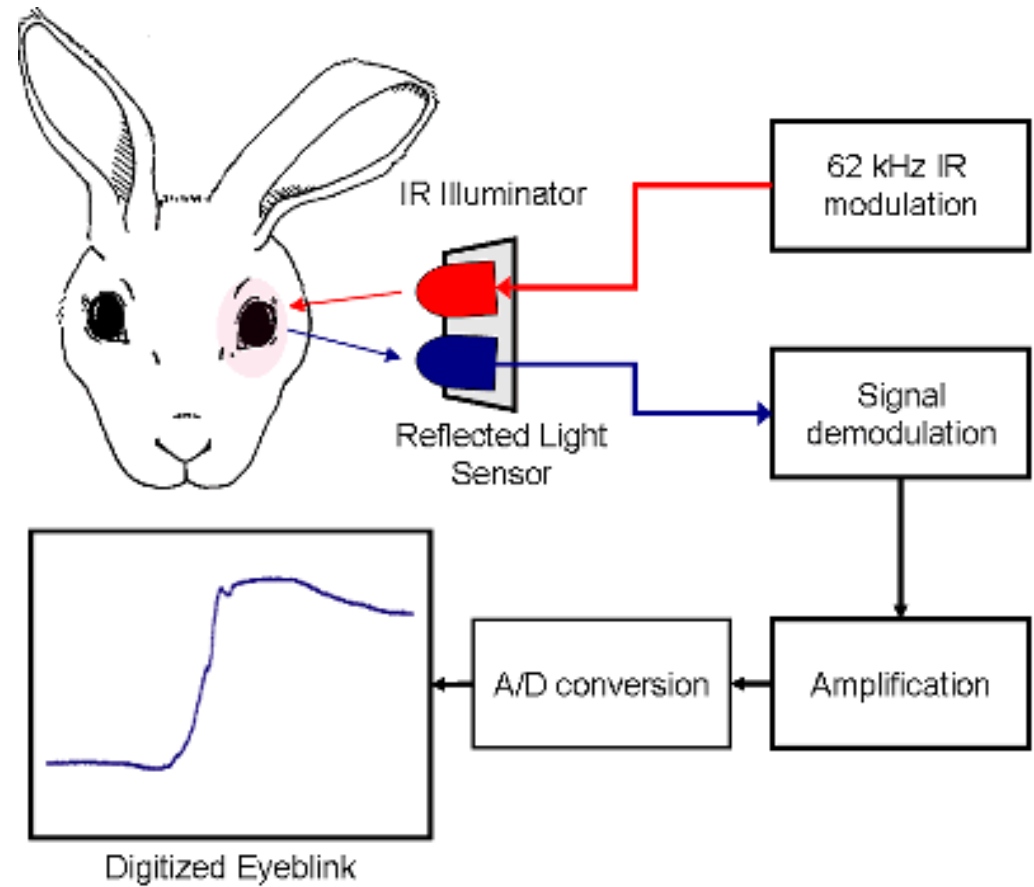
High latency  
Residual errors  
Subject to oscillations if gain too high



*Anticipatory response* gives low latency  
Better accuracy (lower error)  
Sensors tell us the system state  
Control requires an internal model

TRENDS in Neurosciences

# Pavlovian Eyelink Conditioning



# Eyeblink Conditioning in Humans



- Measure cognitive development
- Impaired by mental disorders:
  - Schizophrenia
  - OCD
- Fetal alcohol syndrome

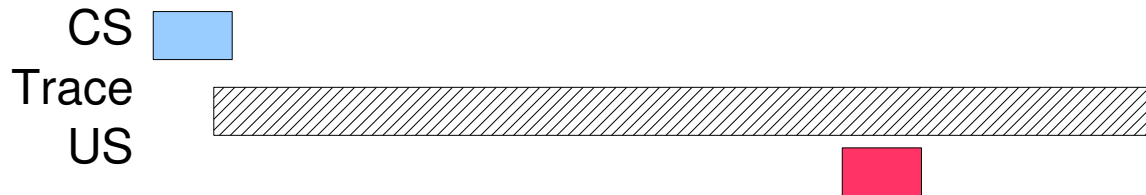
*Eyeblink Conditioning System*  
from San Diego Instruments

# Delay vs. Trace Conditioning

- **Delay conditioning:** CS stays on until US arrives (up to 4 secs)



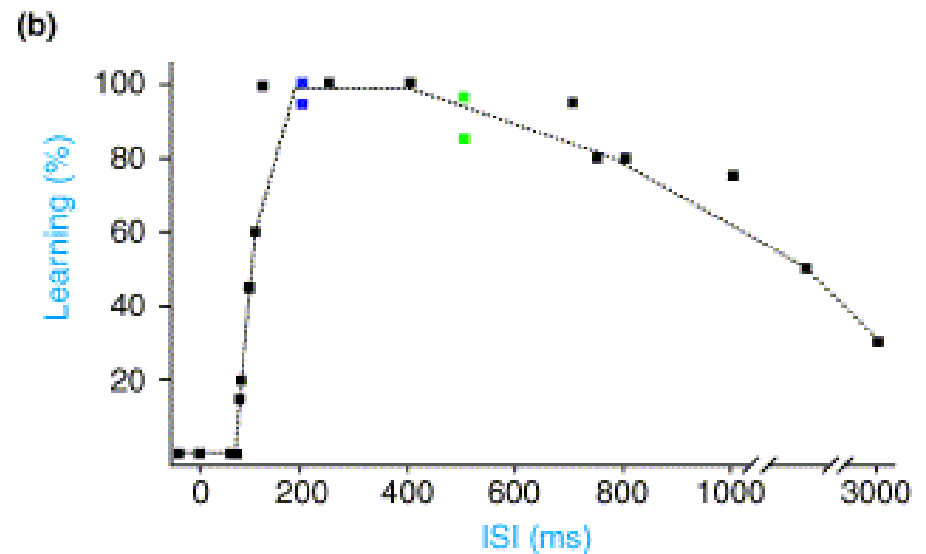
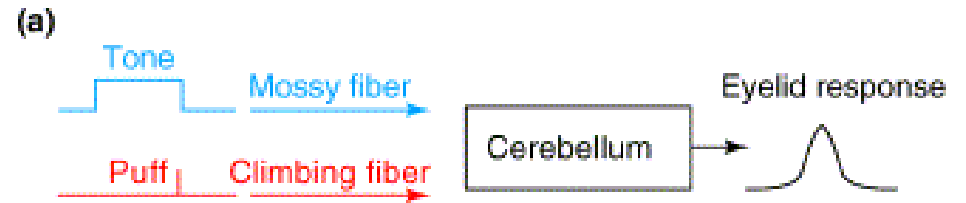
- **Trace conditioning:** CS comes on and then goes off again. US must be associated with the *memory trace* of the CS. Trace can be up to 2 secs in duration.



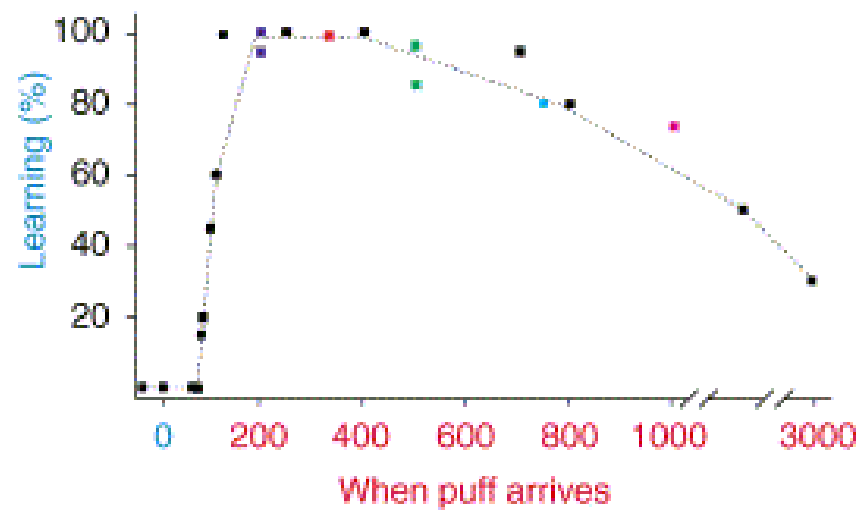
- Trace conditioning takes about 5x as many trials to learn.
- Trace conditioning (but not delay conditioning) is disrupted by lesions of hippocampus or medial prefrontal cortex.

# Effect of Inter-Stimulus Interval (ISI)

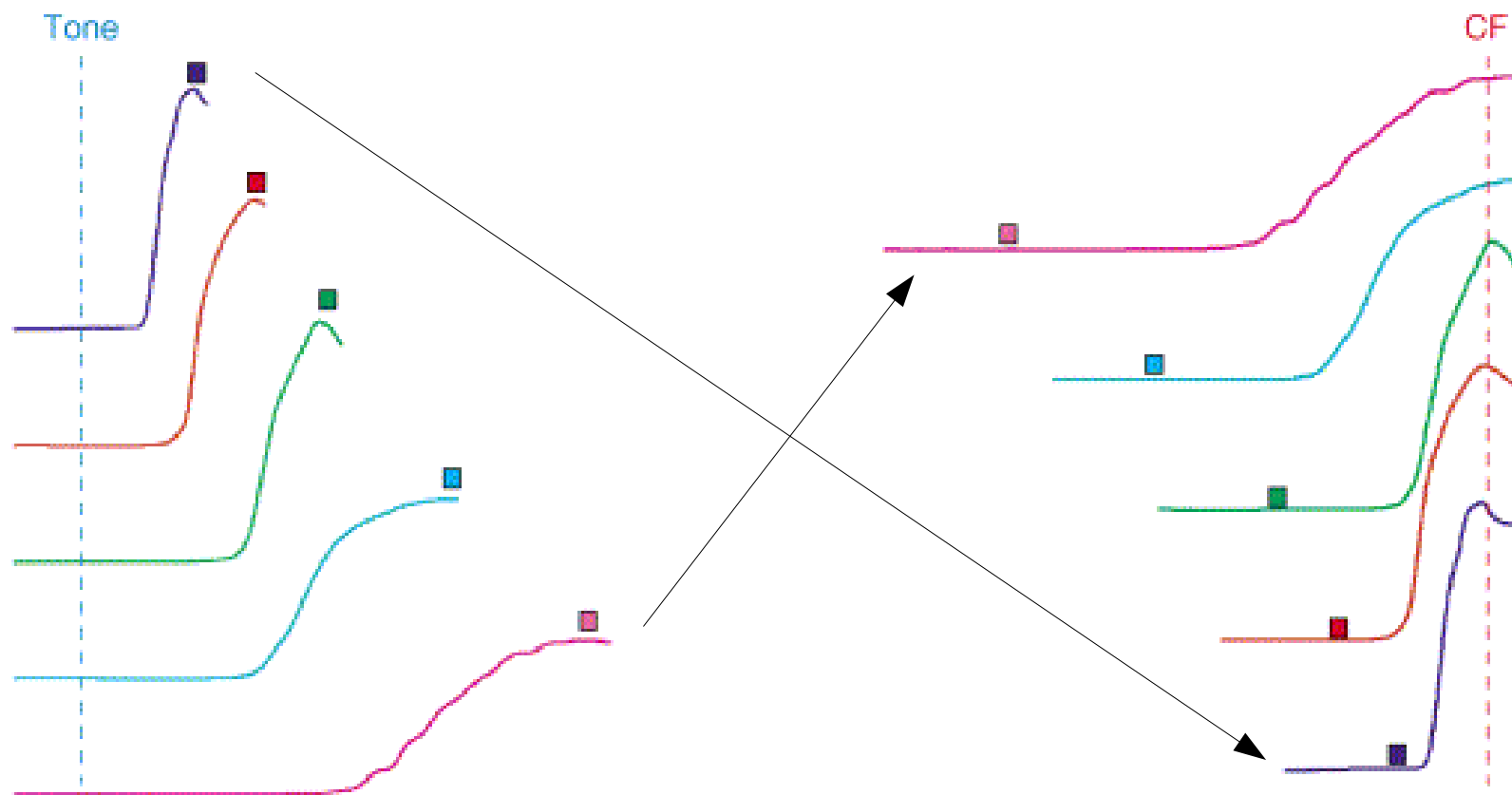
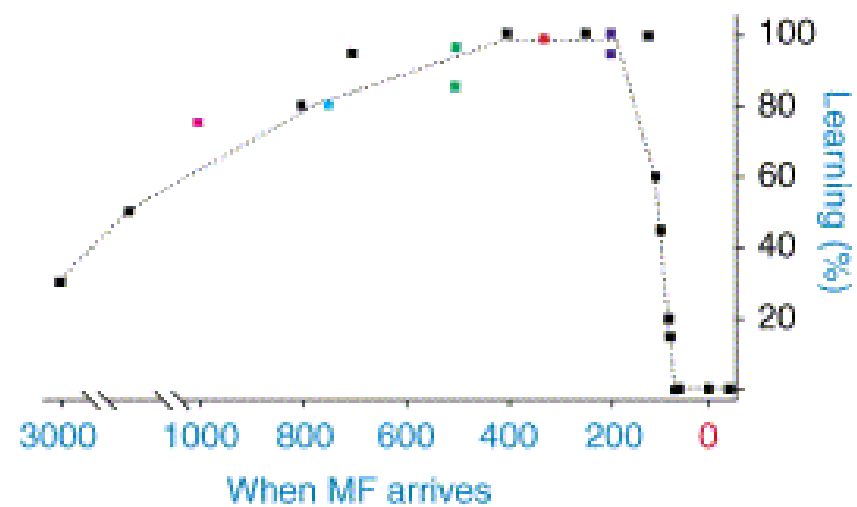
- ISI must be 100-3000 msec (ideal is 200-500 msec)
- The learned CR (blink) is timed to just precede the US (air puff).
- Several hundred trials required for long ISIs
- Long ISIs also generate a broader response



