

## Lecture 27

### Pointer Analysis

- Basics
- Design Options
- Pointer Analysis Algorithms
- Pointer Analysis Using BDDs
- Probabilistic Pointer Analysis

(Slide content courtesy of Greg Steffan, U. of Toronto)

### Pros and Cons of Pointers

- Many procedural languages have pointers
  - e.g., C or C++: `int *p = &x;`
- Pointers are powerful and convenient
  - can build arbitrary data structures
- Pointers can also hinder compiler optimization
  - hard to know where pointers are pointing
  - must be conservative in their presence
- Has inspired much research
  - analyses to decide where pointers are pointing
  - many options and trade-offs
  - open problem: a scalable accurate analysis

### Pointer Analysis Basics: Aliases

- Two variables are *aliases* if:
  - they *reference the same memory location*
- More useful:
  - *prove variables reference different locations*

Alias sets:

```
int x,y;
int *p = &x;
int *q = &y;
int *r = p;
int **s = &q;
```

### The Pointer Alias Analysis Problem

- Decide for *every pair of pointers at every program point*:
  - *do they point to the same memory location?*
- A difficult problem
  - shown to be *undecidable* by Landi, 1992
- **Correctness:**
  - report all pairs of pointers which do/may alias
- **Ambiguous:**
  - two pointers which *may or may not* alias
- **Accuracy/Precision:**
  - *how few pairs of pointers* are reported while *remaining correct*
  - i.e., reduce ambiguity to improve accuracy

## Many Uses of Pointer Analysis

- **Basic compiler optimizations**
  - register allocation, CSE, dead code elimination, live variables, instruction scheduling, loop invariant code motion, redundant load/store elimination
- **Parallelization**
  - instruction-level parallelism
  - thread-level parallelism
- **Behavioral synthesis**
  - automatically converting C-code into gates
- **Error detection and program understanding**
  - memory leaks, wild pointers, security holes

## Challenges for Pointer Analysis

- **Complexity:** huge in **space** and **time**
  - compare every pointer with every other pointer
  - at every program point
  - potentially considering all program paths to that point
- **Scalability vs accuracy trade-off**
  - different analyses motivated for different purposes
  - many useful algorithms (adds to confusion)
- **Coding corner cases**
  - pointer arithmetic (\*p++), casting, function pointers, long-jumps
- **Whole program?**
  - most algorithms require the entire program
  - library code? optimizing at link-time only?

## Pointer Analysis: Design Options

- Representation
- Heap modeling
- Aggregate modeling
- Flow sensitivity
- Context sensitivity

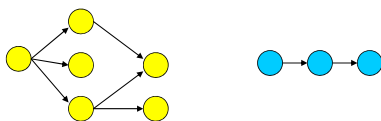
## Representation

- Track **pointer aliases**
  - $\langle *a, b \rangle, \langle *a, e \rangle, \langle b, e \rangle,$   
 $\langle **a, c \rangle, \langle **a, d \rangle, \dots$
  - **More precise, less efficient**
- Track **points-to** information
  - $\langle a, b \rangle, \langle b, c \rangle, \langle b, d \rangle,$   
 $\langle e, c \rangle, \langle e, d \rangle$
  - **Less precise, more efficient**

```
a = &b;  
b = &c;  
b = &d;  
e = b;
```

## Heap Modeling Options

- **Heap merged**
  - i.e. "no heap modeling"
- **Allocation site** (any call to malloc/calloc)
  - Consider each to be a unique location
  - Doesn't differentiate between multiple objects allocated by the same allocation site
- **Shape analysis**
  - Recognize linked lists, trees, DAGs, etc.



