

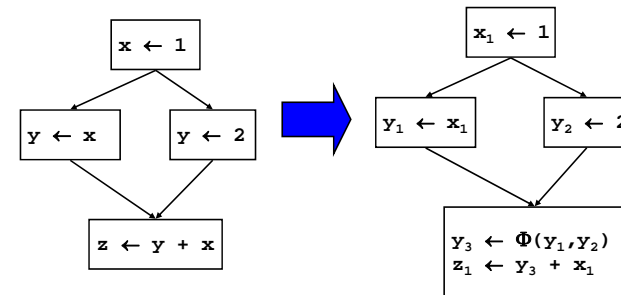
Lecture 13

SSA-Style Optimizations

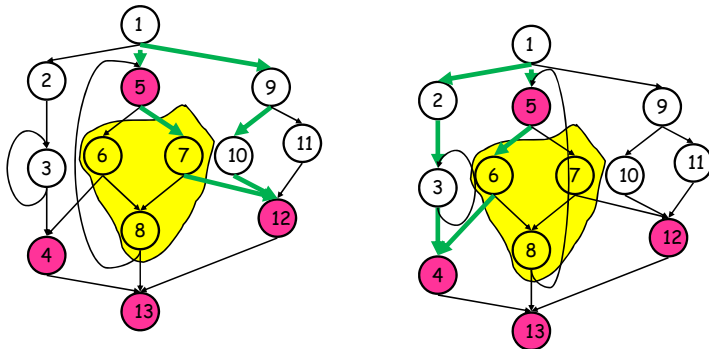
(Slides courtesy of Seth Goldstein.)

Review: Minimal SSA

- Each assignment generates a fresh variable.
- At each join point insert Φ functions for all variables with **multiple outstanding defs.**



Review: Dominance Frontier and Path Convergence



Constant Propagation

- If " $v \leftarrow c$ ", replace all uses of v with c
- If " $v \leftarrow \Phi(c, c, c)$ ", replace all uses of v with c

```

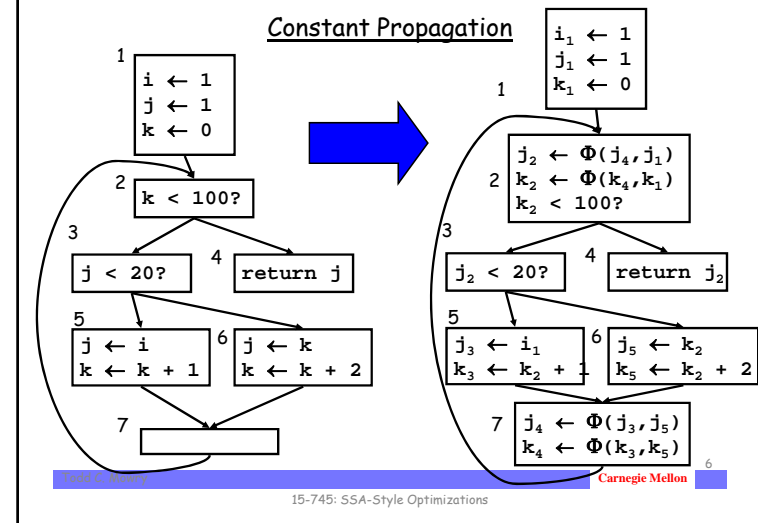
W <- list of all defs
while !W.isEmpty {
  stmt S <- W.removeOne
  if S has form " $v \leftarrow \Phi(c, \dots, c)$ "
    replace S with  $V \leftarrow c$ 
  if S has form " $v \leftarrow c$ " then
    delete S
  foreach stmt U that uses v,
    replace v with c in U
  W.add(U)
}

```

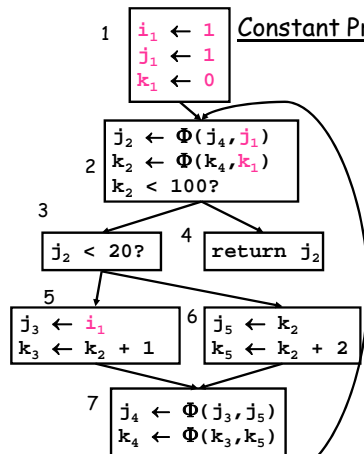
Other Optimizations with SSA

- **Copy propagation**
 - delete " $x \leftarrow \Phi(y,y)$ " and replace all x with y
 - delete " $x \leftarrow y$ " and replace all x with y
- **Constant Folding**
 - (Also, constant conditions too!)
- **Unreachable Code**
 - Remember to delete all edges from unreachable block