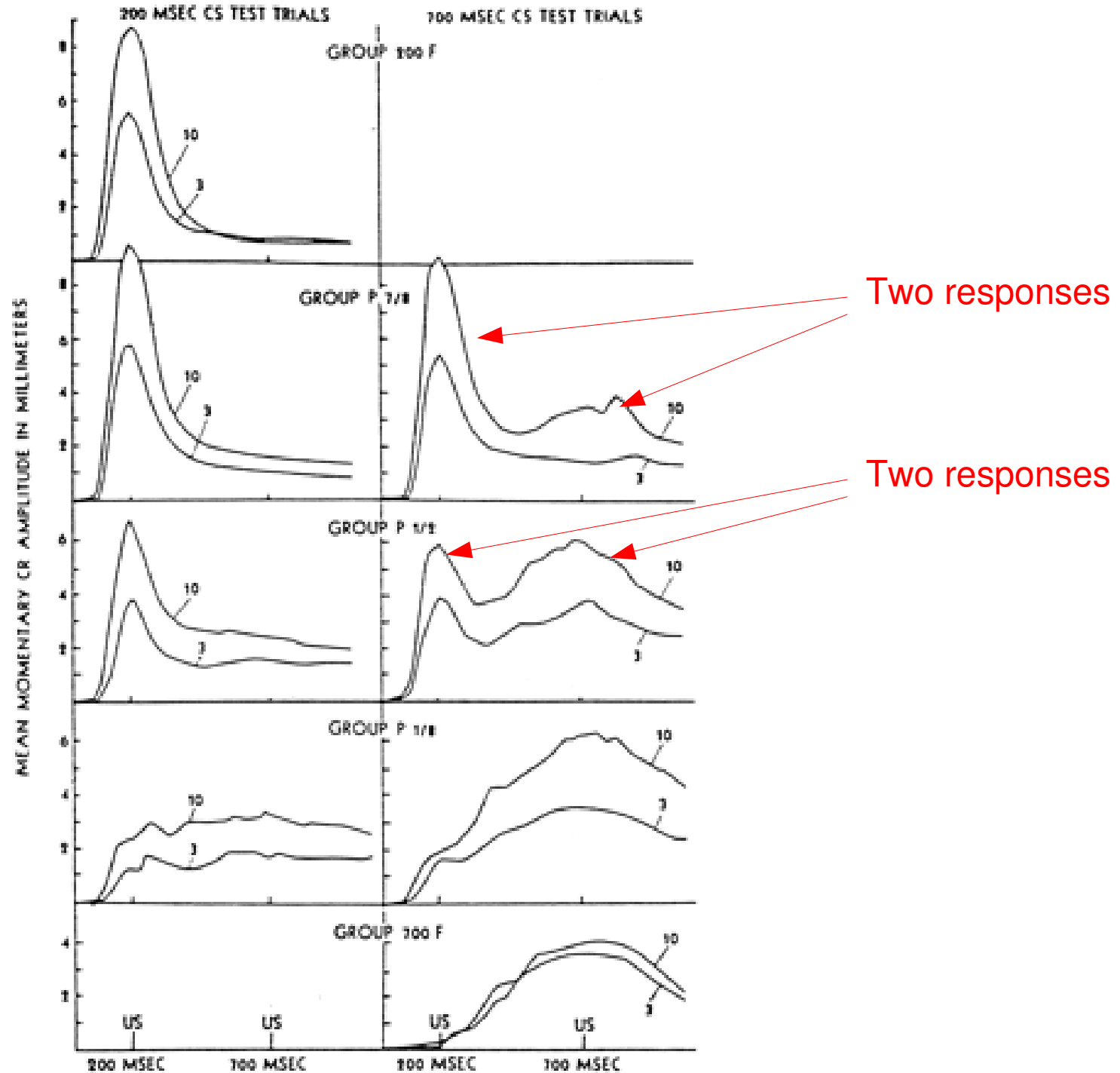
(a)



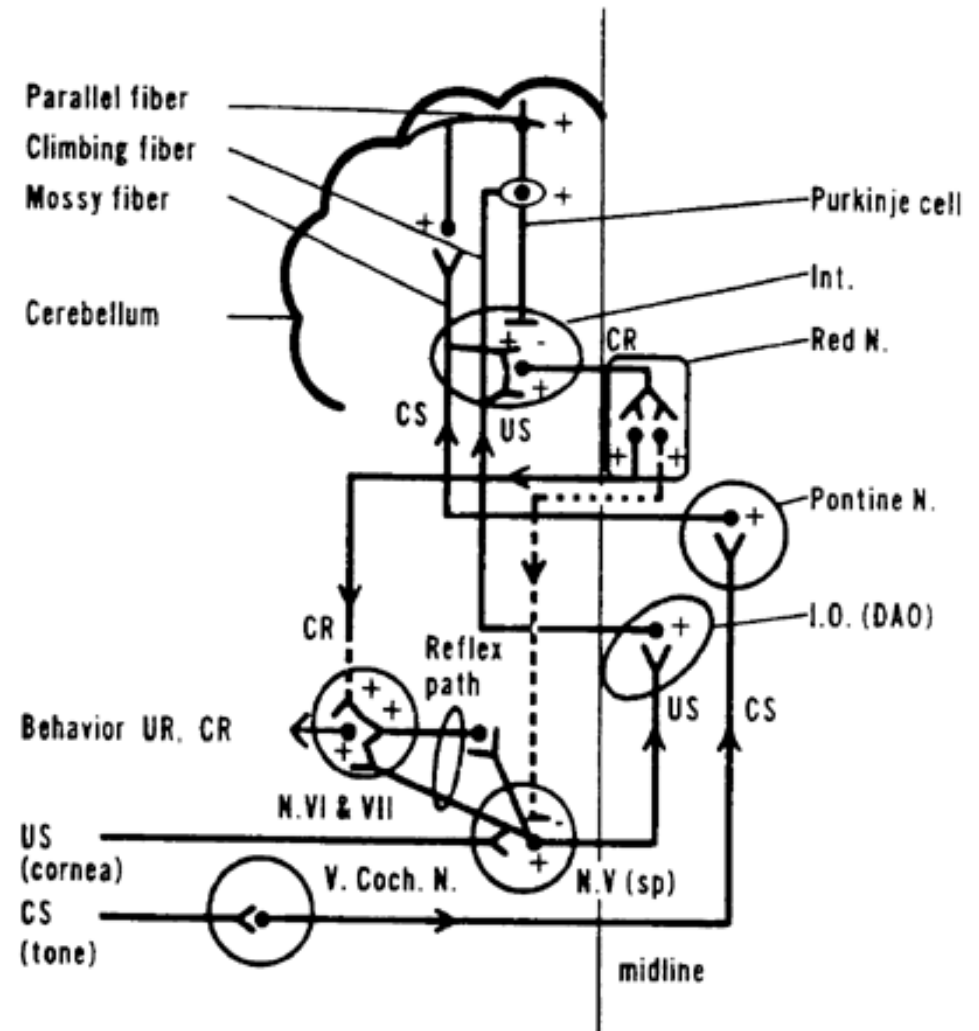
(b)



# Mixing 200 ms and 700 ms ISI Trials

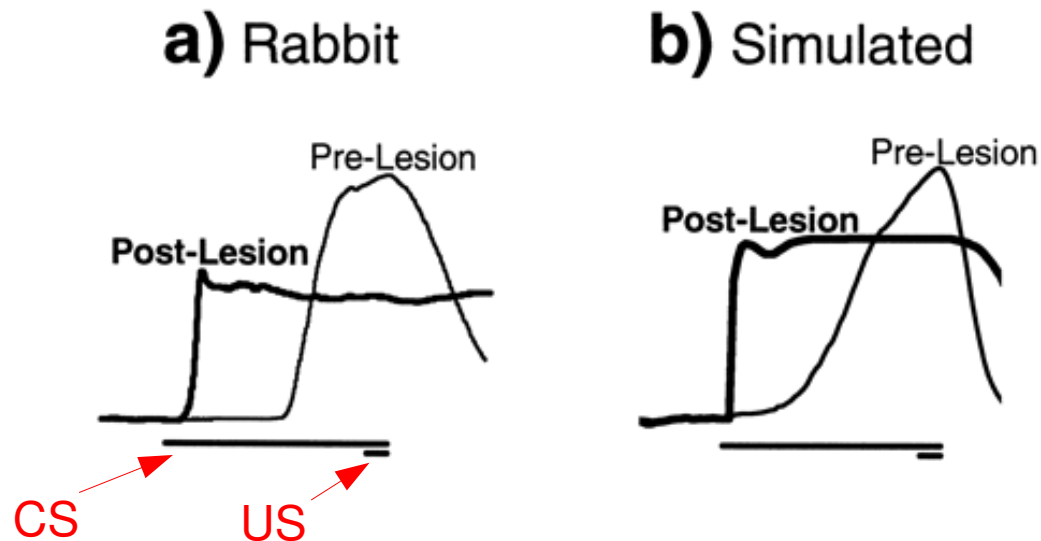


# Eyelid Conditioning Circuitry



# Effects of Lesions

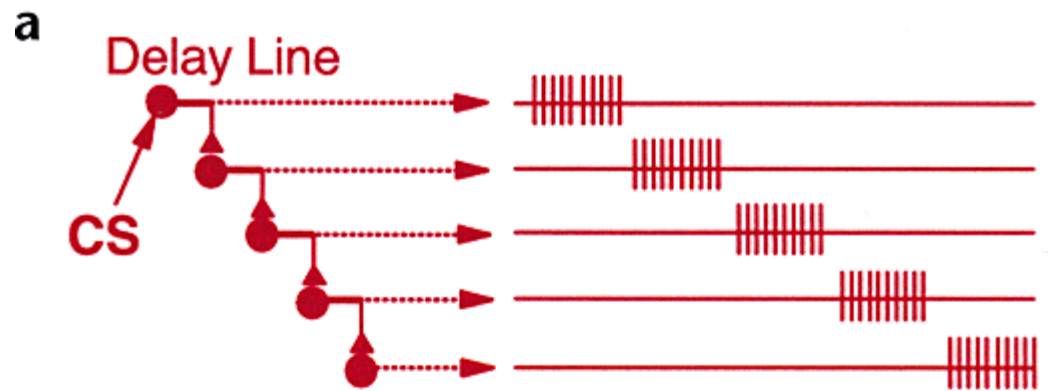
- Lesioning the cerebellar cortex disrupts response timing but does not abolish the response entirely.
- Associative learning can still occur, but responses have very short latency (timing is off).



- Conclusion: two sites of Pavlovian learning in the cerebellum:
  - Interpositus nucleus learns to respond to the CS (mf → nuc)
  - Cerebellar cortex fine tunes the temporal response (pf → Pk)

# Theories of Cerebellar Response Timing

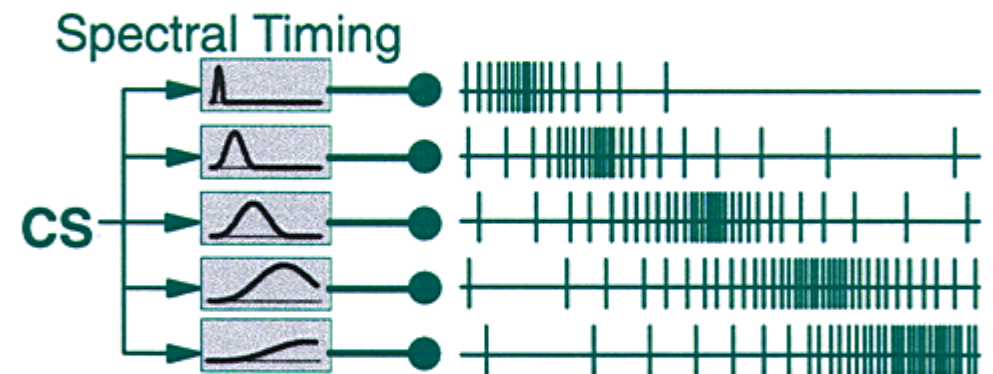
a) Tapped delay lines



b) Spectral timing models

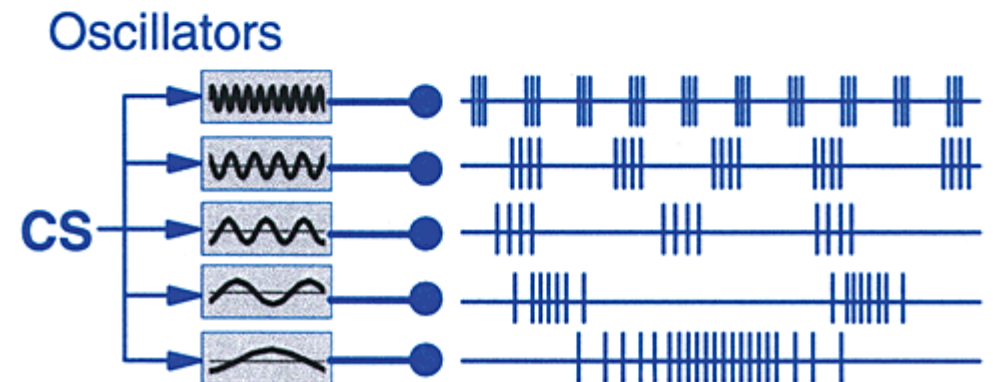
- i) PCs with fixed timing
- ii) PCs w/adjustable timing