## Aggregate Modeling Options

### Arrays



Elements are treated as **individual locations**

or



Treat entire array as a **single location**

or



Treat **first element separate** from others

### Structures



Elements are treated as **individual locations** ("field sensitive")

or



Treat entire structure as a **single location**

## Flow Sensitivity Options

- **Flow insensitive**
  - The order of statements doesn't matter
    - Result of analysis is the same regardless of statement order
  - Uses a single global state to store results as they are computed
  - Not very accurate
- **Flow sensitive**
  - The order of the statements matter
  - Need a control flow graph
  - Must store results for each program point
  - Improves accuracy
- **Path sensitive**
  - Each path in a control flow graph is considered

## Flow Sensitivity Example

(assuming allocation-site heap modeling)

```
S1: a = malloc(...);
S2: b = malloc(...);
S3: a = b;
S4: a = malloc(...);
S5: if(c)
    a = b;
S6: if(!c)
    a = malloc(...);
S7: ... = *a;
```

Flow Insensitive

$a_{S7} \rightarrow$

Flow Sensitive

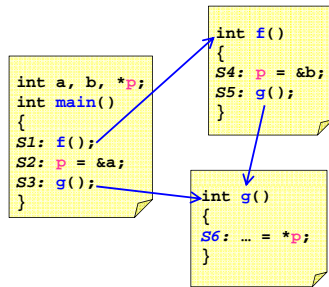
$a_{S7} \rightarrow$

Path Sensitive

$a_{S7} \rightarrow$

## Context Sensitivity Options

- Context insensitive/sensitive
  - whether to consider **different calling contexts**
  - e.g., what are the possibilities for **p** at **s6**?



Context Insensitive:

Context Sensitive:

## Pointer Alias Analysis Algorithms

### References:

- "Points-to analysis in almost linear time", Steensgaard, POPL 1996
- "Program Analysis and Specialization for the C Programming Language", Andersen, Technical Report, 1994
- "Context-sensitive interprocedural points-to analysis in the presence of function pointers", Emami et al., PLDI 1994
- "Pointer analysis: haven't we solved this problem yet?", Hind, PASTE 2001
- "Which pointer analysis should I use?", Hind et al., ISSTA 2000

## Address Taken

- Basic, fast, ultra-conservative algorithm
  - flow-insensitive, context-insensitive**
  - often used in production compilers
- Algorithm:**
  - Generate the set of all variables whose addresses are assigned to another variable.
  - Assume that any pointer can potentially point to any variable in that set.
- Complexity:**  $O(n)$  - linear in size of program
- Accuracy:** very imprecise

## Address Taken Example

```

T *p, *q, *r;

int main() {
  S1: p = alloc(T);
  f();
  g(&p);
  S4: p = alloc(T);
  S5: ... = *p;
}
    
```

```

void f() {
  S6: q = alloc(T);
  g(&q);
  S8: r = alloc(T);
}
    
```

```

g(T **fp) {
  T local;
  if(...)
    S9: p = &local;
}
    
```

**P<sub>S5</sub>** =

## Anderson's Algorithm

- Flow-insensitive, context-insensitive, iterative
- Representation:
  - one **points-to** graph for entire program
  - each node represents exactly one location
- For each statement, build the **points-to** graph:

|           |  |
|-----------|--|
| $y = \&x$ | $y$ points-to $x$  |
| $y = x$   | if $x$ points-to $w$<br>then $y$ points-to $w$                       |
| $*y = x$  | if $y$ points-to $z$ and $x$ points-to $w$<br>then $z$ points-to $w$ |
| $y = *x$  | if $x$ points-to $z$ and $z$ points-to $w$<br>then $y$ points-to $w$ |

- Iterate until graph no longer changes
- Worst case complexity:  $O(n^3)$ , where  $n$  = program size

## Anderson Example

```
T *p, *q, *r;

int main() {
S1: p = alloc(T);
   f();
   g(&p);
S4: p = alloc(T);
S5: ... = *p;
}
```

```
void f() {
S6: q = alloc(T);
   g(&q);
S8: r = alloc(T);
}
```

```
g(T **fp) {
   T local;
   if(...)
S9:   p = &local;
}
```

