15-745 Lecture 5

Control flow analysis Natural loops Classical Loop Optimizations Dependencies

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Based on slides from Lee & Callahan

Common loop optimizations

- Hoisting of loop-invariant computations Scalar opts, DF analysis,
 - pre-compute before entering the loop
- Elimination of induction variables
 - change p=i*w+b to p=b,p+=w, when w,b invariant
- Loop unrolling
 - to improve scheduling of the loop body
- Software pipelining
 - To improve scheduling of the loop body
- Loop permutation
 - to improve cache memory performance

Loops are Key

- Loops are **extremely** important
 - the "90-10" rule
- Loop optimization involves
 - understanding control-flow structure
 - Understanding data-dependence information
 - sensitivity to side-effecting operations
 - extra care in some transformations such as register spilling

Finding Loops

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- To optimize loops, we need to find them!
- Could use source language loop information in the abstract syntax tree...
- BUT:

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- There are multiple source loop constructs: for, while, do-while, even goto in C
- Want IR to support different languages
- Ideally, we want a single concept of a loop so all have same analysis, same optimizations
- <u>Solution</u>: dismantle source-level constructs, then re-find loops from fundamentals

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Control flow analysis

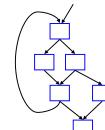
Requires

data dependencies

understanding

Finding Loops

- To optimize loops, we need to find them!
- Specifically:
 - loop-header node(s)
 - nodes in a loop that have immediate predecessors not in the loop
 - back edge(s)
 - control-flow edges to previously executed nodes
 - all nodes in the loop body



Control-flow analysis

- Many languages have goto and other complex control, so loops can be hard to find in general
- Determining the control structure of a program is called control-flow analysis
- Based on the notion of dominators

Dominators

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• a dom b

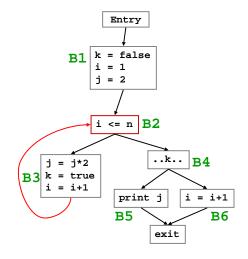
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- node a dominates b if every possible execution path from entry to b includes a
- a sdom b
 - a strictly dominates b if a dom b and a != b
- a idom b
 - a immediately dominates b if a sdom b, AND there is no c such that a sdom c and c sdom b

Back edges and loop headers

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- A control-flow edge from node B3 to B2 is a back edge if B2 dom B3
- Furthermore, in that case node B2 is a loop header



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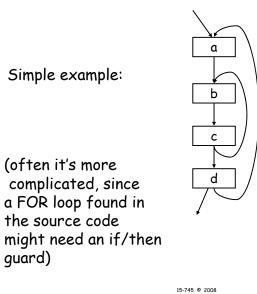
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Natural loop

- Consider a back edge from node n to node h
- The natural loop of n \rightarrow h is the set of nodes L such that for all x \in L:
 - h dom x and
 - there is a path from x to n not containing h

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Examples



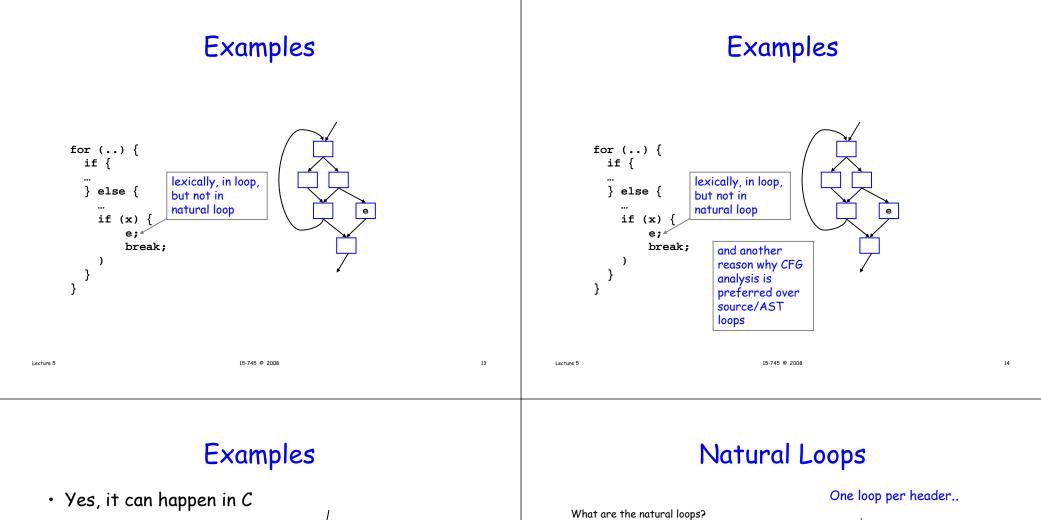
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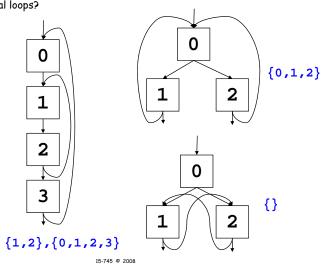
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 $\{1,2,3\}$