**b**



c) Conjunctions of oscillators

**c**



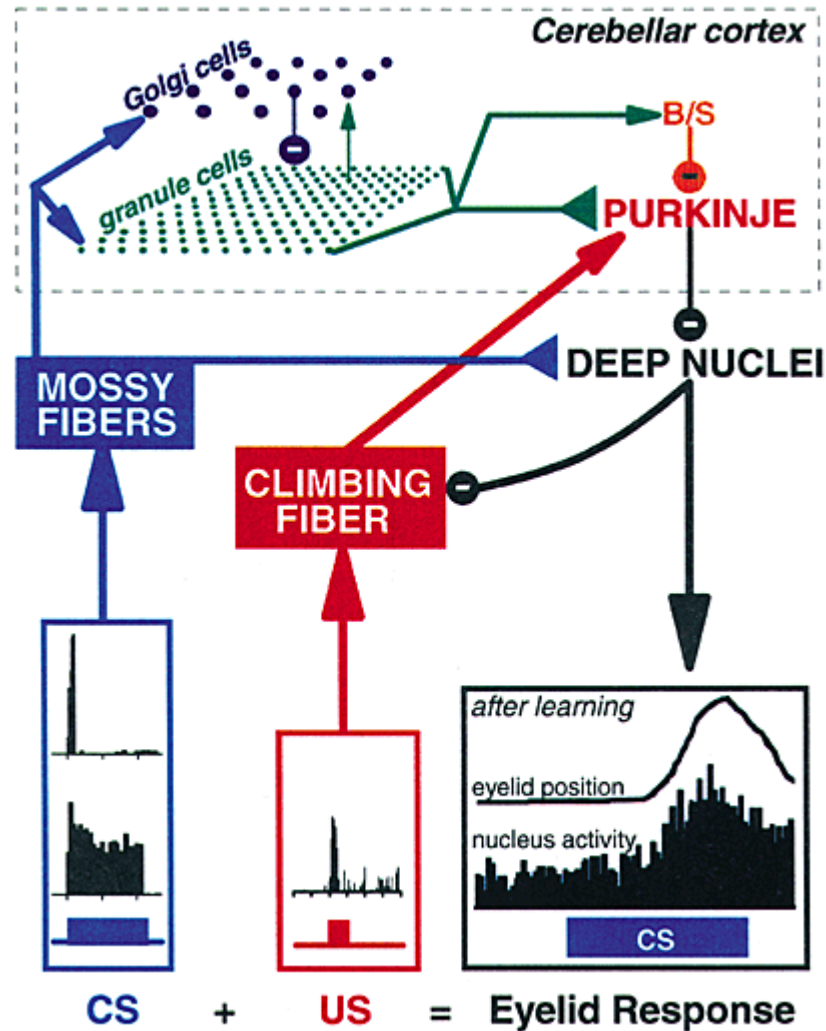
d) State machines:

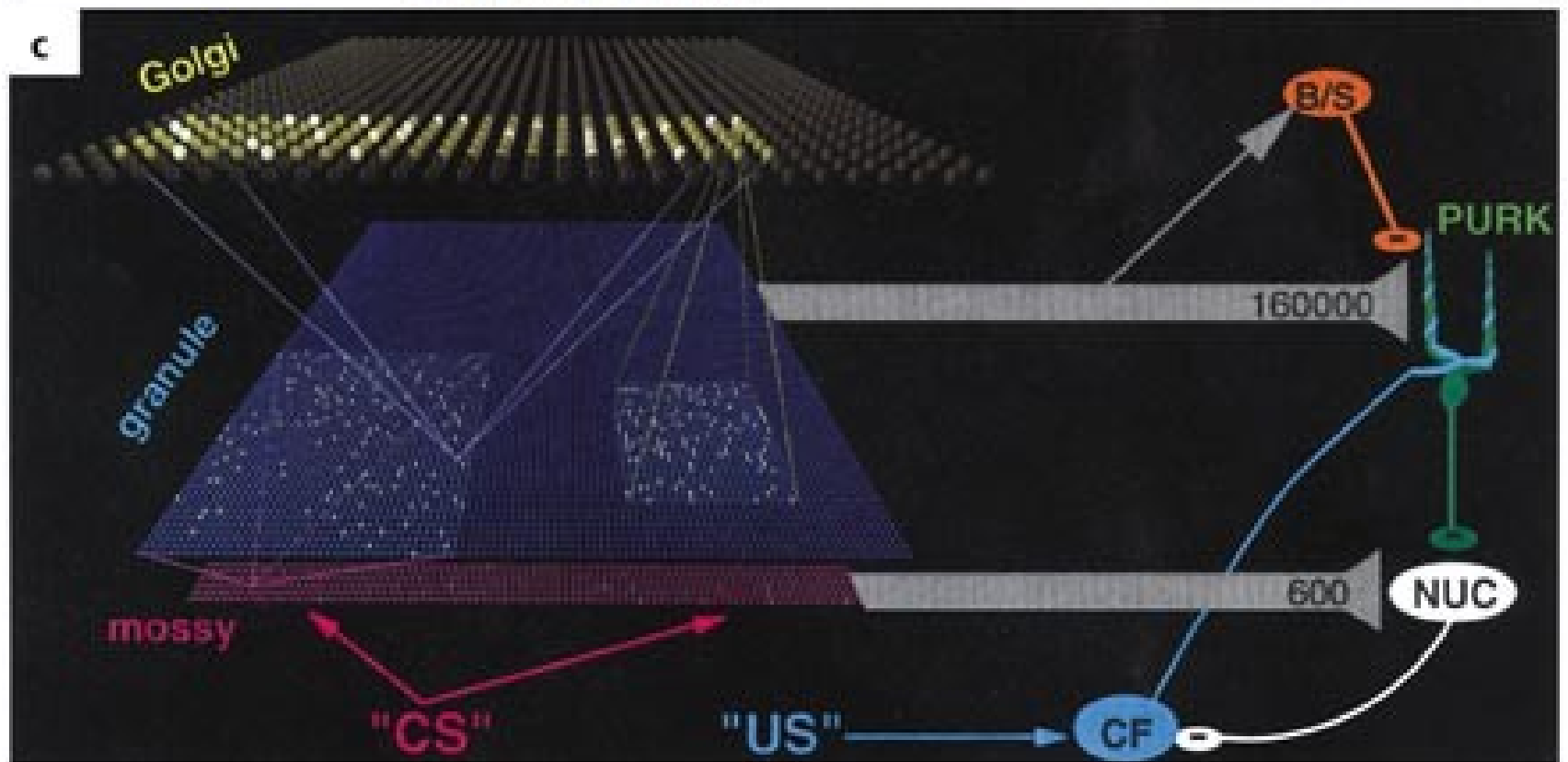
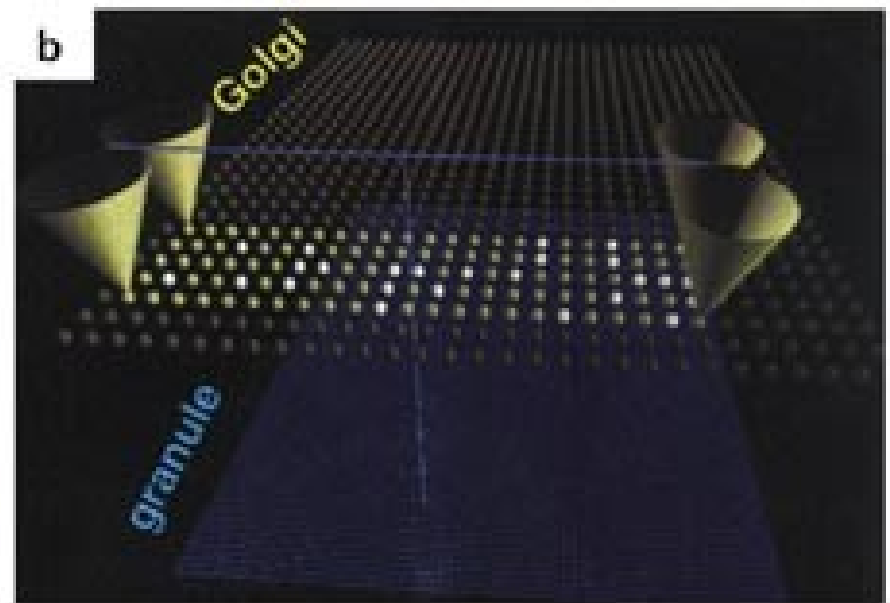
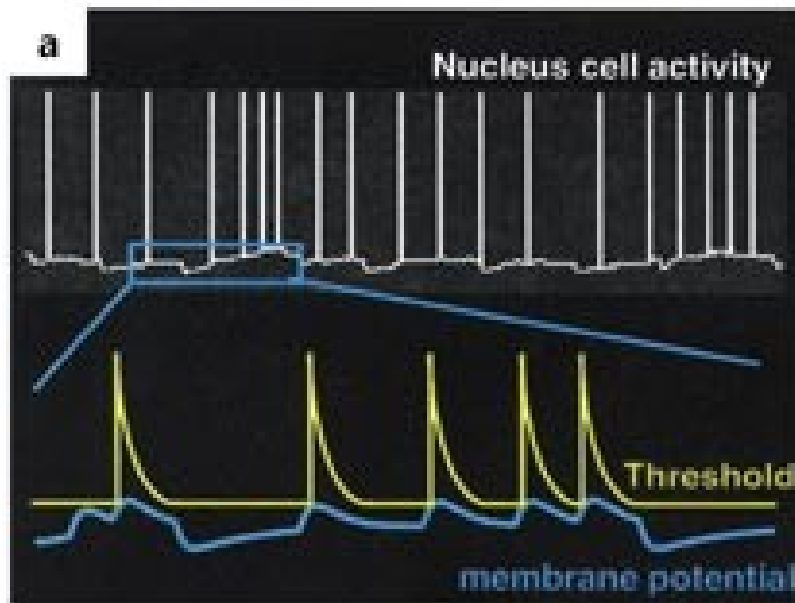
- i) Mauk & colleagues
- ii) liquid state machines

e) Selectable “timing units”

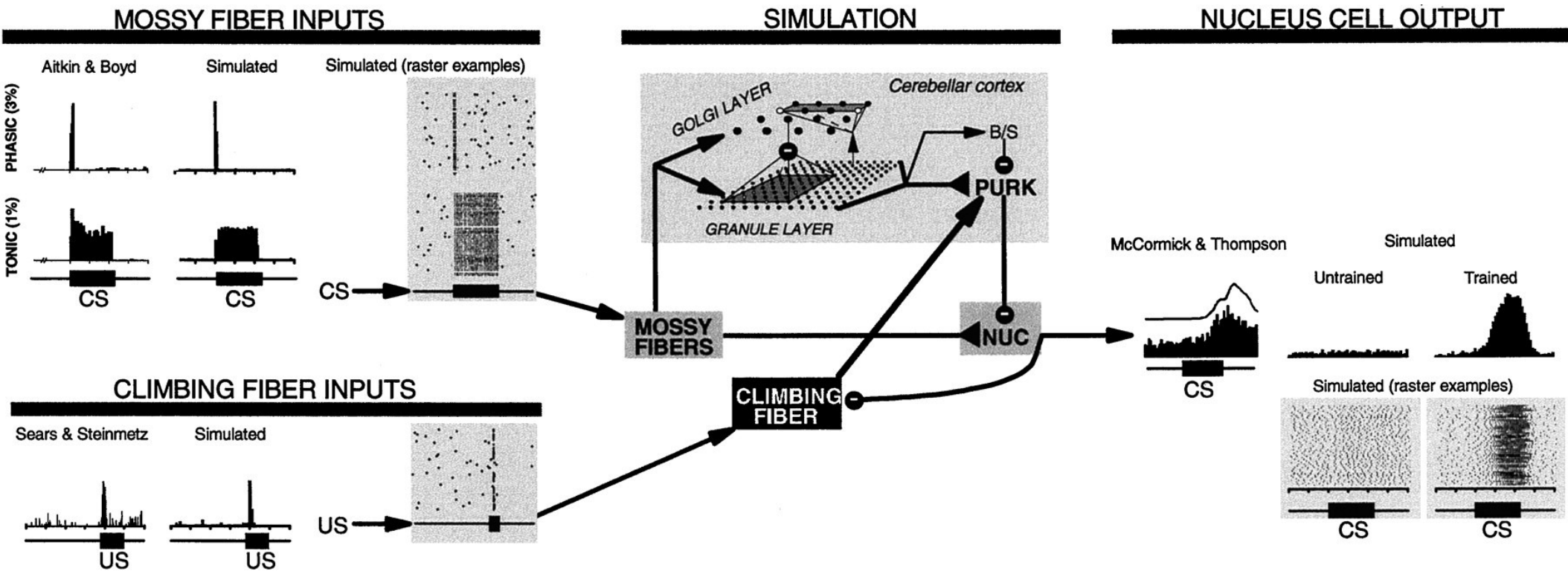
# Medina & Mauk (2000) Simulation

600 mossy fibers  
10,000 granule cells  
900 Golgi cells  
60 basket cells  
20 Purkinje cells  
6 nucleus cells  
> 300,000 synapses