$P_{S5} =$

## Steensgaard's Algorithm

- Flow-insensitive, context-insensitive
- Representation:
  - a **compact points-to** graph for entire program
    - each node can represent **multiple locations**
    - but **can only point to one other node**
      - i.e. every node has a fan-out of 1 or 0
- **union-find** data structure implements fan-out
  - "unioning" while finding **eliminates need to iterate**
- **Worst case complexity**:  $O(n)$
- **Precision**: less precise than Anderson's

## Steensgaard Example

```
T *p, *q, *r;

int main() {
S1: p = alloc(T);
   f();
   g(&p);
S4: p = alloc(T);
S5: ... = *p;
}
```

```
void f() {
S6: q = alloc(T);
   g(&q);
S8: r = alloc(T);
}
```

```
g(T **fp) {
   T local;
   if(...)
S9:   p = &local;
}
```

$P_{S5} =$

## Example with Flow Sensitivity

```
T *p, *q, *r;

int main() {
S1: p = alloc(T);
  f();
  g(&p);
S4: p = alloc(T);
S5: ... = *p;
}
```

```
void f() {
S6: q = alloc(T);
  g(&q);
S8: r = alloc(T);
}
```

```
g(T **fp) {
  T local;
  if(...)
S9: p = &local;
}
```

$P_{S5} =$

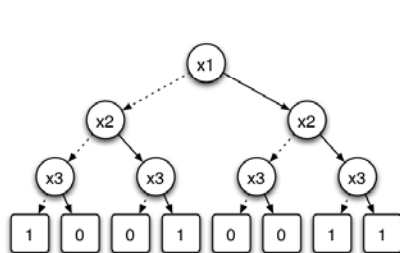
$P_{S9} =$

## Pointer Analysis Using BDDs

### References:

- "Cloning-based context-sensitive pointer alias analysis using binary decision diagrams", Whaley and Lam, PLDI 2004
- "Symbolic pointer analysis revisited", Zhu and Calman, PDLI 2004
- "Points-to analysis using BDDs", Berndt et al, PDLI 2003

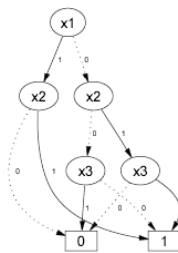
## Binary Decision Diagram (BDD)



Binary Decision Tree

| x1 | x2 | x3 | f |
|----|----|----|---|
| 0  | 0  | 0  | 1 |
| 0  | 0  | 1  | 0 |
| 0  | 1  | 0  | 0 |
| 0  | 1  | 1  | 1 |
| 1  | 0  | 0  | 0 |
| 1  | 0  | 1  | 0 |
| 1  | 1  | 0  | 1 |
| 1  | 1  | 1  | 1 |

Truth Table



BDD

## BDD-Based Pointer Analysis

- Use a BDD to represent transfer functions
  - encode procedure as a function of its calling context
  - compact and efficient representation
- Perform context-sensitive, inter-procedural analysis
  - similar to dataflow analysis
  - but across the procedure call graph
- Gives accurate results
  - and scales up to large programs

## Probabilistic Pointer Analysis

**References:**

- "A Probabilistic Pointer Analysis for Speculative Optimizations", DaSilva and Steffan, ASPLOS 2006
- "Compiler support for speculative multithreading architecture with probabilistic points-to analysis", Shen et al., PPOPP 2003
- "Speculative Alias Analysis for Executable Code", Fernandez and Espasa, PACT 2002
- "A General Compiler Framework for Speculative Optimizations Using Data Speculative Code Motion", Dai et al., CGO 2005
- "Speculative register promotion using Advanced Load Address Table (ALAT)", Lin et al., CGO 2003

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## Pointer Analysis: Yes, No, & Maybe

$*a = \sim$   
 $\sim = *b$

?

Pointer Analysis

|                |
|----------------|
| Definitely     |
| Definitely Not |
| Maybe          |

- Do pointers a and b point to the same location?
  - Repeat for every pair of pointers at every program point
- How can we optimize the "maybe" cases?