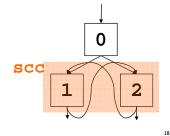
Nested Loops

- Unless two natural loops have the same header, they are either disjoint or nested within each other
- If A and B are loops (sets of blocks) with headers a and b such that $a \neq b$ and $b \in A$
 - B A
 - loop B is nested within A
 - B is the inner loop
- Can compute the loop-nest tree

General Loops

- A more general looping structure is a *strongly connected component* of the control flow graph
 - subgraph <N_{scc}, E_{scc}> such that

every block in N_{scc} is reachable from every other node using only edges in Esco



Not very useful definition of a loop

Reducible Flow Graphs

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There is a special class of flow graphs, called reducible flow graphs, for which several codeoptimizations are especially easy to perform.

In reducible flow graphs loops are unambiguously defined and dominators can be efficiently computed.

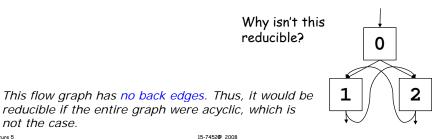
Reducible flow graphs

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Definition: A flow graph G is reducible iff we can partition the edges into two disjoint groups, forward edges and back edges, with the following two properties.

1. The forward edges form an acyclic graph in which every node can be reached from the initial node of G.

2. The back edges consist only of edges whose heads dominate their tails.



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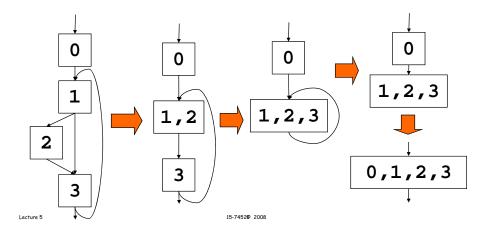
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not the case.

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Alternative definition

 Definition: A flow graph G is reducible if we can repeatedly collapse (reduce) together blocks (x,y) where x is the only predecessor of y (ignoring self loops) until we are left with a single node



Properties of Reducible Flow Graphs

• In a reducible flow graph,

all loops are natural loops

- Can use DFS to find loops
- Many analyses are more efficient
 - polynomial versus exponential

Good News

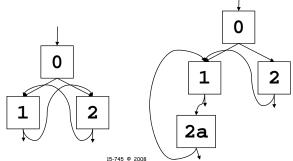
- Most flow graphs are reducible
- Languages prohibit irreducibility
 - goto free C
 - Java
- Programmers usually don't use such constructs even if they're available
 - >90% of old Fortran code reducible

Dealing with Irreducibility

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• Don't

- Can split nodes and duplicate code to get reducible graph
 - possible exponential blowup
- Other techniques...



Loop optimizations: Hoisting of loop-invariant computations

Loop-invariant computations

- \cdot A definition
 - t = x op y

in a loop is (conservatively) loop-invariant if

- x and y are constants, or
- all reaching definitions of x and y are outside the loop, or
- only one definition reaches x (or y), and that definition is loop-invariant
 - \cdot so keep marking iteratively

Loop-invariant computations

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• Be careful:

Of course, not an issue in SSA

• Even though t's two L2: each invariant, s is not invariant...