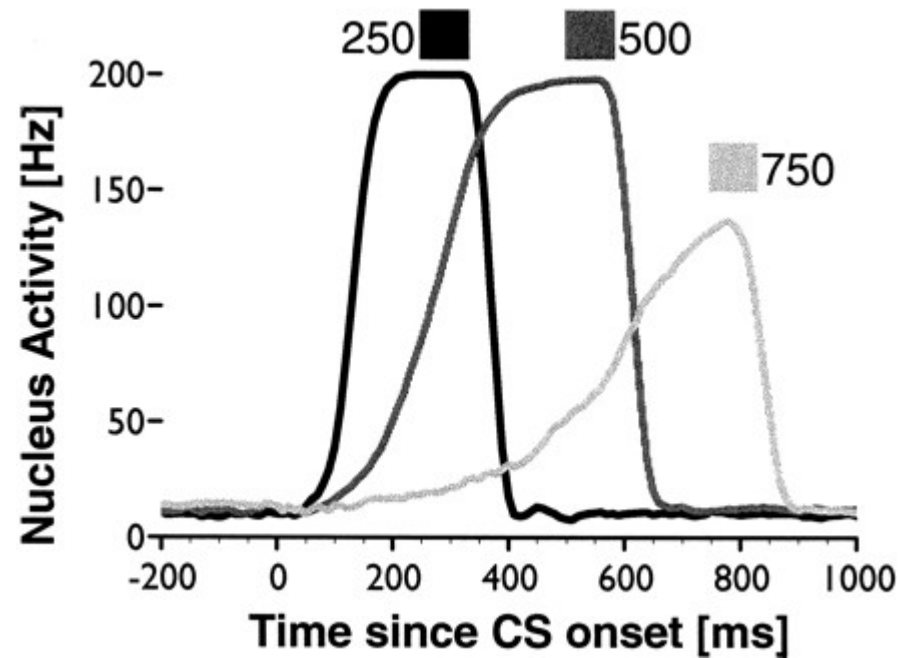


# More Simulation Details in the J.Neurosci. Paper



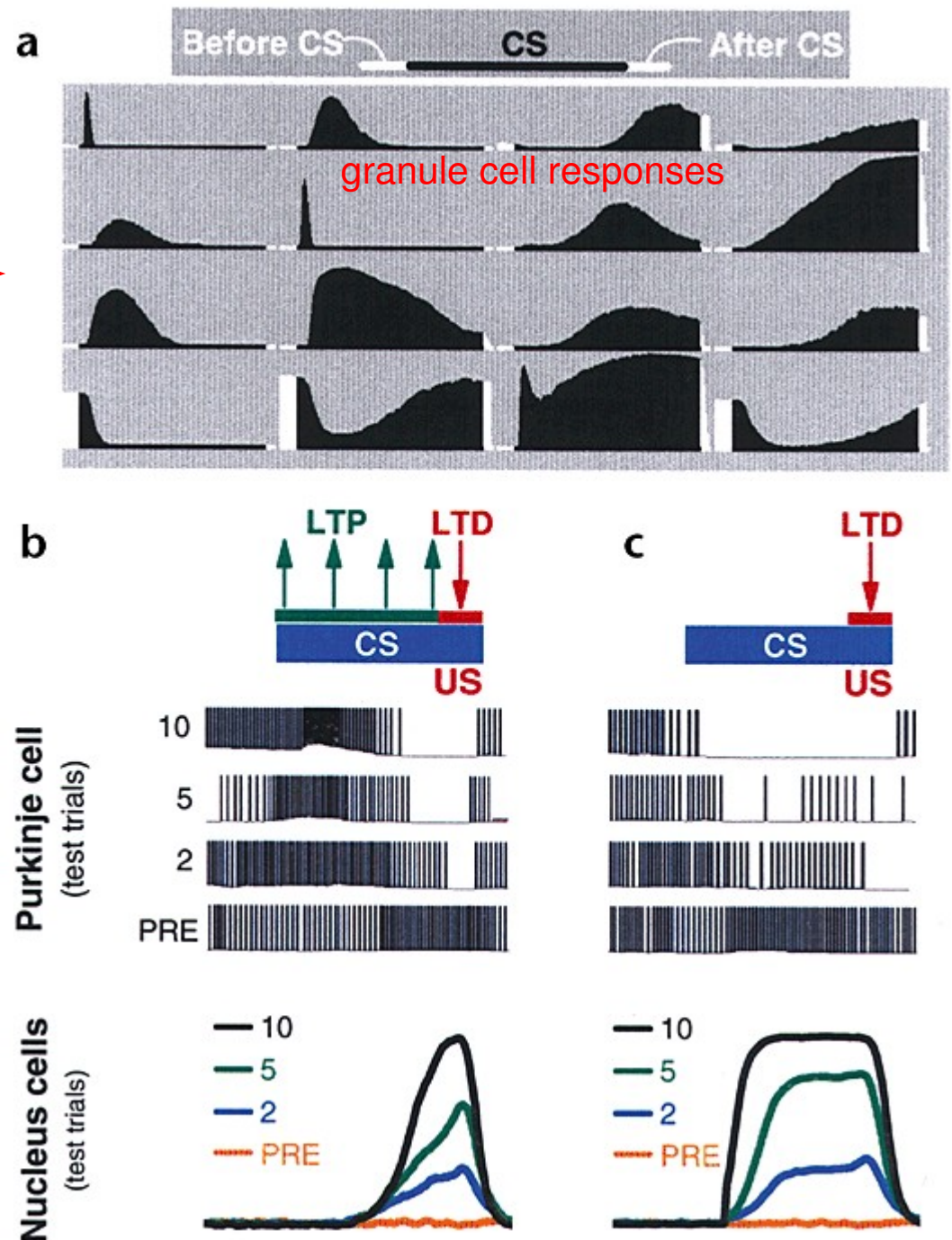
Realistic mossy and climbing fiber inputs based on experimental data.

# Response Timing in the Model

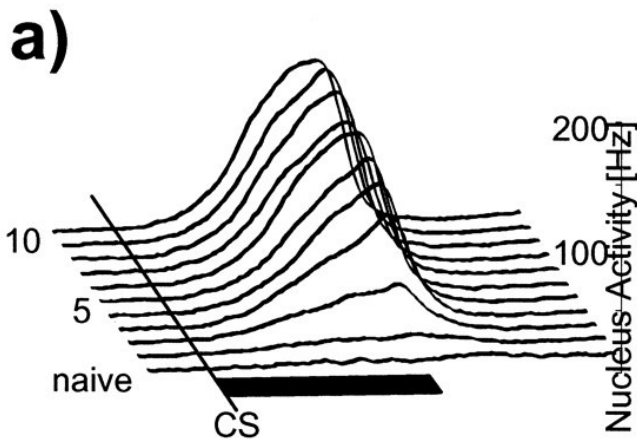


# LTP + LTD

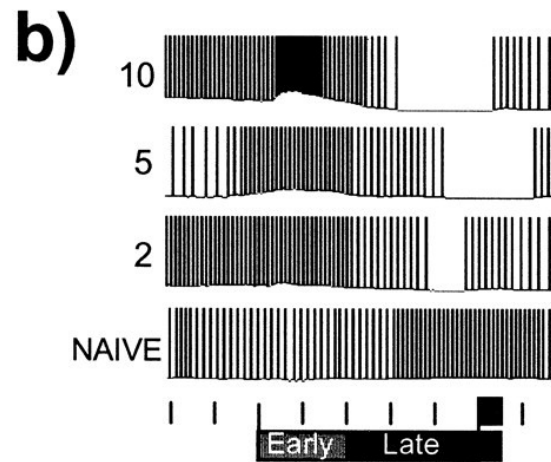
- Granule cells exhibit a variety of broad temporal responses →
- LTD alone produces an overly broad CR (right).
- But LTP + LTD together produces a precisely timed response by combining inputs from multiple Purkinje cells to keep the DCN inhibited until just before the US is expected to arrive.



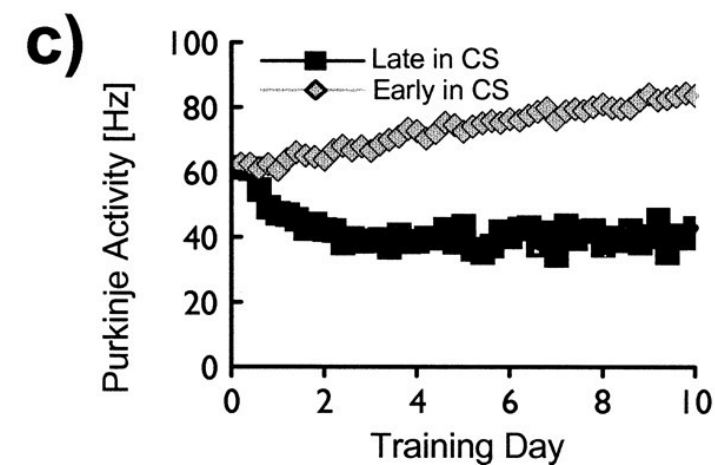
# Time Course of Learning and Response Shaping



Nuclear cell

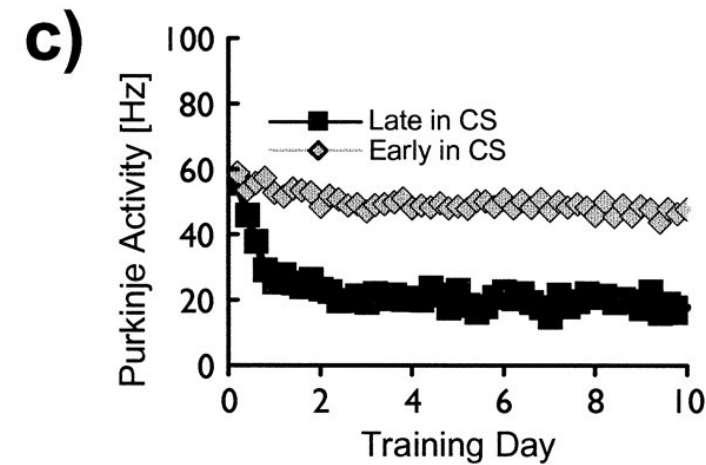
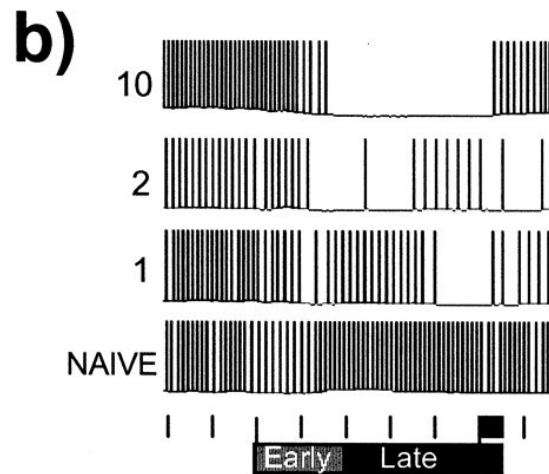
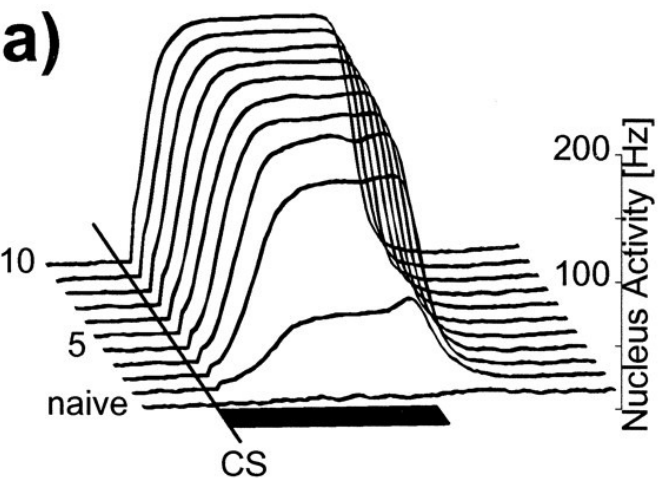