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## Let's Speculate

- Implement a **potentially unsafe** optimization
  - **Verify** and **Recover** if necessary

```
int *a, x;
...
while(...)
{
  x = *a;
  ...
}
```

a is probably loop invariant

```
int *a, x, tmp;
...
tmp = *a;
while(...)
{
  x = tmp;
  ...
}
<verify, recover?>
```

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## Data Speculative Optimizations

- EPIC Instruction sets
  - Support for speculative load/store instructions (e.g., Itanium)
- Speculative compiler optimizations
  - Dead store elimination, redundancy elimination, copy propagation, strength reduction, register promotion
- Thread-level speculation (TLS)
  - Hardware and compiler support for speculative parallel threads
- Transactional programming
  - Hardware and software support for speculative parallel transactions

*Heavy reliance on detailed profile feedback*

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### Can We Quantify "Maybe"?

- Estimate the potential benefit for speculating:

Ideally "maybe" should be a probability.

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### Conventional Pointer Analysis

- Do pointers **a** and **b** point to the same location?
  - Repeat for every pair of pointers at every program point

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### Probabilistic Pointer Analysis

- Potential advantage of Probabilistic Pointer Analysis:
  - it doesn't need to be safe

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### PPA Research Objectives

- Accurate points-to probability information
  - at every static pointer dereference
- Scalable analysis
  - Goal: entire SPEC integer benchmark suite
- Understand scalability/accuracy tradeoff
  - through flexible static memory model

*Improve our understanding of programs*

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## Algorithm Design Choices

### Fixed:

- Bottom Up / Top Down Approach
- Linear transfer functions (for scalability)
- One-level context and flow sensitive

### Flexible:

- Edge profiling (or static prediction)
- Safe (or unsafe)
- Field sensitive (or field insensitive)

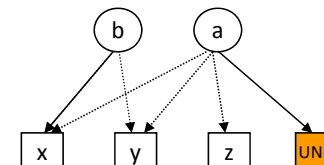
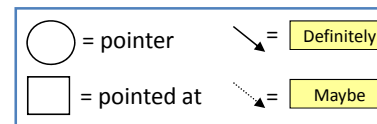
## Traditional Points-To Graph

```
int x, y, z, *b = &x;
void foo(int *a) {
```

```
  if(...)
    b = &y;
```

```
  if(...)
    a = &z;
  else(...)
    a = b;
```

```
  while(...) {
    x = *a;
    ...
  }
}
```



Results are inconclusive

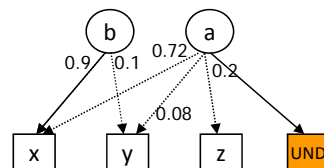
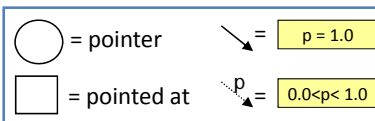
## Probabilistic Points-To Graph

```
int x, y, z, *b = &x;
void foo(int *a) {
```

```
  if(...) ⇒0.1 taken(edge profile)
    b = &y;
```

```
  if(...) ⇒0.2 taken(edge profile)
    a = &z;
  else
    a = b;
```

```
  while(...) {
    x = *a;
    ...
  }
}
```



Results provide more information

## Probabilistic Pointer Analysis Results Summary

- Matrix-based, transfer function approach
  - SUIF/Matlab implementation
- Scales to the SPECint 95/2000 benchmarks
  - One-level context and flow sensitive
- As accurate as the most precise algorithms
- Interesting result:
  - ~90% of pointers tend to point to only one thing

## Pointer Analysis Summary

- Pointers are hard to understand at compile time!
  - accurate analyses are large and complex
- Many different options:
  - Representation, heap modeling, aggregate modeling, flow sensitivity, context sensitivity
- Many algorithms:
  - Address-taken, Steensgarde, Anderson, Emami
  - BDD-based, probabilistic
- Many trade-offs:
  - space, time, accuracy, safety
- Choose the right type of analysis given how the information will be used