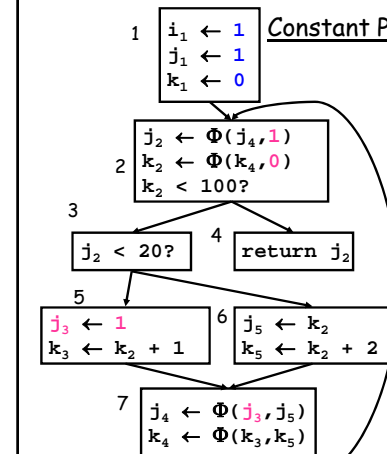
Constant Propagation

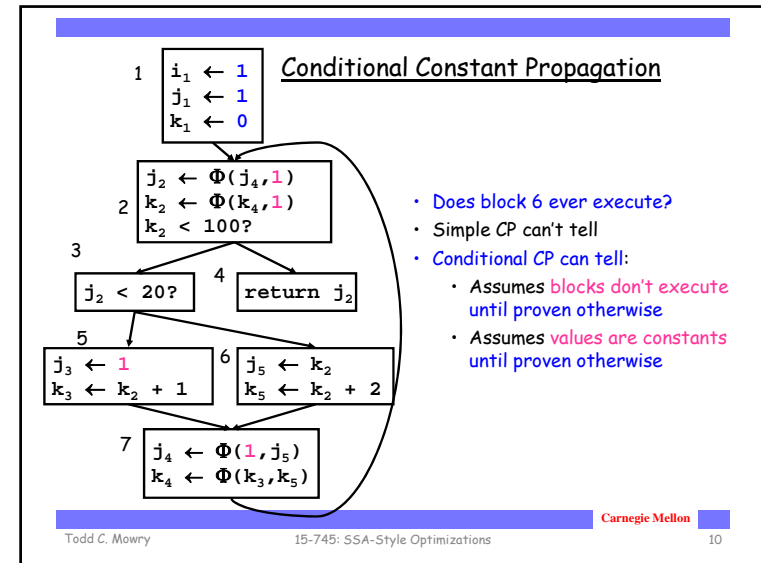
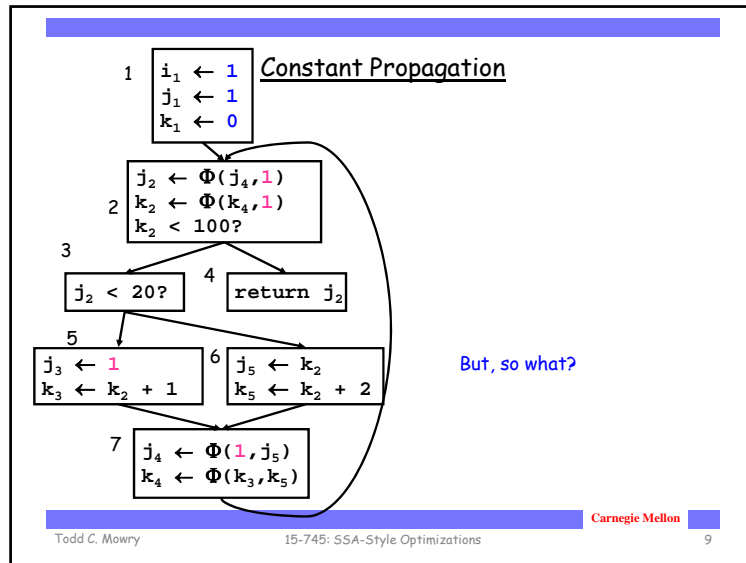


Constant Propagation



Constant Propagation





Conditional Constant Propagation Algorithm

Keeps track of:

- **Blocks**
 - assume unexecuted until proven otherwise
- **Variables**
 - assume not executed (only with proof of assignments of a non-constant value do we assume not constant)