Simulated Purkinje cell

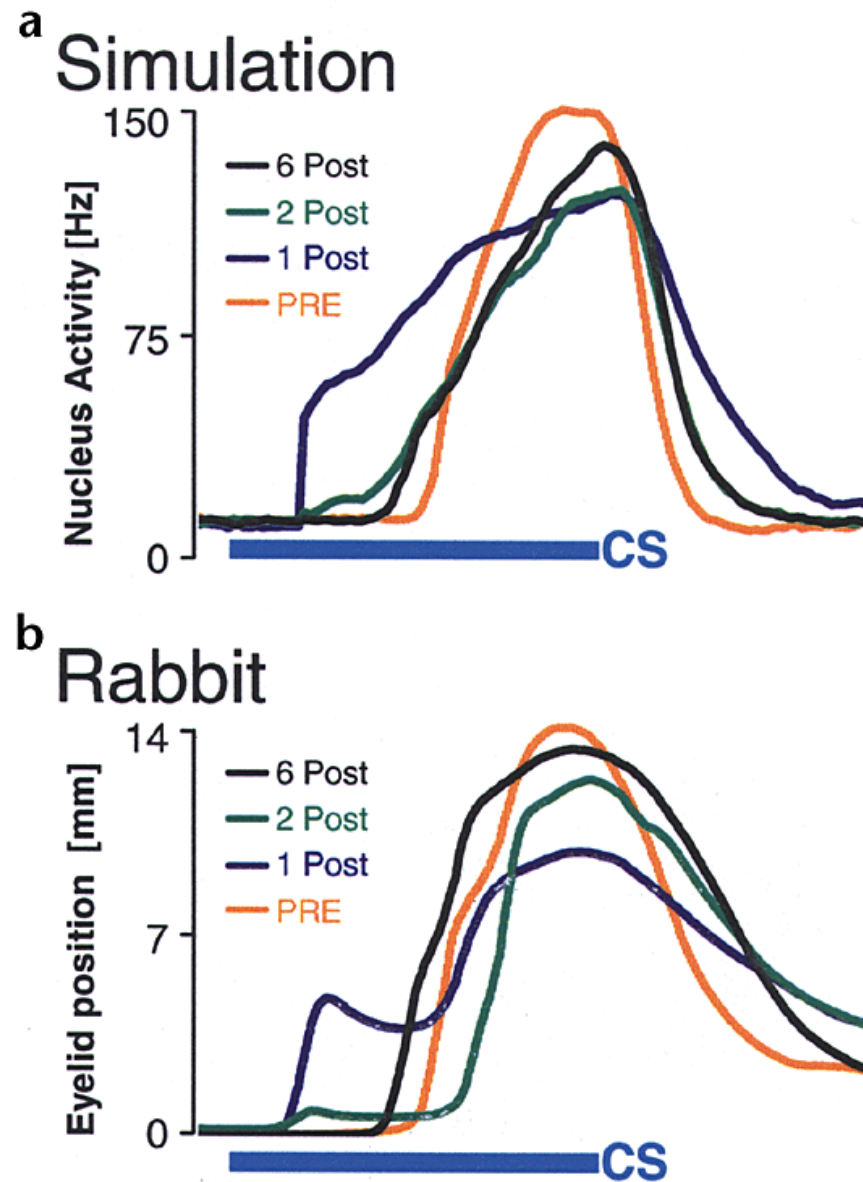


Early LTP + Late LTD

# Learning With LTP Disengaged: Response Timing is Poor

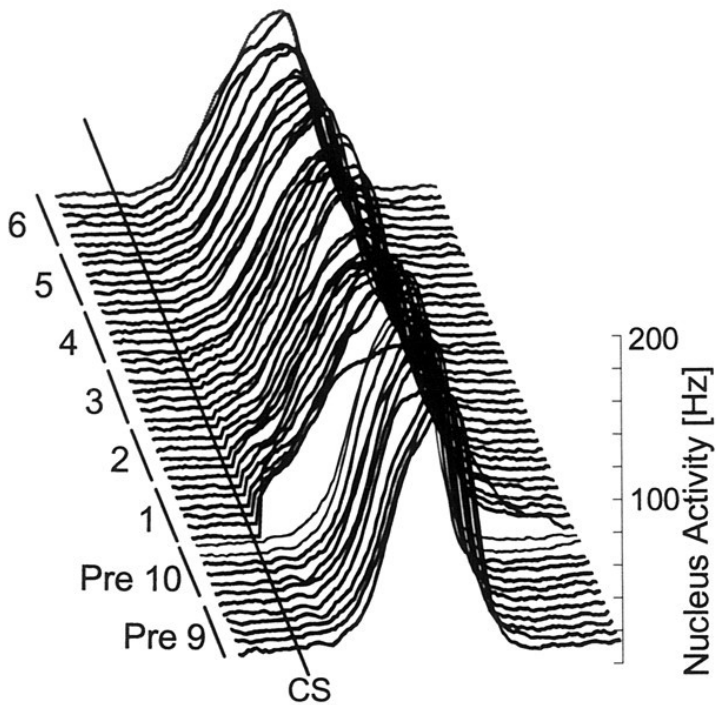


# Recovery After Partial Lesion to Cerebellar Cortex

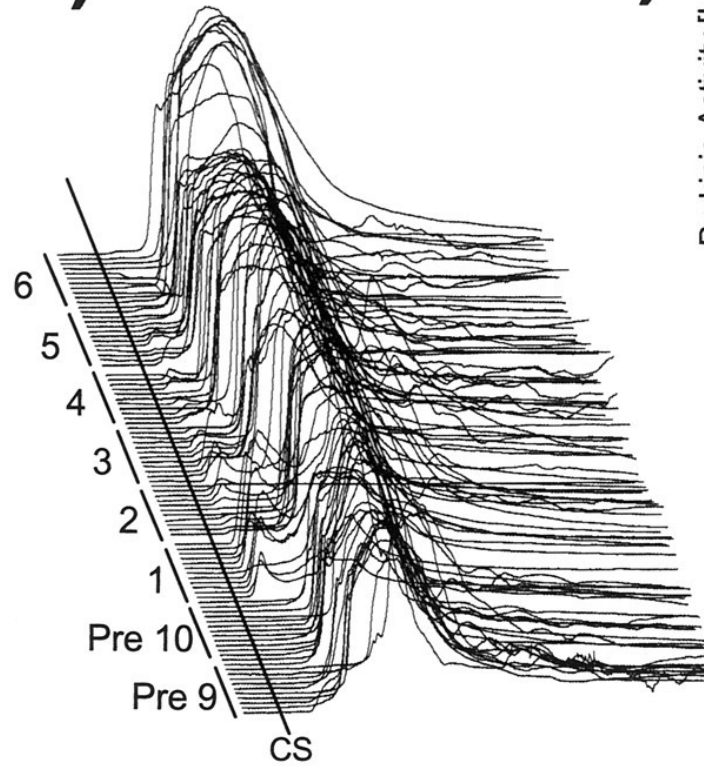


# Recovery After Lesioning Cerebellar Cortex

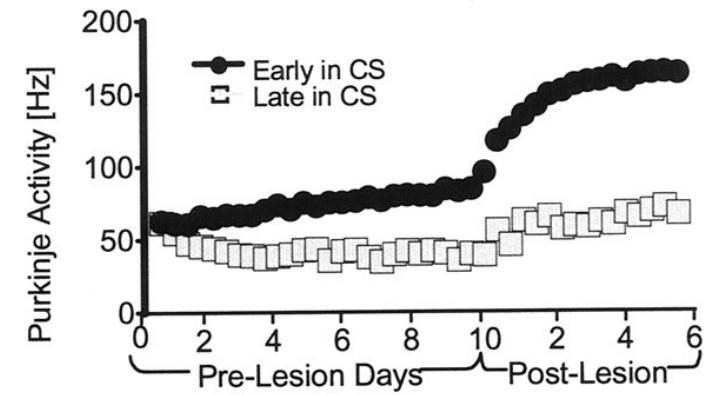
**a)** Simulation



**b)** Rabbit



**c)**

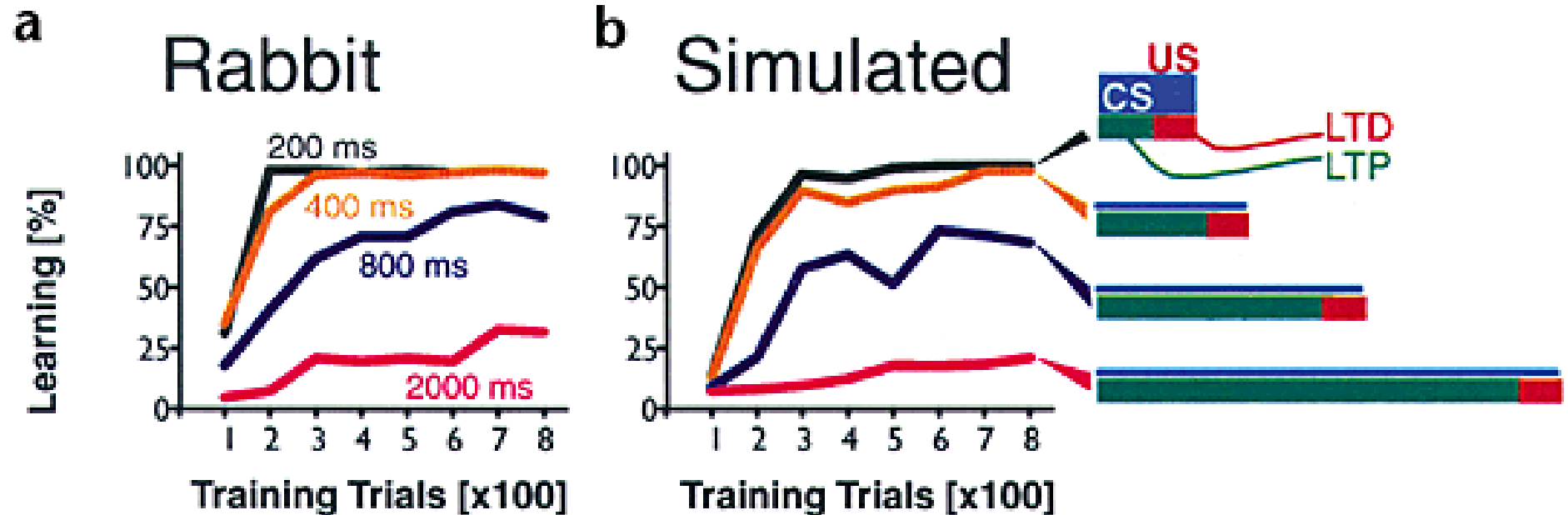


**d)**



# Why Do Long ISIs Prevent Learning?

## Hypothesis: Too Much LTP Overwhelms LTD

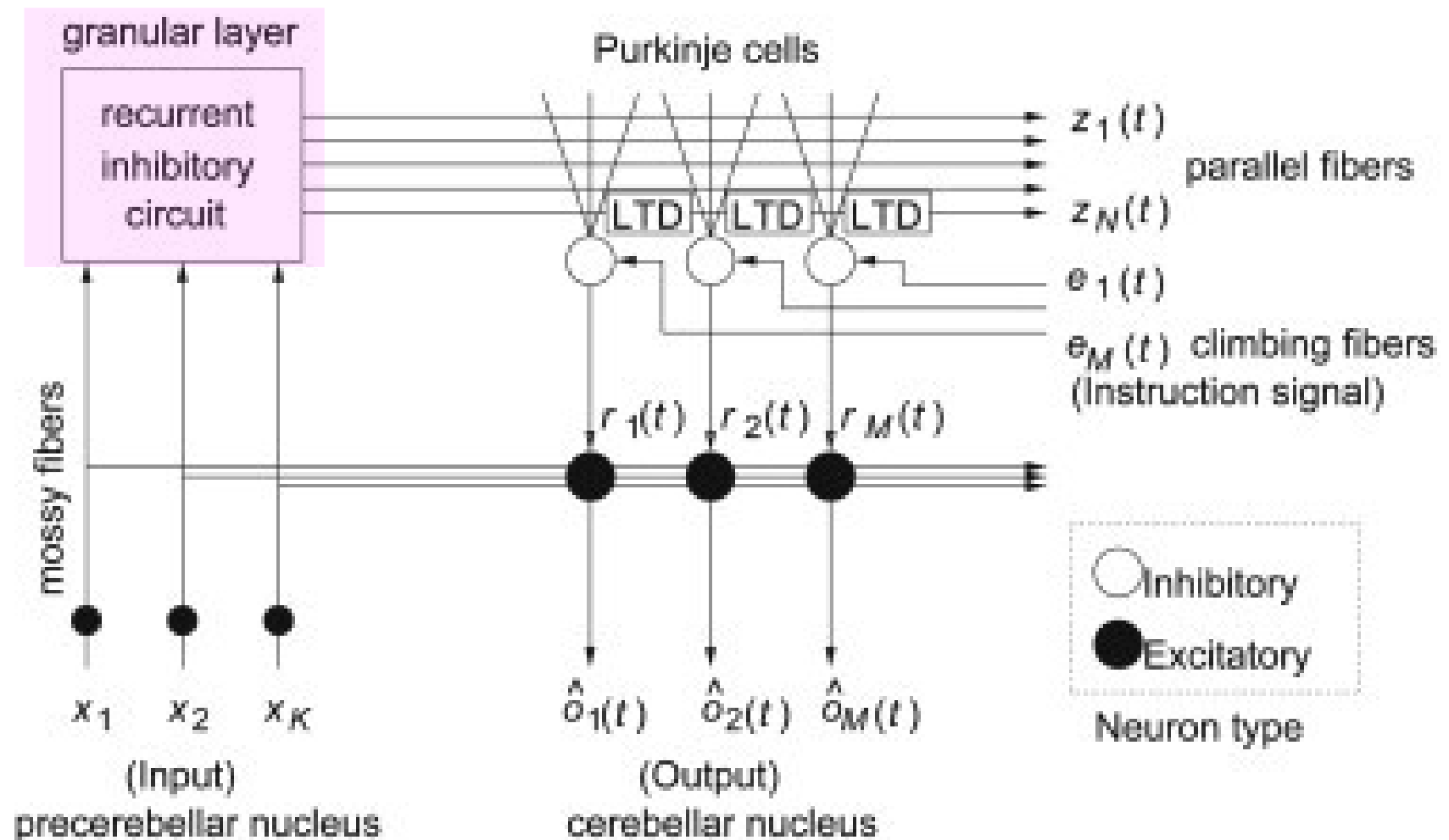


# Scaling Up to 1 Million Granule Cells

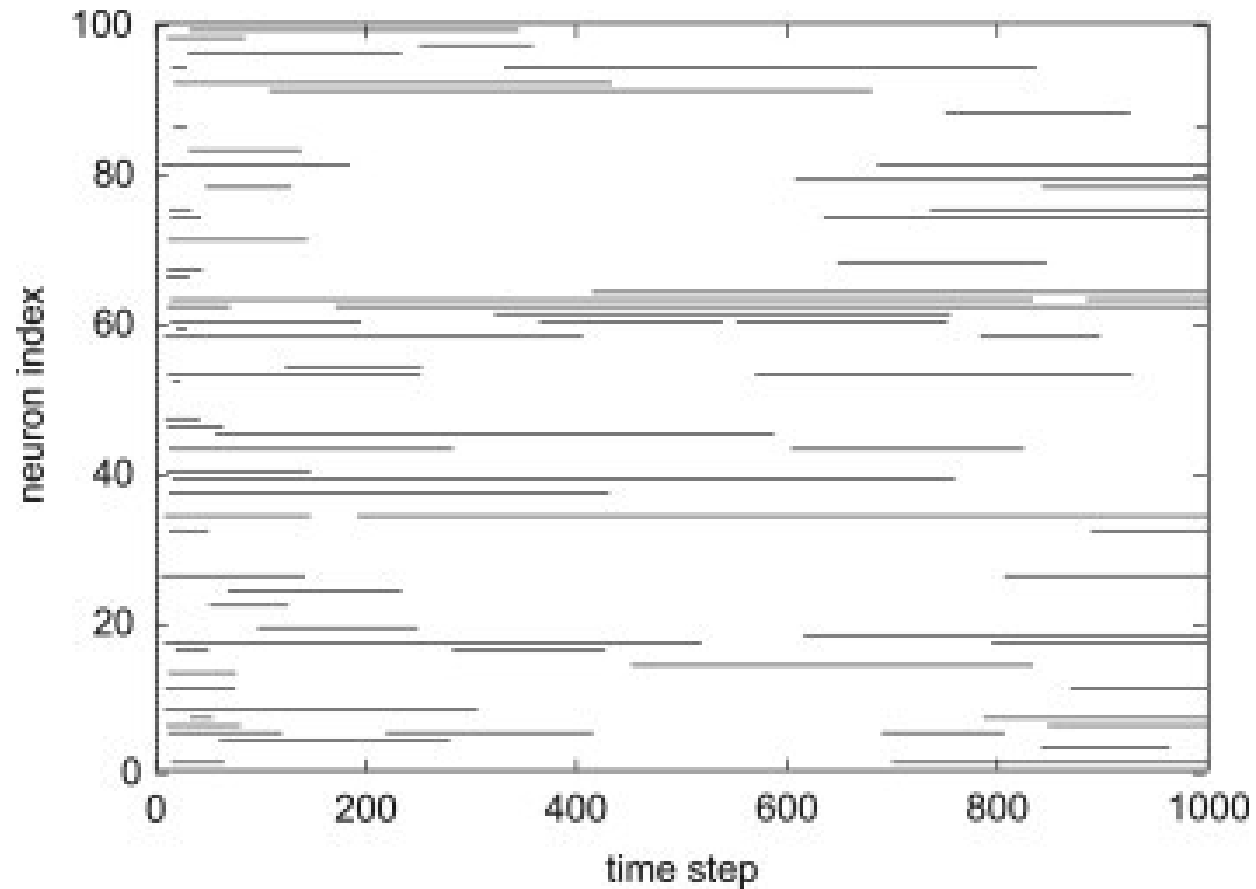
- Li et al. (2013) scale up the model using a GPU.
- Components:
  - $2^{20} = 1,048,567$  granule cells
  - 32 Purkinje cells (each with 32,768 granule cell synapses)
  - 128 basket cells, 512 stellate cells