Hoisting

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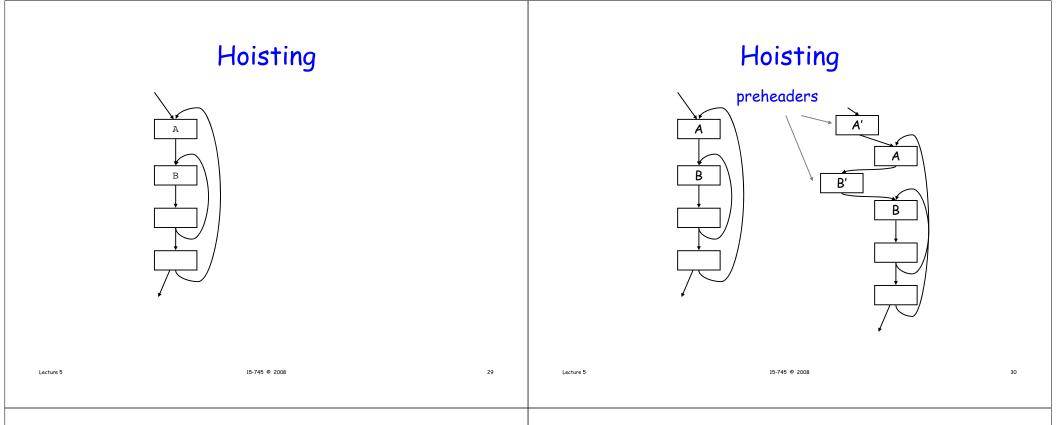
- In order to "hoist" a loop-invariant computation out of a loop, we need a place to put it
- We could copy it to all immediate predecessors (except along the back-edge) of the loop header...
- ...But we can avoid code duplication by inserting a new block, called the pre-header

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Hoisting conditions

• For a loop-invariant definition

d: t = x op y

- we can hoist d into the loop's pre-header only if
 - 1. d's block dominates all loop exits at which t is liveout, and
 - 2. d is only the only definition of t in the loop, and
 - 3. t is not live-out of the pre-header

We need to be careful...

• All hoisting conditions must be satisfied!

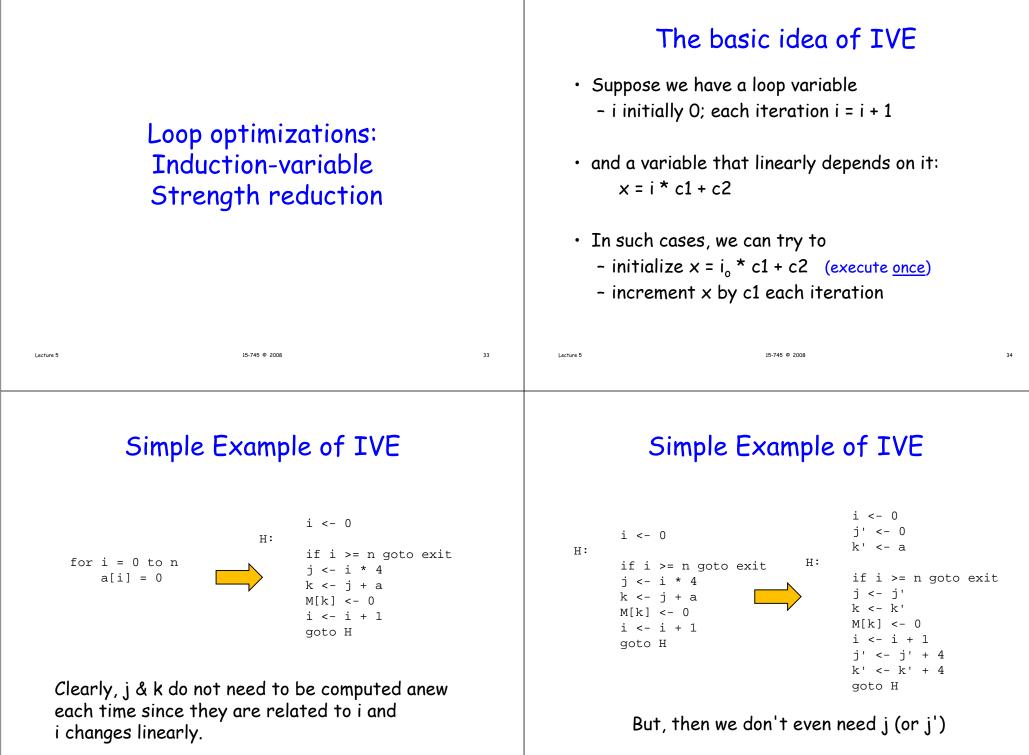
L0:	L0:	L0:
t = 0	t = 0	t = 0
L1:	L1:	L1:
i = i + 1	if i>=N goto L2	i = i + 1
t = a * b	i = i + 1	t = a * b
M[i] = t	t = a * b	M[i] = t
if i <n goto="" l1<="" td=""><td>M[i] = t</td><td>t = 0</td></n>	M[i] = t	t = 0
L2:	goto L1	M[j] = t
x = t	L2:	if i <n goto="" l1<="" td=""></n>
	$\mathbf{x} = \mathbf{t}$	L2:
		L