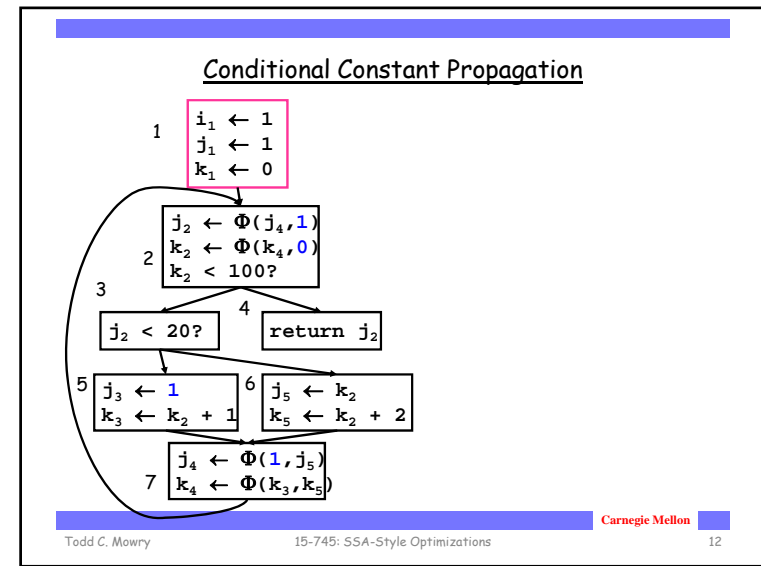
Lattice for representing variables:

T not executed

$\dots -2 -1 0 1 2 \dots$ we have seen evidence that the variable has been assigned a constant with the value

\perp we have seen evidence that the variable can hold different values at different times

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Conditional Constant Propagation

1 $i_1 \leftarrow 1$
 $j_1 \leftarrow 1$
 $k_1 \leftarrow 0$

2 $j_2 \leftarrow \Phi(j_4, 1)$
 $k_2 \leftarrow \Phi(k_4, 0)$
 $k_2 < 100?$

3 $j_2 < 20?$ 4 **return j_2**

5 $j_3 \leftarrow 1$
 $k_3 \leftarrow k_2 + 1$ 6 $j_5 \leftarrow k_2$
 $k_5 \leftarrow k_2 + 2$

7 $j_4 \leftarrow \Phi(1, j_5)$
 $k_4 \leftarrow \Phi(k_3, k_5)$

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Conditional Constant Propagation

1 $i_1 \leftarrow 1$
 $j_1 \leftarrow 1$
 $k_1 \leftarrow 0$

2 $k_2 \leftarrow \Phi(k_3, 0)$
 $k_2 < 100?$

3 $k_3 \leftarrow k_2 + 1$ 4 **return 1**

5 $j_3 \leftarrow 1$
 $k_3 \leftarrow k_2 + 1$ 6 $j_5 \leftarrow k_2$
 $k_5 \leftarrow k_2 + 2$

7 $j_4 \leftarrow \Phi(1, j_5)$
 $k_4 \leftarrow \Phi(k_3, k_5)$

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Dead Code Elimination

```

W ← list of all defs
while !W.isEmpty {
  Stmt S ← W.removeOne
  if |S.users| != 0 then continue
  if S.hasSideEffects() then continue
  foreach def in S.definers {
    def.users ← def.users - {S}
    if |def.users| == 0 then
      W ← W UNION {def}
  }
  delete S
}

```

Since we are using SSA, this is just a list of all variable assignments.

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Example DCE

B0 $i_0 \leftarrow 0$
 $j_0 \leftarrow 0$

B1 $i_1 \leftarrow i * 2$
 $j \leftarrow j + 1$
 $j < 10?$

B2 **return j**

B1 $j_1 \leftarrow \Phi(j_0, j_2)$
 $i_1 \leftarrow \Phi(i_0, i_2)$
 $i_2 \leftarrow i_1 * 2$ (Zombie)
 $j_2 \leftarrow j_1 + 1$
 $j_2 < 10?$

B2 **return j_2**

Standard DCE leaves Zombies!

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Aggressive Dead Code Elimination

Assume a statement is dead until proven otherwise.

```

init:
  mark as live all stmts that have side-effects:
  - I/O
  - stores into memory
  - returns
  - calls a function that MIGHT have side-effects
  As we mark S live, insert S.defs into W

while (|W| > 0) {
  S ← W.removeOne()
  if (S is live) continue;
  mark S live, insert S.defs into W
}
  
```

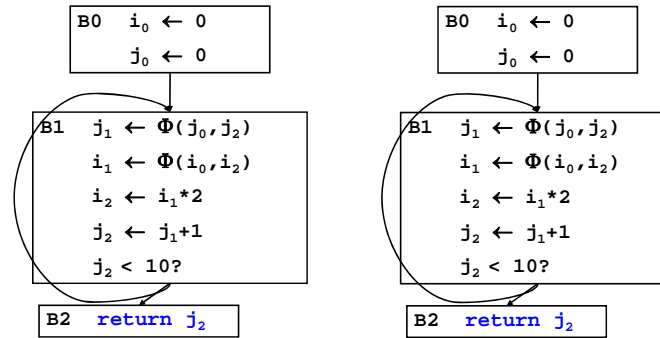
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Example DCE



Problem!