- Results for eyeblink:
  - Original model couldn't handle 1000 msec ISI
  - New model can (sort of) handle 1000 msec ISI
  - New model still can't handle 1150 msec ISI
- Results for cart-pole balancing task:
  - Mossy fibers encode pole angle, angular velocity, and acceleration
  - Two groups of opposed output cells, for left and right motion
  - Sort of works, with no special tuning

# Cerebellar Cortex As a Liquid State Machine

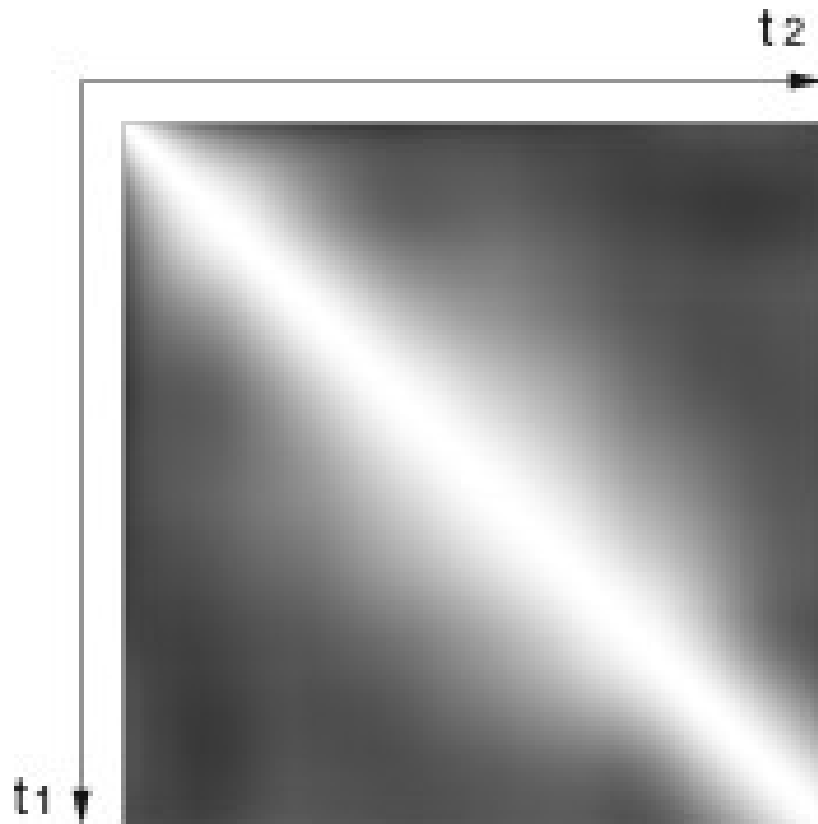
Yamazaki and Tanaka, *Neural Networks*, 20(3):290-297, April 2007



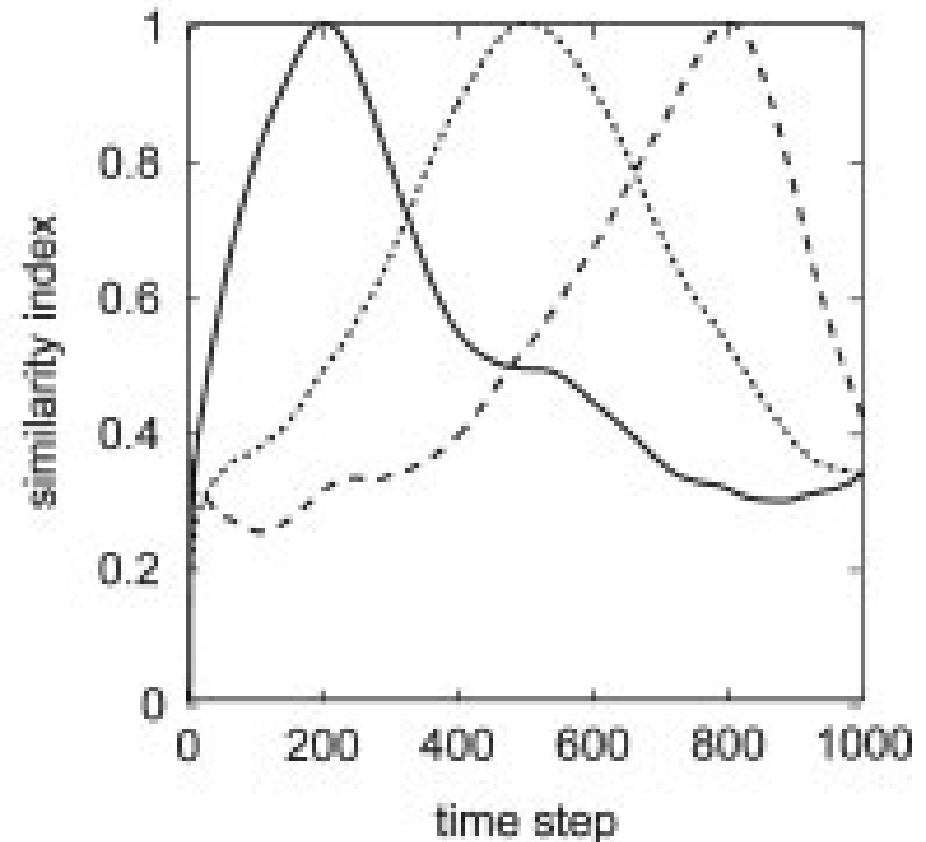
# Rich Variety of Granule Cell Activity Patterns (Medina & Mauk Noted This Too)



# Similarity Index: Granule Cell Activity Patterns Evolve Over Time

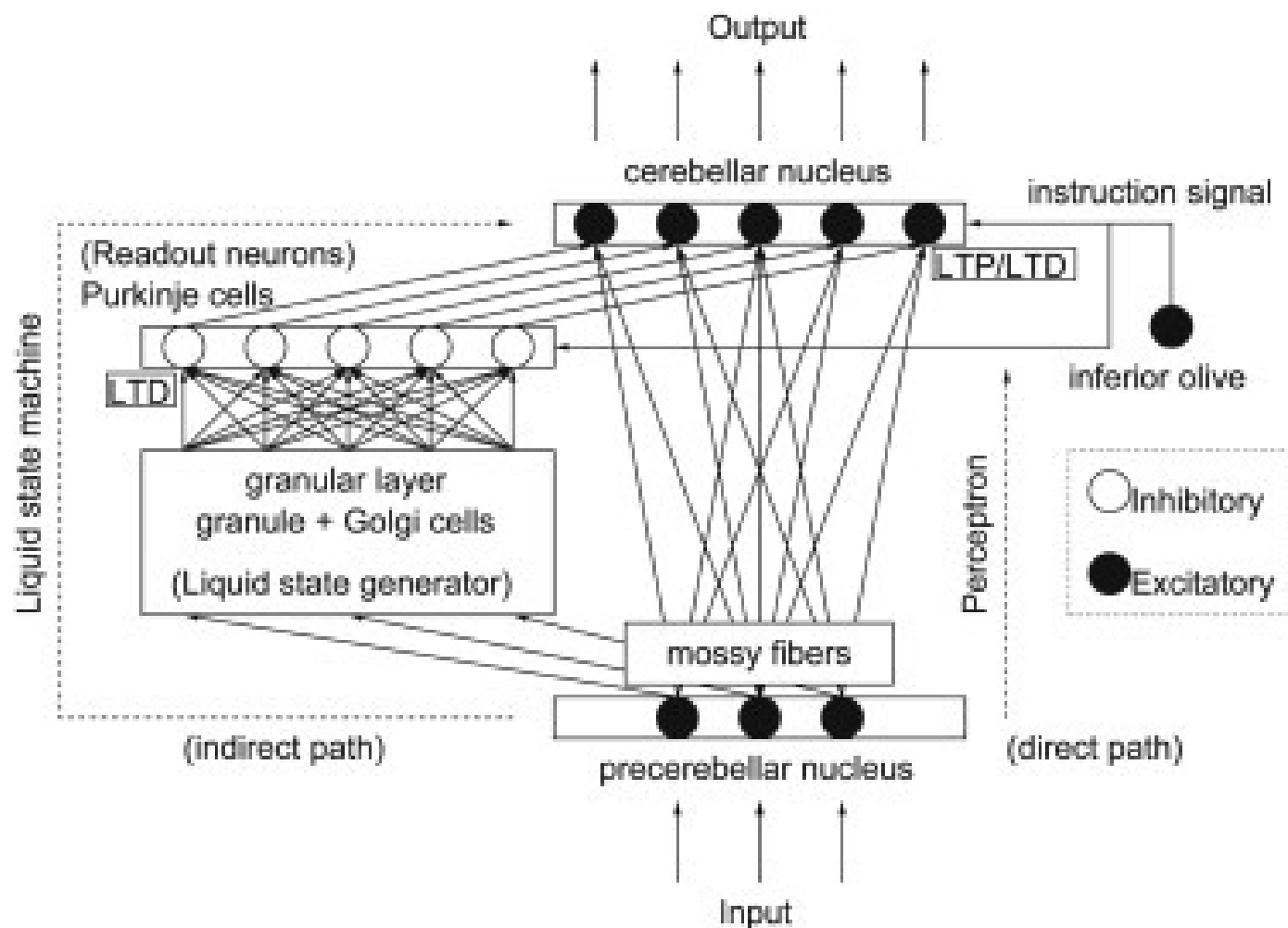


Correlation of LSM activity patterns at times  $t_1$  and  $t_2$ .