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violates 1,3

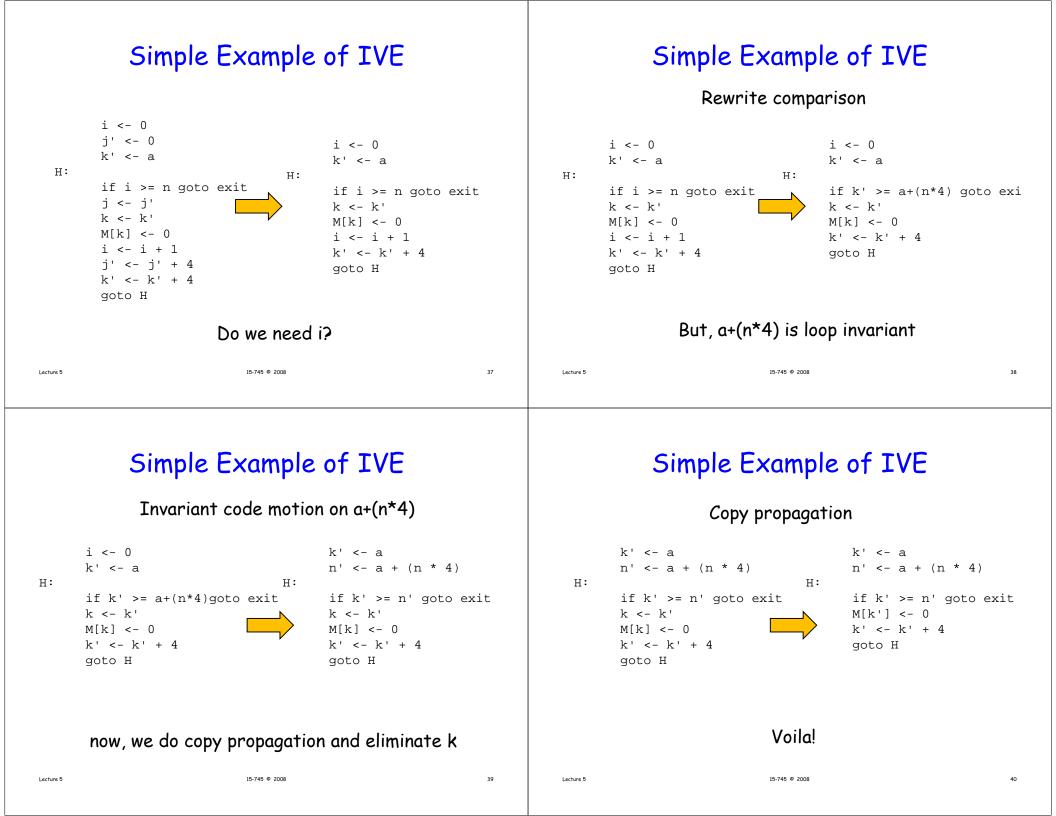
violates 2



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Simple Example of IVE What we did Compare original and result of IVE identified induction variables (i,j,k) strength reduction (changed * into +) k' <- a i <- 0 n' < -a + (n * 4) dead-code elimination (j <- j') н: н: if i >= n qoto exit