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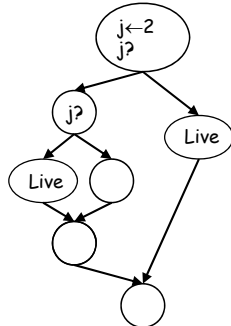
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Fixing DCE

if **S** is live, then
if **T** determines if **S** can execute, **T** should be live



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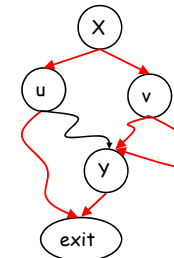
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Control Dependence

Y is **control-dependent** on **X** if

- **X** branches to **u** and **v**
- \exists a path $u \rightarrow \text{exit}$ which does not go through **Y**
- \forall paths $v \rightarrow \text{exit}$ go through **Y**

i.e. **X** can determine whether or not **Y** is executed.



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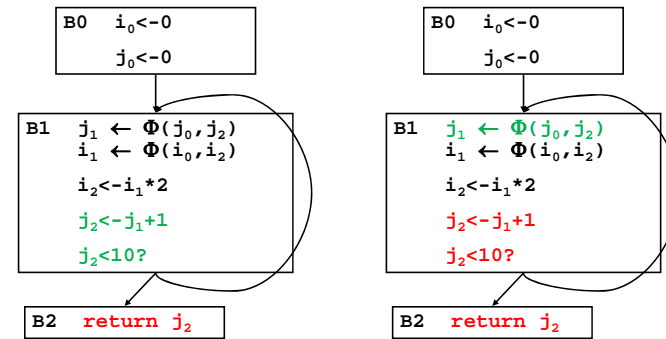
Aggressive Dead Code Elimination

Assume a statement is dead until proven otherwise.

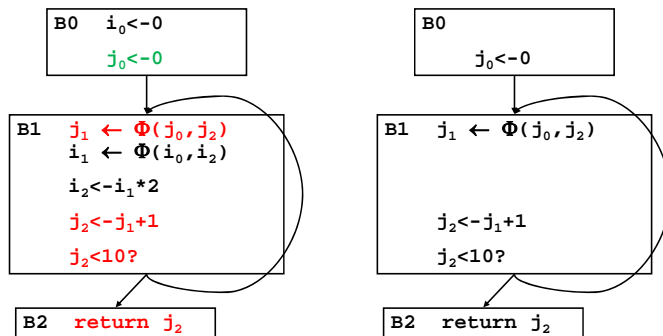
```

while (|W| > 0) {
  S <- W.removeOne()
  if (S is live) continue;
  mark S live, insert:
    - forall operands, S.operand.definers into W
    - S.CD-1 into W
}
    
```

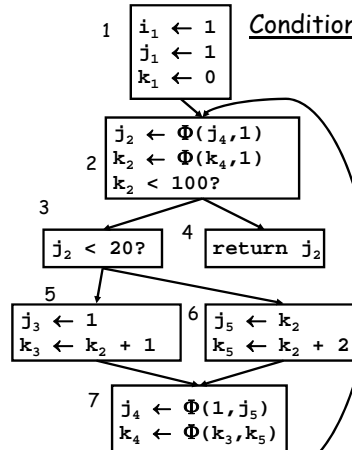
Example DCE



Example DCE



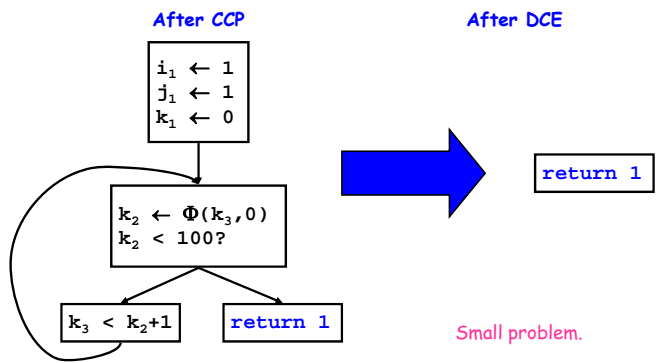
Conditional Constant Propagation



(Recall from earlier.)