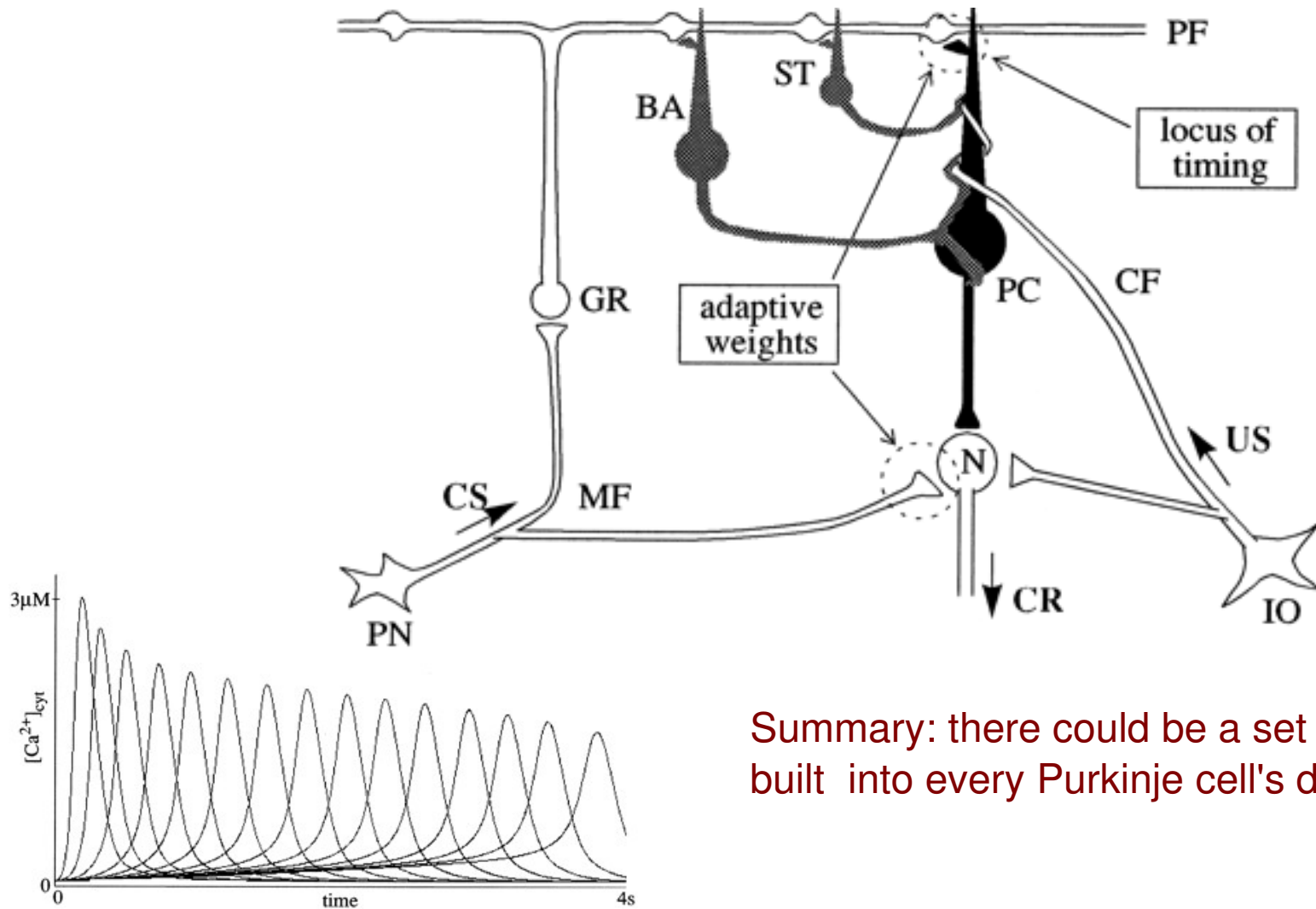
Slices through the graph at left at  $t=200$ ,  $t=500$ , and  $t=800$  show that similarity changes smoothly.

# Cerebellum = Liquid State Machine + Perceptron



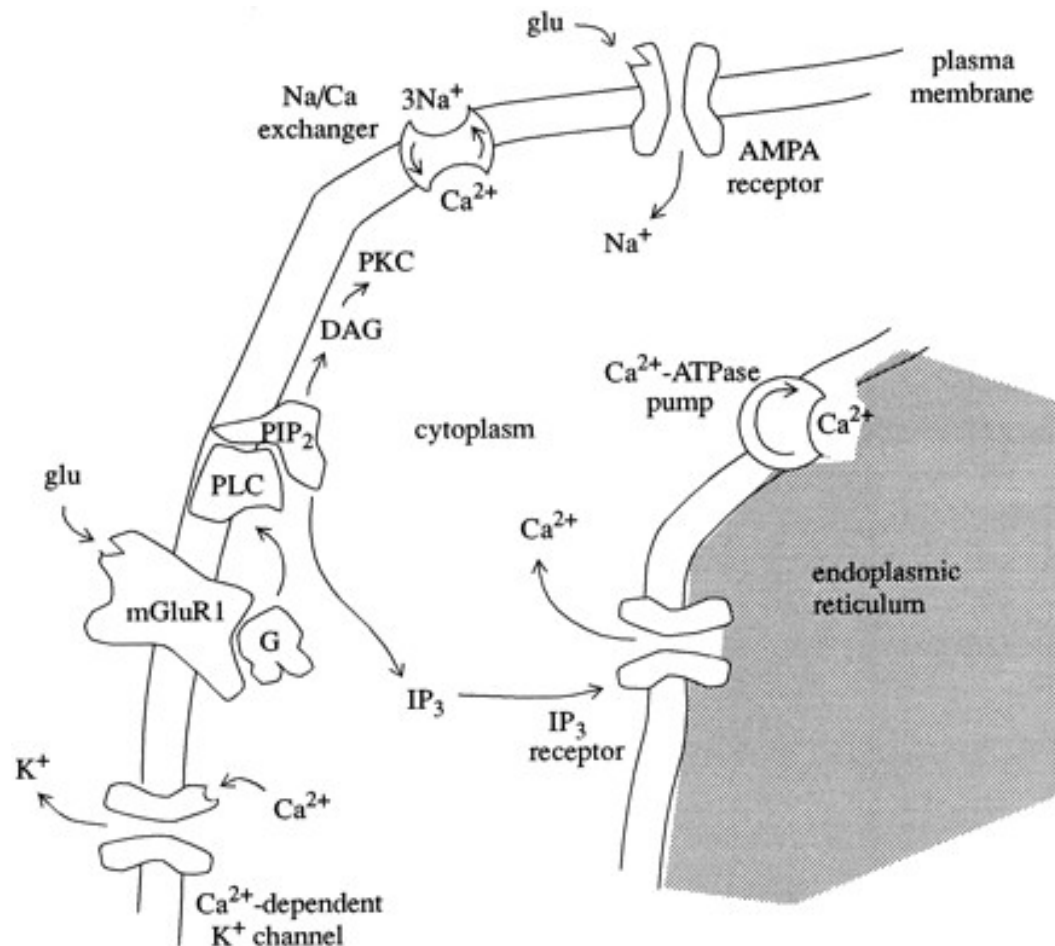
# Fiala et al. Spectral Timing Model

Fiala, Grossberg, and Bullock, *J. Neurosci.* 16(11):3760-3774, 1996



Summary: there could be a set of delay lines built into every Purkinje cell's dendritic tree.

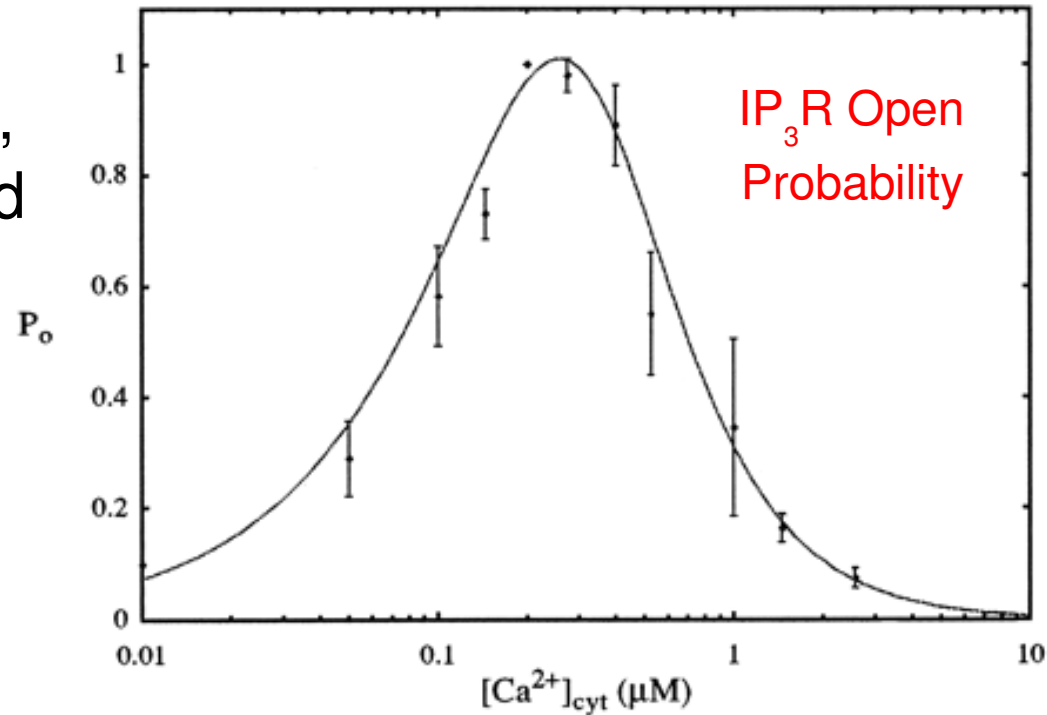
# Metabolic Transmission Pathway in Purkinje Cell Dendrites



*DAG* = diacylglycerol  
*G* = guanine nucleotide-binding protein  
*mGluR1* = metab. glutamate receptor  
*PKC* = phospholipase C  
*PIP<sub>2</sub>* = phosphatidylinositol  
                     4,5-bisphosphate  
*IP<sub>3</sub>* = inositol 1,4,5-triphosphate,  
                     a second messenger  
*IP<sub>3</sub>R* = *IP<sub>3</sub>* receptor

# Basic Story

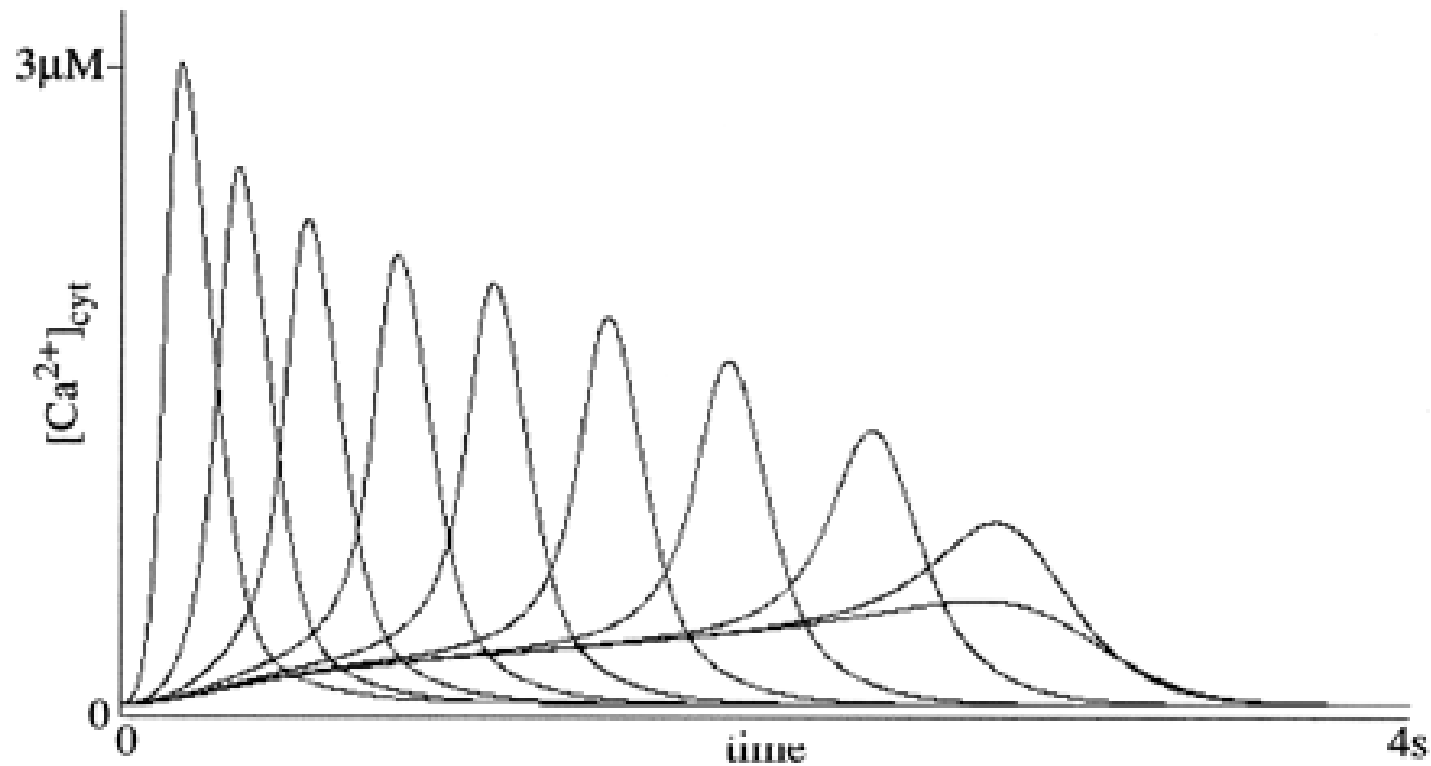
- Glutamate binds to *mGluR1* receptors, causing second messenger  $\text{IP}_3$  to bind to  $\text{IP}_3\text{R}$  receptor.
- $\text{IP}_3\text{R}$  receptor causes release of calcium from storage in the endoplasmic reticulum (ER).
- $\text{Ca}^{2+}$  activates calcium-dependent potassium channels, hyperpolarizing the dendrite and pausing the cell.
- When  $\text{Ca}^{2+}$  concentration gets too high, the  $\text{IP}_3\text{R}$  receptor closes again.  $\longrightarrow$