if k' >= n' goto exit

M[k'] < -0

goto H

k' < -k' + 4

- useless-variable elimination $(j' \leftarrow j' + 4)$ (This can also be done with ADCE)
- loop invariant identification & code-motion
- almost useless-variable elimination (i)
- copy propagation

Voila

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i <- i * 4

k <- j + a

i <- i + 1 goto H

M[k] < -0

Is it faster?

- On some hardware, adds are much faster than multiplies
- Furthermore, one fewer value is computed,
 - thus potentially saving a register
 - and decreasing the possibility of spilling

Loop preparation

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- Before attempting IVE, it is best to first perform :
 - constant propagation & constant folding
 - copy propagation
 - loop-invariant hoisting

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How to do it, step 1

First, find the basic IVs

scan loop body for defs of the form
x = x + c or x = x - c
where c is loop-invariant
record these basic IVs as
x = (x, 1, c)
this represents the IV: x = x * 1 + c

Representing IVs

• Characterize all induction variables by:

(base-variable, offset, multiple)

- where the offset and multiple are loopinvariant
- IOW, after an induction variable is defined it equals:

offset + multiple * base-variable

How to do it, step 2

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• Scan for derived IVs of the form

k = i * c1 + c2

- where i is a basic IV,
 this is the only def of k in the loop, and
 c1 and c2 are loop invariant
- We say k is in the family of i
- Record as k = (i, c1, c2)

How to do it, step 3

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- Iterate, looking for derived IVs of the form
 - k = j * c1 + c2
 - where IV j =(i, a, b), and
 - this is the only def of k in the loop, and
 - there is no def of i between the def of j and the def of k
 - c1 and c2 are loop invariant
- Record as k = (i, a*c1, b*c1+c2)

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<pre>i <- 0 H:</pre>		• Fi • Fi -	 Finding the IVs Maintain three tables: basic & maybe & other Find basic Ivs: Scan stmts. If var ∉ maybe, and of proper form, put into basic. Otherwise, put var in other and remove from maybe. Find compound Ivs: If var defined more than once, put into other IV For all stmts of proper form that use a basic IV * FIX THIS SLIDE 		
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	How to do it, step 4 he strength reduction step	• Tł	How to do it, step 5 nis is the comparison rewriting step		
 For an induction variable k = (i, c1, c2) initialize k = i * c1 + c2 in the preheader replace k's def in the loop by k = k + c1 make sure to do this after i's def 		- - • Re	 For an induction variable k = (i, a_k, b_k) If k used only in definition and comparison There exists another variable, j, in the same class and is not "useless" and j=(i, a_j, b_j) Rewrite k < n as j < (b_j/b_k)(n-a_k)+a_j Note: since they are in same class: (j-a_j)/b_j = (k-a_k)/b_k 		
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Notes

- Are the c1, c2 constant, or just invariant?
 - if constant, then you can keep folding them: they're always a constant even for derived IVs
 - otherwise, they can be expressions of loopinvariant variables
- But if constant, can find IVs of the type
 x = i/b
 and know that it's least if b evenly divides

and know that it's legal, if b evenly divides the stride...

Is it faster? (2)

- On some hardware, adds are much faster than multiplies
- But...not always a win!
 - Constant multiplies might otherwise be reduced to shifts/adds that result in even better code than IVE
 - Scaling of addresses (i*4) might come for free on your processor's address modes

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 So maybe: only convert i*c1+c2 when c1 is loop invariant but <u>not</u> a constant

Common	loop	optim	izations
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Requires understanding

data dependencies 53