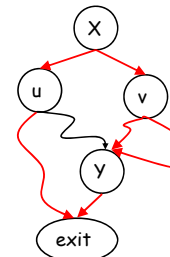
- Does block 6 ever execute?
- Simple CP can't tell
- Conditional CP can tell:
 - Assumes blocks don't execute until proven otherwise
 - Assumes values are constants until proven otherwise

Applying Dead Code Elimination to the Result of CCP

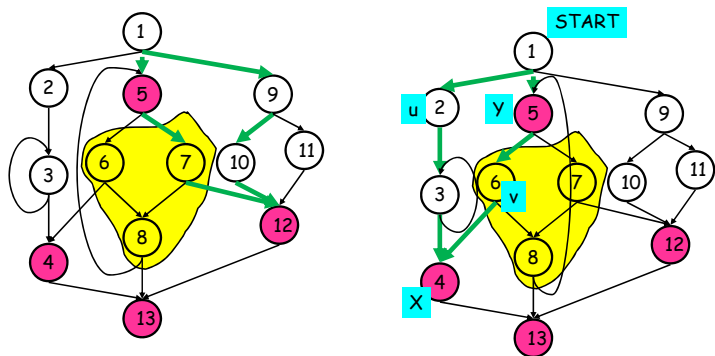


Finding the Control Dependence Graph

- Y is **control-dependent** on X if
- X branches to u and v
 - \exists a path $u \rightarrow \text{exit}$ which does not go through Y
 - \forall paths $v \rightarrow \text{exit}$ go through Y
- i.e. X can determine whether or not Y is executed.



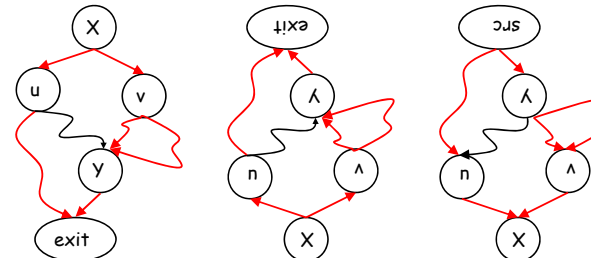
Dominance Frontier and Path Convergence



Any ideas?

Finding the Control Dependence Graph

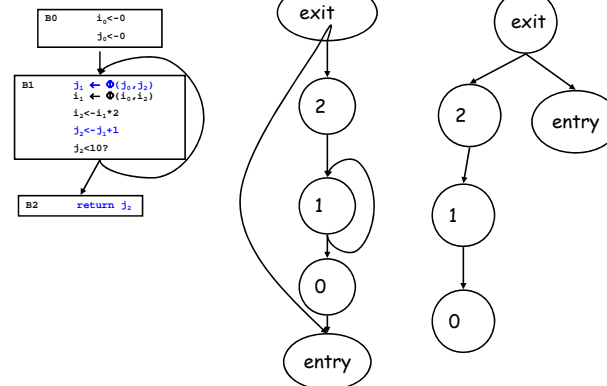
- Y is **control-dependent** on X if
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- i.e. X can determine whether or not Y is executed.



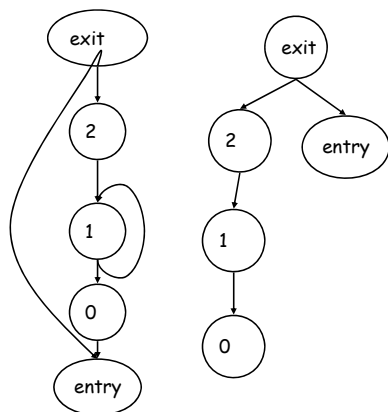
Finding the CDG

- Construct CFG
- Add entry node and exit node
- Add (entry,exit)
- Create G' , the reverse CFG
- Compute D-tree in G' (post-dominators of G)
- Compute $DF_e(y)$ for all $y \in G'$ (post-DF of G)
- Add $(x,y) \in G$ to CDG if $x \in DF_e(y)$

CDG of example



CDG of example



```

exit: {}
2: {entry}
1: {1,entry}
0: {entry}
entry: {}
    
```