# Spectral Timing

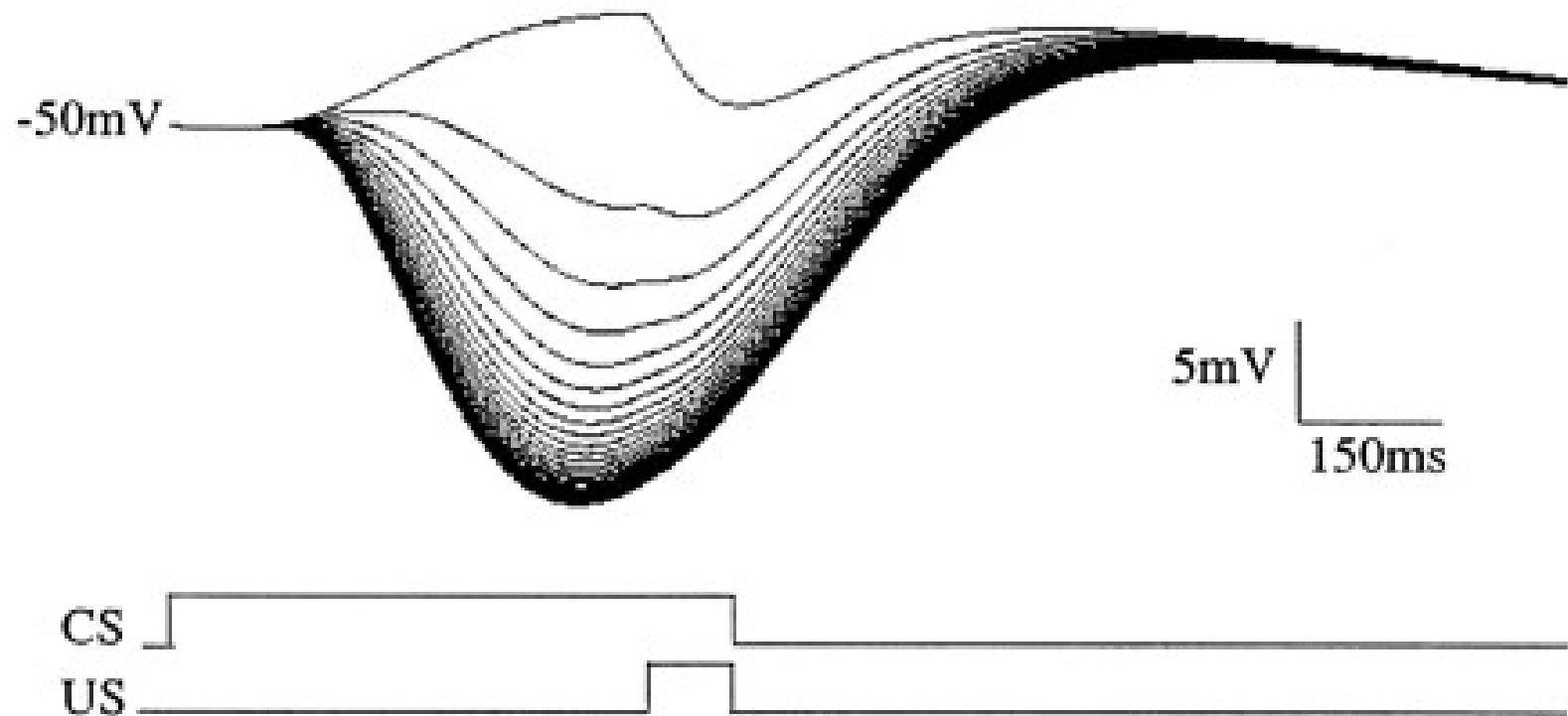
- Calcium level in the dendrite builds slowly as  $IP_3$  accumulates.
- Positive feedback on  $IP_3$  production and  $IP_3R$  channel opening results in a rapid rise in calcium level.
- But when  $Ca^{2+}$  level high enough,  $IP_3R$  channels close again.
- The speed at which this happens depends on the number of *mGluR1* receptors in the synapse.
- Different concentrations of *mGluR1* receptors produce different timing characteristics.
- High calcium level hyperpolarizes the dendrite through calcium-dependent potassium channels and inhibits firing.

# Spectral Timing: Calcium Concentration Profiles



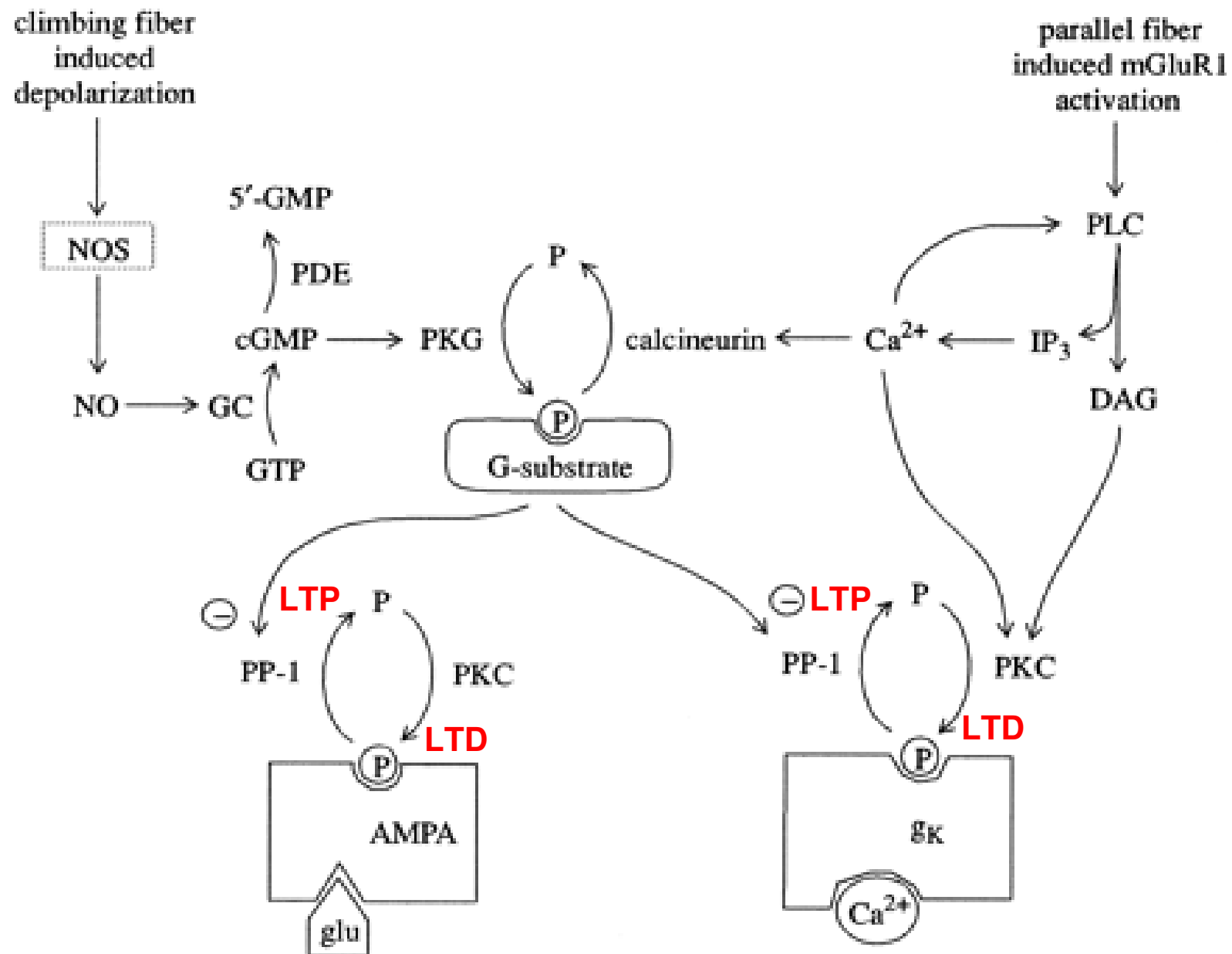
Fiala et al. simulation: responses to 50 msec glutamate application produced by varying  $B_{max}$  parameter.

# Learning Performance of the Model Using a Population of Purkinje Cells



30 trials; ISI = 500 msec

# Learning in Purkinje Cell Dendrites



# Problems with Spectral Timing Models

- Fiala et al. assume that each Purkinje cell (or each dendrite) has a fixed number of mGluRs, giving a fixed latency value.
  - But Jirenhed & Hesslow (2011) show that any Purkinje cell can learn any CS-US interval.
- Alternative model by Steuber and Willshaw (2004) assumes that learning modulates the number of mGluRs. This predicts that CR latency should decrease as learning proceeds.
  - But Jirenhed et al. (2007) found that while CR magnitude increases with learning, CR latency remained constant.
  - Changing the CS-US interval should cause a gradual shift in latency, but experiments show simultaneous extinction and acquisition.
  - Model can't account for double peak CRs seen in animals.

# Summary

- Two sites of cerebellar learning for eyeblink conditioning:
  - Cells in interpositus nucleus learn to respond to tone CS
  - Purkinje cells in cerebellar cortex learn timing of the response
- Purkinje cells require both LTP and LTD to produce temporally accurate responses.
- Granule cells have diverse response profiles
- Multiple hypotheses about how the cerebellum keeps time: delay lines, spectral timing, oscillators, liquid state machines
- Two hypotheses for why learning fails at long ISIs:
  - Medina et al: long period of LTP overwhelms LTD
  - Medina & Mauk recurrent network (= LSM) model: granule cell activity sequence gradually diverges

# Are All These Models Wrong?

- Hesslow et al. (2013) find problems with all existing models:
  - Purkinje cells have an intrinsic spiking mechanism that does not depend on parallel fiber input, so LTD of the pf→Pk synapse should not be sufficient to silence the cell.
  - The time course of LTD does not agree with that of eyeblink conditioning. (But in vitro slice experiments aren't a direct match for behavioral experiments.)
  - Granule cells may not have the rich variety of temporal responses these models assume.
  - A single Purkinje cell can learn a range of CS-US timings, so spectral timing models that assign a specific delay to each Purkinje cell cannot be correct.
  - Models that learn by adapting a cell's delay value cannot account for dual-peak responses, or for the fact that changing the ISI after training simultaneously extinguishes the old CR latency and potentiates a new one; it does not gradually shift the latency.

# Hesslow et al.'s Proposal (2013)

- Each Purkinje cell has a family of “timer units” with different latencies.
- Learning CR timing is done by selecting the units with the correct latency value.
- Once a timer is activated (by parallel fiber input), it runs autonomously and triggers hyperpolarization with its characteristic latency.
- Double-peak responses are explained by having more than one set of timer units selected.

Lots of open questions:

- *What is the neurophysiological basis of timer units?*
- *How do timer units become selected?*
- *How do timers become activated?*

# A New Proposal

- Hesslow et al. (2013) theorize about a new mechanism:
  - Doesn't depend on parallel fiber input timing.
  - Mechanism is intrinsic to the Purkinje cell or interneurons.
  - After training, pf input activates a molecular mechanism with a particular constant time delay that turns on a hyperpolarizing response for a specific duration.
  - The delay is fixed, not adjustable.
  - There is a family of these “timer units”, and the learning process *selects* the appropriate timer to use.
  - Once a timer has been activated, it runs its course independent of further inputs, so extending the duration of the CS will not affect the CR.